



$R(D)$ & $R(D^*)$ measurements at Belle

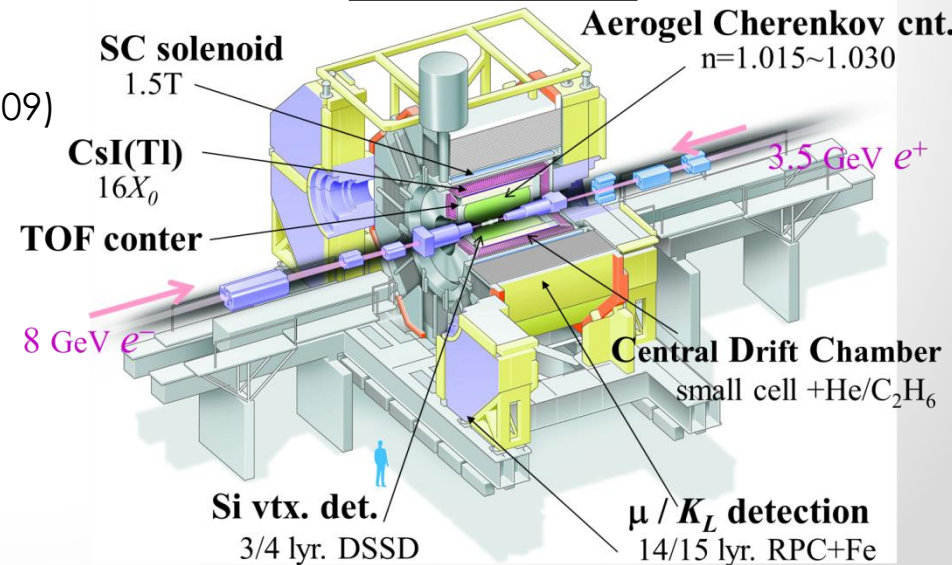
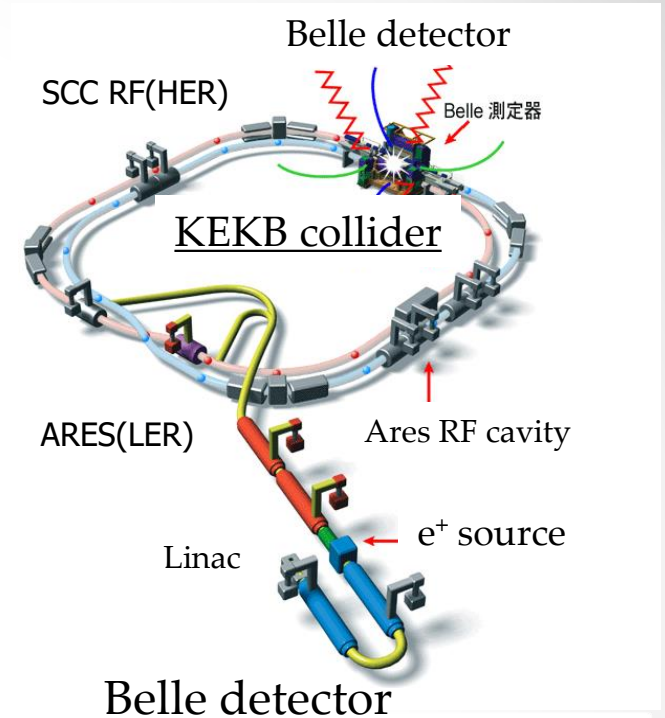
Koji Hara (KEK)

for the Belle Collaboration

Oct. 3, 2019

18th international conference on B-physics at frontier machines

Belle and KEKB

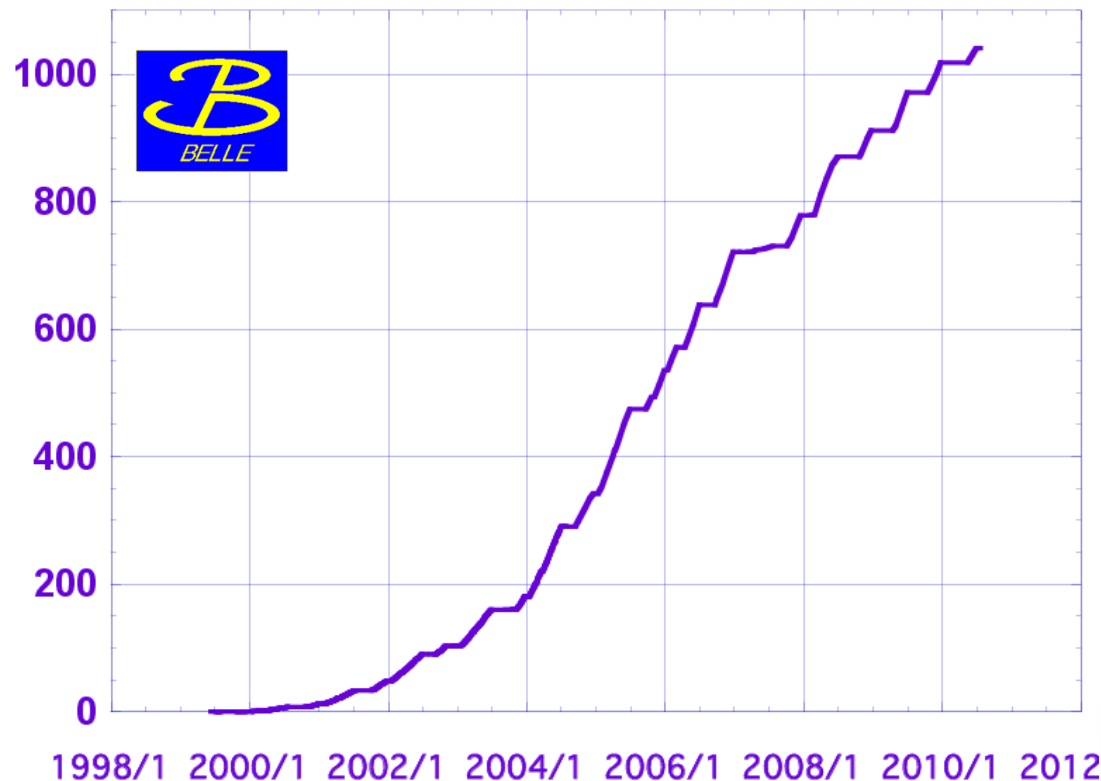


- KEKB
 - Achieved World Highest Luminosity (as of 2009)
 - $L = 2.1 * 10^{34} / \text{cm}^2/\text{sec} \sim 20 \overline{B\overline{B}}$ pairs / sec
 - Asymmetric energy to boost B mesons
 - $8.0\text{GeV } e^- \times 3.5\text{GeV } e^+$
- Belle
 - Multi-purpose 4π detector
 - Vertexing, tracking, EM calorimeter, PID
- Data taking for 1999-2010

Belle Integrated Luminosity

- The world largest integrated luminosity of $> 1 \text{ ab}^{-1}$
- 711 fb^{-1} on $Y(4S)$ resonance \rightarrow **$772 \times 10^6 \text{ BB pairs}$**

Integrated Luminosity[fb⁻¹]



On resonance:

Y(5S): 121 fb⁻¹

Y(4S): 711 fb⁻¹

Y(3S): 3 fb⁻¹

Y(2S): 25 fb⁻¹

Y(1S): 6 fb⁻¹

Off reson./scan:

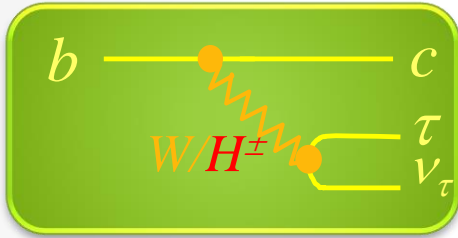
~100 fb⁻¹

Semi-tauonic B decay: $B \rightarrow D^{(*)} \tau \nu$

■ Sensitive to new physics

Ratio of τ to μ, e could be reduced/enhanced

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)} \quad L=e, \mu$$

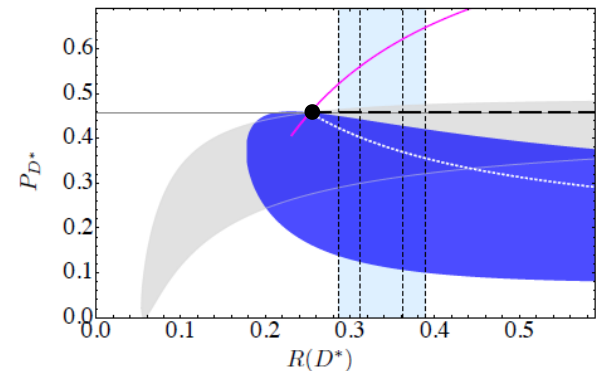
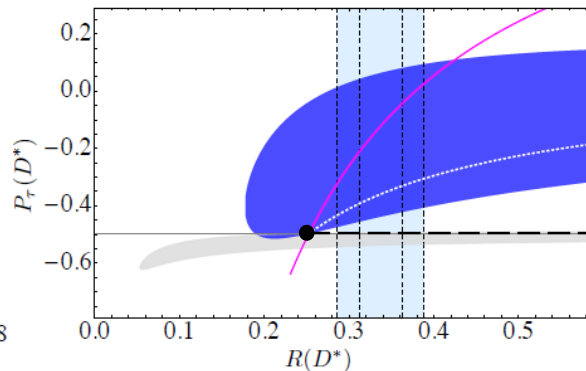
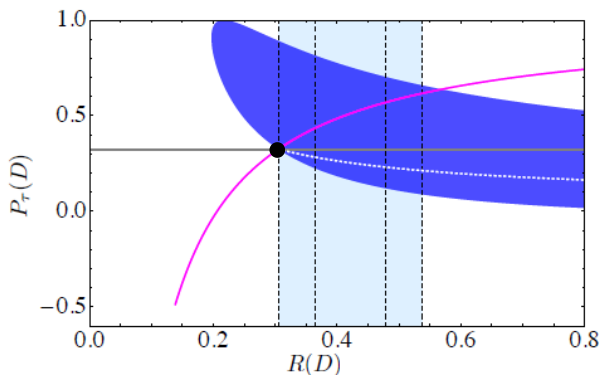


Polarizations of τ and D^* can probe the NP model

$$P_\tau(D^{(*)}) = \frac{\Gamma^+ - \Gamma^-}{\Gamma^+ + \Gamma^-} \quad F_L^{D^*} = \frac{\Gamma(D_L^*)}{\Gamma(D_L^*) + \Gamma(D_T^*)}$$

NP type (vector, scalar, tensor) dependence

[M. Tanaka and R. Watanabe PRD 87, 034028 (2013)]



Meas.(2013)

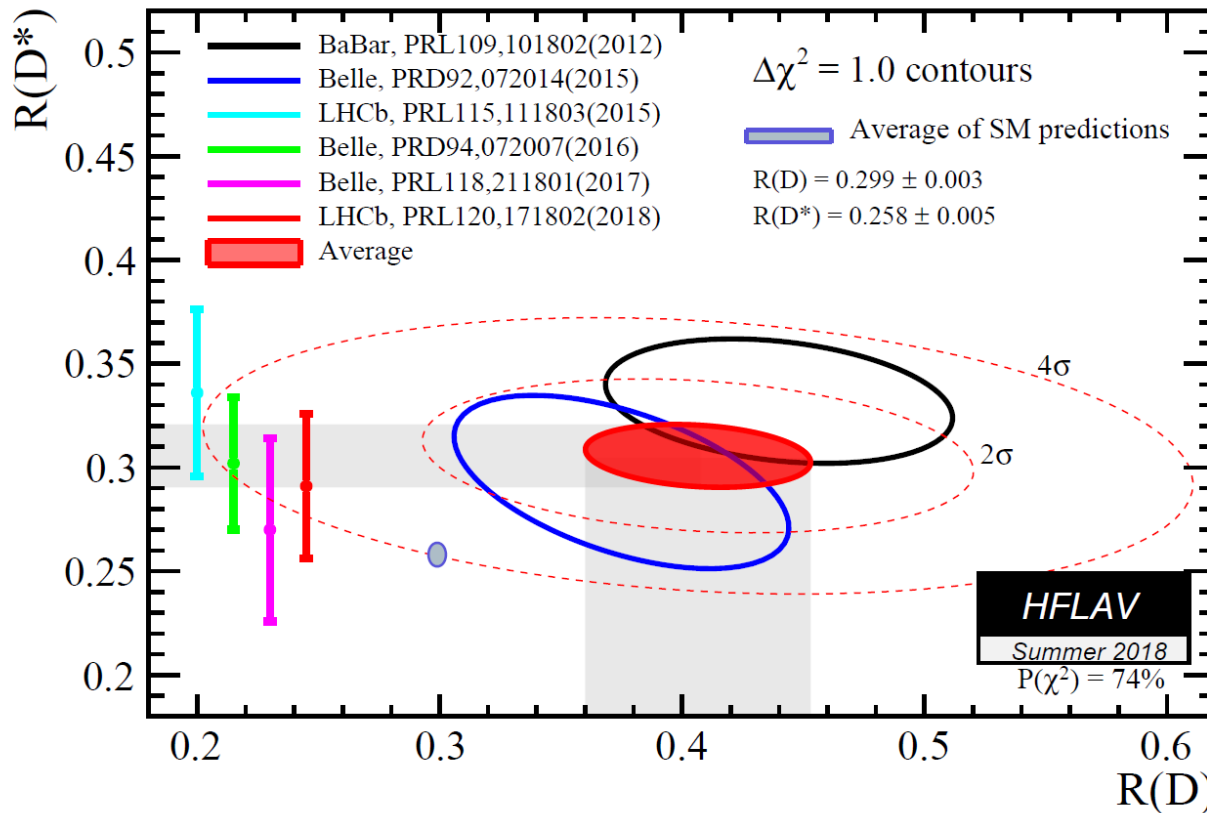
• SM
Beauty 2019

— Scalar

○ Vector

● Tensor

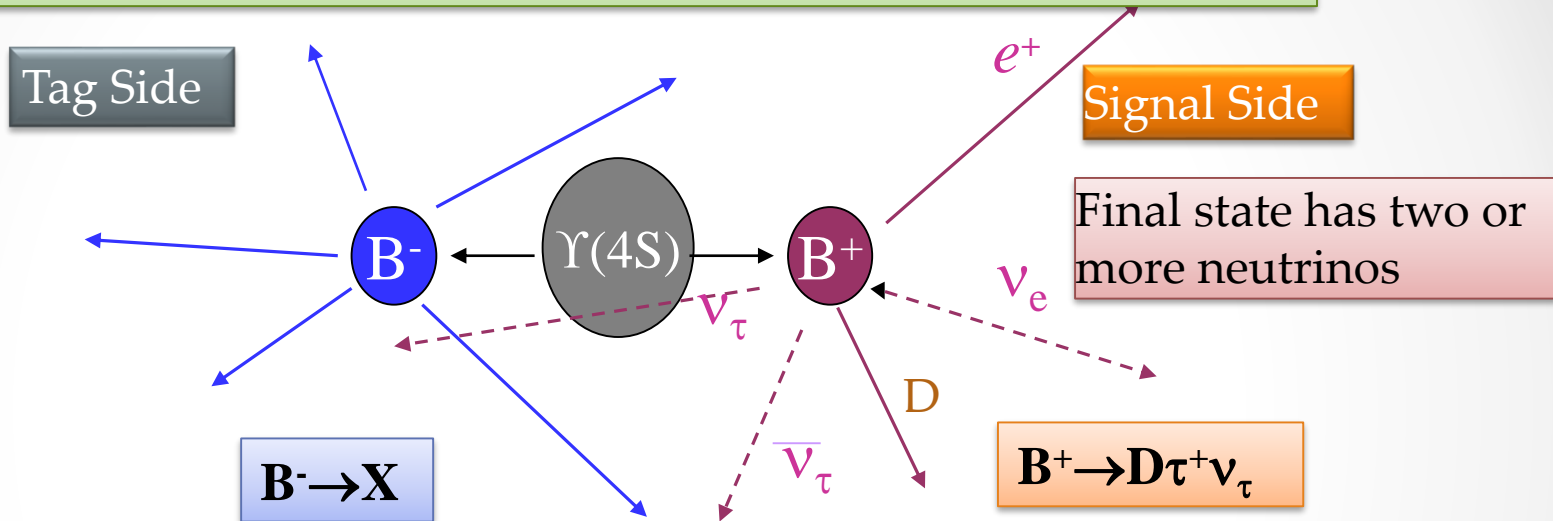
Previous $R(D^{(*)})$ Situation



- **3.8 σ deviation from the SM expectation in 2018**
→ **New Belle $R(D)$ and $R(D^*)$ results in 2019**

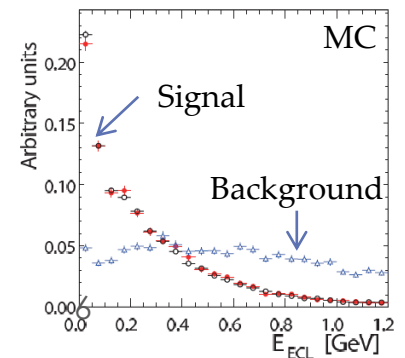
$B \rightarrow D^{(*)} \tau \nu$ Analysis at Belle

Utilize the B factory specific feature :
only one B-meson pair is produced



Tag B pair event by reconstructing one B meson in hadronic or semileptonic B Decay
→ Provide pure single B event

Require **no** particle remains after removing products of tagging B and the particle(s) from signal decays
← Remaining energy in the calorimeter (E_{ECL})



Tagging Methods

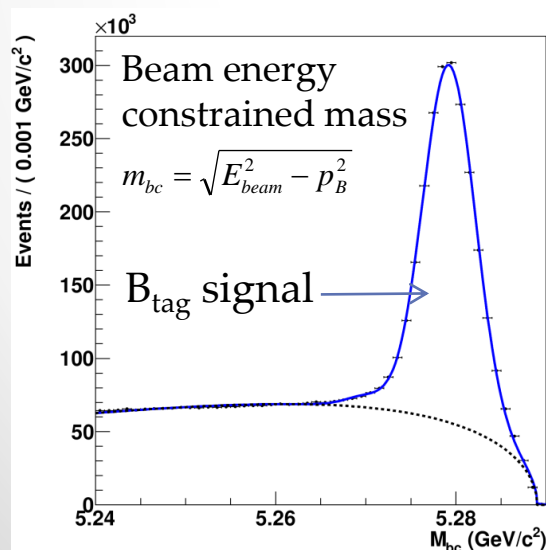
Hadronic Tag

Exclusive tag

- Fully reconstruct in $B \rightarrow DX$ decays
 - ~1100 exclusive decay channels [NIM A 654, 432 (2011)]
- Tagging efficiency ~ 0.2 %
- Less background

Inclusive tag

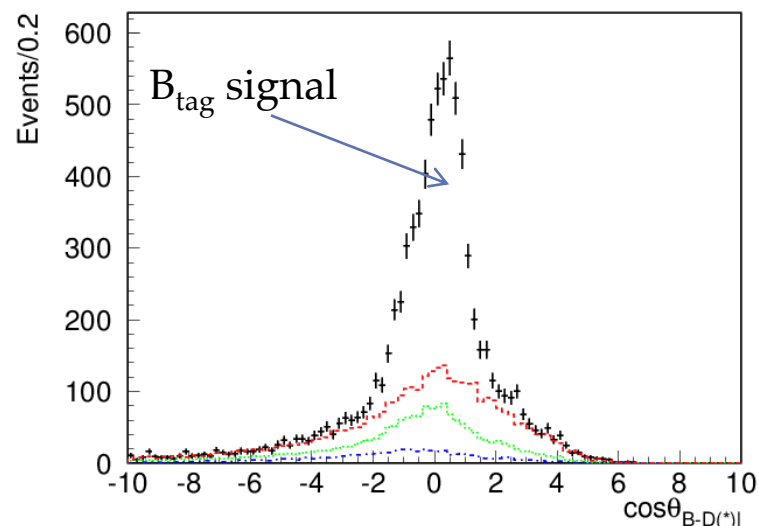
- Reconstruct tag-side B with all particles except signal-side
- Higher efficiency than exclusive tag
- Need clean signal-side final state



Semileptonic Tag

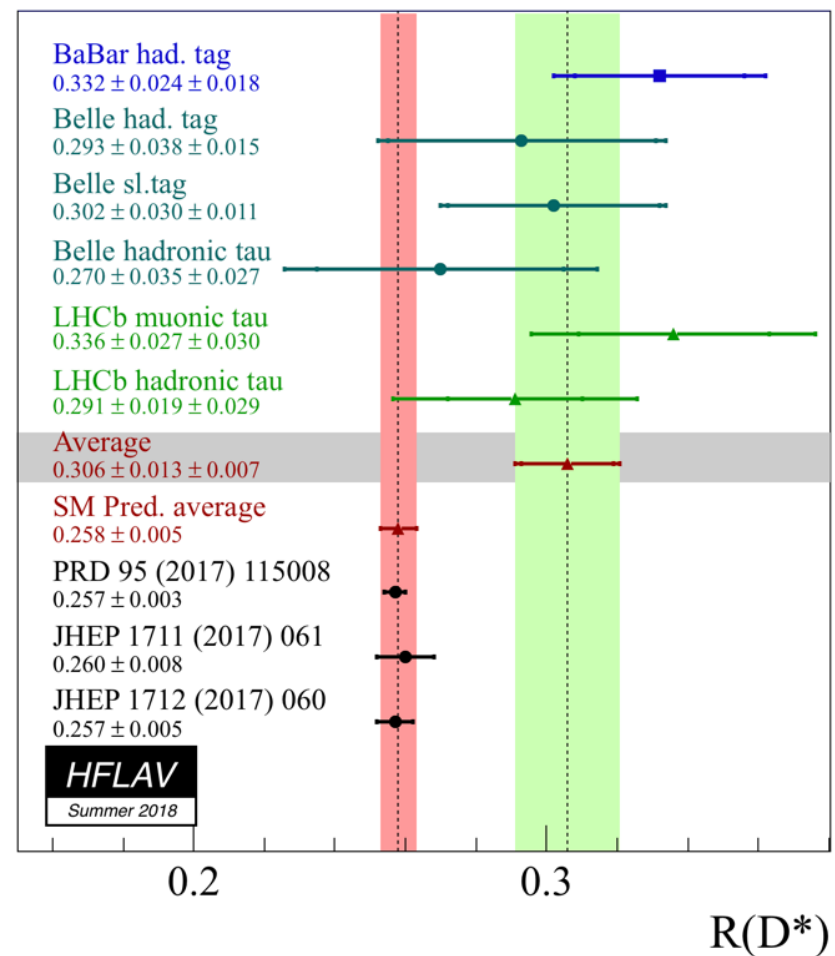
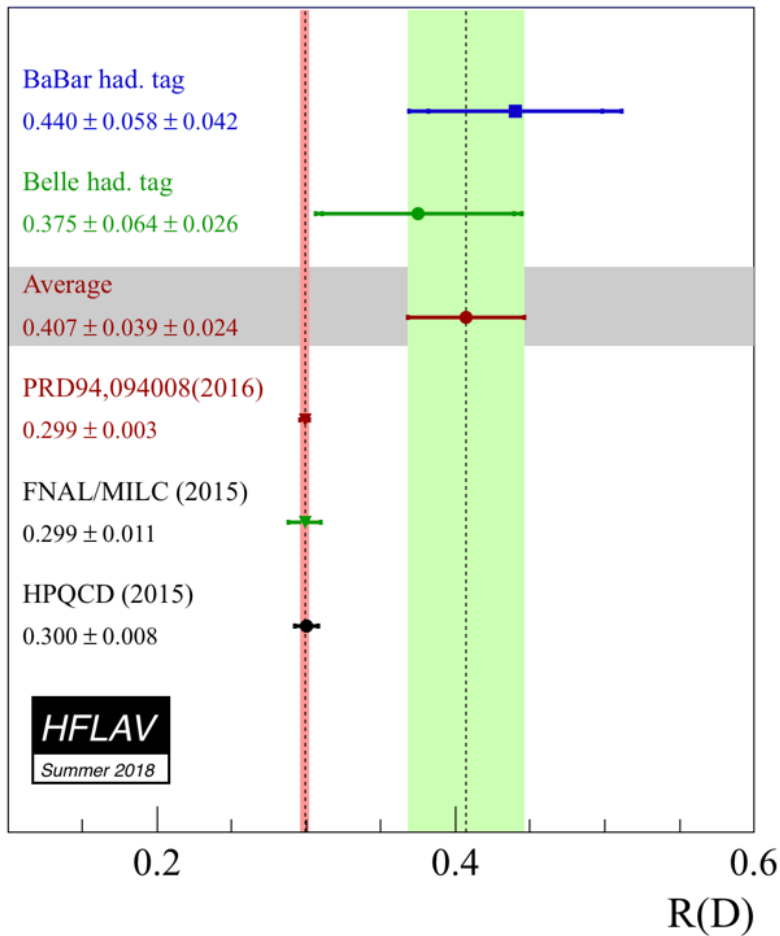
- Reconstruct $B \rightarrow D^{(*)} l \nu$
 - Partial reconstruction with
 - $E_B = E_{beam}$
 - Undetected neutrino mass ~ 0
- Tagging efficiency ~ 0.5%
- More background

Belle $B \rightarrow TV$ analysis [PRD 82, 071101(R) (2010)]



$$\cos \theta_{B,D^{(*)}l} = \frac{2E_{beam}^{cms} E_{D^{(*)}l}^{cms} - m_B^2 - M_{D^{(*)}l}^2}{2P_B^{cms} \cdot P_{D^{(*)}l}^{cms}}$$

Previous $R(D)$ and $R(D^*)$



- Only two $R(D)$ measurements with hadronic tag
→ New Belle analysis of $R(D)$ with semileptonic tag

New $R(D^{(*)})$ Measurement with Semileptonic Tag

- Previous Belle Semileptonic tag [PRD94,072007(2016)]

Measure $R(D^{*})$ with $B^0 \rightarrow D^{*-} \tau^+ \nu$ (and charge conjugate) decays

- Good signal purity by using clean $D^{*-} \rightarrow D^0 \pi^-$ decays

- New Semileptonic Analysis [arXiv:1904.08794] **preliminary**

- Full Event Interpretation (FEI) tool developed in BelleII software framework [Comput. Softw. Big. Sci. (2019) 3:6]

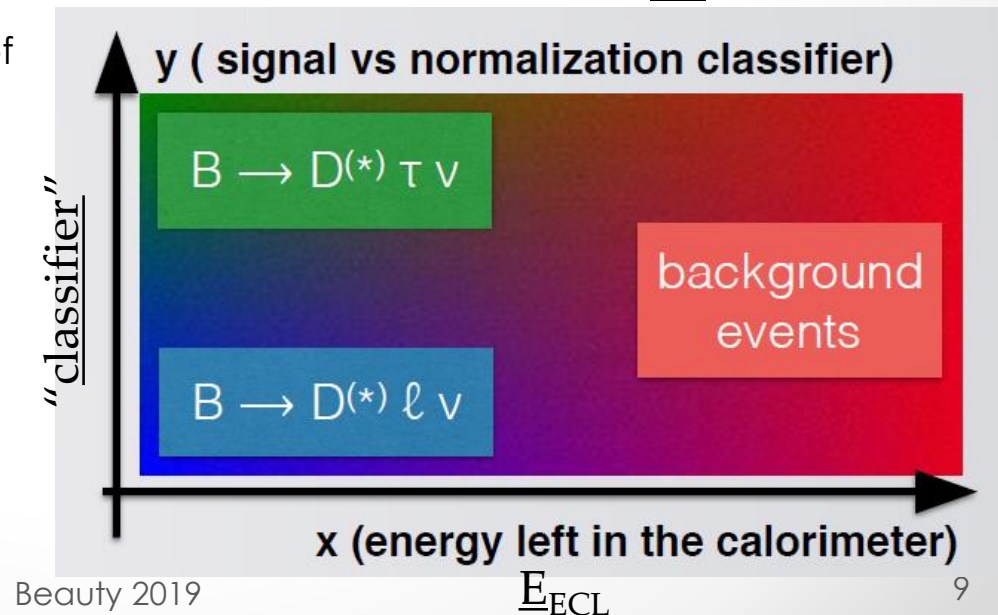
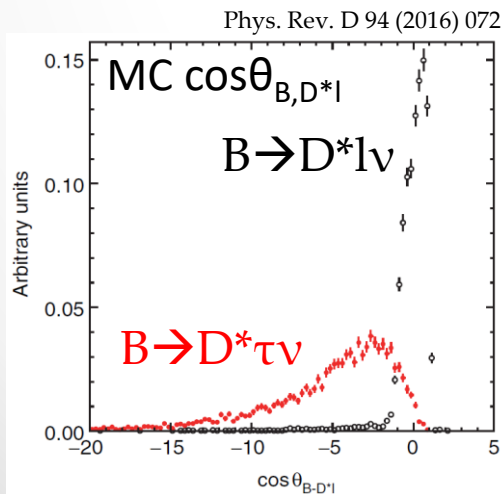
- Multivariate analysis with Boosted-Decision Tree classifier

→ Better efficiency and enable to use more signal decay modes

- Both $R(D)$ and $R(D^{*})$ with both B^0 and $B^+ \rightarrow D^{*} \tau \nu$

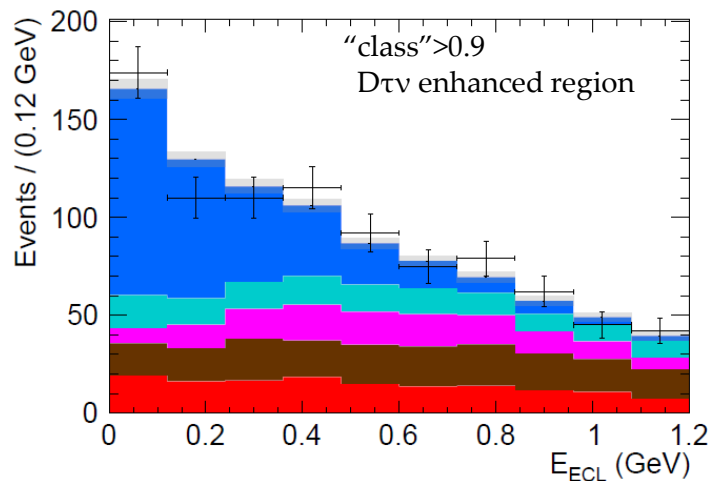
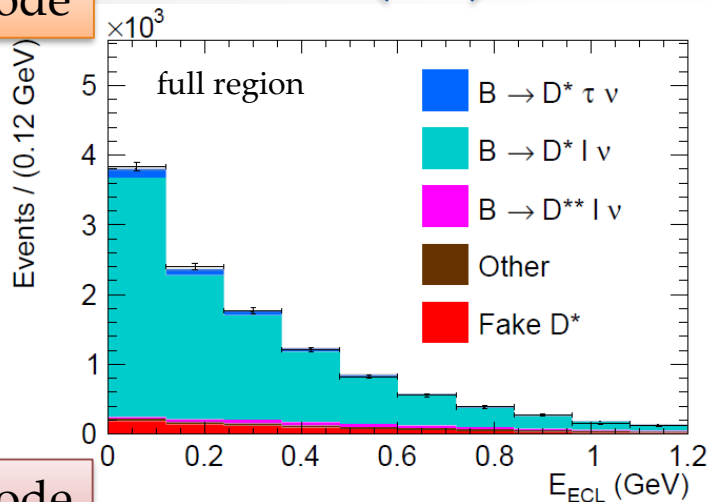
- 2D extended maximum-likelihood fit on “classifier” and E_{ECL}

Classifier: Boosted decision tree output of $\cos\theta_{B,D^{(*)}}$, M_{miss2} , E_{vis}

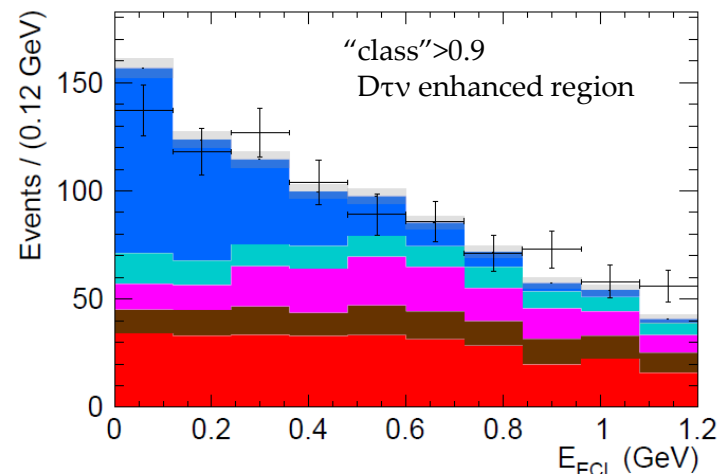
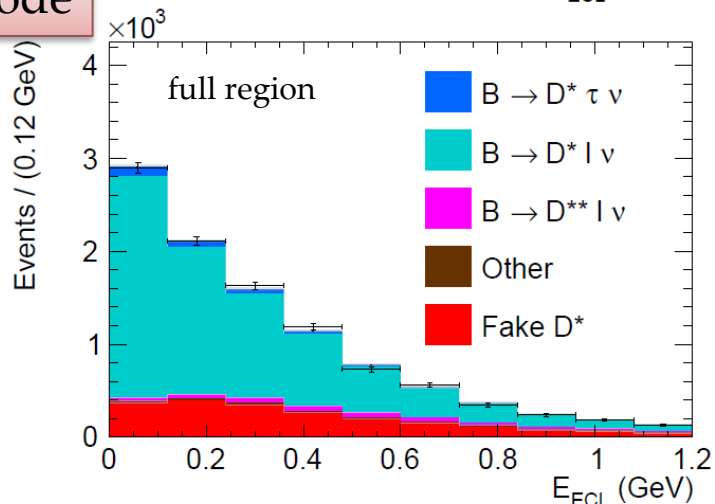


NewR(D) Semileptonic Tag Result

D^{*+1} mode



D^{*01} mode



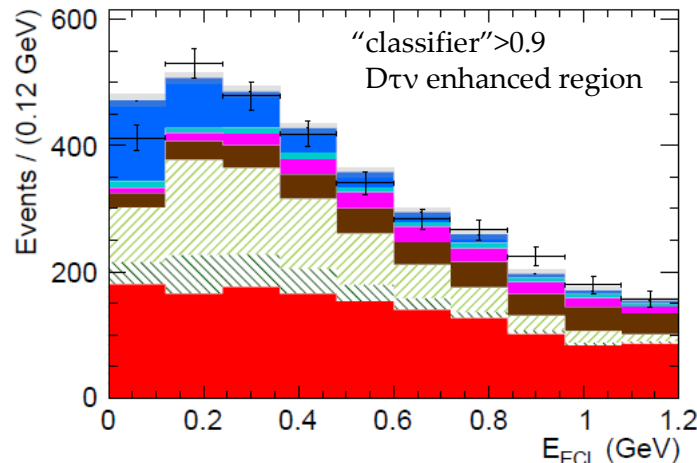
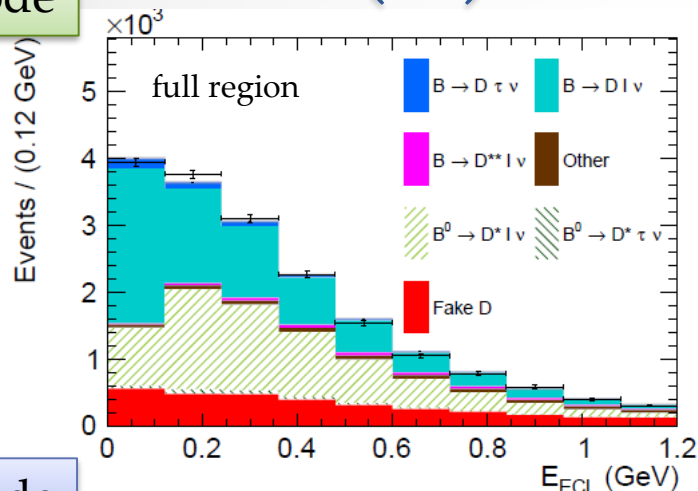
D ^{*+1} ℓ^-	$B \rightarrow D^{*+} \tau \nu$	376 ± 36
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preliminary

$$\mathcal{R}(D^*) = 0.283 \pm 0.018 \pm 0.014$$

NewR(D) Semileptonic Tag Result

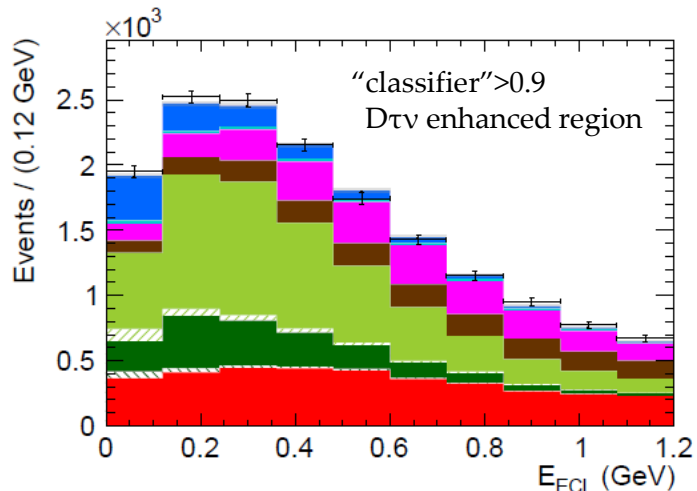
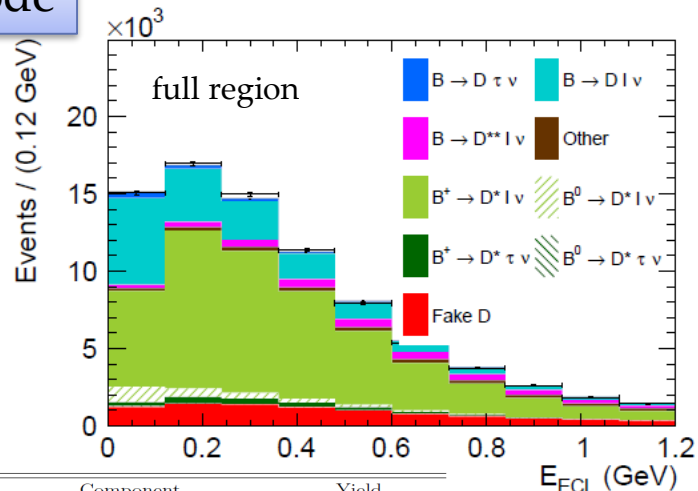
D⁺l mode



Signal

- B → D l ν
- B → D τ ν

D⁰l mode



Channel	Component	Yield
D ⁺ ℓ ⁻	B → Dτν	307 ± 65
	B → Dℓν	6800 ± 179
	B ⁰ → D*ℓν	6370 ± 225
	B ⁰ → D*τν	269 ± 24
	B → D**ℓν	413 ± 110
	Fake D	3072 ± 129 (Fixed)
	Other	506 ± 23 (Fixed)
	D ⁰ ℓ ⁻	B → Dτν
B → Dℓν		16096 ± 436
B ⁺ → D*ℓν		45042 ± 563
B ⁰ → D*ℓν		2302 ± 531
B ⁺ → D*τν		1704 ± 177
B ⁰ → D*τν		123 ± 11
B → D**ℓν		3595 ± 252
Fake D		8708 ± 418 (Fixed)
Other		2131 ± 83 (Fixed)

preliminary

$$\mathcal{R}(D) = 0.307 \pm 0.037 \pm 0.016$$

First R(D) measurement with Semileptonic tag

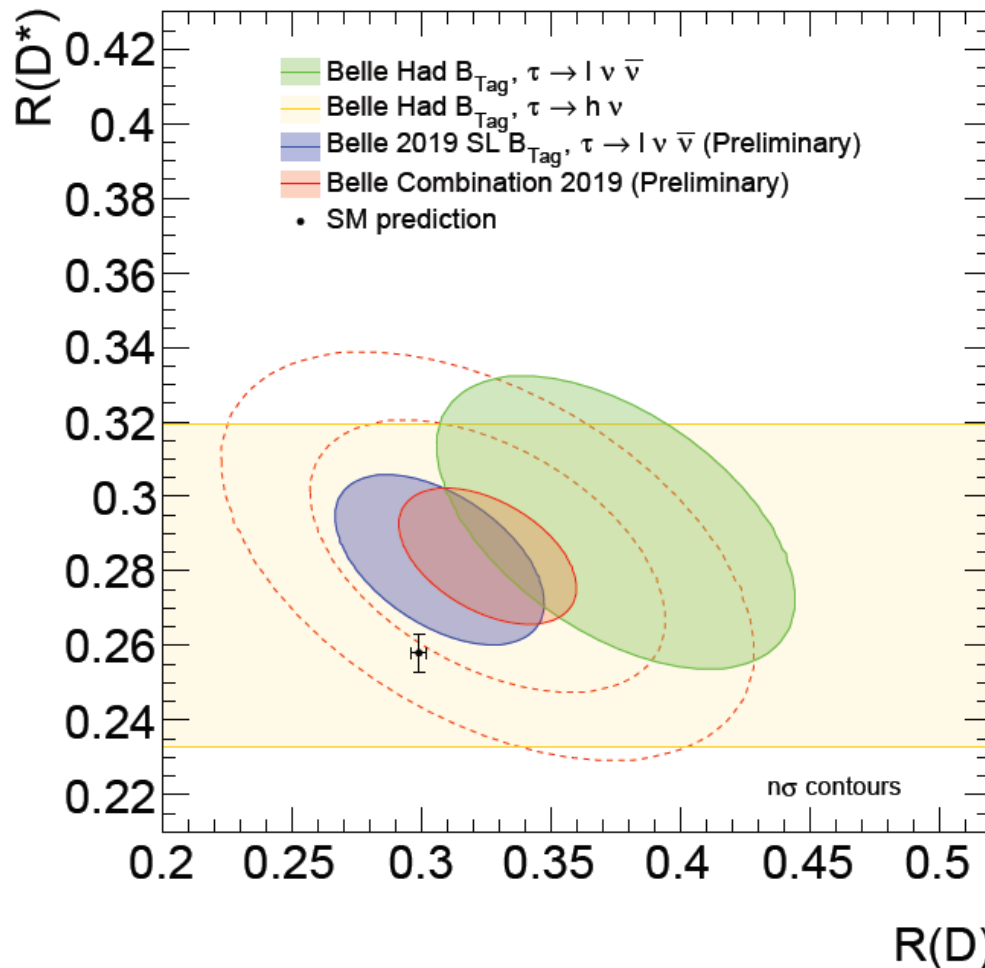
Belle $\mathcal{R}(D^{(*)})$ Results

New semileptonic tag (preliminary, [arXiv:1904.08794])

$$\mathcal{R}(D) = 0.307 \pm 0.037 \pm 0.016$$

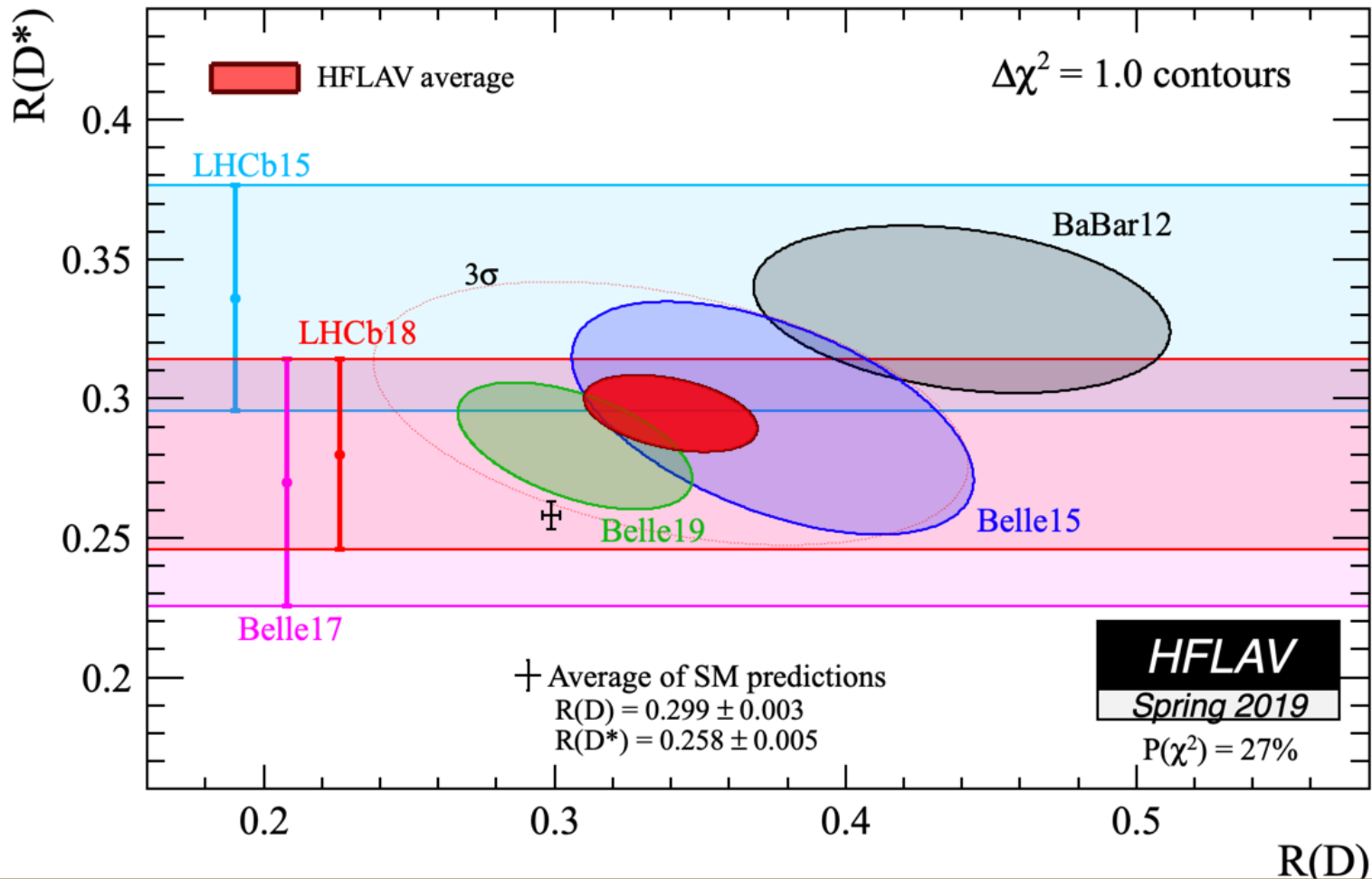
$$\mathcal{R}(D^*) = 0.283 \pm 0.018 \pm 0.014$$

New semileptonic tag results
consistent with SM in 1.2σ



Belle combined result
at about 2σ from SM

Latest R(D) and R(D*) Situation



Belle new semileptonic tag results are the most precise $R(D^{(*)})$ measurements

Deviation from SM reduced to 3.1σ

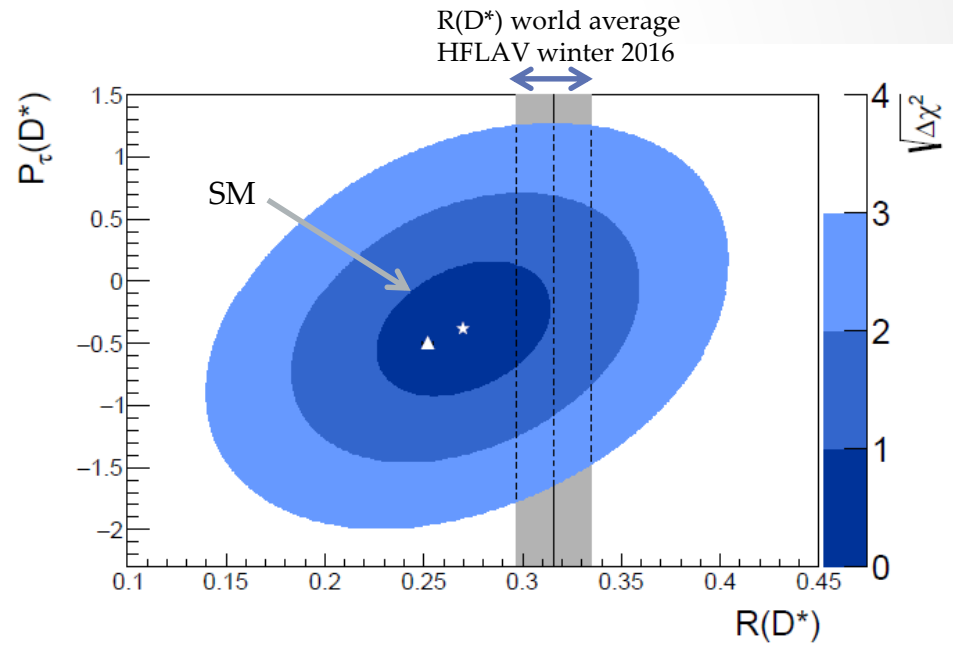
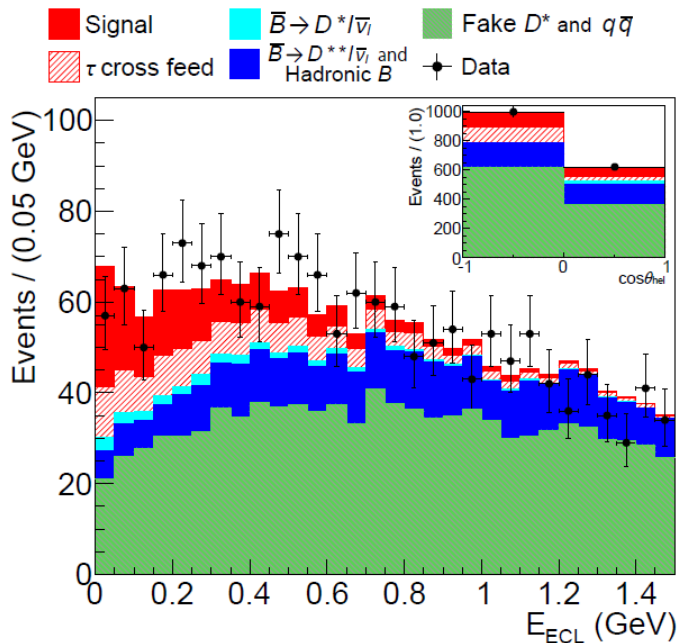
τ Polarization Measurement

- Hadronic tag
- Two body tau decays : $\tau \rightarrow \pi \nu, \rho \nu$
 - Helicity angle sensitive to the tau polarization
- $P_\tau(D^*)_{SM} = -0.497 \pm 0.013$
[Tanaka, Watanabe, PRD 87, 034028 (2013)]

[PRL118, 211801 (2017) PRD97, 012004 (2018)]

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{\text{hel}}} = \frac{1}{2} (1 + \alpha \cdot \mathcal{P}_\tau \cos \theta_{\text{hel}})$$

$$\alpha = \begin{cases} 1 & \text{for } \tau \rightarrow \pi^- \nu \\ 0.45 & \text{for } \tau \rightarrow \rho^- \nu \end{cases}$$

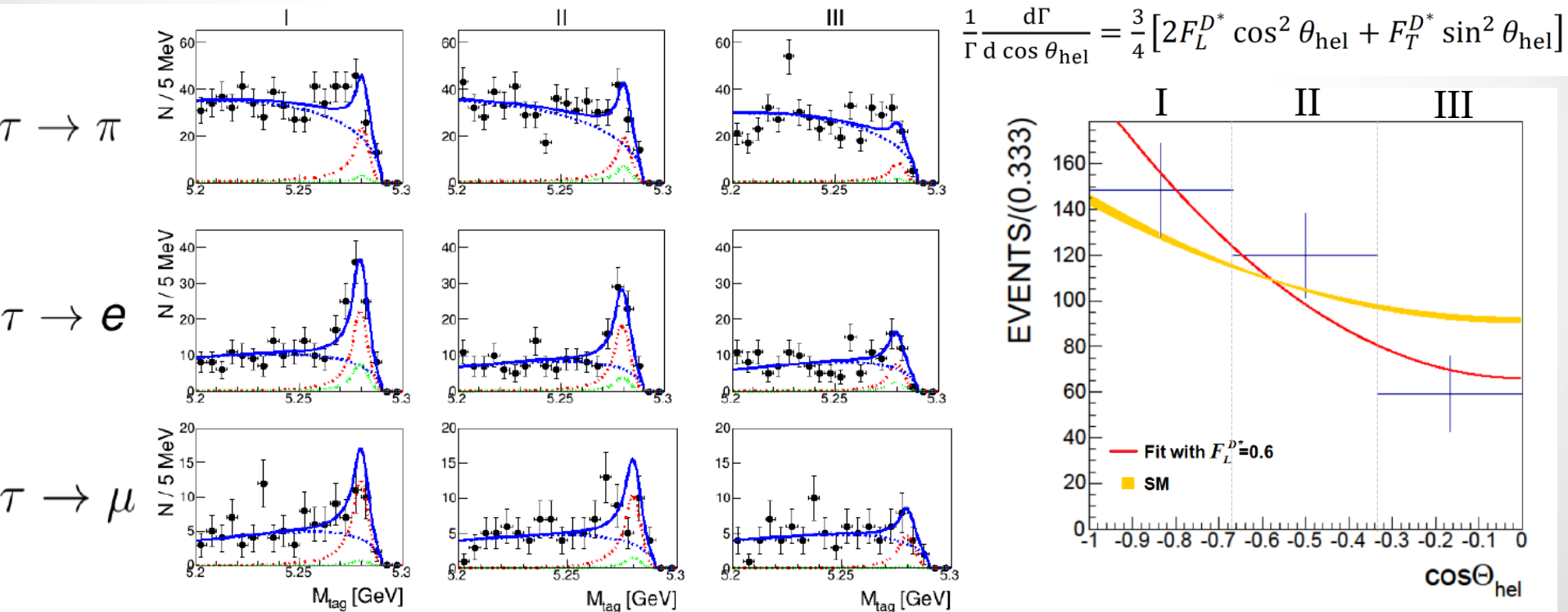


$$R(D^*) = 0.270 \pm 0.035(\text{stat})_{-0.025}^{+0.028}(\text{syst}),$$

$$P_\tau(D^*) = -0.38 \pm 0.51(\text{stat})_{-0.16}^{+0.21}(\text{syst}),$$

D* Polarization Measurement

- Reconstruct $B^0 \rightarrow D^* \tau \nu$
- Utilized **inclusive tag** method
- Extract signal yield in three $D^* \rightarrow D\pi$ helicity angle regions
- Fit the helicity angle distribution



$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{\text{hel}}} = \frac{3}{4} [2F_L^{D^*} \cos^2 \theta_{\text{hel}} + F_T^{D^*} \sin^2 \theta_{\text{hel}}]$$

preliminary

[arXiv:1903.03102]

$$F_L^{D^*} = 0.60 \pm 0.08(\text{stat}) \pm 0.04(\text{syst})$$

cf. in SM

$$- F_L^{D^*} = 0.46 \pm 0.03 \text{ [PRD95, 115038(2017)]}$$

$$- F_L^{D^*} = 0.441 \pm 0.006 \text{ [arXiv: 1808: 03565]}$$

within 2σ of SM

Summary

- $B \rightarrow D^{(*)} \tau \nu$ decays are good probes for New Physics
- Tension exists between measurements and SM

- New Belle Semileptonic tag $R(D)$ and $R(D^*)$ results:

$$\mathcal{R}(D) = 0.307 \pm 0.037 \pm 0.016 \quad (\text{preliminary})$$

$$\mathcal{R}(D^*) = 0.283 \pm 0.018 \pm 0.014 \quad \text{within } 1.2 \sigma \text{ from SM}$$

- First $R(D)$ measurement with Semileptonic tag
- Most precise $R(D)$ and $R(D^*)$ measurement
- τ and D^* polarizations are also measured at Belle
 - First D^* polarization measurement in $B^0 \rightarrow D^{*} \tau \nu$ decays

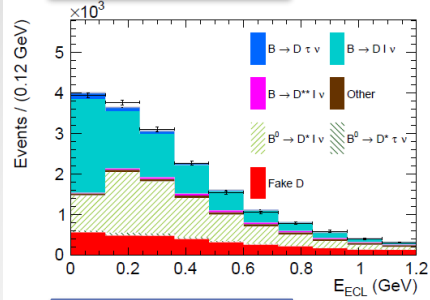
$$F_L^{D^*} = 0.60 \pm 0.08(\text{stat}) \pm 0.04(\text{syst}) \quad (\text{preliminary})$$

within 2σ from SM

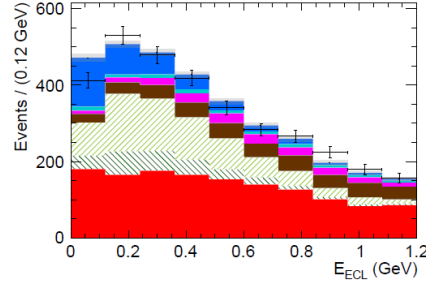
- Still there is large tension in $R(D)$ - $R(D^*)$
- Belle II has started \rightarrow More interesting results in future

New R(D) Semileptonic Tag Result

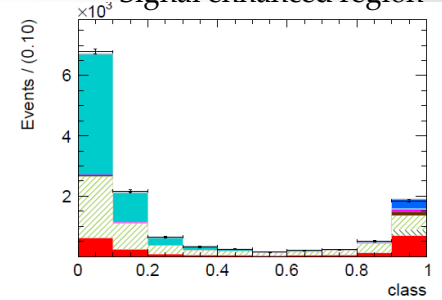
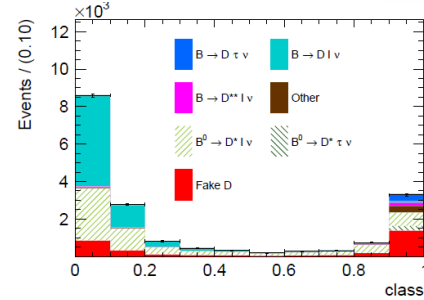
D⁺l mode



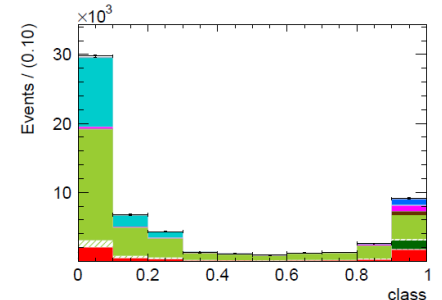
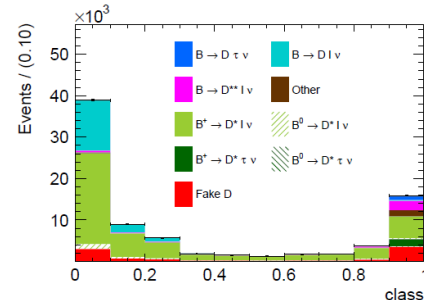
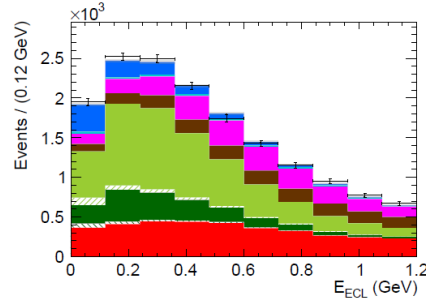
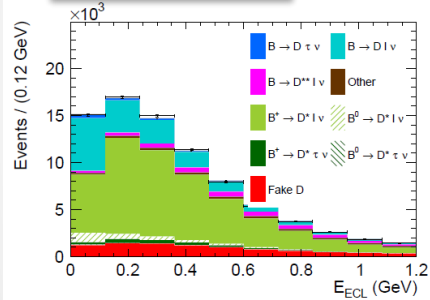
"class">0.9
Dτν enhanced region



E_{ECL} < 0.48 GeV
Signal enhanced region



D⁰l mode



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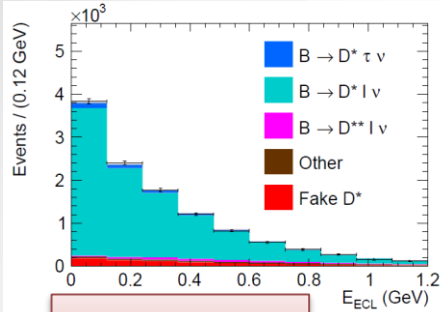
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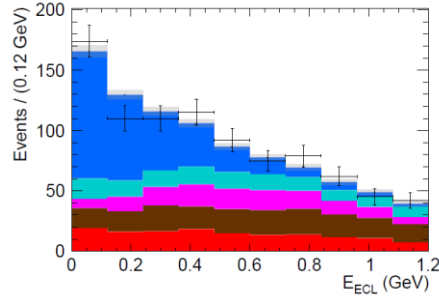
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New $R(D^*)$ Semileptonic Tag Result

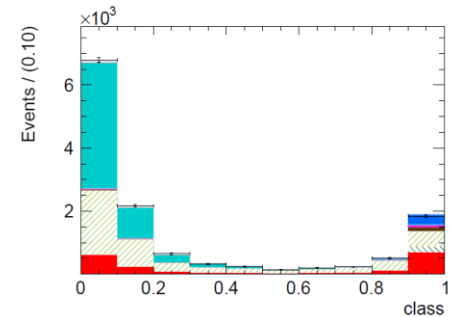
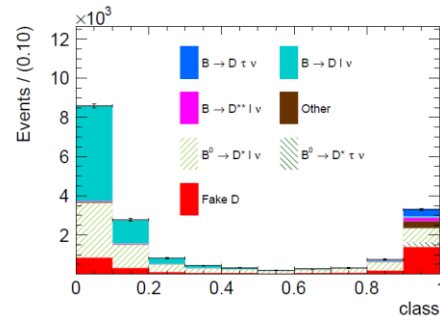
$D^{*+}l$ mode



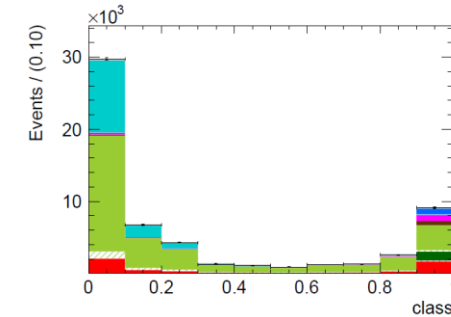
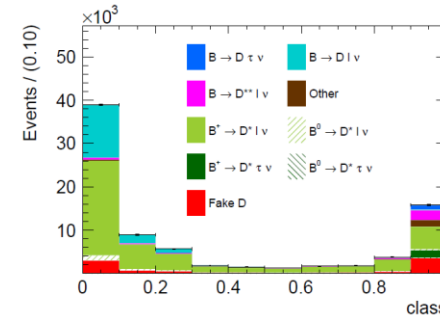
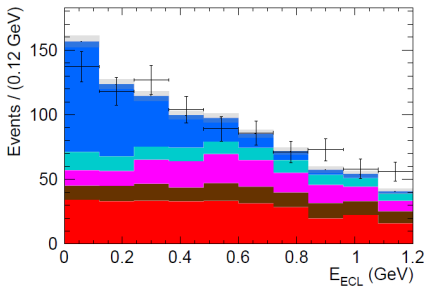
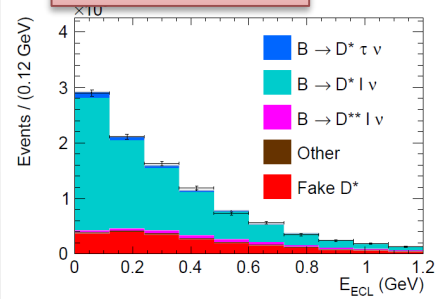
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 $D^{*+}\tau\nu$ enhanced region



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preliminary

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$\mathcal{R}(D^{(*)})$ Systematic Errors

TABLE I. Systematic uncertainties contributing to the $\mathcal{R}(D^{(*)})$ results.

Source	$\Delta R(D)$ (%)	$\Delta R(D^*)$ (%)
D^{**} composition	0.62	1.26
Fake $D^{(*)}$ calibration	0.18	0.10
B_{tag} calibration	0.06	0.04
Feed-down factors	1.52	0.37
Efficiency factors	1.73	3.60
Lepton efficiency and fake rate	0.33	0.28
Slow pion efficiency	0.07	0.07
MC statistics	3.94	1.92
B decay form factors	0.50	0.24
Luminosity	0.09	0.04
$\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)$	0.05	0.02
$\mathcal{B}(D)$	0.31	0.12
$\mathcal{B}(D^*)$	0.04	0.02
$\mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)$	0.13	0.12
Total	4.66	4.32

τ Hadronic decay: $R(D^*)$, τ Polarization

Systematic Errors

TABLE II. The systematic uncertainties in $R(D^*)$ and $P_\tau(D^*)$, where the values for $R(D^*)$ are relative errors. The group “common sources” identifies the common systematic uncertainty sources in the signal and the normalization modes, which cancel to a good extent in the ratio of these samples. The reason for the incomplete cancellation is described in the text.

Source	$R(D^*)$	$P_\tau(D^*)$
Hadronic B composition	+7.7% -6.9%	+0.134 -0.103
MC statistics for PDF shape	+4.0% -2.8%	+0.146 -0.108
Fake D^*	3.4%	0.018
$\bar{B} \rightarrow D^{**} \ell^- \bar{\nu}_\ell$	2.4%	0.048
$\bar{B} \rightarrow D^{**} \tau^- \bar{\nu}_\tau$	1.1%	0.001
$\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell$	2.3%	0.007
τ daughter and ℓ^- efficiency	1.9%	0.019
MC statistics for efficiency estimation	1.0%	0.019
$\mathcal{B}(\tau^- \rightarrow \pi^- \nu_\tau, \rho^- \nu_\tau)$	0.3%	0.002
$P_\tau(D^*)$ correction function	0.0%	0.010
Common sources		
Tagging efficiency correction	1.6%	0.018
D^* reconstruction	1.4%	0.006
Branching fractions of the D meson	0.8%	0.007
Number of $B\bar{B}$ and $\mathcal{B}(\Upsilon(4S) \rightarrow B^+ B^-$ or $B^0 \bar{B}^0)$	0.5%	0.006
Total systematic uncertainty	+10.4% -9.4%	+0.21 -0.16

D* Polarization Systematic Errors

TABLE I. Summary of systematic uncertainties

Source		$\Delta F_L^{D^*}$
Monte Carlo statistics	AR shape and peaking background	± 0.032
	CB shape	± 0.010
	Background scale factors	± 0.001
Background modeling	$B \rightarrow D^{**} \ell \nu$	± 0.003
	$B \rightarrow D^{**} \tau \nu$	± 0.011
	$B \rightarrow$ hadrons	± 0.005
	$B \rightarrow \bar{D}^* M$	± 0.004
Signal modeling	Form factors	± 0.002
	$\cos \theta_{\text{hel}}$ resolution	± 0.003
	Acceptance non-uniformity	+0.015 -0.005
Total		+0.039 -0.037