

## Direct *CP* Violation in *B* Decays Status and Prospects for Belle II

Pablo Goldenzweig

Flavour Physics with High-Luminosity Experiments MIAPP, Munich Oct. 24 - Nov. 18, 2016



### Outline



- Conditions for Direct *CPV*.
- $K\pi$ -puzzle:
  - Test-of-sum rule for  $B \to K\pi$ .
  - Extension to  $B \to K^*\pi$  and  $B \to K^{(*)}\rho$  systems.
  - Comparison with (N)NLO calculations.
- Triple product asymmetries in  $B \rightarrow VV$  decays.
- Large local *CP* asymmetries in 3-body final states.
- DCPV in  $B_s$  decays.
- Expectations from Belle II, both with increased data and detector improvements will be discussed throughout.

### Introduction



- Direct *CPV* is observed by comparing the decay rate of particles  $\Gamma(P \to f)$  and anti-particles  $\Gamma(\overline{P} \to \overline{f})$ , where f and  $\overline{f}$  are *CP*-conjugate final states.
- Stated simply, if

 $\Gamma(P \to f) \neq \Gamma(\overline{P} \to \overline{f}) \quad \Rightarrow \quad CP \text{ Violation in decay}$ 

We can express this as an asymmetry:

$$\mathcal{A}_{CP} = \frac{\Gamma(P \to f) - \Gamma(\overline{P} \to \overline{f})}{\Gamma(P \to f) + \Gamma(\overline{P} \to \overline{f})}$$
$$= \frac{|\overline{A}|^2 - |A|^2}{|\overline{A}|^2 + |A|^2} = \frac{2|a_1||a_2|\sin(\phi_1 - \phi_2)\sin(\delta_1 - \delta_2)}{|a_1|^2 + |a_2|^2 + |a_1||a_2|\cos(\phi_1 - \phi_2)\cos(\delta_1 - \delta_2)}$$

- To observe *CP*-violating effects by comparing  $\Gamma(P \to f)$  and  $\Gamma(\overline{P} \to \overline{f})$  we need:
  - A minimum of 2 amplitudes contributing to a given decay process.
  - Both *CP*-violating and non-*CP*-violating phases.

 $B \to K\pi$ 



Belle, Phys. Rev. D 87, 031103(R) (2013)



**Figure 17.4.4.** The dominant Tree-level (a) and Penguin-loop (b) Feynman diagrams in the two-body decays  $B \to K\pi$  and  $B \to \pi\pi$  (Lin, 2008).



 Measurements of DCPV in B<sup>+</sup> → K<sup>+</sup>π<sup>0</sup> found to be different than the same quantity in B<sup>0</sup> → K<sup>+</sup>π<sup>-</sup>, contrary to the naive expectation from the presence of electroweak penguin diagrams.

 $\mathcal{A}_{K^+\pi^0} - \mathcal{A}_{K^+\pi^-} = 0.112 \pm 0.027 \pm 0.007 \ (4\sigma)$ 

- The difference could be due to:
  - Neglected diagrams contributing to B<sup>±</sup> decays (theoretical uncertainty is still large).
  - Some unknown NP effect that violates isospin.
- $\Rightarrow In combination with other K\pi measurements and with the larger Belle II dataset, strong interaction effects can be controlled and the validity of the SM can be tested in a model-independent way.$

## Additional diagrams





Tree Penguin



 $\mathbf{C} = \text{color suppressed}$  $P_{EW}$  = electroweak penguin  $P_{EW}^{C}$  = color suppressed electroweak penguin  $\mathbf{A} =$ annihilation

### New Physics here?





- Enhancement of C is required C > T
  - $\Rightarrow$  breakdown of theory understanding
- Enhancement of  $P_{EW}$ 
  - $\Rightarrow$  would indicate new physics

Many theory papers trying to explain the data... C.-W.Chaing, et al., PRD 70, 034020

- Y.-Y.Charng, et al., PRD 71, 014036
- W.-S.Hou, et al., PRL 95, 141601
- S.Baek, et al., PRD 71, 057502
- S.Baek, et al., PLB 653, 249
- H.-n.Li,et al., PRD 72, 114005

P. Goldenzweig

## $B ightarrow K\pi$ : Test of sum rule



Test-of-sum (isospin) rule for NP nearly free of theoretical uncertainties, where the SM can be tested by measuring all observables:

$$\begin{split} I_{K\pi} &= \mathcal{A}_{K+\pi^-} + \mathcal{A}_{K0}_{\pi} + \frac{\mathcal{B}(K^0\pi^+)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K+\pi^0} \frac{\mathcal{B}(K^+\pi^0)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K0}_{\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)} \\ I_{K\pi} &= -0.270 \pm 0.132 \pm 0.060 \ (1.9\sigma) \end{split}$$

Isospin sum rule can be presented as a band in the  $\mathcal{A}_{K^0\pi^0}$  vs.  $\mathcal{A}_{K^0\pi^+}$  plane.



→ Most demanding measurement is  $K^0 \pi^0$  final state. With Belle II, the uncertainty on  $\mathcal{A}(B \to K^0 \pi^0)$  from time-dep. analyses is expected to reach ~ 4% ⇒ sufficient for NP studies.

P. Goldenzweig



### More data:

### Extrapolate Belle measurements to 5 and 50 $ab^{-1}$

• Systematic uncertainties scale primarily with integrated luminosity, with the exception of  $A_{CP}$  measurements of channels with  $K_S^0$ :

 $\Rightarrow$  asymmetry of K<sup>0</sup>/ $\overline{K}^0$  interactions in material ( $\sigma_{ired} \approx 0.2\%$ )

Phys. Rev. D 84, 111501 (2011)

- Ideally separate the reducible and irreducible systematic errors (unchanged throughout data accumulation) when extrapolating.
  - Few modes are systematically limited, so treat all syst. errors as redcible.
  - Apply scaling to all stat. and syst. errors to Belle results via:

$$\sigma_{Belle \ II} = \sqrt{(\sigma_{stat}^2 + \sigma_{syst}^2) \frac{\mathcal{L}_{Belle}}{\mathcal{L}_{BelleII}} + \sigma_{ired}^2}$$



### How will Belle II help to improve our measurements?

- Increase hermiticity.
- Increase  $K_S^0$  efficiency.
- Improve IP and secondary vertex resolution.
- Improve  $K/\pi$  separation.
- Improve  $\pi^0$  efficiency.
- Add PID in endcaps.
- Add μ ID in endcaps.



# $K/\pi$ Separation

Two RICH systems covering full momentum range

- Barrel: Time of Propagation (TOP) counter (16 modules)
- Forward Endcap: Aerogel Ring Imaging Cherenkov detector (ARICH)



	Belle PID (%)	Belle II PID (%)
Ave. K efficiency	88	94
$\pi$ fake rate	9	4





### $\Rightarrow$ Average K efficiency / $\pi$ fake rate improved: Fake rate decreases by $\approx 2.5$ for the same $\varepsilon$ .

P. Goldenzweig

Direct CPV in B Decays

# $\pi^0$ Reconstruction



Re-usage of Belle's CsI(TI) crystal calorimeter, but with new electronics with 2MHz wave form sampling to compensate for the larger beam-related backgrounds and the long decay time of CsI(TI) signals.  $\Rightarrow$  Resolution much better at Belle II



### REF LUIGIS TALK FOR KS, QR AND QQ SUP?

# Breakdown of the Systematic Errors in $K\pi$



Systematic errors on  $\mathcal{B}$  (in %):

- Most of the multiplicative errors, such as those due to tracking and PID are obtained from data control samples, and scale with luminosity.
- There is also room for improvement with the error due to  $\pi^0$  reconstruction, with more data, improved detector, and more sophisticated methods.

Source	$K^+\pi^-$	$K^+\pi^0$	$K^0\pi^+$	$K^0\pi^0$
Tracking	0.70	0.35	0.35	
PID	1.65	0.78	0.86	
R > 0.2	0.55	0.59	0.80	1.04
MC statistics	0.16	0.18	0.19	0.23
$N_{B\bar{B}}$	1.37	1.37	1.37	1.37
$\pi^0$		4.0		4.0
$K_S^0$			1.68	1.68
Signal PDF	0.28	0.43	0.18	1.80
Feed-across	0.49	0.42	0.18	
Fit bias	0.45			
PHOTOS	1.20		1.20	
Charmless $B$	1.25	0.35	0.97	0.51

Belle, Phys. Rev. D 87, 031103(R) (2013)

- For the systematic error on  $A_{CP}$ , fit PDF and detector bias due to tracking acceptance and PID selection will improve.
- Improvements to K<sub>s</sub> reconstrction (ε: 86.9%→ 93.6%), signal & tag-side vertex resolution, flavour tagging (ε: 29%→ 32%). (See talk by Luigi Li Gioi)
- Ongoing studies with deep neural networks for flavor tagging and continuum suppression are showing great promise.



### Complete set of measurements from Belle and BaBar.

	$\mathcal{B}(10^{-6})$				
Mode	BABAR	Belle	LHCb		
$K^+\pi^-$	$19.1\pm0.6\pm0.6$	$20.0 \pm 0.34 \pm 0.60$			
$K^+\pi^0$	$13.6 \pm 0.6 \pm 0.7$	$12.62 \pm 0.31 \pm 0.56$			
$K^0\pi^+$	$23.9 \pm 1.1 \pm 1.0$	$23.97 \pm 0.53 \pm 0.71$			
$K^0\pi^0$	$10.1\pm0.6\pm0.4$	$9.68 \pm 0.46 \pm 0.50$			

	$A_{CP}$					
Mode	BABAR	Belle	LHCb			
$K^+\pi^-$	$-0.107 \pm 0.016^{+0.006}_{-0.004}$	$-0.069 \pm 0.014 \pm 0.007$	$-0.080 \pm 0.007 \pm 0.003$			
$K^+\pi^0$	$0.030 \pm 0.039 \pm 0.010$	$0.043 \pm 0.024 \pm 0.002$				
$K^0\pi^+$	$-0.029 \pm 0.039 \pm 0.010$	$-0.011 \pm 0.021 \pm 0.006$	$-0.022\pm0.025\pm0.010$			
$K^0\pi^0$	$-0.13 \pm 0.13 \pm 0.03$	$0.14 \pm 0.13 \pm 0.06$				



## $B \to K \pi$ : Projections for Belle II

- Perform a 2D scan of  $\mathcal{A}_{K^0\pi^0}$  vs.  $I_{K\pi}$  for different Belle II scenarios.
- The only possible correlated errors for the  $A_{CP}$ measurements are caused by the detector bias, which is estimated with different methods for each channel.  $\Rightarrow$  Assume that the bias errors are not correlated.
- Additionaly the systematic uncertainties are conservatively provided and they are still smaller than the statistical errors.



Projections for the	$B \to K\pi$ is	ospin sum rule	parameter, $I_{K\pi}$ , at the	Belle measured	central value.
---------------------	-----------------	----------------	--------------------------------	----------------	----------------

Scenario	$\mathcal{A}_{K^0\pi^0}$			$I_{K\pi}$
	Value	Stat.	(Red., Irred.)	
Belle	0.14	0.13	(0.06, 0.02)	$-0.27\pm0.14$
Belle + $B \rightarrow K^0 \pi^0$ at Belle II 5 ab <sup>-1</sup>		0.05	(0.02, 0.02)	$-0.27\pm0.07$
Belle II 50 ab <sup>-1</sup>		0.01	(0.01, 0.02)	$-0.27\pm0.03$

# $K^*\pi$ and $K^{(*)}\rho$ systems



### Expect analogous sum rules by replacing:

$$\begin{split} K &\to K^* \\ I_{K^*\pi} &= \mathcal{A}_{K^{*+}\pi^-} + \mathcal{A}_{K^{*0}\pi^+} \frac{\mathcal{B}(K^{*0}\pi^+)}{\mathcal{B}(K^{*+}\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^{*+}\pi^0} \frac{\mathcal{B}(K^{*+}\pi^0)}{\mathcal{B}(K^{*+}\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^{*0}\pi^0} \frac{\mathcal{B}(K^{*0}\pi^0)}{\mathcal{B}(K^{*+}\pi^-)} \\ \pi &\to \rho \\ I_{K\rho} &= \mathcal{A}_{K^+\rho^-} + \mathcal{A}_{K^0\rho^+} \frac{\mathcal{B}(K^0\rho^+)}{\mathcal{B}(K^+\rho^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^+\rho^0} \frac{\mathcal{B}(K^+\rho^0)}{\mathcal{B}(K^+\rho^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^0\rho^0} \frac{\mathcal{B}(K^0\rho^0)}{\mathcal{B}(K^+\rho^-)} \end{split}$$

$$\begin{split} K &\to K^* \And \pi \to \rho \\ I_{K^*\rho} &= \mathcal{A}_{K^{*+}\rho^-} + \mathcal{A}_{K^{*0}\rho^+} \frac{\mathcal{B}(K^{*0}\rho^+)}{\mathcal{B}(K^{*+}\rho^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^{*+}\rho^0} \frac{\mathcal{B}(K^{*+}\rho^0)}{\mathcal{B}(K^{*+}\rho^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^{*0}\rho^0} \frac{\mathcal{B}(K^{*0}\rho^0)}{\mathcal{B}(K^{*+}\rho^-)} \frac{\mathcal{B}(K^{*0}\rho^0)}{\mathcal{B}(K^{*0}\rho^-)} \frac{\mathcal{B}(K^{*0}\rho^0)}{\mathcal{B}(K^{*0}\rho^-)} \frac{\mathcal{B}(K^{*0}\rho^0)}{\mathcal{B}(K^{*0}\rho^-)} \frac{\mathcal{B}(K^{*0}\rho^0)}{\mathcal{B}(K^{*0}\rho^-)} \frac{\mathcal{B}(K^{*0}\rho^-)}{\mathcal{B}(K^{*0}\rho^-)} \frac{\mathcal{B}(K^{*0}\rho^-)}{\mathcal{B}$$

For each set of decays<sup>1</sup>, perform a 2D scan of  $A_{CP}$  (for most limiting final state) vs. the isospin sum rule parameter.

 $\Rightarrow$  Compare with (N)NLO calculations<sup>2</sup>.

 $^{2}$ No NNLO calc. for VV system, as longitudinal  $A_{CP}$  fraction n/a for all final states.

P. Goldenzweig

<sup>&</sup>lt;sup>1</sup> For the PV & VV systems, BaBar  $\mathcal{B}$  and  $A_{CP}$  used for projections (Belle results n/a) - see BKUP slides.



#### Two-loop current-current operator contribution to the non-leptonic QCD penguin amplitude



#### G. Bell<sup>a</sup>, M. Beneke<sup>b</sup>, T. Huber<sup>c</sup>, Xin-Qiang Li<sup>d,e,\*</sup>

\* Rudolf Peierls Centre for Theoretical Physics, University of Oxford, J Keble Road, Oxford OKT 3NP, United Kingdom

<sup>b</sup> Physik Department T31, Technische Universität Mänchen, James-Franck-Straße 1, D-85748 Garching, Germany

\* Theoretische Physik I, Naturwissenschaftlich-Technische Fakultät, Untversität Siegen, Walter-Hew-Strasse 3, D-57068 Siegen, Germany

<sup>4</sup> Institute of Particle Physics and Key Laboratory of Quark and Lepton Physics (MOE), Central China Normal University, Wuhan, Hubel 430079, PR China

\* State Key Laboratory of Theoretical Physics, Institute of Theoretical Physics, Chinese Academy of Sciences, Beijing 100190, PR China

A R T I C L E I N F O Article history: Received 17 July 2015 Accepted 15 September 2015 Available online 24 September 2015

#### BSTRACT

The computation of direct CP asymmetries in charmless I decays at next-to-next-to-leading order (NNLO) in QCD is of interest to assortable the short-distance contribution. Here we compute the two-loop perguinal contractions of the current -current operators  $Q_{1,2}$  and provide a first estimate of NNLO CP asymmetries in meaning-dominated  $b \rightarrow s$  transitions.

 $^{6}$  2015 The Authors, Published by Elbevier IIX. This is an open access article under the CC IP (knows (http://crathwors/mglkenesr/ly/4/0)). Funded by SCOMP.  $(M, M, (n, ib) = im^{2} \int e^{MM} (m) \int_{-\infty}^{1} dm e^{-m(m)} e^{-m(m)} dm$ 

#### 1. Introduction

Bon-leptonic exclusive decays of 2 mesons play a crucial inde in indusing the COM mechanism of quark favore mrising and in quantifying the phenomenon of Q violation, Berec C violation is and arises if the decay simplifies its compared of at least the partial amplitudes with different re-scattering (throng) phases, which are multiple of Q different COM natareties including the CPviolating phase can be obtained from combining different decay modes, whose partial amplitudes are related by the approximate descrimed from the data methods and a set of the decay of the descrimed from the data.

The direct computation of the partial amplitudes is a complicated strong interaction problem, which can, however, be aldressed in the heavy-quark limit. The QCD factorization approach [2-4] employs arch-collinear factorization in this limit to express the hadronic matrix elements in terms of form factors and comouloss of perturbative objects (hard-scattering kernels) with nonperturbative light-cone distribution amplitudes (LCDAs). At leading order in A/ms.

+ 
$$(M_1 \leftrightarrow M_2)$$
  
+  $\int_0^{\infty} d\omega \int_0^{1} du dv T_1^{\mu}(\omega, v, u) \hat{f}_0 \phi_{\mathcal{B}}(\omega)$   
×  $f_{M_1} \phi_{M_1}(v) f_{M_2} \phi_{M_2}(u)$ .

where Q<sub>1</sub> is a generic operator from the effective work limitionmian. At this offer the re-starting phases are generated at the scale n<sub>1</sub> ox<sub>0</sub>, and reside in the loop corrections to the hardscattering levents, behaves are therefored or dorter c<sub>1</sub>, n<sub>0</sub>, solar tions to the scature given the loading order c<sub>1</sub>, n<sub>0</sub>, solar tions to the scattering bareness behaves are therefored or dorter c<sub>1</sub>, n<sub>0</sub>, solar to the direct C2 asymptotics to show whether the sharedistance or long-distance contribution dominates in particles, incomspant (rom being parametrically small, beth could be numerically of similar size.

The short-distance contribution to the direct CP asymmetries is fully known only to the first non-vanishing order (that is,  $O(\alpha_1)$ ) through the one-loop computations of the vertex kernels  $T_1^2$  performed long age [2.4.5]. A reliable result presumably requires the next-to-next-to-leading order  $O(\alpha_1^2)$  hard-scattering kernels,  $\pi_1^2$ least their imaginary parts. For the spectator-scattering kernels  $T_1^2$ 

Corresponding author at: Institute of Particle Physics and Key Laboratory of Quark and Lepten Physics (MOE), Central China Normal University, Wuhan, Hubei 430079, PK China.

E-mail address: xqli@itp.ac.cn (X,-Q, Li)



#### Two-loop current-current operator contribution to the non-leptonic OCD penguin amplitude

#### G. Bell<sup>a</sup>, M. Beneke<sup>b</sup>, T. Huber<sup>c</sup>, Xin-Oiang Li<sup>d,e,\*</sup>

\* Rudolf Peierls Centre for Theoretical Physics, University of Oxford, J Keble Road, Oxford OKT 3NP, United Kingdom

<sup>b</sup> Physik Department T31, Technische Universität München, James-Franck-Straße 1, D-85748 Garching, Germany

<sup>4</sup> Institute of Particle Physics and Key Laboratory of Quark and Letton Physics (MOE), Central Oring Normal University, Wykun, Hubei 430079, PR Oring State Key Laboratory of Theoretical Physics, Institute of Theoretical Physics, Chinese Academy of Sciences, Beiling 100150, PR China

ARTICLE INFO Received 17 July 2015 Accepted 15 September 2015 Available online 24 September 2015

The computation of direct CP asymmetries in charmless 8 decays at next-to-next-to-leading order (NNLO) in QCD is of interest to ascertain the short-distance contribution. Here we compute the two-loop penguin contractions of the current-current operators Q in and provide a first estimate of NNLO CP asymmetries in penguin-dominated  $b \rightarrow s$  transitions.

(M-M-I)

© 2015 The Authors, Published by Elsevier B.V. This is an onen access article under the CC BY license [http://creativecommons.org/licenses/by/4.0/], Funded by SCOAP3,

#### 1. Introduction

Non-leptonic exclusive decays of B mesons play a crucial role in studying the CKM mechanism of quark flavour mixing and in quantifying the phenomenon of CP violation. Direct CP violation is related to the rate difference of  $B \rightarrow f$  decay and its CP-conjugate and arises if the decay amplitude is composed of at least two nartial amplitudes with different re-scattering ("strong") phases. which are multiplied by different CKM matrix elements. Very often useful information on the CKM narameters including the CPviolating phase can be obtained from combining different decay modes, whose partial amplitudes are related by the approximate flavour symmetries of the strong interaction [1], which are then determined from data.

The direct computation of the partial amplitudes is a complicated strong interaction problem, which can, however, be addressed in the heavy-quark limit. The OCD factorization approach [2-4] employs soft-collinear factorization in this limit to express the hadronic matrix elements in terms of form factors and convolutions of perturbative objects (hard-scattering kernels) with nonperturbative light-cone distribution amplitudes (LCDAs). At leading order in A/ma.

$$\begin{aligned} Q_l(\vec{B}) &= im_B^2 \left\{ f_{\pm}^{(M)}(0) \int_0^l du \ T_l^l(u) \ f_{M_0} \phi_{M_1}(u) \right. \\ &+ (M_1 \leftrightarrow M_2) \\ &+ \int_0^{\infty} d\omega \int_0^l du du \ T_l^{(0)}(\omega, v, u) \ f_{B} \phi_B(\omega) \\ &\times f_{M_1} \phi_{M_1}(v) \ f_{M_2} \phi_{M_2}(u) \right\}. \end{aligned}$$

where Q<sub>1</sub> is a generic operator from the effective weak Hamiltonian. At this order the re-scattering phases are generated at the scale m<sub>b</sub> only, and reside in the loop corrections to the hardscattering kernels. Beyond the leading order factorization does not hold, and re-scattering occurs at all scales. The leading contributions to the strong phases are therefore of order  $\alpha_{*}(m_{*})$  orland  $\Lambda/m_h$ , it is of paramount importance for the predictivity of the approach for the direct CP asymmetries to know whether the shortdistance or long-distance contribution dominates in practice, since apart from being parametrically small, both could be numerically of similar size.

The short-distance contribution to the direct CP asymmetries is fully known only to the first non-vanishing order (that is,  $O(\alpha_5)$ ) through the one-loop computations of the vertex kernels T<sub>1</sub> performed long ago [2,4,5]. A reliable result presumably requires the next-to-next-to-leading order  $O(\alpha^2)$  hard-scattering kernels, at least their imaginary parts. For the spectator-scattering kernels T<sup>R</sup>

For table on next slide:

- The  $A_{CP}$  and isospin identity parameters listed in the Exp. (WA) column are taken from HFAG 2014 results (arXiv:1412.7515).
- However, the B2 fit projections were computed with results from *a single* experiment:  $K\pi$  Belle;  $K^*\pi \& K\rho$ BaBar.
- The results of the GammaCombo fits are added in the last column. Also shown are the  $A_{CP}$  input used in the 2D fit ( $A_{CP}$  vs  $I_x$ ).
- The results of projecting to 5 and 50  $ab^{-1}$  are shown in ().

<sup>\*</sup> Corresponding author at: Institute of Particle Physics and Key Laboratory of Quark and Lepton Physics (MOE), Central China Normal University, Wuhan, Hubei

E-mail address: soli@itn.ac.cn (X-Q. Li)

### Comparison w/theory (Modified Table I)



f	NLO	NNLO	NNLO + LD	Exp (WA)	Exp (GC fit and B2 proj.)
$\pi^- \bar{K}^0$	$_{0.71+0.13+0.21}_{-0.14-0.19}$	$_{0.77+0.14+0.23}_{-0.15-0.22}$	$_{0.10}\substack{+0.02\\-0.02}\substack{+1.24\\-0.27}$	$-1.7 \pm 1.6$	Belle input
$\pi^{0} K^{-}$	$9.42  {}^{+1.77  +1.87}_{-1.76  -1.88}$	$10.18  {+1.91  +2.03 \atop -1.90  -2.62}$	$-1.17  {}^{+0.22}_{-0.22}  {}^{+20.00}_{-6.62}$	$4.0\pm2.1$	
$\pi^+ K^-$	$7.25 {}^{+1.36}_{-1.36} {}^{+2.13}_{-2.58}$	$8.08 {}^{+1.52}_{-1.51} {}^{+2.52}_{-2.65}$	$-3.23  {}^{+0.61}_{-0.61} {}^{+19.17}_{-3.36}$	$-8.2\pm0.6$	
$\pi^0 \bar{K}^0$	$-4.27_{-0.77}^{+0.83}_{-2.23}^{+1.48}$	$-4.33_{-0.78}^{+0.84}_{-2.32}^{+3.29}$	$^{-1.41}_{-0.25}\substack{+0.27\\-5.54\\-0.25}_{-6.10}$	$1 \pm 10$	$-14 \pm 13$
$\Delta A_{CP}$	$\scriptstyle 2.17  {+0.40  +1.39} \\ \scriptstyle -0.40  -0.74$	$_{2.10+0.39+1.40}_{-0.39-2.86}$	$\scriptstyle{2.07+0.39+2.76\\-0.39-4.55}$	$12.2\pm2.2$	
$I_{K\pi}$	$-1.15  {}^{+0.21}_{-0.22}  {}^{+0.55}_{-0.84}$	$-0.88 \substack{+0.16 + 1.31 \\ -0.17 - 0.91}$	$-0.48 {}^{+0.09}_{-0.09} {}^{+1.09}_{-1.15}$	$-14 \pm 11$	$-27 \pm 14(7)(3)$
$\pi^- \bar{K}^{*0}$	$\substack{1.36 \\ -0.26 \\ -0.47} + 0.25 \\ -0.47 + 0.60 \\ -0.40 \\ -0.40 \\ -0.40 \\ -0.40 \\ -0.40 \\ -0.40 \\ -0.40 \\ -0.40$	$\substack{1.49 \\ -0.29 \\ -0.56} + 0.69$	$0.27 \substack{+0.05 + 3.18 \\ -0.05 - 0.67}$	$-3.8\pm4.2$	BaBar input
$\pi^{0} K^{*-}$	$13.85 \substack{+2.40 \\ -2.70 \\ -5.86}$	$18.16  {+3.11 + 7.79 \atop -3.52 - 10.57}$	$-15.81 \substack{+3.01 \\ -2.83 \\ -15.39} \substack{+3.01 \\ -2.83 \\ -15.39}$	$-6 \pm 24$	$-6 \pm 24$
$\pi^+ K^{*-}$	${}^{11.18}_{-2.15}{}^{+2.00}_{-10.62}{}^{+9.75}_{-10.62}$	${}^{19.70}_{-3.80}{}^{+3.37}_{-11.42}{}^{+10.54}_{-11.42}$	$-23.07_{-4.05}^{+4.35}_{-20.64}^{+86.20}$	$-23\pm6$	
$\pi^0 \bar{K}^{*0}$	$-17.23  {+3.33 + 7.59 \atop -3.00  -12.57}$	$^{-15.11}_{-2.65}\substack{+2.93\\-12.34}_{-10.64}$	$2.16 {}^{+0.39}_{-0.42} {}^{+17.53}_{-36.80}$	$-15\pm13$	
$\Delta A_{CP}$	$2.68  {}^{+0.72}_{-0.67} {}^{+5.44}_{-4.30}$	$^{-1.54}_{-0.58}\substack{+0.45+4.60\\-0.58-9.19}$	$7.26  {}^{+1.21}_{-1.34} {}^{+12.78}_{-20.65}$	$17\pm25$	
${}^{I}{}_{K^{\ast}\pi}$	$-7.18  {+1.38  +3.38 \atop -1.28  -5.35}$	$\substack{-3.45 \\ -0.59 \\ -4.95}$	$^{-1.02}_{-0.18}\substack{+0.19\\-0.18}\substack{+4.32\\-7.86}$	$-5 \pm 45$	$69 \pm 32(15)(6)$
$\rho^- \bar{K}^0$	$_{0.38}\substack{+0.07}_{-0.07}\substack{+0.16\\-0.27}$	$_{0.22}^{+0.04}\substack{+0.19\\-0.04}\limits_{-0.17}$	$_{0.30}\substack{+0.06\\-0.06}\substack{+2.28\\-2.39}$	$-12 \pm 17$	BaBar input
$\rho^{0} K^{-}$	$-19.31_{-3.61}^{+3.42}_{-8.96}^{+13.95}$	$-4.17  {}^{+0.75  +19.26}_{-0.80  -19.52}$	$43.73 {}^{+7.07}_{-7.62} {}^{+44.00}_{-137.77}$	$37 \pm 11$	
$\rho^+ K^-$	$-5.13  {}^{+0.95}_{-0.97} {}^{+6.38}_{-4.02}$	$\substack{1.50 \\ -0.27 \\ -10.36}$	$25.93 \substack{+4.43 \\ -4.90 \\ -75.63} \substack{+25.40 \\ -75.63}$	$20 \pm 11$	
$\rho^0 \bar{K}^0$	$8.63  {}^{+1.59}_{-1.65}  {}^{+2.31}_{-1.69}$	$8.99 {}^{+1.66}_{-1.71} {}^{+3.60}_{-7.44}$	$-0.42 {}^{+0.08}_{-0.08} {}^{+19.49}_{-8.78}$	$6 \pm 20$	$5\pm26$
$\Delta A_{CP}$	$-14.17 {+2.80}_{-2.96} {+7.98}_{-5.39}$	$-5.67  {}^{+0.96}_{-1.01}  {}^{+10.86}_{-9.79}$	${}^{17.80}_{-3.01}{}^{+3.15}_{-62.44}{}^{+19.51}_{-10}$	$17\pm16$	
$I_{K\rho}$	$-8.75_{-1.66}^{+1.62}_{-6.48}^{+4.78}$	$-10.84  {+1.98  {+11.67} \atop -2.09  {-9.09} }$	$-2.43 \substack{+0.46 + 4.60 \\ -0.42 - 19.43}$	$-37\pm37$	$-44 \pm 49(25)(11)$

P. Goldenzweig





Uncertainty much improved in  $K\pi$  but still too large in  $K^*\pi$  and  $K^{(*)}\rho$  systems to be conclusive.

P. Goldenzweig

8.11.2016 18 / 35

## $B \to VV$



- Decays to spin-1 final states with pairs formed from ω, K\*, ρ, and φ can be used to determine the helicity amplitudes of the decay.
- Channels have low  $\mathcal{B}$  and high background.

Full angular analysis requires large statistics (e.g.,  $B^0 \rightarrow \phi K^{*0}$ ). With the current datasets most analysis are limited to integrating over the angle between the decay planes  $\Phi$ , and reporting the longitudinal polarization fraction ( $f_L$ )

 $(1-f_L)\sin^2\theta_1\sin^2\theta_2 + 4f_L\cos^2\theta_1\cos^2\theta_2$ 



Highlights to seach for with more data include:

- Angular analysis of  $K^* \rho$  channels.
  - ⇒ Observation that there is an enhanced contribution proportional to electromagnetic penguins, which would be revealed in a polarisation analysis. hep-ph/0512258
- Contribution of electroweak penguins in the hierarchy of the decays to  $\omega K^{*0}$  and  $\omega \phi$ .
- Triple-product asymmetries, which provide a measure of *CP* violation that does not require flavor tagging or a time-dependent analysis.

Phys. Rev. D 84, 096013 (2011)



Full angular analysis and search for DCPV in  $B^0 \rightarrow \phi K^{*0}$ .

- At Belle/BaBar full angular analysis limited to low-background decays such as B<sup>0</sup> → φK<sup>\*0</sup>.
- In the final Belle analysis, a 9D extended unbinned ML fit is used to extract the 26 parameters related to polarization and CPV.
- Figure shows projections onto 6 of the 9 fitted observables.
- All phase ambiguities have been resolved and all parameters related to *CP* violation are consistent with 0.
- $\Rightarrow Belle II's large dataset is needed to perform$ full angular analyses on many other $<math>B \rightarrow VV$  channels.

### Belle, Phys. Rev. D 88, 072004 (2013)





### Statistics-limited for most quantities...

TABLE VII. Summary of the results on the  $B^0 \rightarrow \phi K^*$  system. See Table II and Eq. (32) for the parameter definition. In this table, we give the fit fraction  $FF_J$  per partial wave instead of the branching fraction  $\mathcal{B}_J$ , which is given in Table VIII together with the yields per partial wave. The first error is statistical and the second is due to systematics.

Parameter	$\phi(K\pi)_0^* J = 0$	$\phi K^*(892)^0 J = 1$	$\phi K_2^*(1430)^0 J = 2$
FF <sub>J</sub>	$0.273 \pm 0.024 \pm 0.021$	$0.600 \pm 0.020 \pm 0.015$	$0.099^{+0.016}_{-0.012} \pm 0.018$
$f_{LJ}$		$0.499 \pm 0.030 \pm 0.018$	$0.918^{+0.029}_{-0.060}\pm0.012$
$f_{\perp J}$		$0.238 \pm 0.026 \pm 0.008$	$0.056^{+0.050}_{-0.035}\pm0.009$
$\phi_{\parallel J}$ (rad)		$2.23 \pm 0.10 \pm 0.02$	$3.76 \pm 2.88 \pm 1.32$
$\phi_{\perp J}$ (rad)		$2.37 \pm 0.10 \pm 0.04$	$4.45^{+0.43}_{-0.38}\pm0.13$
$\delta_{0J}$ (rad)		$2.91 \pm 0.10 \pm 0.08$	$3.53 \pm 0.11 \pm 0.19$
$\mathcal{A}_{CPJ}$	$0.093 \pm 0.094 \pm 0.017$	$-0.007 \pm 0.048 \pm 0.021$	$-0.155^{+0.152}_{-0.133}\pm0.033$
$\mathcal{A}^{0}_{CPJ}$		$-0.030\pm 0.061\pm 0.007$	$-0.016^{+0.066}_{-0.051}\pm0.008$
$\mathcal{A}_{CPJ}^{\perp}$		$-0.14 \pm 0.11 \pm 0.01$	$-0.01^{+0.85}_{-0.67}\pm0.09$
$\Delta \phi_{\parallel J}$ (rad)		$-0.02 \pm 0.10 \pm 0.01$	$-0.02 \pm 1.08 \pm 1.01$
$\Delta \phi_{\perp J}$ (rad)		$0.05 \pm 0.10 \pm 0.02$	$-0.19 \pm 0.42 \pm 0.11$
$\Delta \delta_{0J}$ (rad)		$0.08 \pm 0.10 \pm 0.01$	$0.06 \pm 0.11 \pm 0.02$

 $\Rightarrow$  Statistical errors  $\approx 7x$  smaller with 50 ab<sup>-1</sup> of Belle II data.

P. Goldenzweig

CPV in  $B \rightarrow 3h$ 



### Large CPV effects not associated with resonances $\Rightarrow$ QCD effects to be understood



⇒ Unidentified structure in the  $m_{K^+K^-}^2$  projection in  $KK\pi$  decays at < 1.5 GeV<sup>2</sup>/c<sup>4</sup>. Only present in the B<sup>+</sup> mass projection and gives rise to a large local CP asymmetry. [\*Updated measurement: arXiv: 1408.5373]

P. Goldenzweig

Direct CPV in B Decays



### **Direct CP violation in 3-body B**<sub>u.d</sub> decays

	Theory (%)	Expt (%)	
$\pi^+\pi^-\pi^-$	8.7 <sup>+1.7</sup> -1.9	5.8±1.4	
K+ K- K-	-7.1 <sup>+4.8</sup> -4.1	-3.6±0.8	Inclusive CP
K- π+ π-	2.7+0.7-0.8	2.5±0.9	asymmetries
K+ K- π-	-10.0+2.1	-12.3±2.2	
			_
$K^{-}K^{+}\pi^{0}$	-9.2 <sup>+0.0</sup> -0.0		
K-K⁺K <sub>s</sub>	-5.5 <sup>+1.5</sup> -1.1		- predictions
K⁻K <sub>s</sub> K <sub>s</sub>	3.5+0.3_0.2	4±5	prodictione
$K_S \pi^+ \pi^0$	0.64+0.07	7±5± <u>3</u> ±4	
		~	→BaBar
(π⁺ π⁻ π⁻) <sub>region I</sub>	22.5 <sup>+2.9</sup> -3.3	58.4±8.7	7
(K <sup>+</sup> K <sup>-</sup> K <sup>-</sup> ) <sub>region I</sub>	-17.7 <sup>+4.9</sup> -2.9	-22.6±2.2	not updated
(K <sup>-</sup> π <sup>+</sup> π <sup>-</sup> ) <sub>region I</sub>	<b>14.1</b> <sup>+13.9</sup> -11.7	67.8±8.5	yet by LHCb
(K <sup>+</sup> K <sup>-</sup> π <sup>-</sup> ) <sub>region I</sub>	-18.2 <sup>+1.8</sup> -1.8	-64.8±7.2	

See talk by Hai-Yang Cheng at first B2TIP workshop

# Enhancements in $M_{K^+K^-}$



• Enhancement observed by Belle in the  $M_{K^+K^-}$ invariant mass in  $B^0 \rightarrow K^+K^-\pi^0$  decays. V. Gaur *et al.*, (Belle Collaboration) Phys. Rev. D 87, 091101(R) (2013)

 BaBar observes a large enhancement due to a broad structure at low M<sub>K+K</sub><sup>−</sup> invariant mass in B<sup>+</sup> → K<sup>+</sup>K<sup>−</sup>π<sup>+</sup> decays, which accounts for half of the total events.

B. Aubert *et al.*, (BABAR Collaboration) Phys. Rev. Lett. **99**, 221801 (2007)



⇒ Detailed interpretation requires an amplitude analysis with higher statistics at Belle II.

# DCPV in $B_s$ Decays

- First measurment of  $A_{CP}$  in  $B_s$  decays by LHCb: Phys. Rev. Lett. 110, 221601 (2013)  $A_{CP}(B_s \rightarrow K^+\pi^-) =$  $0.27 \pm 0.04 \pm 0.01(6.5\sigma).$
- Allows for a stringent test of (Ref)  $\Delta = \frac{A_{CP}(B^0 \rightarrow K^+ \pi^-)}{A_{CP}(B_s \rightarrow K^- \pi^+)} + \frac{A_{CP}(B^0 \rightarrow K^- \pi^+)\tau_d}{A_{CP}(B_s \rightarrow K^+ \pi^-)\tau_s}$   $= -0.02 \pm 0.05 \pm 0.04$

No evidence for a deviation from 0 is observed.



At  $e^+e^-$ ,  $\Upsilon(5S)$  decays are well-suited for studying large multiplicity  $B_s$  decays due to the lower particle momenta, the almost 100% trigger  $\varepsilon$ , and the excellent  $\pi/K$  separation. First observation of  $B_s \to K^0 \overline{K}^0$  by Belle with 121fb<sup>-1</sup>: Phys. Rev. Lett. 116, 161801 (2016)





# Additional Highlights for Belle & LHCb





- $\Rightarrow expected to proceed dominantly via$  $b \rightarrow s penguin transitions as the b \rightarrow u$ transition is color-suppressed.
- Large direct *CP* asymmetry expected in:  $B^+ \rightarrow \eta \rho^+$   $B^+ \rightarrow \eta \pi^+$   $B^+ \rightarrow \eta' \pi^+$ 
  - ⇒ where the b → u and b → s amplitudes are of similar size to  $B^+ \rightarrow \eta K^+$ , which measured  $A_{CP} = -0.37 \pm 0.09$ .





• New insight into  $K\pi$  puzzle with  $A_{CP}(\mathcal{B} \to K^0\pi^0)$  reaching 3-4%? Surprises on the way from  $K^*\pi$  and  $K\rho$ ? Large errors in (N)NLO computations and current experimental results make comparison difficult. Large Belle II dataset required for enough precision to see differences with theory.

Full angular analysis and triple-product-asymmetries will become feasible in additional B → VV channels.
 More surprises on the way from angular analysis in b → s penguin decays, e.g., K\*ρ?

- Observation of large local  $A_{CP}$  in additional 3-body decays?  $B^0 \to K_S^0 K^+ K^-, B^0 \to K^+ K^- \pi^0 \dots$  New resonances in  $M_{K^+K^-}$  spectrum?
- Large improvements in PID  $(K/\pi \text{ separation}), \pi^0$  and  $K_s$ , reconstruction efficiency, tracking, algorithms and more. *Simulation studies showing increased performance as expected*.

BKUP



	$\mathcal{B}(10^{-6})$				
Mode	BABAR	Belle	LHCb		
$K^{*+}\pi^{-}$	$8.2 \pm 0.9$	$8.4 \pm 1.1^{+1.0}_{-0.9}$			
$K^{*+}\pi^0$	$8.2\pm1.5\pm1.1$				
$K^{*0}\pi^+$	$10.8\pm0.6^{+1.2}_{-1.4}$	$9.7 \pm 0.6^{+0.8}_{-0.9}$			
$K^{*0}\pi^{0}$	$3.3\pm0.5\pm0.4$	< 3.5			

	$A_{CP}$					
Mode	BABAR	Belle	LHCb			
$K^{*+}\pi^-$	$-0.24 \pm 0.07 \pm 0.02$	$-0.21 \pm 0.11 \pm 0.07$				
$K^{*+}\pi^0$	$-0.06 \pm 0.24 \pm 0.04$					
$K^{*0}\pi^+$	$0.032 \pm 0.052 \substack{+0.016 \\ -0.013}$	$-0.149 \pm 0.064 \pm 0.022$				
$K^{*0}\pi^0$	$-0.15 \pm 0.12 \pm 0.04$					

- $A_{K^{*+}\pi^{-}}$  measured by both Belle and BaBar with high precision.
- Most challenging mode  $K^{*+}\pi^0$ .<sup>3</sup>  $\mathcal{A}_{cp}(K^{*+}(K^+\pi^0)\pi^0)) = -0.06 \pm 0.24 \pm 0.04$

<sup>3</sup>Unpublished BaBar measurement not included [arXiv:1501.00705]:  $A_{cp}(K^{*+}(K_{\rm S}\pi^+)\pi^0)) = -0.52 \pm 0.14 \pm 0.04 \pm 0.04$ 

### $K^*\pi$ : Test of sum rule



- Calculate I<sub>K\*</sub> and projections for Belle II using BaBar's complete set of measurements.
- Given that A<sub>K\*+π0</sub> is not systematically limited, treat all errors as reducible for sensitivity study.
- $I_{K^*\pi}$  values result of GammaCombo fit.
- $\Rightarrow$  Large positive identity parameter  $I_{K^*\pi}$ .



Projections for the  $B \to K^*\pi$  isospin sum rule parameter,  $I_{K^*\pi}$ , at the BaBar measured central value.

Scenario	$\mathcal{A}_{K^{*+}\pi^0}$		$I_{K^*\pi}$
	Value	Stat.	
BaBar	-0.06	0.24	$0.69\pm0.32$
Belle II 5 ab <sup>-1</sup>			$0.69\pm0.15$
Belle II 50 $ab^{-1}$			$0.69\pm0.06$



$\mathcal{B}(10^{-6})$			
Mode	BABAR	Belle	
$K^+\rho^-$	$6.6\pm0.5\pm0.8$	$15.1^{+3.4+2.4}_{-3.3-2.6}$	
$K^+ \rho^0$	$3.56 \pm 0.45^{+0.57}_{-0.46}$	$3.89 \pm 0.47^{+0.43}_{-0.41}$	
$K^0 \rho^+$	$8.0^{+1.4}_{-1.3} \pm 0.6$		
$K^0  ho^0$	$4.4\pm0.7\pm0.3$	$6.1 \pm 1.0^{+1.1}_{-1.2}$	

A <sub>CP</sub>				
Mode	BABAR	Belle		
$K^+ \rho^-$	$0.20 \pm 0.09 \pm 0.08$	$0.22^{+0.22+0.06}_{-0.23-0.02}$		
$K^+ \rho^0$	$0.44 \pm 0.10^{+0.06}_{-0.14}$	$0.30 \pm 0.11^{+0.11}_{-0.05}$		
$K^0 \rho^+$	$-0.12\pm 0.17\pm 0.02$			
$K^0  ho^0$	$0.05 \pm 0.26 \pm 0.10 \pm 0.03$	$0.03^{+0.23}_{-0.24}\pm0.11\pm0.10$		

• Most limiting mode  $\mathcal{A}_{K^0\rho^0}$ .



## $K\rho$ : Test of sum rule

- Calculate I<sub>K</sub> and projections for Belle II using BaBar's complete set of measurements.
- Again, stat. limited so treat all syst. errors as reducible.
- $I_{K\rho}$  values result of GammaCombo fit.
- $\Rightarrow Large negative identity parameter I_{K\rho}.$ Same (different) sign as  $I_{K\pi}$  ( $I_{K^*\pi}$ ).



Projections for the  $B \to K\rho$  isospin sum rule parameter,  $I_{K\rho}$ , at the BaBar measured central value.

Scenario	$\mathcal{A}_{K^0\rho^0}$		$I_{K\rho}$		
	Value	Stat.			
BaBar Belle II 5 ab <sup>-1</sup> Belle II 50 ab <sup>-1</sup>	0.05	0.26	$-0.44 \pm 0.49$ $-0.44 \pm 0.25$ $-0.44 \pm 0.11$		

$$K^*
ho$$
: Status



For  $B \rightarrow VV$  decays, must separate out the longitudinal and transverse components:

- NNLO computation not possible for transverse amplitudes: power-suppressed and there is no QCD factorization theorem for them.
- For longitudinal component, comparison of NNLO computation to experiment not possible since A<sub>CP</sub> not available for individual helicity amplitudes in K<sup>\*+</sup>ρ<sup>-</sup>.
- NLO computation available for comparison.

$\mathcal{B}(10^{-6})$				
Mode	BABAR	Belle		
$K^{*+}\rho^{-}$	$10.3 \pm 2.3 \pm 1.3$			
$K^{*+}\rho^0$	$4.6\pm1.0\pm0.4$			
$K^{*0} ho^+$	$9.6\pm1.7\pm1.5$			
$K^{*0}\rho^0$	$5.1\pm0.6^{+0.6}_{-0.8}$	$2.1\substack{+0.8+0.9\\-0.7-0.5}$		

$A_{CP}$			
Mode	BABAR		
$K^{*+}\rho^{-}$	$0.21 \pm 0.15 \pm 0.02$		
$K^{*+}\rho^0$	$0.31 \pm 0.13 \pm 0.03$		
$K^{*0}\rho^+$	$-0.01 \pm 0.16 \pm 0.02$		
$K^{*0}\rho^0$	$-0.06 \pm 0.09 \pm 0.02$		

• Most limiting mode  $\mathcal{A}_{K^{*0}\rho^+}$ .



### Reducible

- The systematic uncertainties of the PDF parameters.
- Particle identification requirements.
- The possible CP violation effect in the accompanying B meson decays.
- Vertex resolution.
- $\Delta t$  resolution function parametrization.
- Tag-side interference.

### Irreducible

- Uncertainties in the interaction-point profile.
- Dependence on the vertex selection-criteria.
- The effect of detector misalignment.
- Possible bias in the  $\Delta Z$  determination.
- $K^{\pm} \pi^{\pm}, \pi^0$  detection efficiency.
- Uncertainty in branching fraction measurements.
- Asymmetry of charged particle detection efficiency (in A measurements).
- Vertex reconstruction uncertainty originating from the SVD mis-alignment (in S measurements)

## $B \rightarrow VV$ : $f_L$ @ Belle II

- Heirarchy of  $f_L$  observed with tree-dominated modes ( $\rho\rho$ ) near 1, and penguin-dominated modes ( $\phi K^{*0}$ ) near 0.5.
- Hierarchy based on the masses of the vector mesons, with larger masses having smaller  $f_L$ .
- $\Rightarrow$  Results from other channels necessary to understand these patterns.

Mode	BABAR	Belle Bel				Belle I	$I(\sigma_{total})$
			Ref.	$fb^{-1}$	$\sigma_{total}$	$5 \ ab^{-1}$	$50 \ ab^{-1}$
$\omega K^{*0}$	$0.72 \pm 0.14 \pm 0.02$	$0.56 \pm 0.29^{+0.18}_{-0.08}$	25	657	0.341	0.124	0.039
$\omega K_2^* (1430)^0$	$0.45 \pm 0.12 \pm 0.02$						
$K^{*0}\rho^{0}$	$0.40 \pm 0.08 \pm 0.11$						
$K^{*+}\rho^{-}$	$0.38 \pm 0.13 \pm 0.03$						
$\phi K^{*0}$	$0.494 \pm 0.034 \pm 0.013$	$0.499 \pm 0.030 \pm 0.018$	22	772	0.035	0.014	0.004
$K^{*0}\overline{K}^{*0}$	$0.80^{+0.10}_{-0.12} \pm 0.06$						
$\phi K_2^* (1430)^0$	$0.901^{+0.046}_{-0.058} \pm 0.037$						
$a_{1}^{\pm}a_{1}^{\mp}$	$0.31 \pm 0.22 \pm 0.10$						
Mode	BABAR	Belle Belle II			$(\sigma_{total})$		
		R	tef. f	$b^{-1}$	$\sigma_{total}$	$5 \ ab^{-1}$	$50 \ ab^{-1}$
$\omega K^{*+}$	$0.41 \pm 0.18 \pm 0.05$						
$\omega K_2^*(1430)^+$	$0.56 \pm 0.10 \pm 0.04$						
$\bar{K}^{*+}\rho^{0}$	$0.78 \pm 0.12 \pm 0.03$						
$K^{*0}\rho^{+}$	$0.52 \pm 0.10 \pm 0.04$	$0.43 \pm 0.11^{+0.05}_{-0.02}$	23	253	0.121	0.027	0.009
$K^{*+}\overline{K}^{*0}$	$0.75^{+0.16}_{-0.26} \pm 0.03$						
$\phi K^{*+}$	$0.49 \pm 0.05 \pm 0.03$	$0.52 \pm 0.08 \pm 0.03$	22 :	253	0.085	0.019	0.006
$\phi K_1(1270)^+$	$0.46^{+0.12+0.06}_{-0.13-0.07}$						
$\phi K_2^*(1430)^+$	$0.80^{+0.09}_{-0.10} \pm 0.03$						
$\omega \rho^+$	$0.90 \pm 0.05 \pm 0.03$						

