

Resonances in QCD

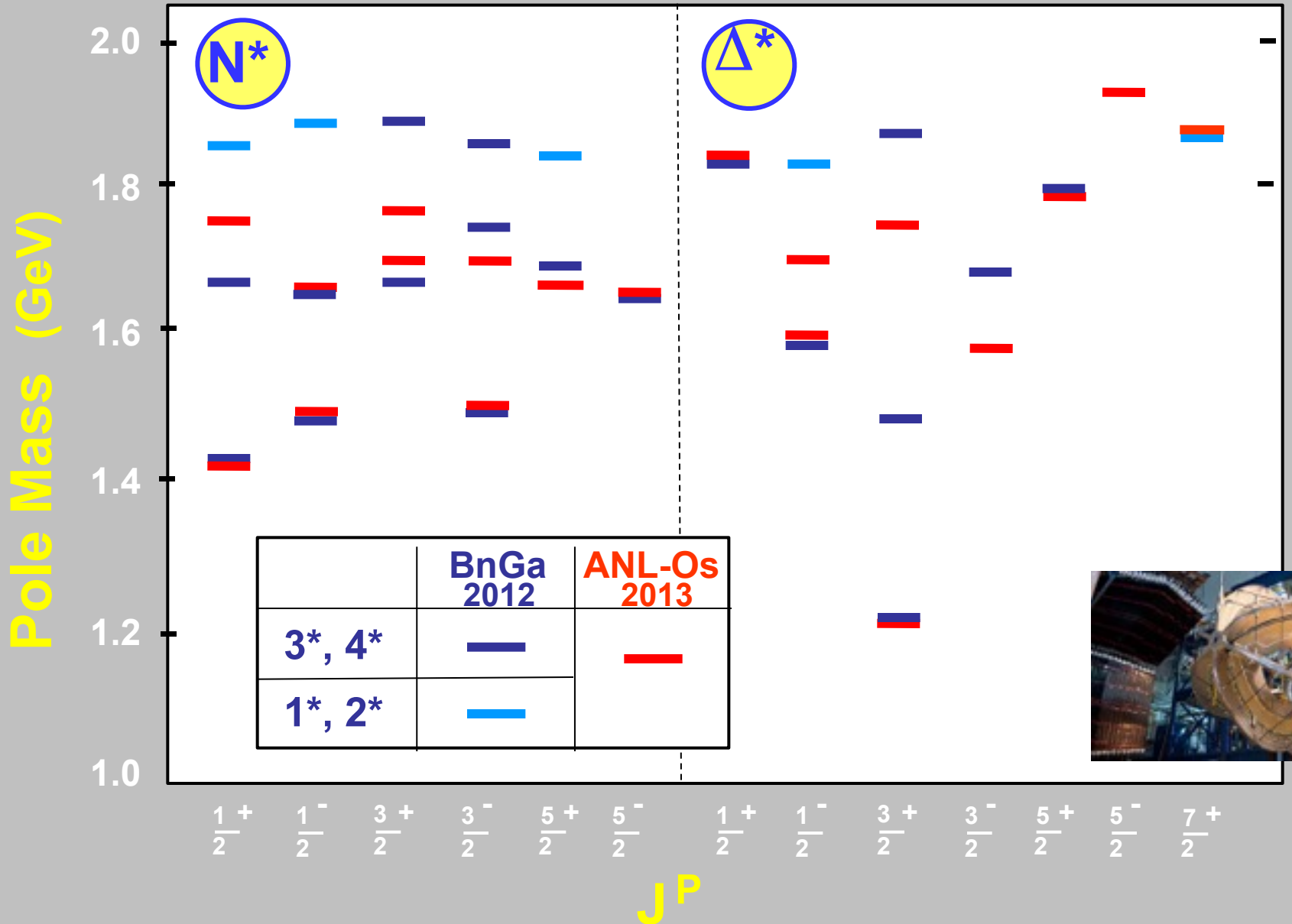
Hadrons: effective degrees of freedom

how do these depend on flavor, s, c, b

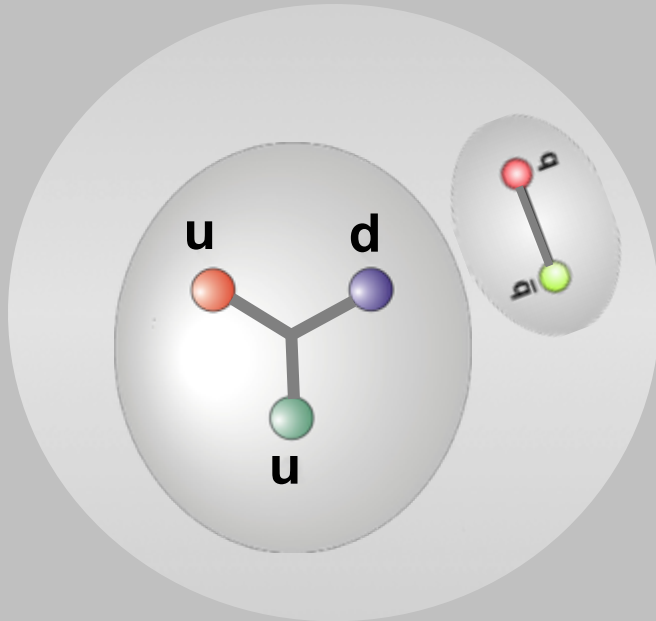
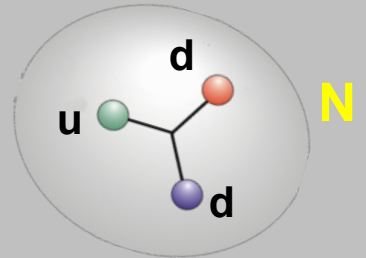
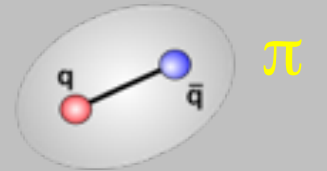
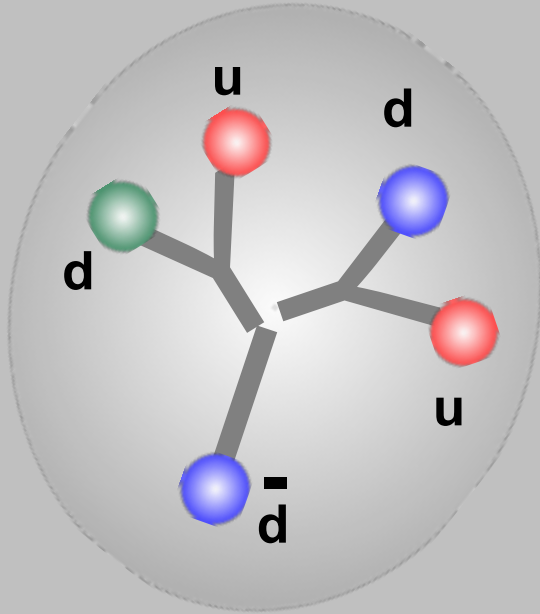
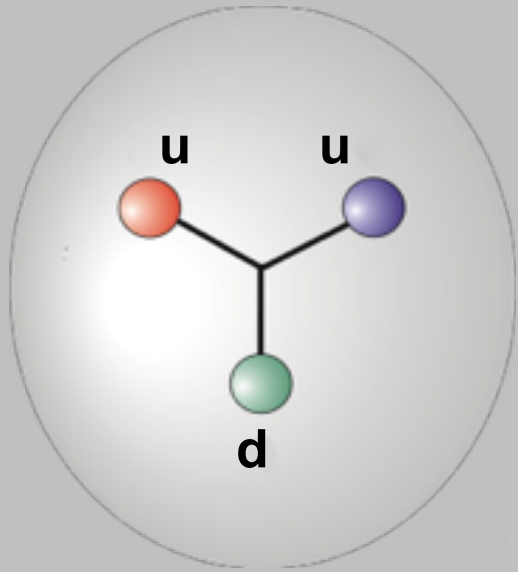
Hadron interactions: universality

$$\mathcal{L}_{\text{QCD}} = \sum_{q=u,d,s,c,b,t} \bar{q} (i\gamma_{\mu} D^{\mu} - m_q) q - \frac{1}{4} F^{\mu\nu} F_{\mu\nu}$$

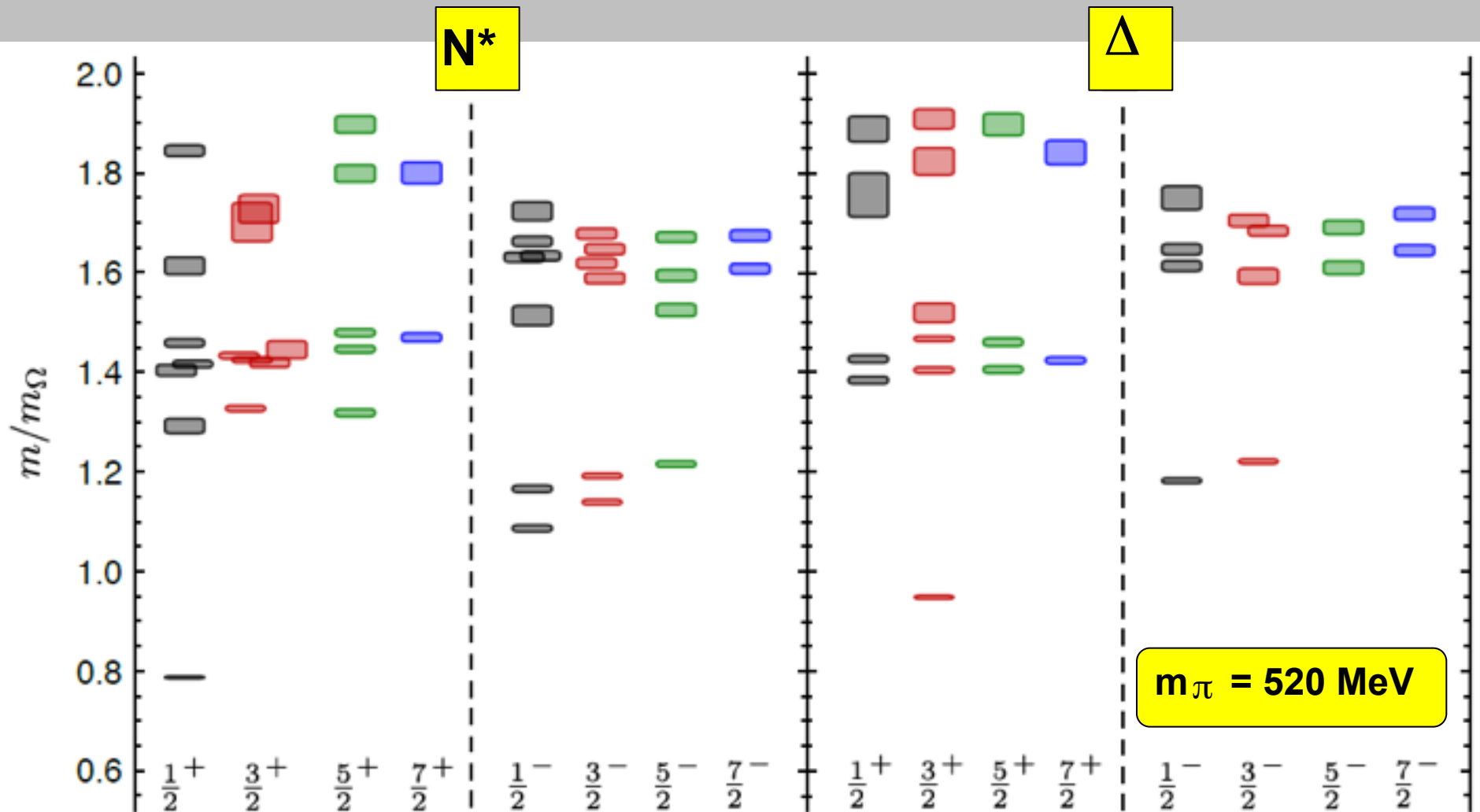
Baryon spectrum from ANL-Osaka & Bonn-Ga



N*(1440)



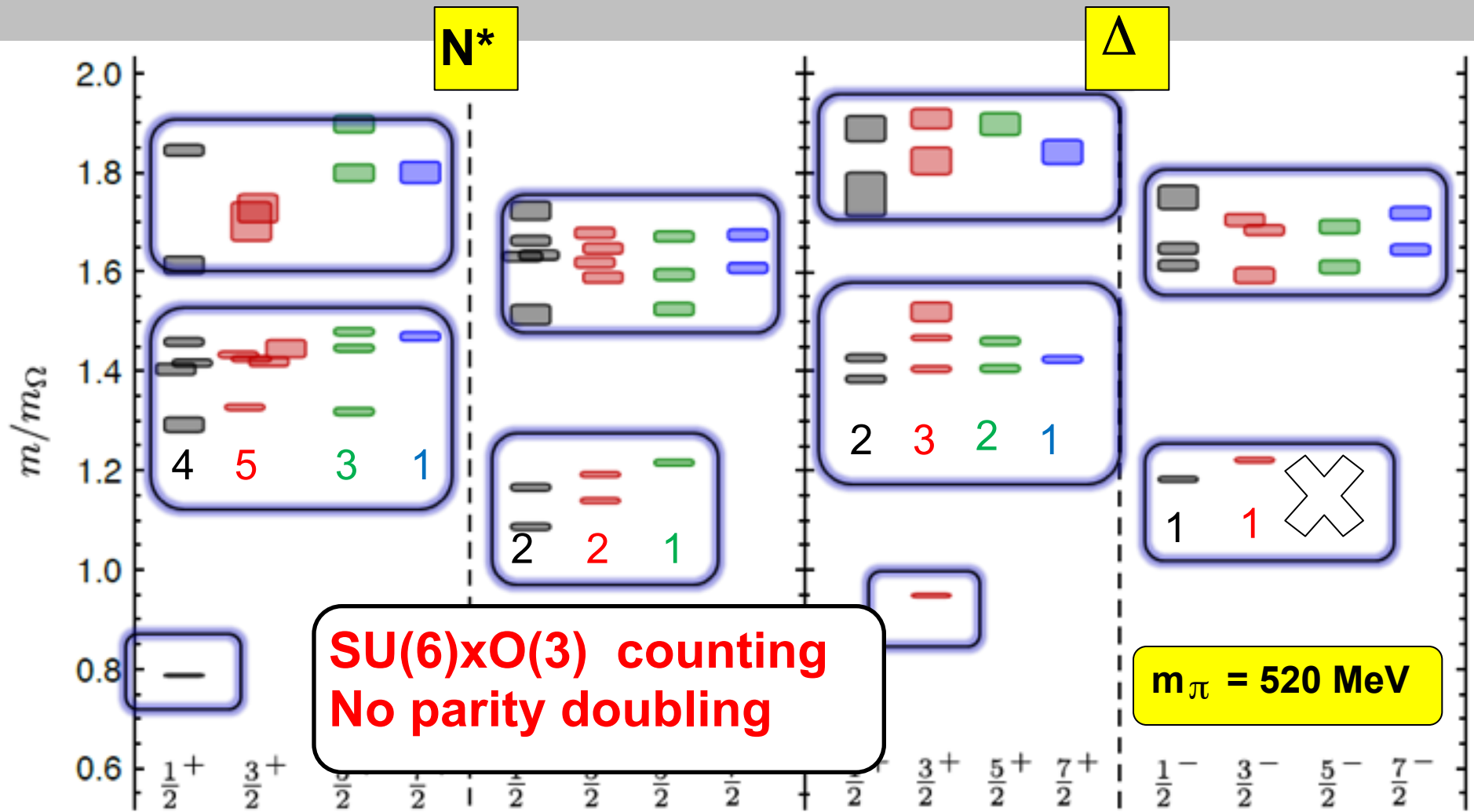
Spin identified N^* and Δ states

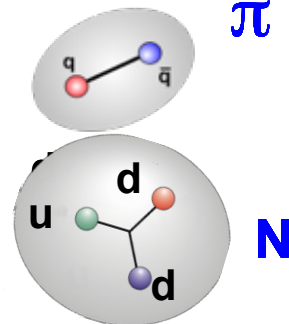
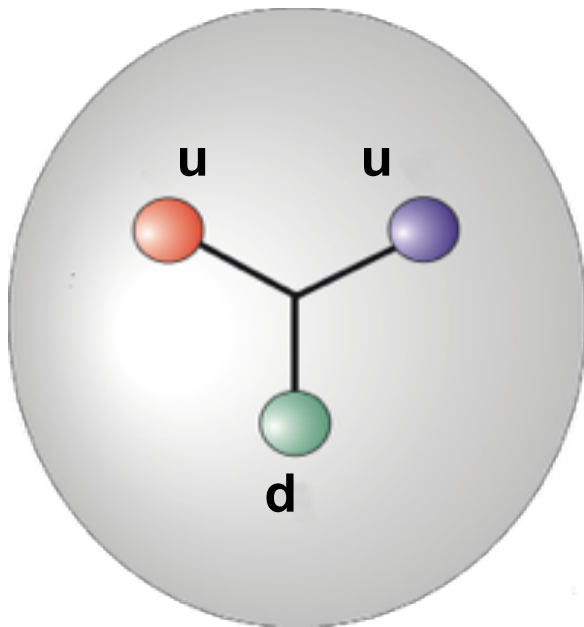


Modelling

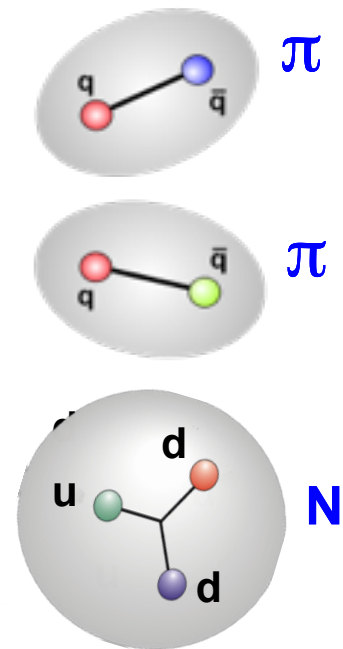
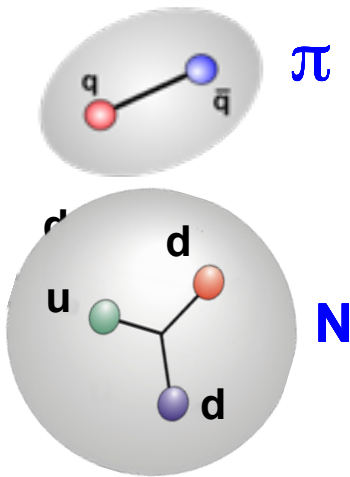
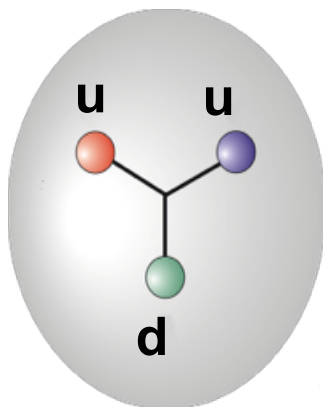
Edwards, Dudek, Wallace & Richards

Spin identified N^* and Δ states

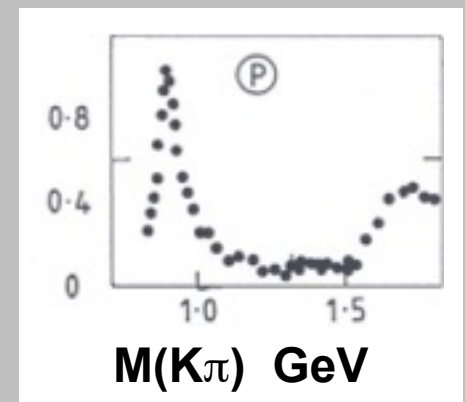
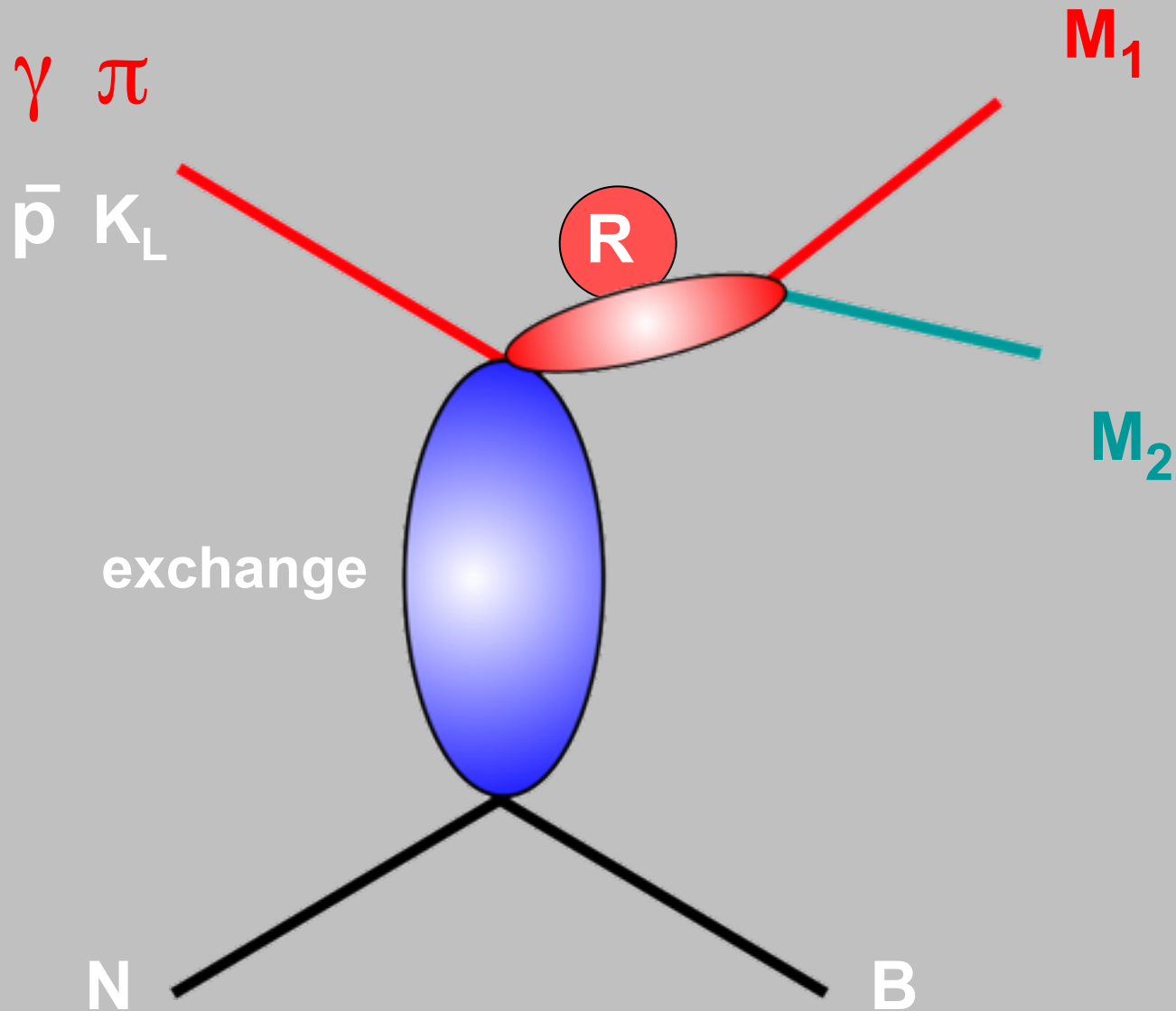




m_π



Hadroproduction



Hadroproduction

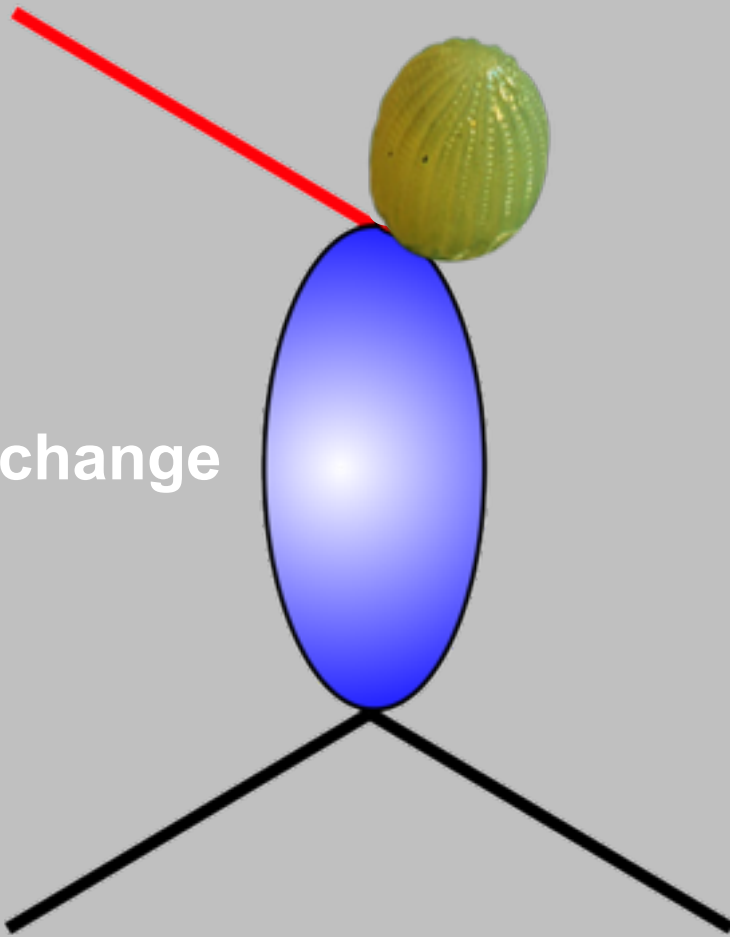
γ π

\bar{p} K_L

exchange

N

B



Hadroproduction

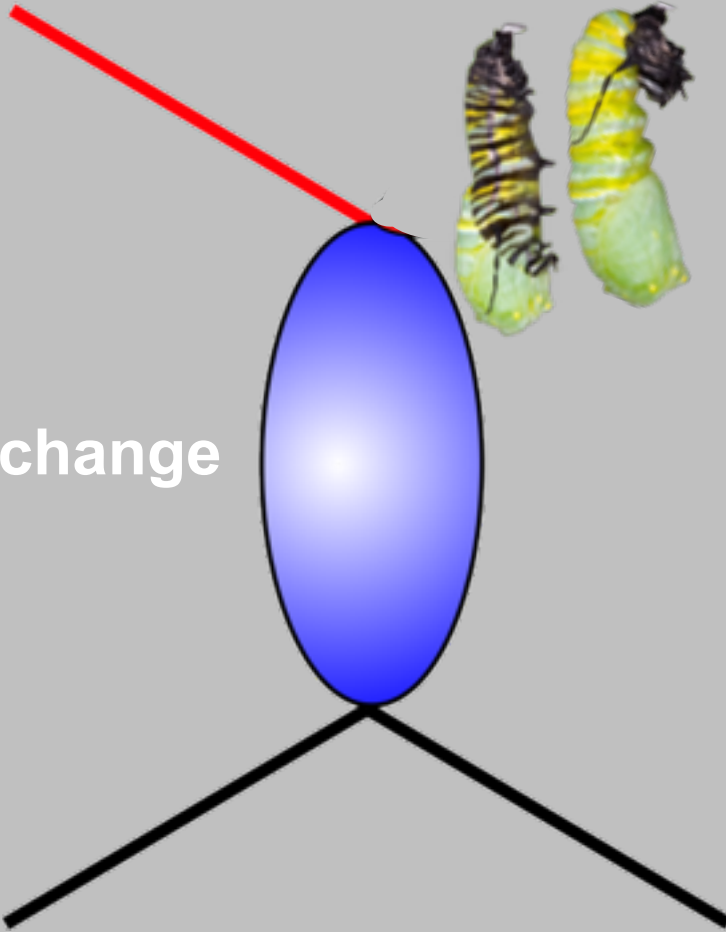
γ π

\bar{p} K_L

exchange

N

B



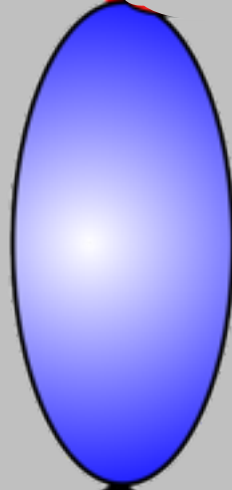
Hadroproduction

γ π

\bar{p} K_L



exchange



N

B

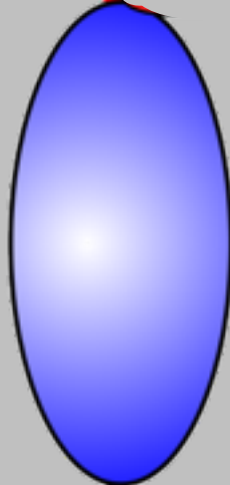
Hadroproduction

γ π

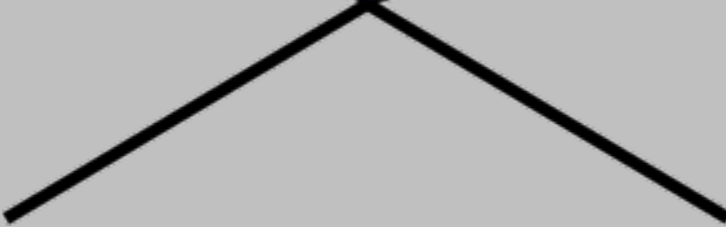
\bar{p} K_L



exchange



N



B

Hadroproduction

γ π

\bar{p} K_L

exchange

N

B



Hadroproduction

γ π

\bar{p} K_L

exchange

N

B



Hadroproduction

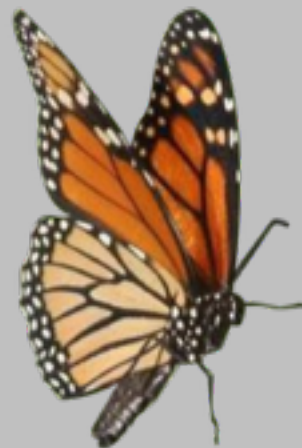
γ π

\bar{p} K_L

exchange

N

B



Hadroproduction

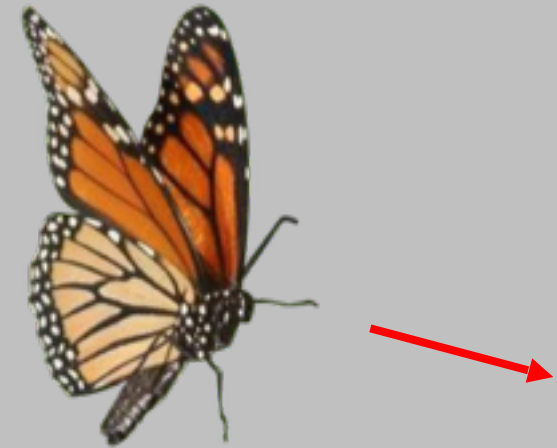
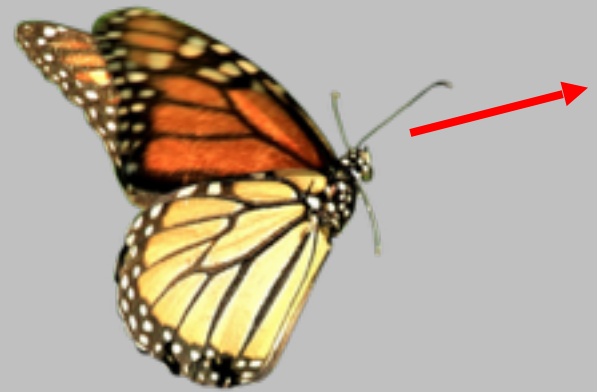
γ π

\bar{p} K_L

exchange

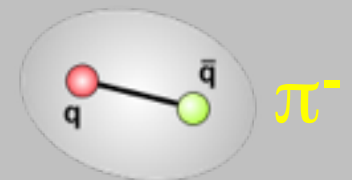
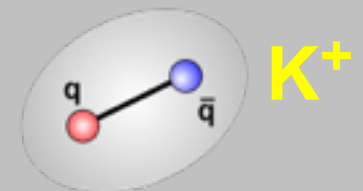
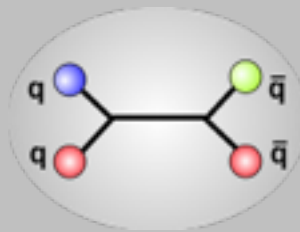
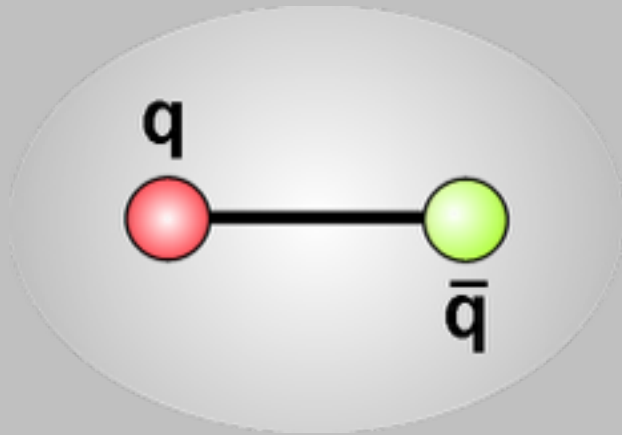
N

B

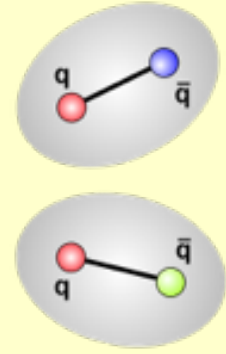
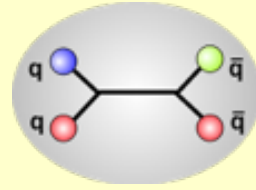
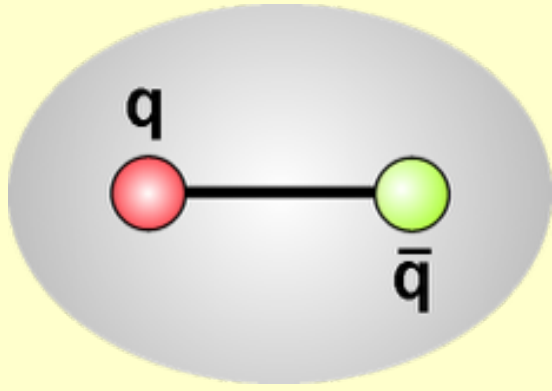


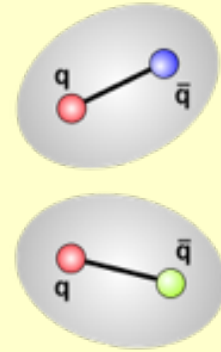
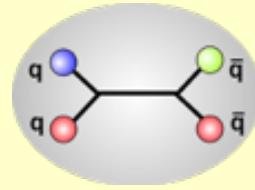
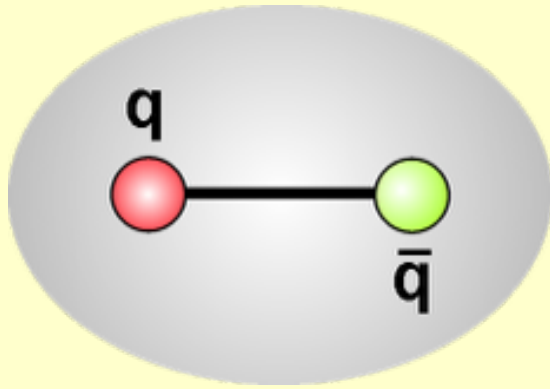
$K^*(892)$

$$J^{PC} = 1^{- -}$$

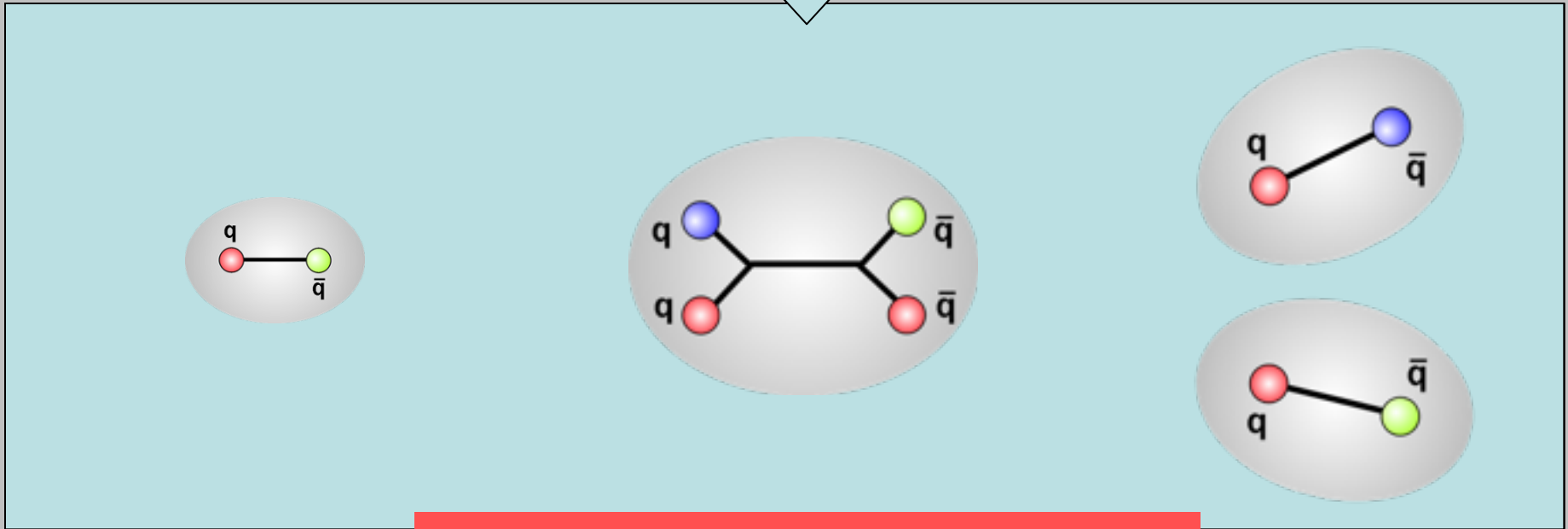
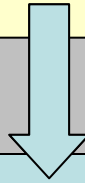
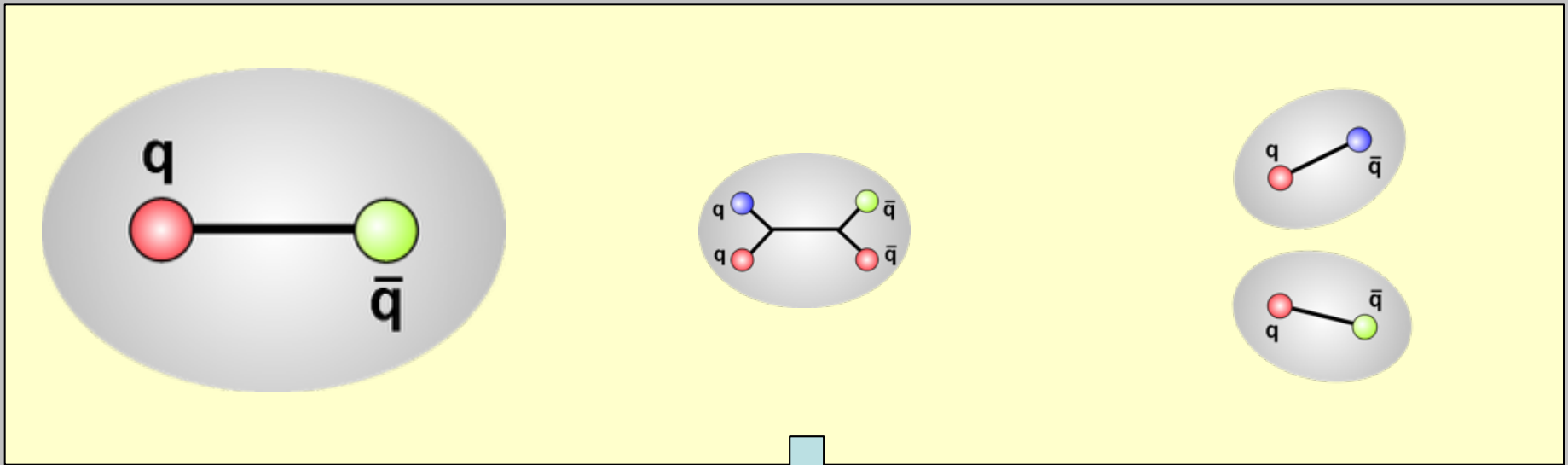


degrees of freedom





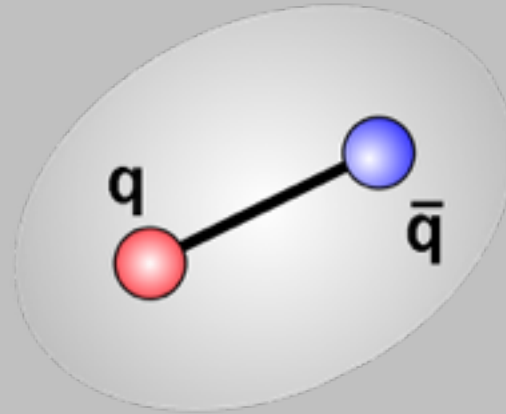
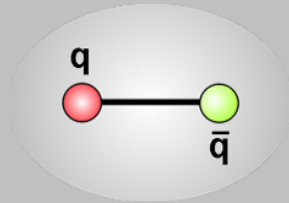
Degrees of freedom



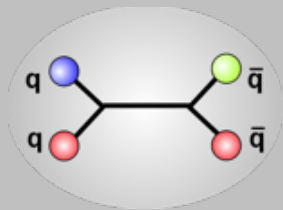
Dynamically generated states

K (600)

$$J^{PC} = 0^+_{+}$$



K

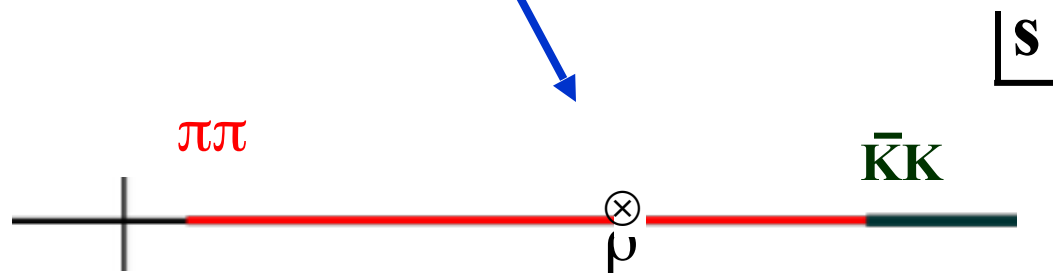
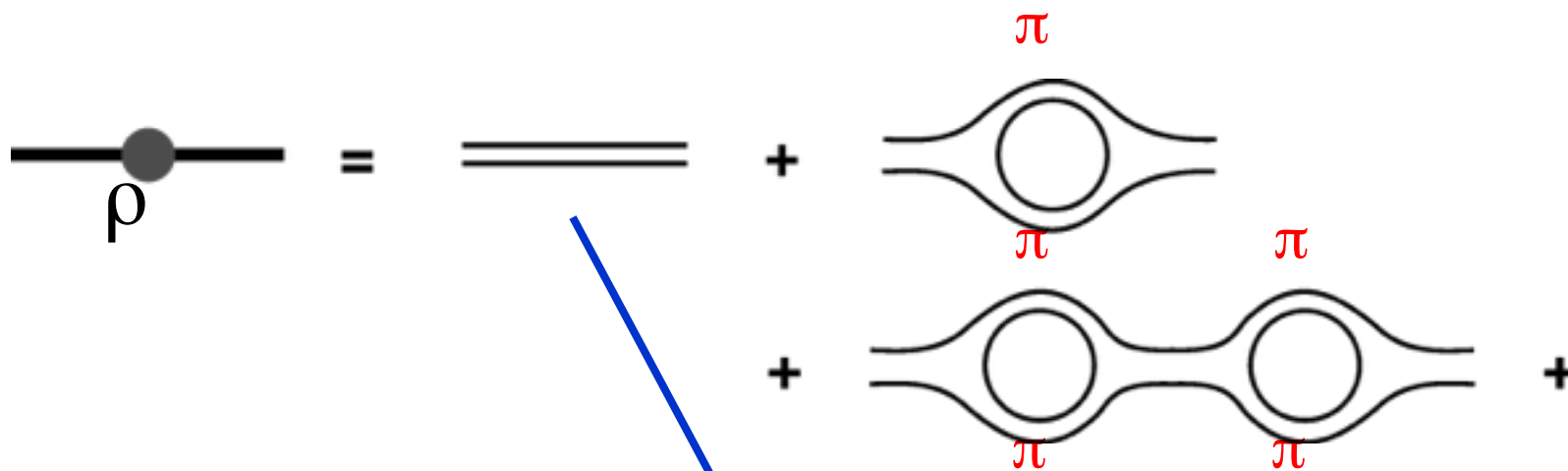


π

X, Y, Z, ...

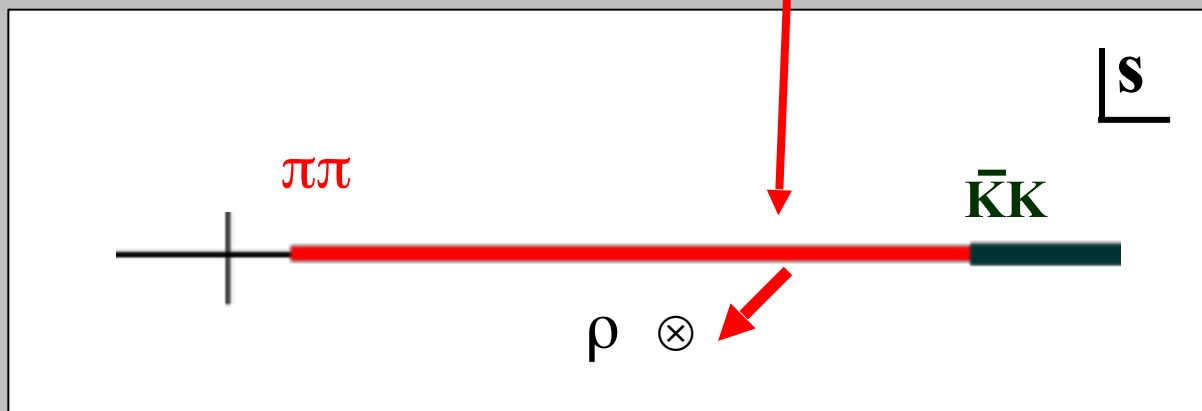
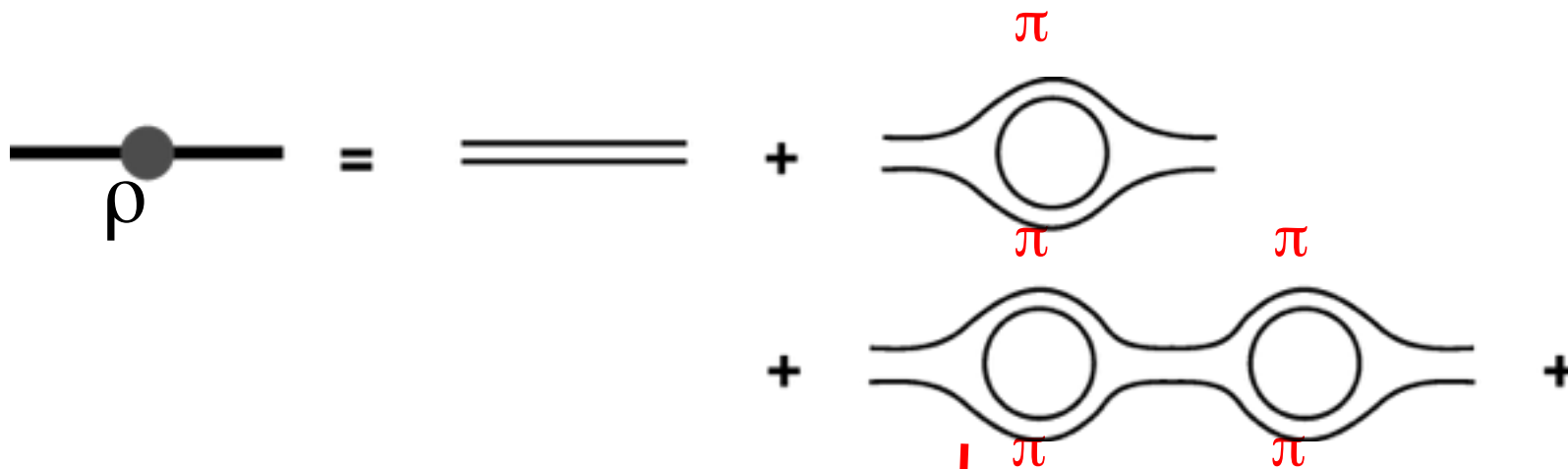
Vector multiplet

shifting of masses

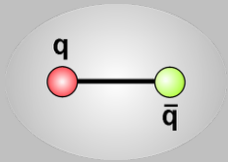
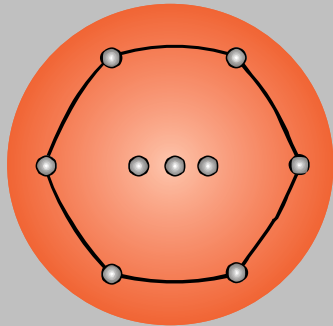


Vector multiplet

shifting of masses



Scalar mesons



$\bar{s}s$ ————— f_0

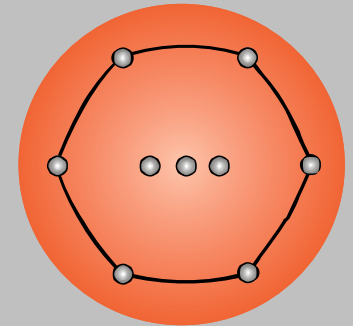
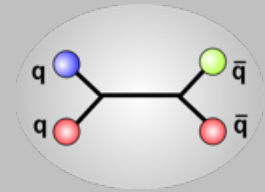
$\bar{s}n$ ————— K_0

$\bar{n}n$ ————— a_0/f_0

$\bar{s}s\bar{n}n$ ————— a_0/f_0

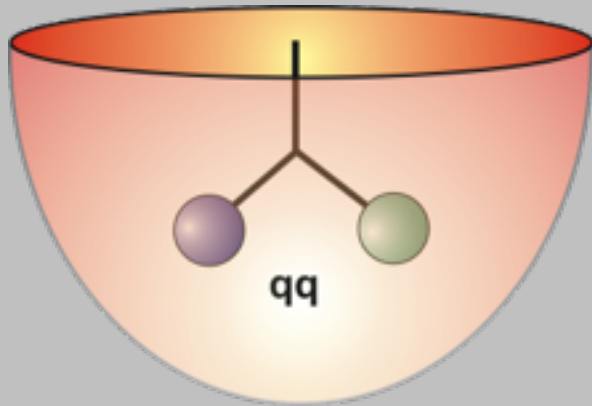
$\bar{s}n\bar{n}n$ ————— K_0 \mathbf{K}

$\bar{n}n\bar{n}n$ ————— f_0 $\mathbf{\sigma}$



$n = u, d$

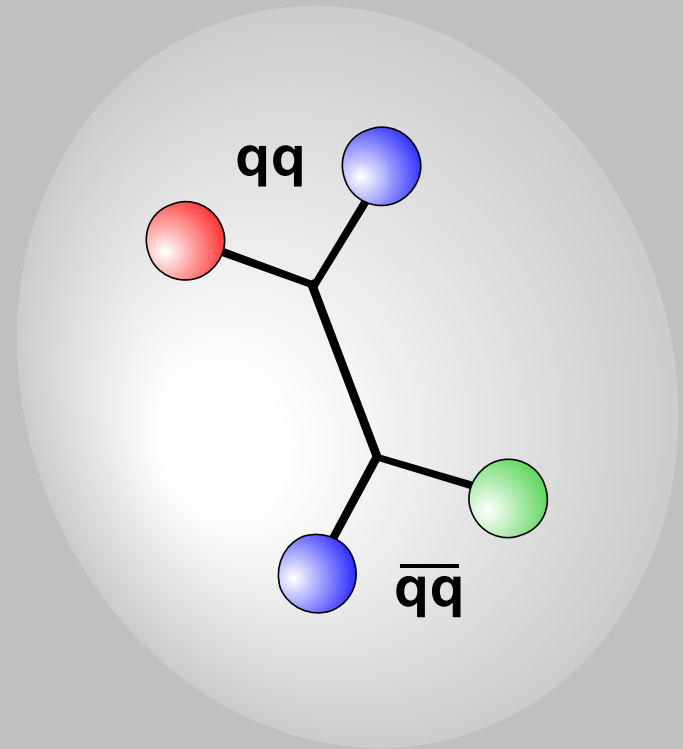
diquarks: color



Jaffe & Wilczek



tetraquark



Scalar diquarks

[ud]

[us]

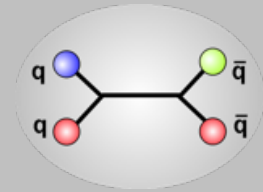
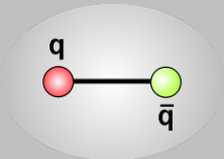
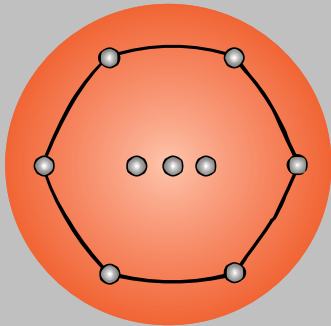
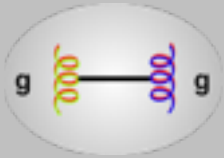
[ds]

[cd]

[cu]

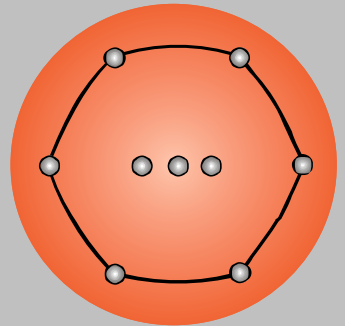
[cs]

Scalar mesons



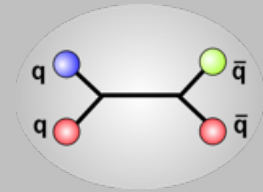
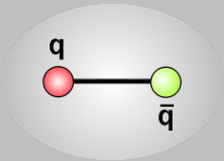
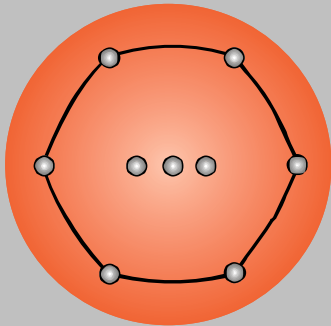
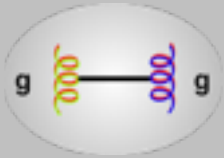
gg ————— f_0
 $\bar{s}s$ ————— f_0
 $\bar{s}n$ ————— K_0
 $\bar{n}n$ ————— a_0/f_0

$\bar{s}s\bar{n}n$ ————— a_0/f_0
 $\bar{s}n\bar{n}n$ ————— K_0 \mathbf{K}
 $\bar{n}n\bar{n}n$ ————— f_0 $\mathbf{\sigma}$



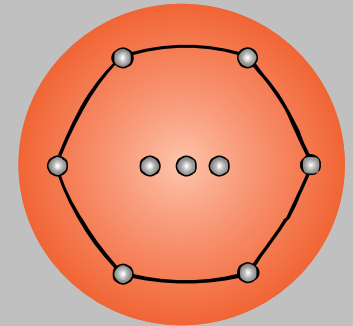
$n = u, d$

Scalar mesons



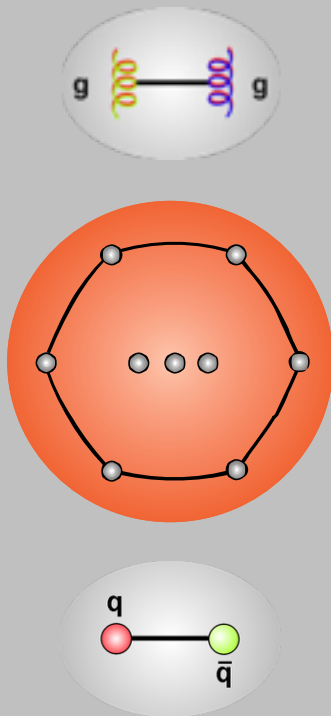
gg ————— f_0
 $\bar{s}s$ ————— f_0
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$\bar{s}s\bar{n}n$ ————— a_0/f_0
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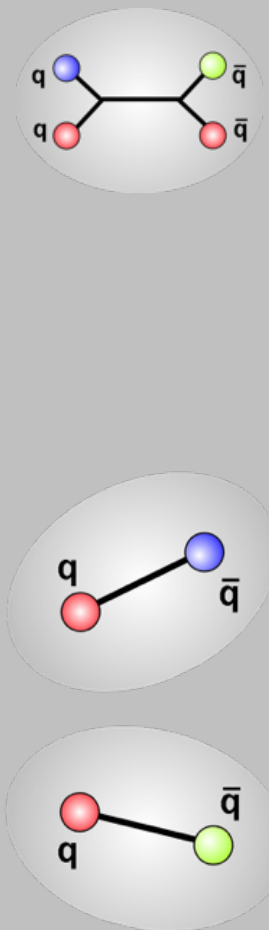
$n = u, d$

Scalar mesons



gg ————— f_0
 $\bar{s}s$ ————— f_0
 $\bar{s}n$ ————— K_0
 $\bar{n}n$ ————— a_0/f_0

$\bar{s}s\bar{n}n$ ————— a_0/f_0
 $\bar{s}n\bar{n}n$ ————— K_0 \mathbf{K}
 $\bar{n}n\bar{n}n$ ————— f_0 $\mathbf{\sigma}$



Scalar multiplet

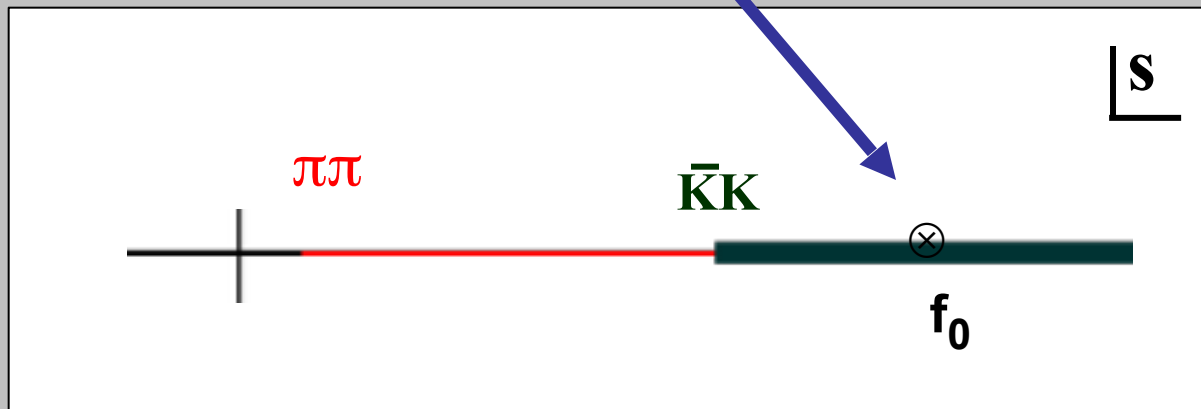
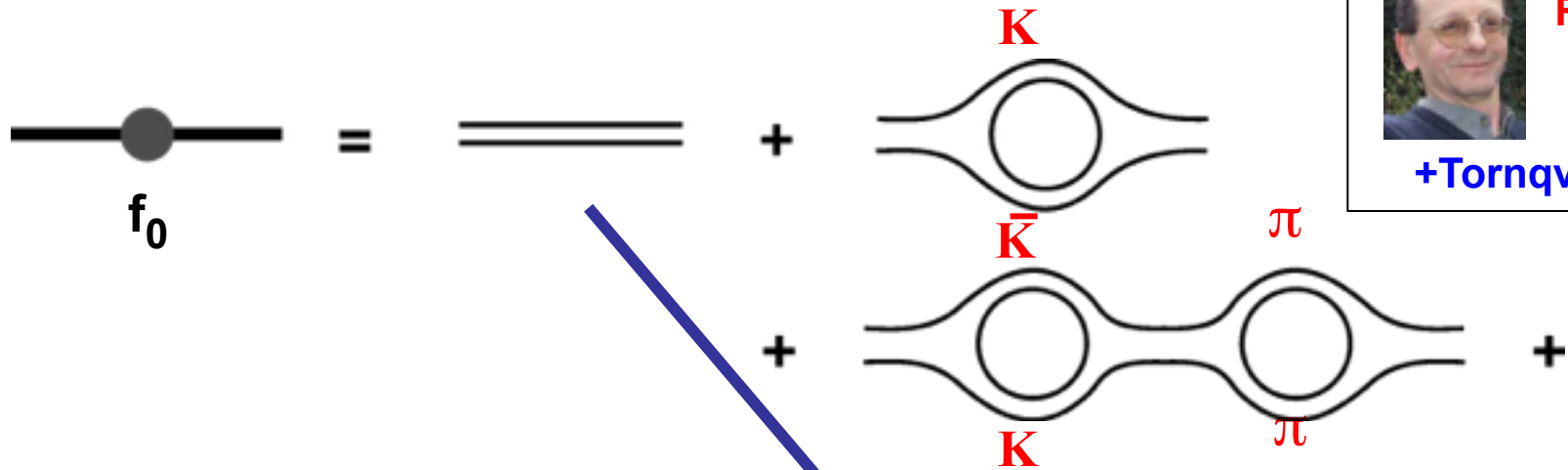


Van
Beveren



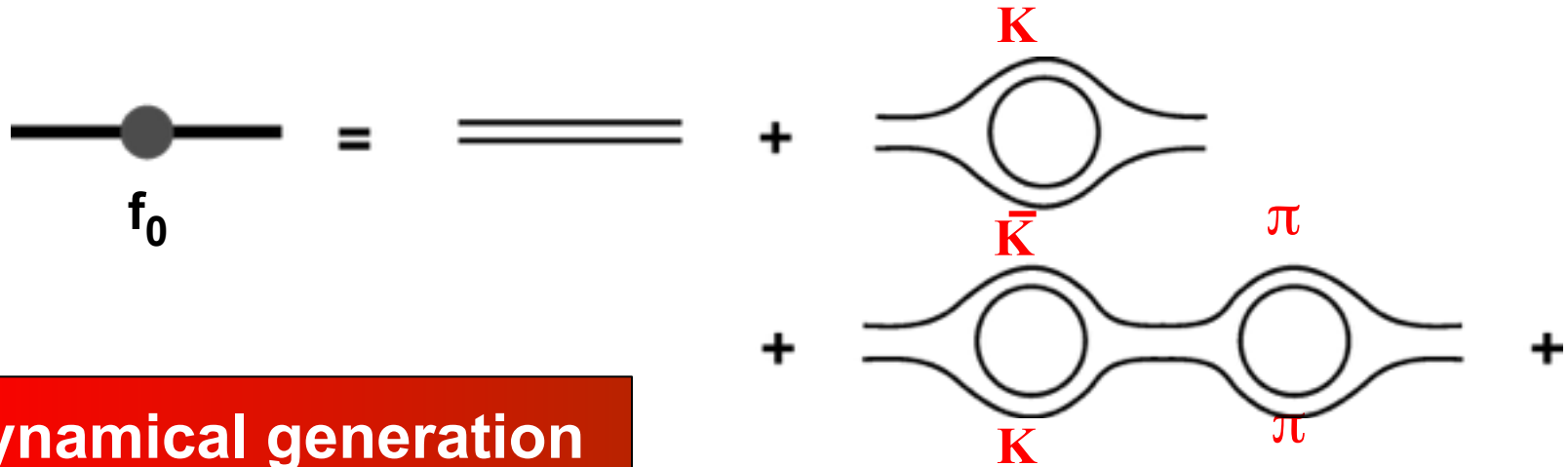
Rupp

+Tornqvist



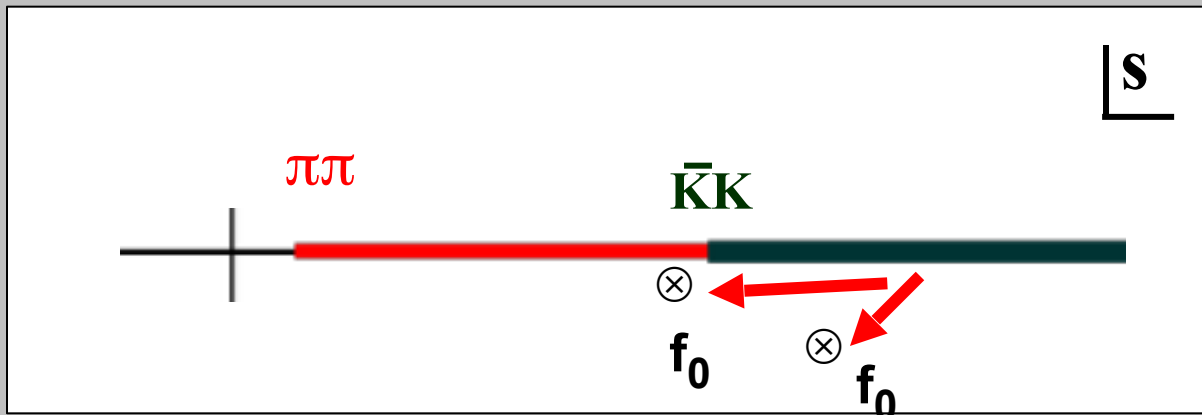
Scalar multiplet

shifting of masses



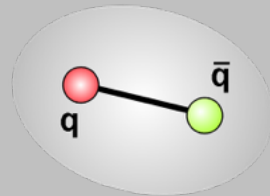
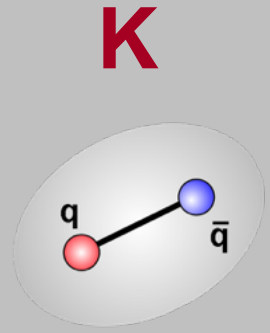
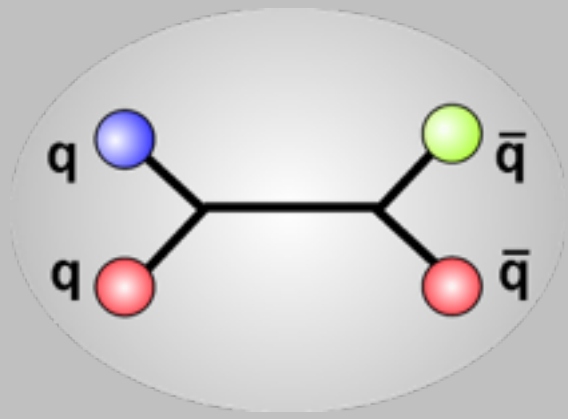
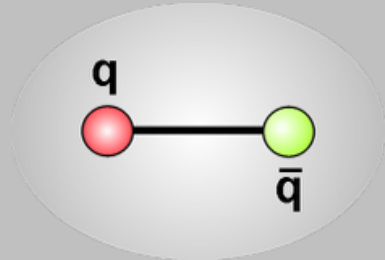
dynamical generation

$\bar{s}s$



$f_0(980)$

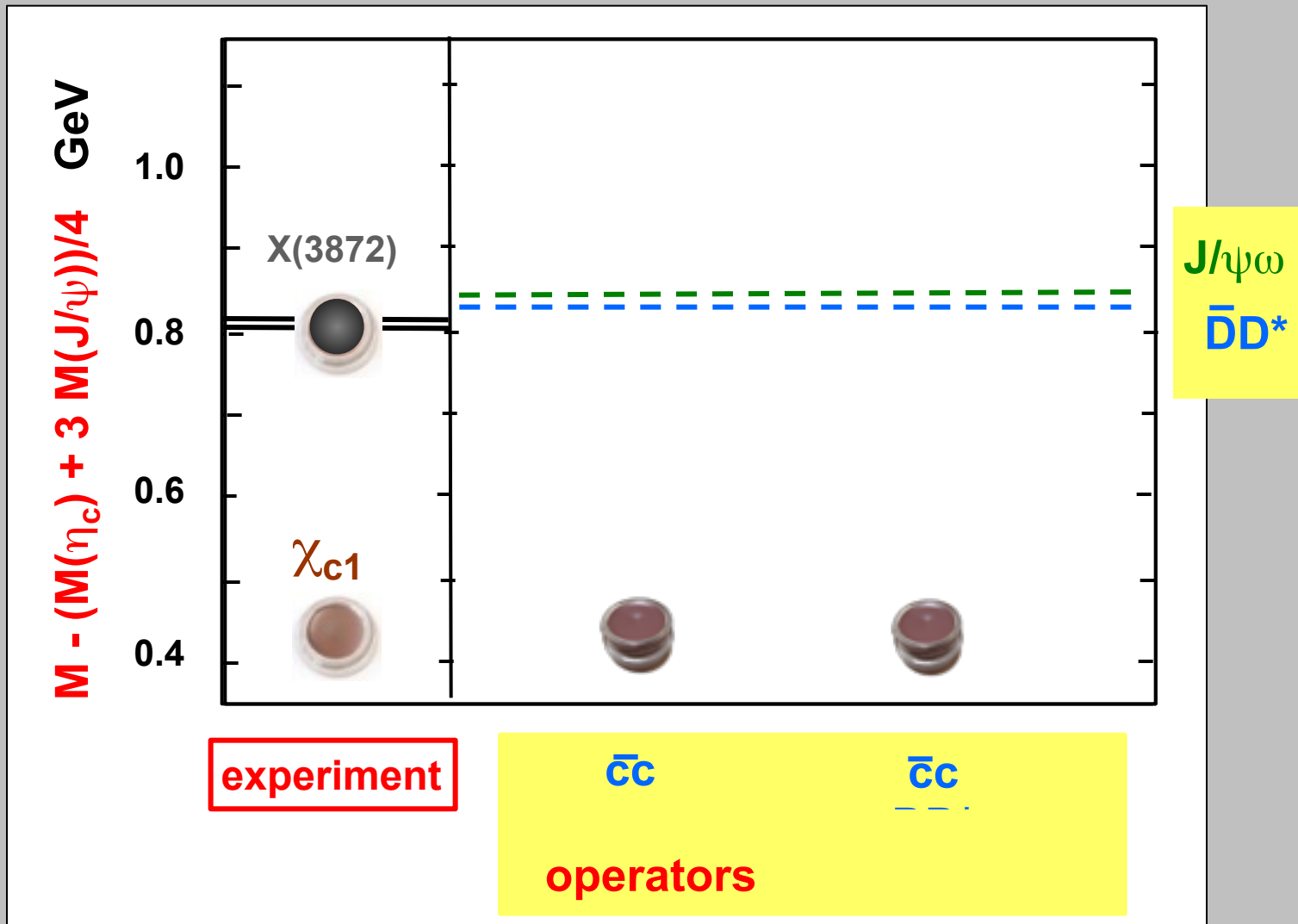
?



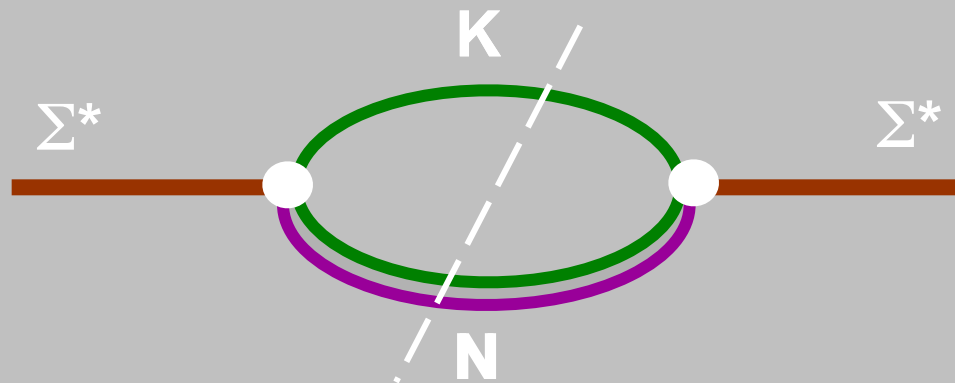
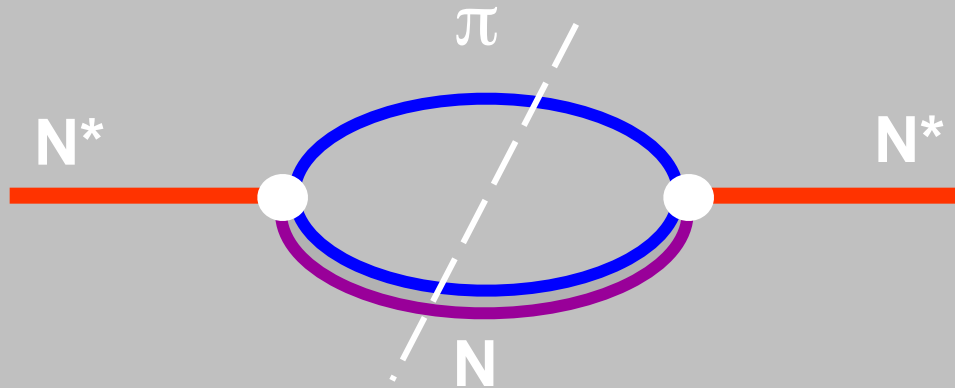
\bar{K}

X(3872) & 1^{++} charmonium

m_{π} 296 MeV



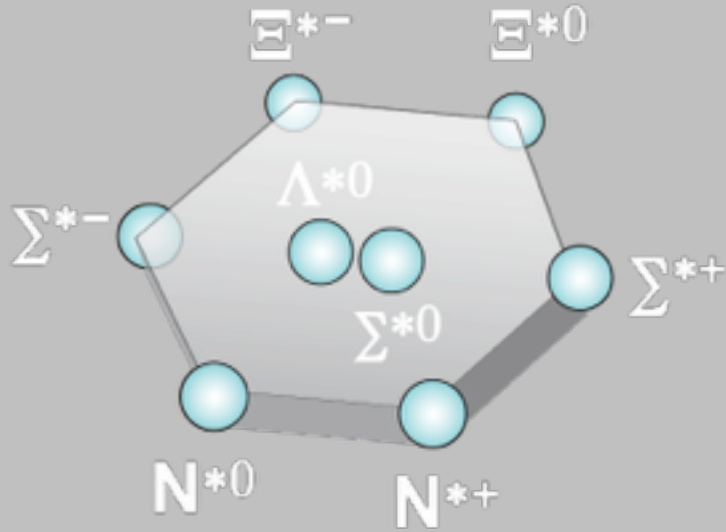
Contributions to baryon decays



when S-wave interactions
shift most from quark model simplicity

Baryon octet

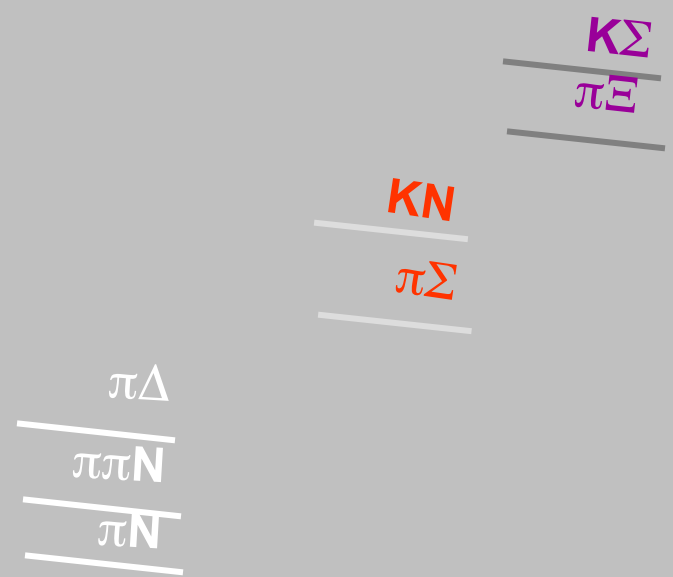
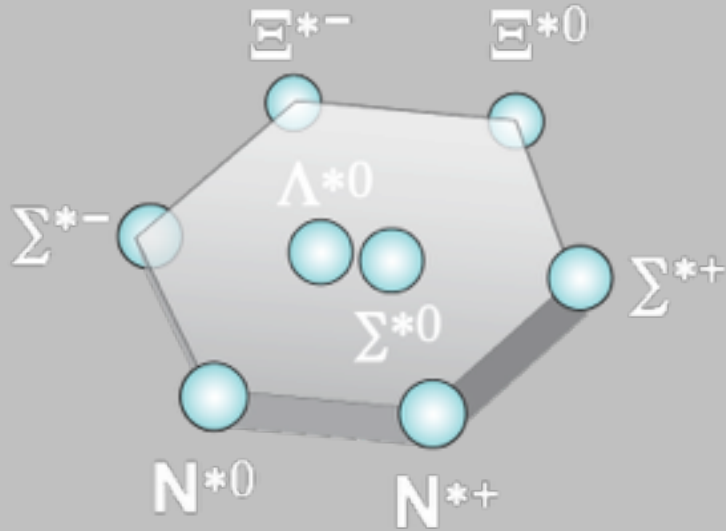
↑
Mass



Baryon octet

decay channels

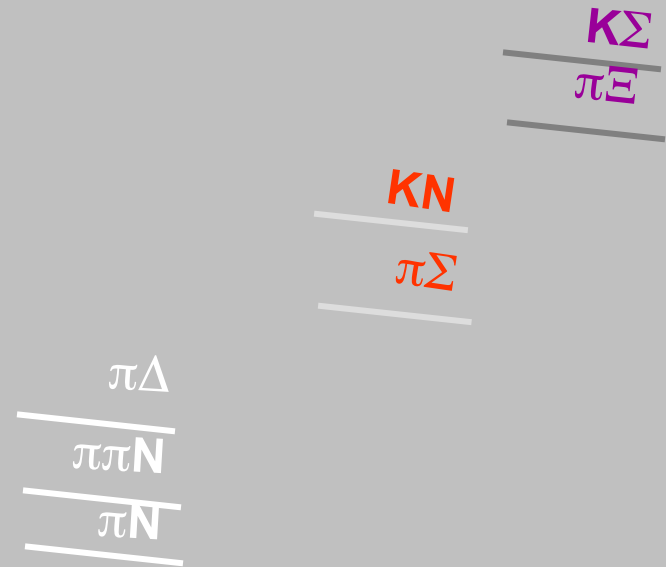
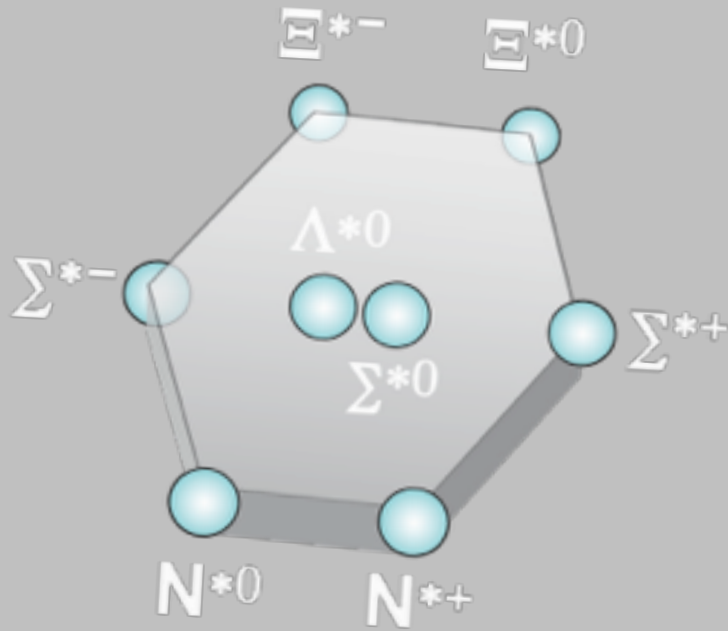
↑
Mass



Baryon octet

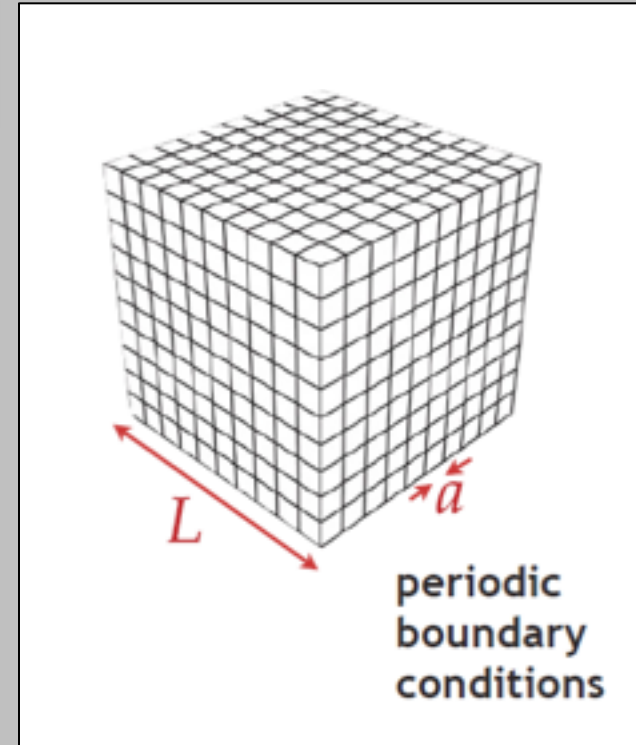
decay channels

↑
Mass



Scattering in a box: LQCD

From his '90 "Thesis"

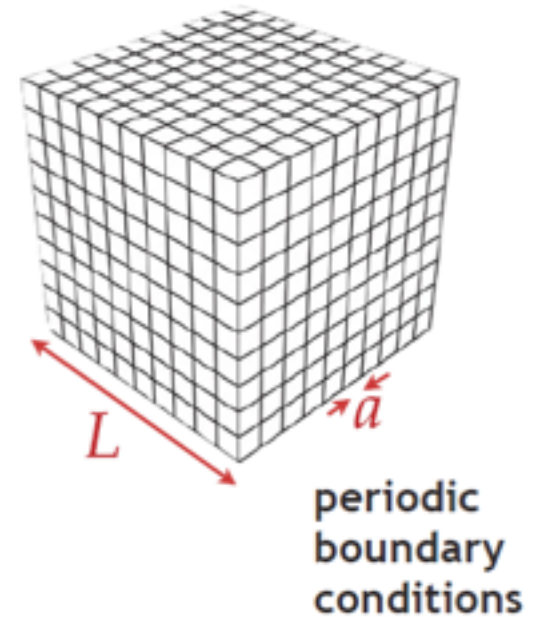
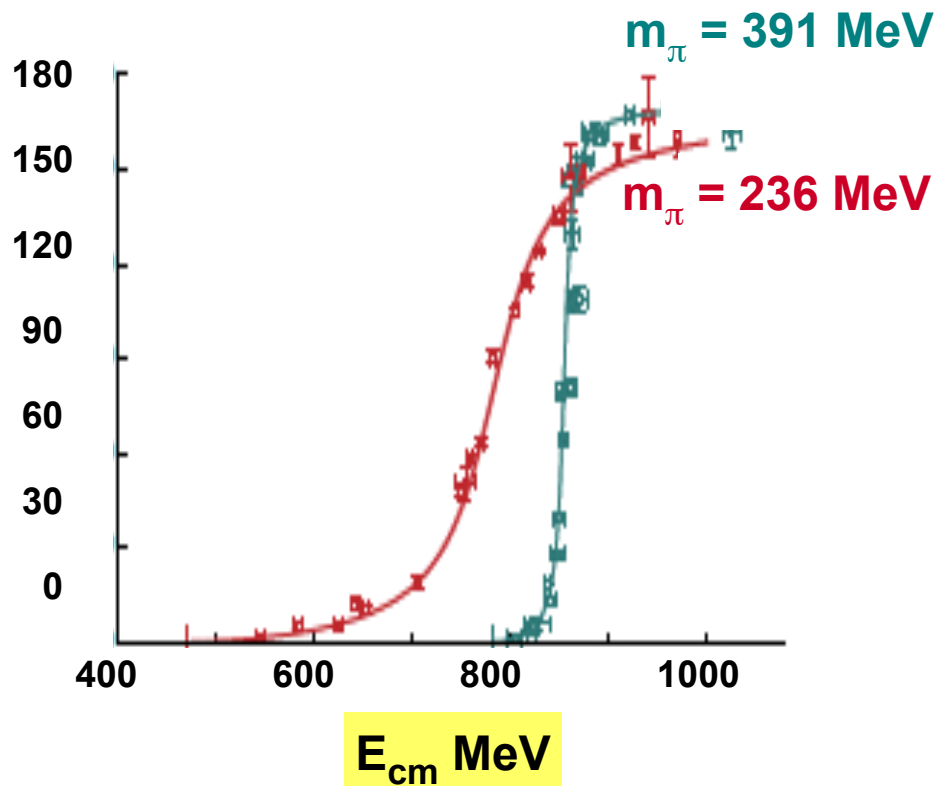


how to connect the finite to the infinite

Scattering in a box: LQCD

$$I = J = 1 \quad \pi\pi \rightarrow \pi\pi$$

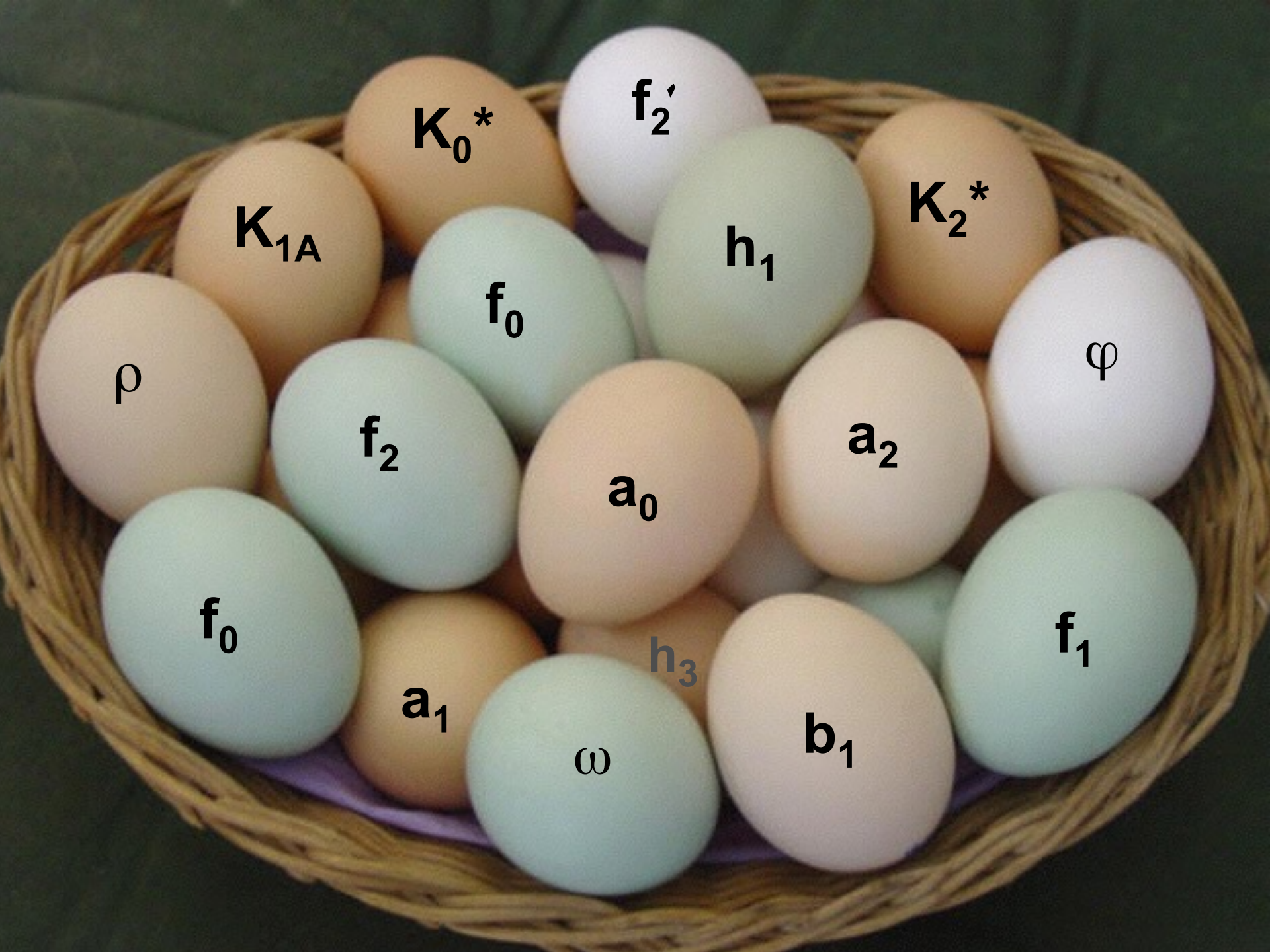
δ_1



Lüscher method applied

Hadron Spectrum Collaboration
Wilson *et al.*

Lifecycle of a hadron



K_0^*

f_2'

K_{1A}

K_2^*

h_1

f_0

φ

ρ

f_2

a_0

a_2

f_0

a_1

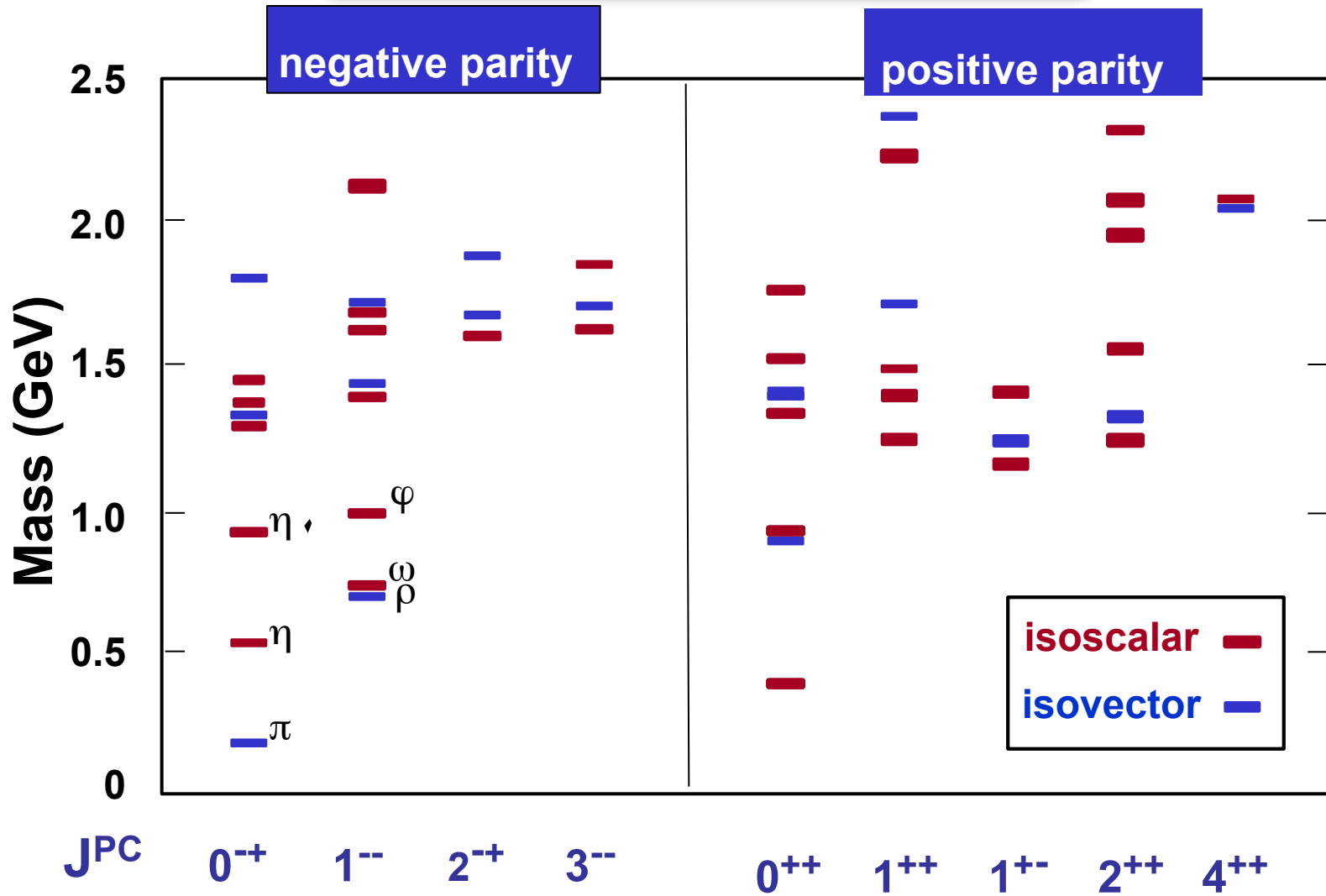
h_3

f_1

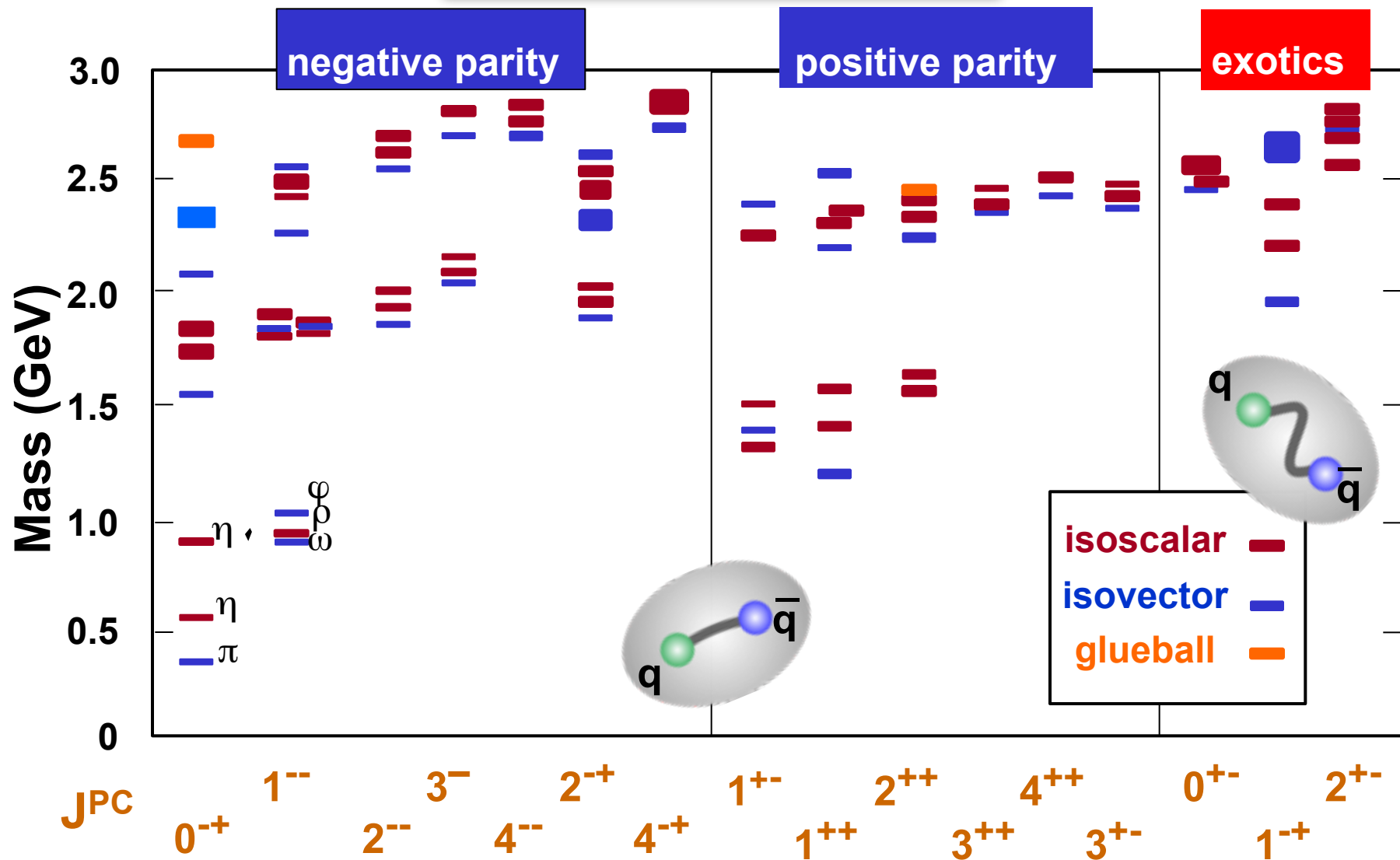
ω

b_1

Light Meson Spectrum



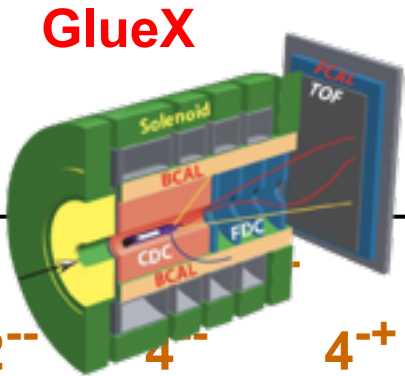
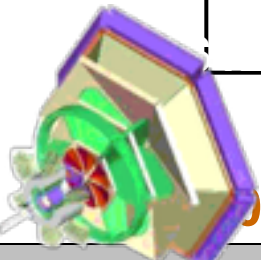
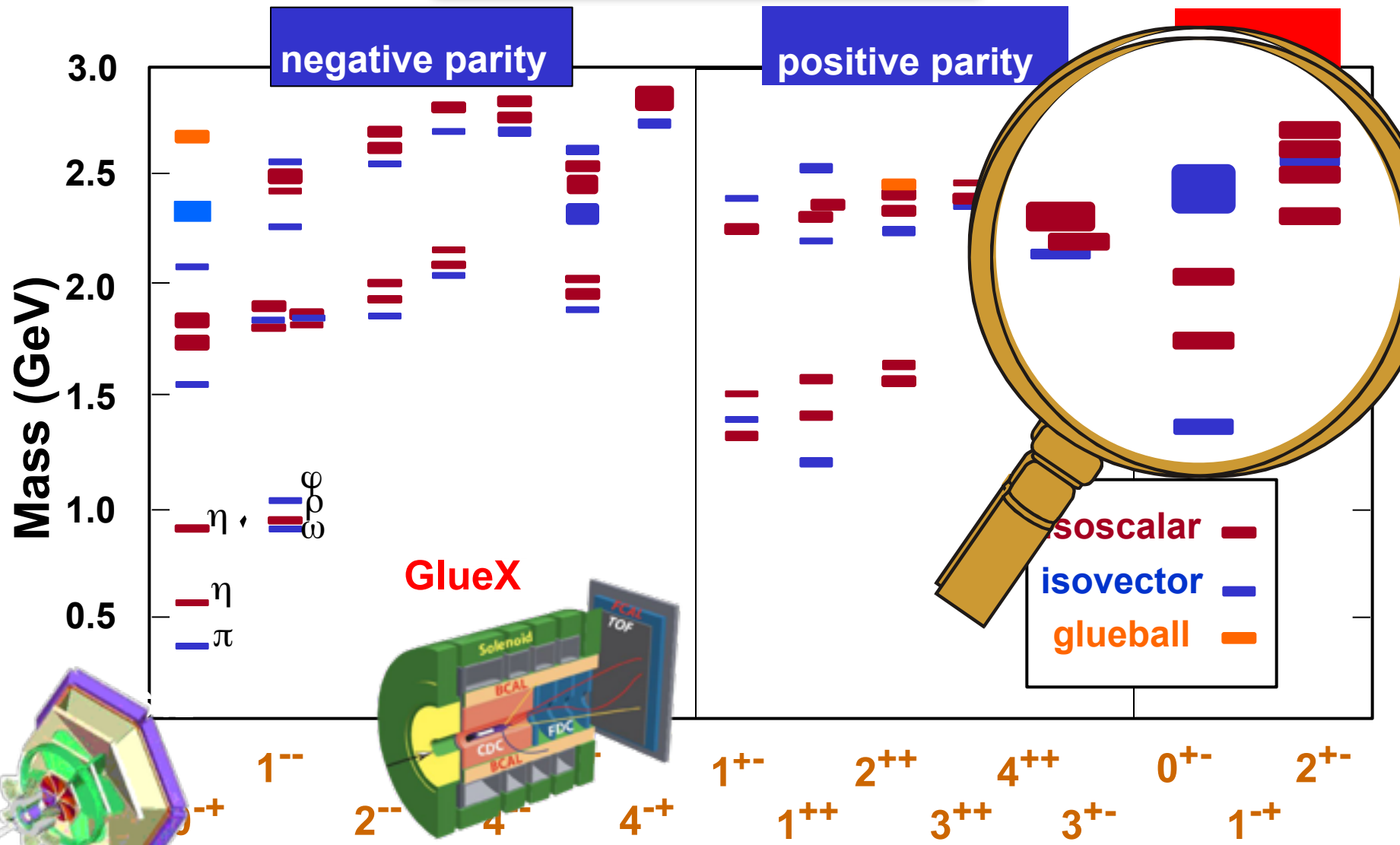
Meson spectrum



Dudek et al

$m_{\pi} = 396 \text{ MeV}$

Meson spectrum



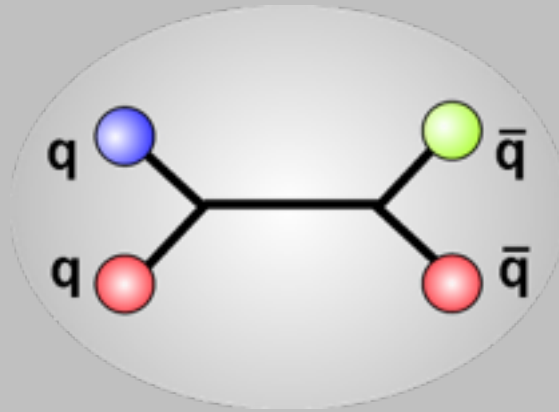
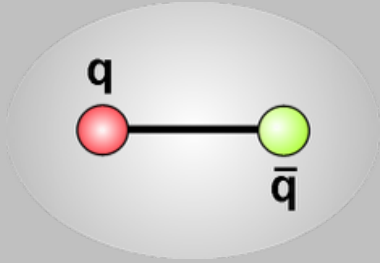
CLAS12

Dudek et al

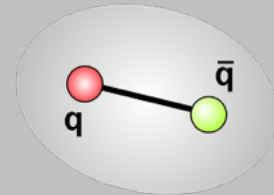
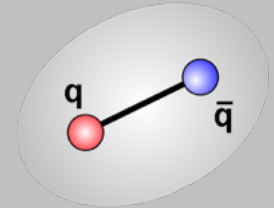
$m_{\pi} = 396 \text{ MeV}$

$f_0(980)$

?

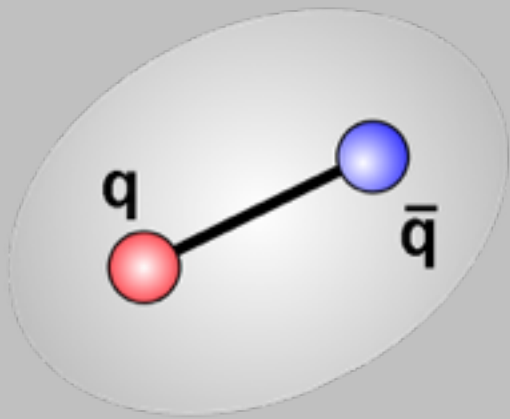
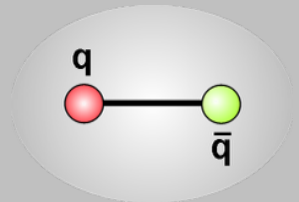


K

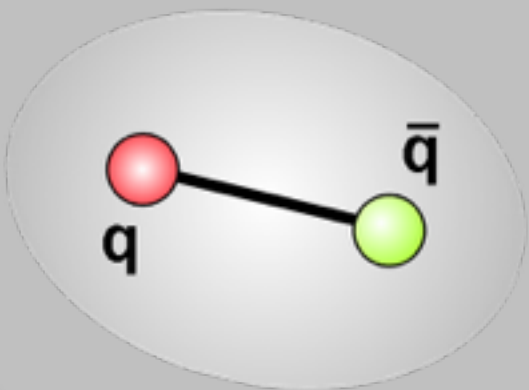
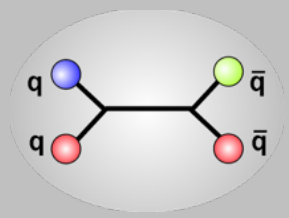


\bar{K}

$f_0(980)$



K

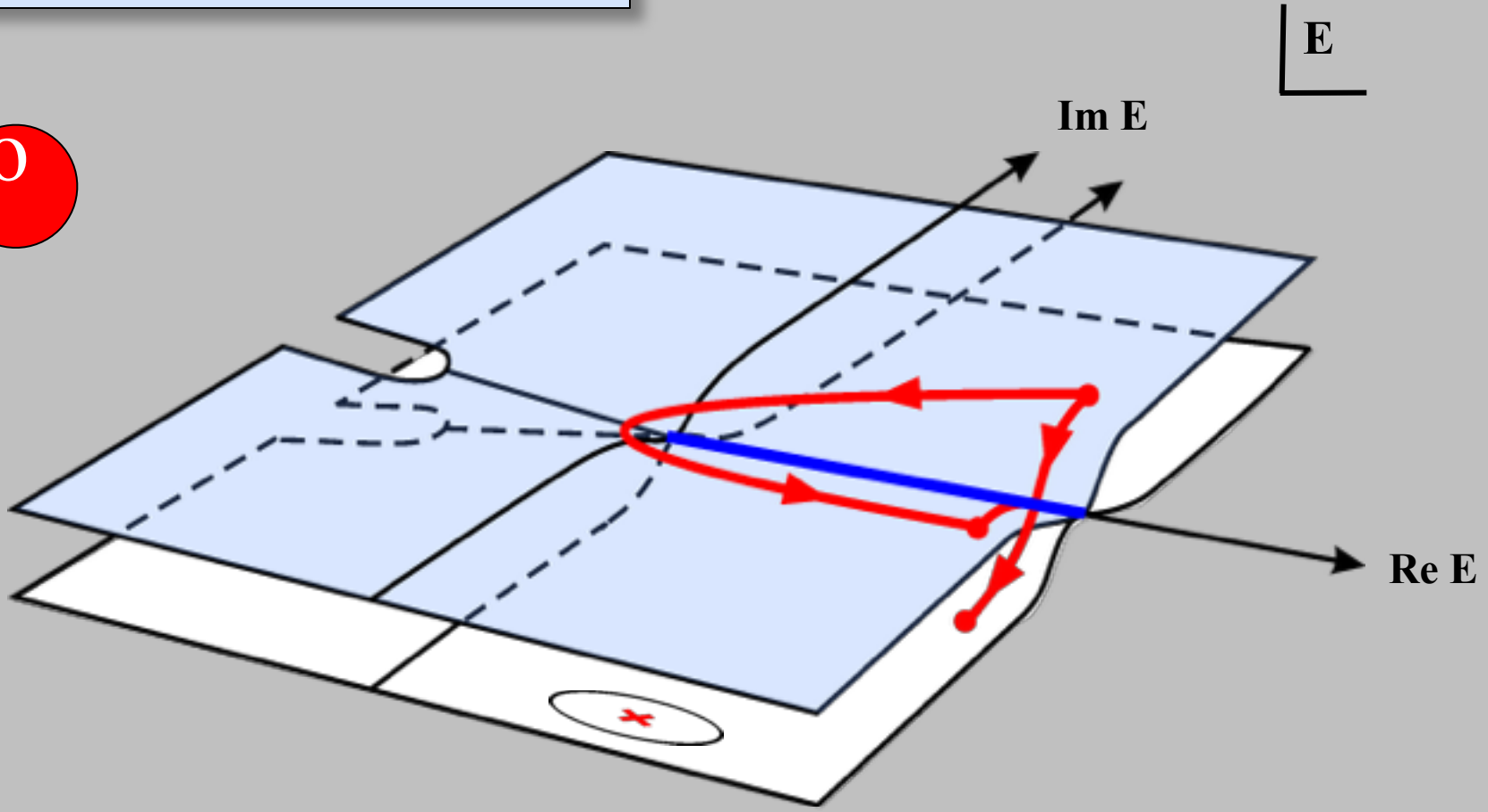


\bar{K}

?

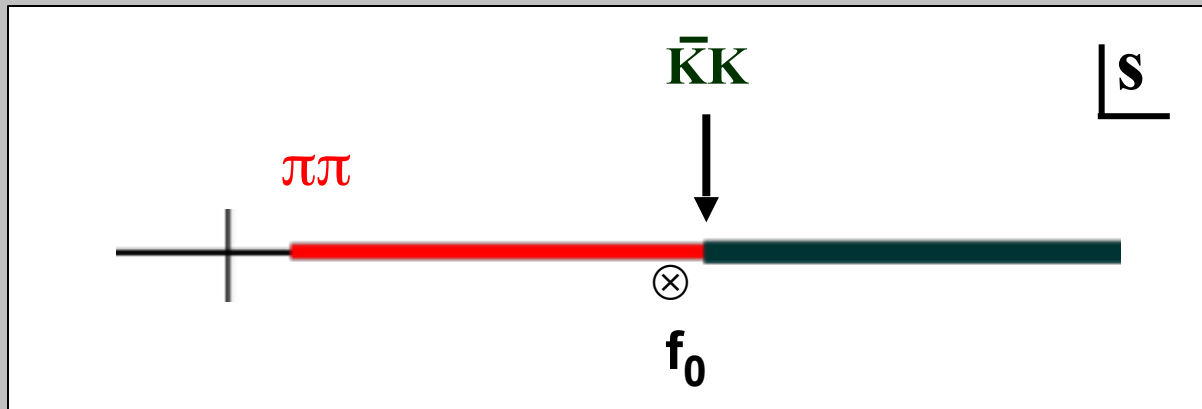
Into the complex plane

ρ



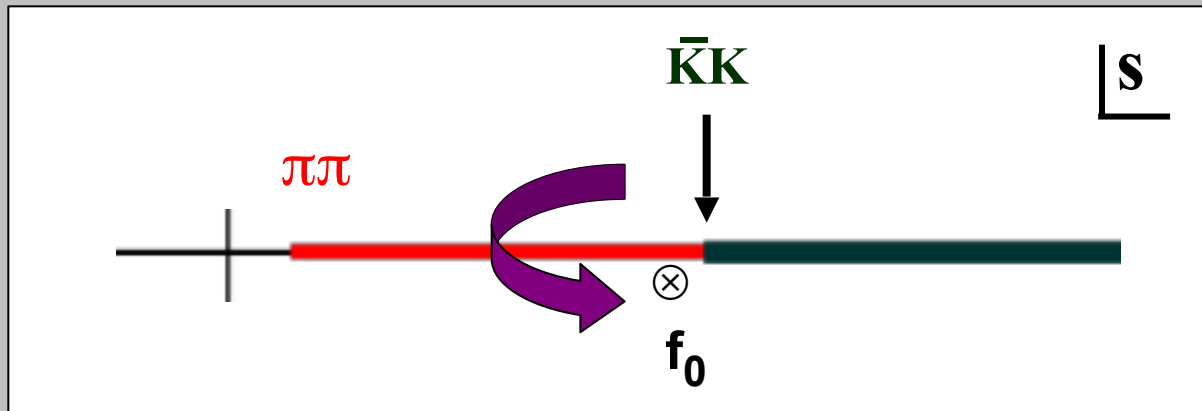
Scalar meson

poles in complex plane

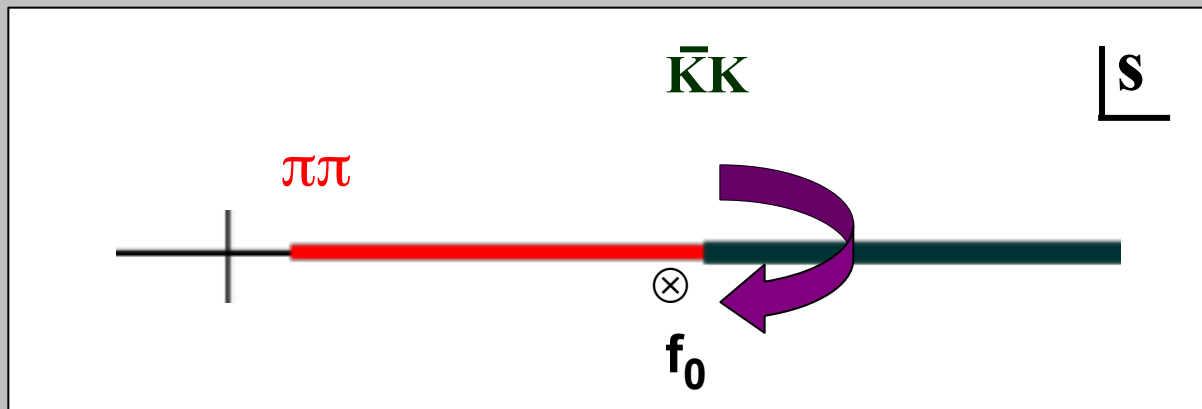


Scalar meson

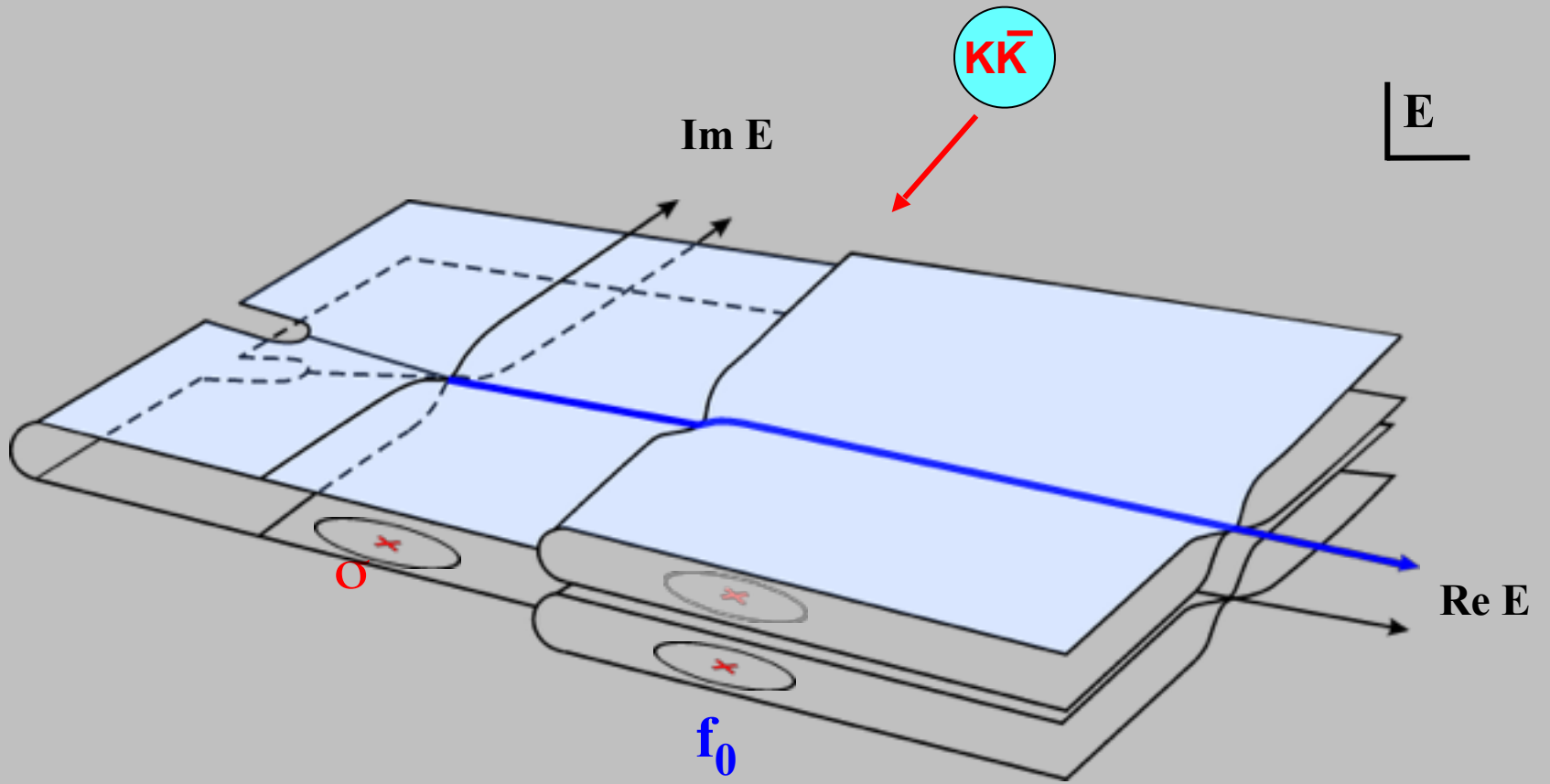
poles in complex plane



Is there a mirror pole?

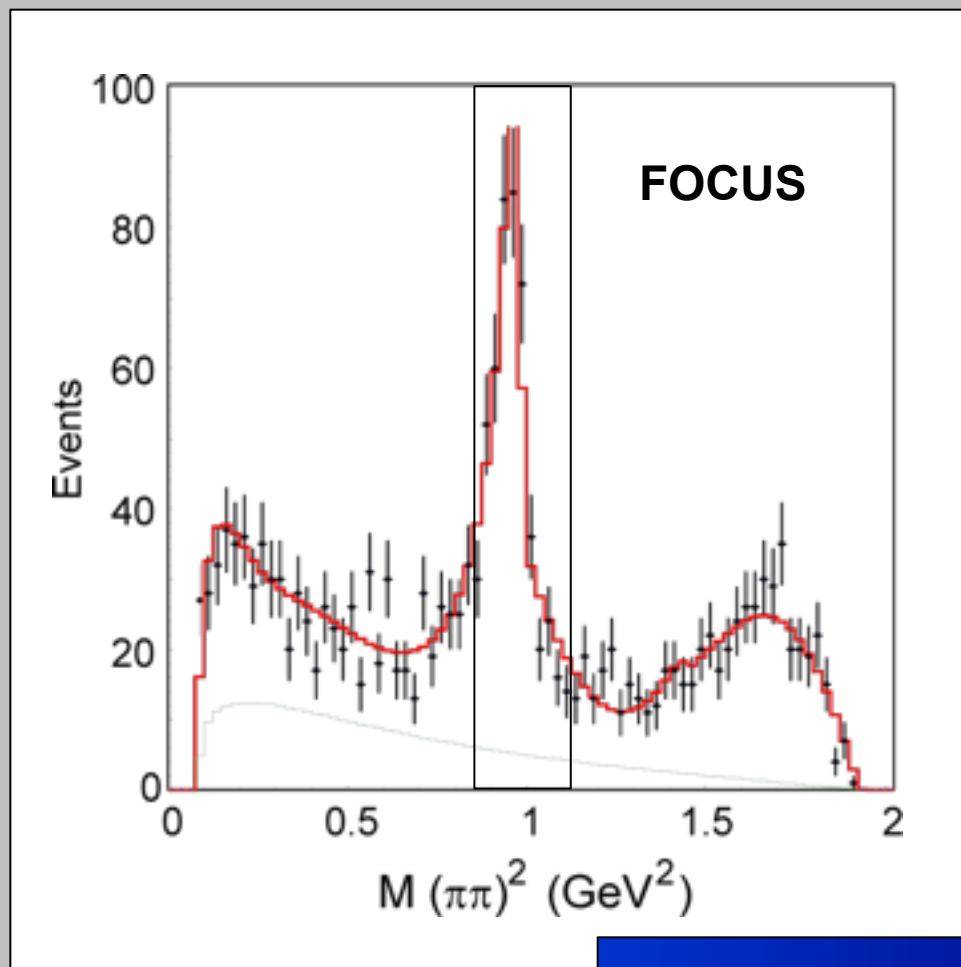


Quark state v Molecule

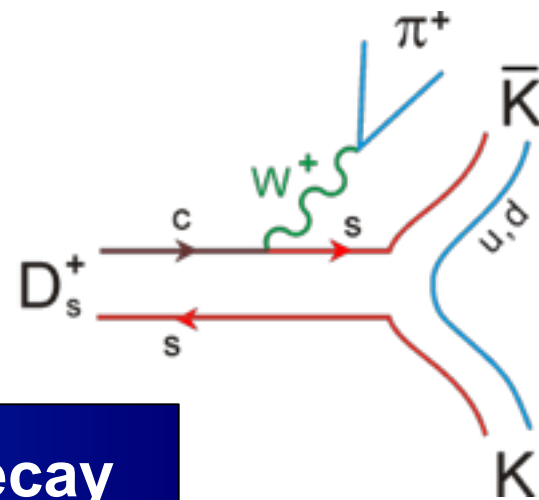
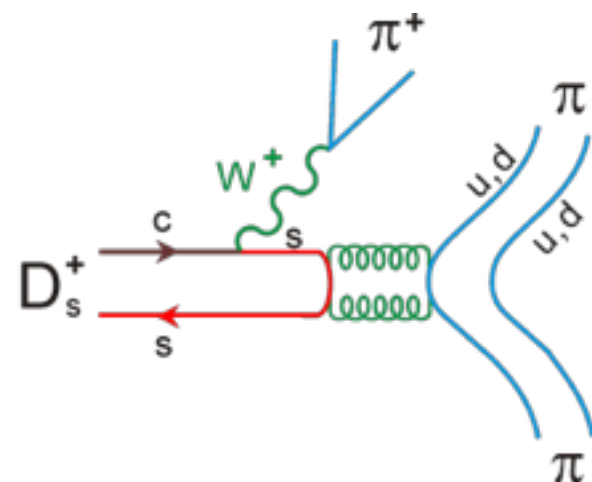


Weinberg
Morgan

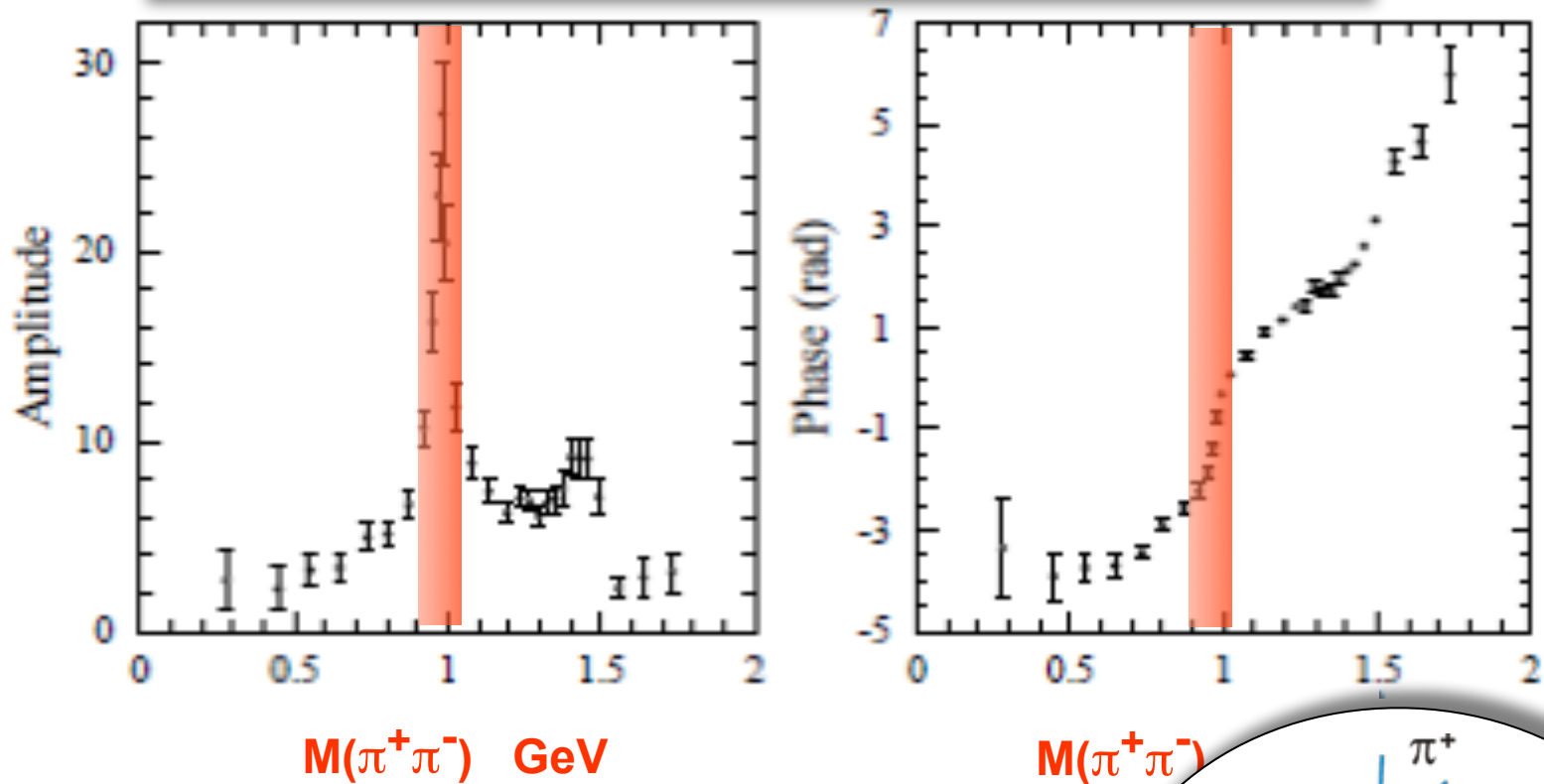
Heavy flavor decays



$D_s \rightarrow (MM) \pi$ decay

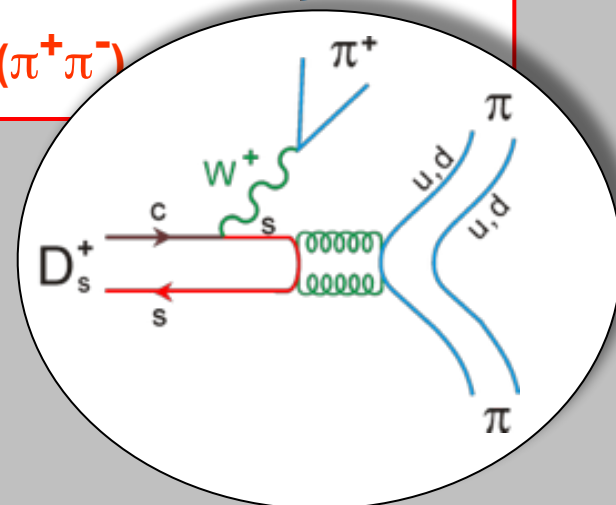


$\pi\pi$ S-wave in $D_s \rightarrow \pi(\pi\pi)$ decay

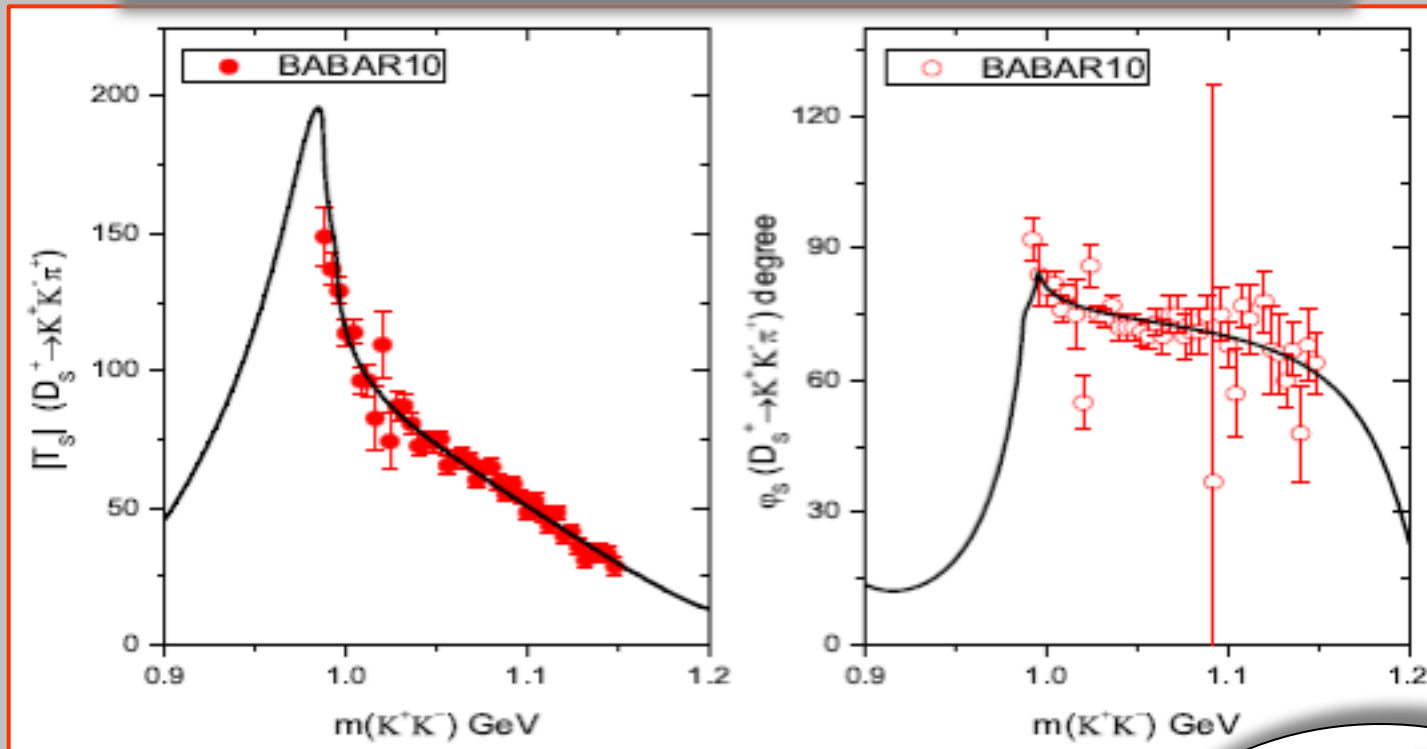


BaBar pwa

Pappagallo, P et al.

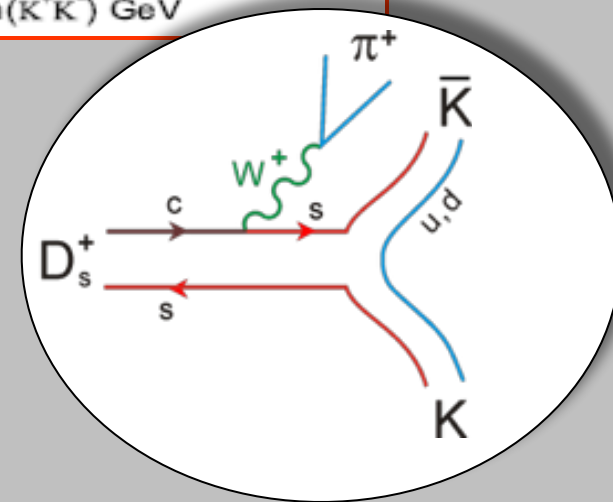


$\bar{K}K$ S-wave in $D_s \rightarrow \pi(\bar{K}K)$ decay

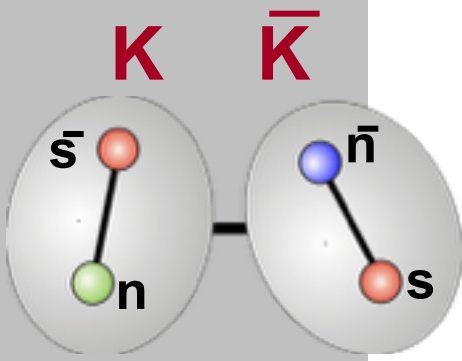


BaBar pwa

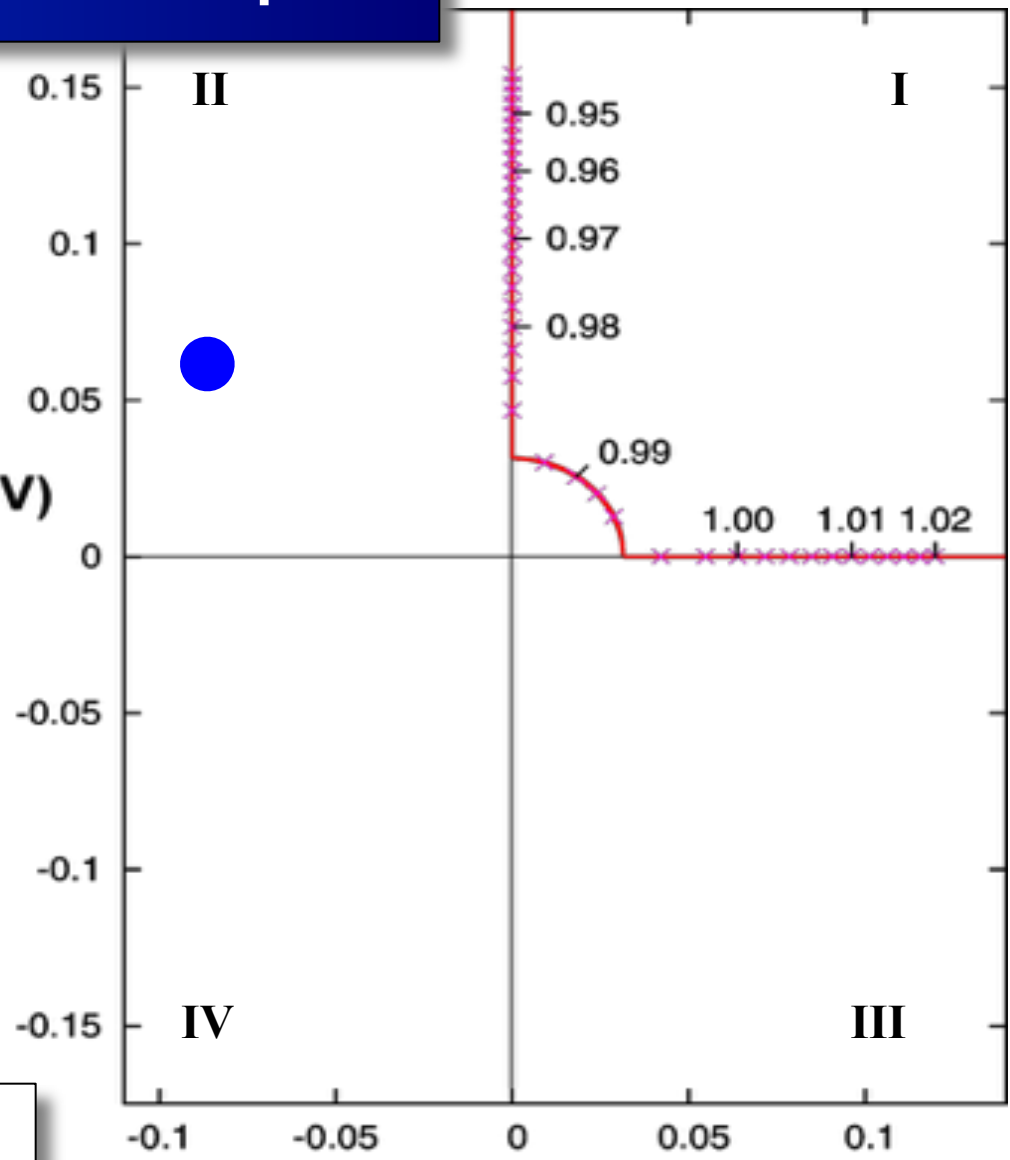
Pappagallo, P et al.



Jost function: 1 pole v 2 pole

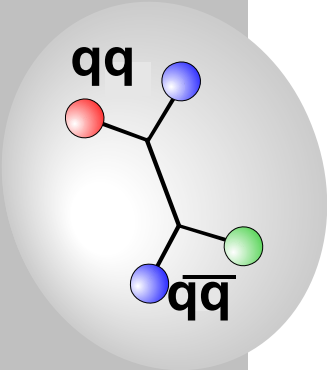
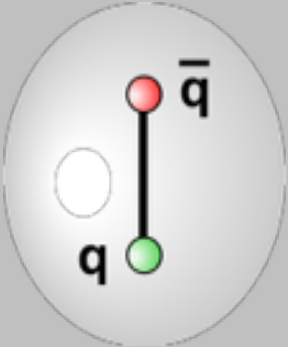


k_2 (GeV)

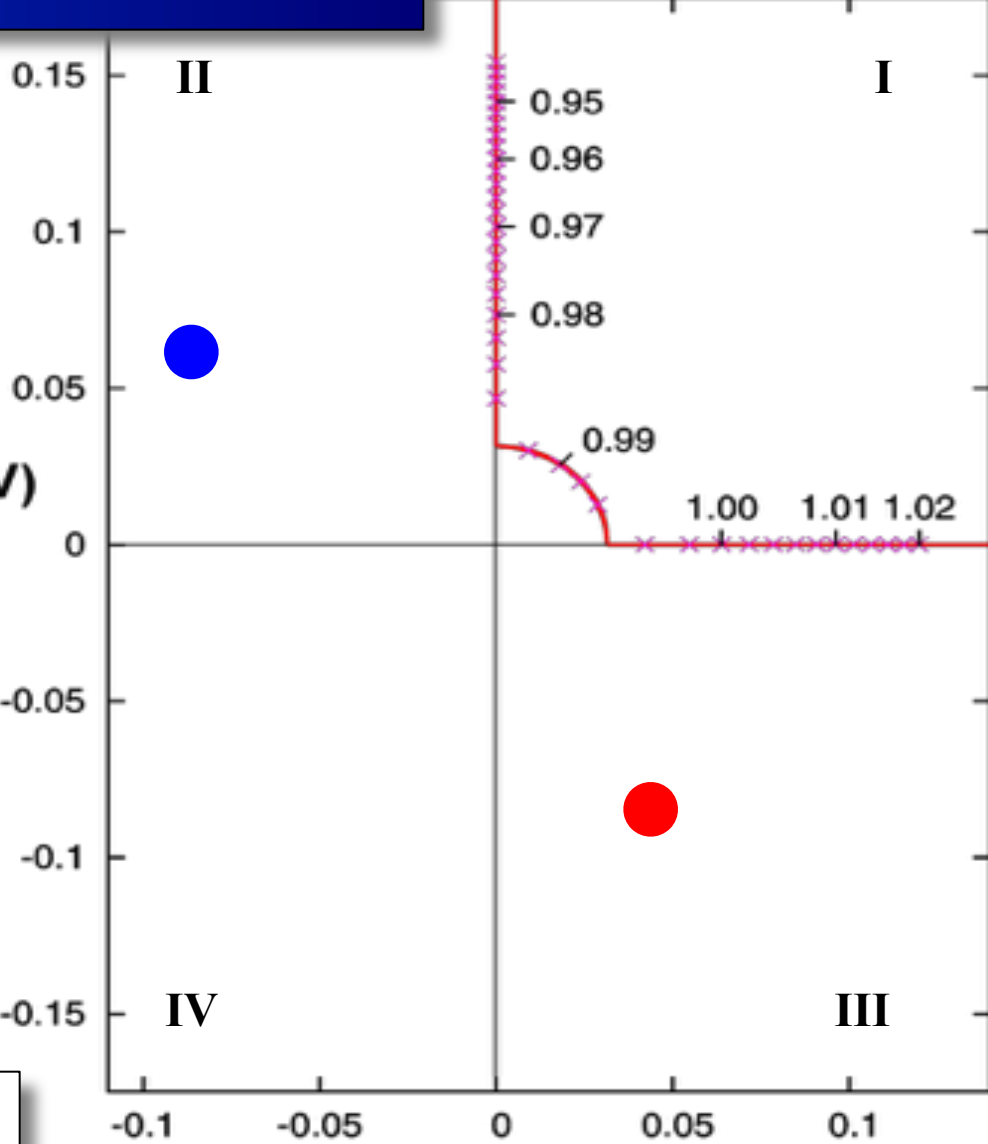


k_2 plane
 ($K\bar{K}$ c.m. momentum)

Jost function: 1 pole v 2 pole



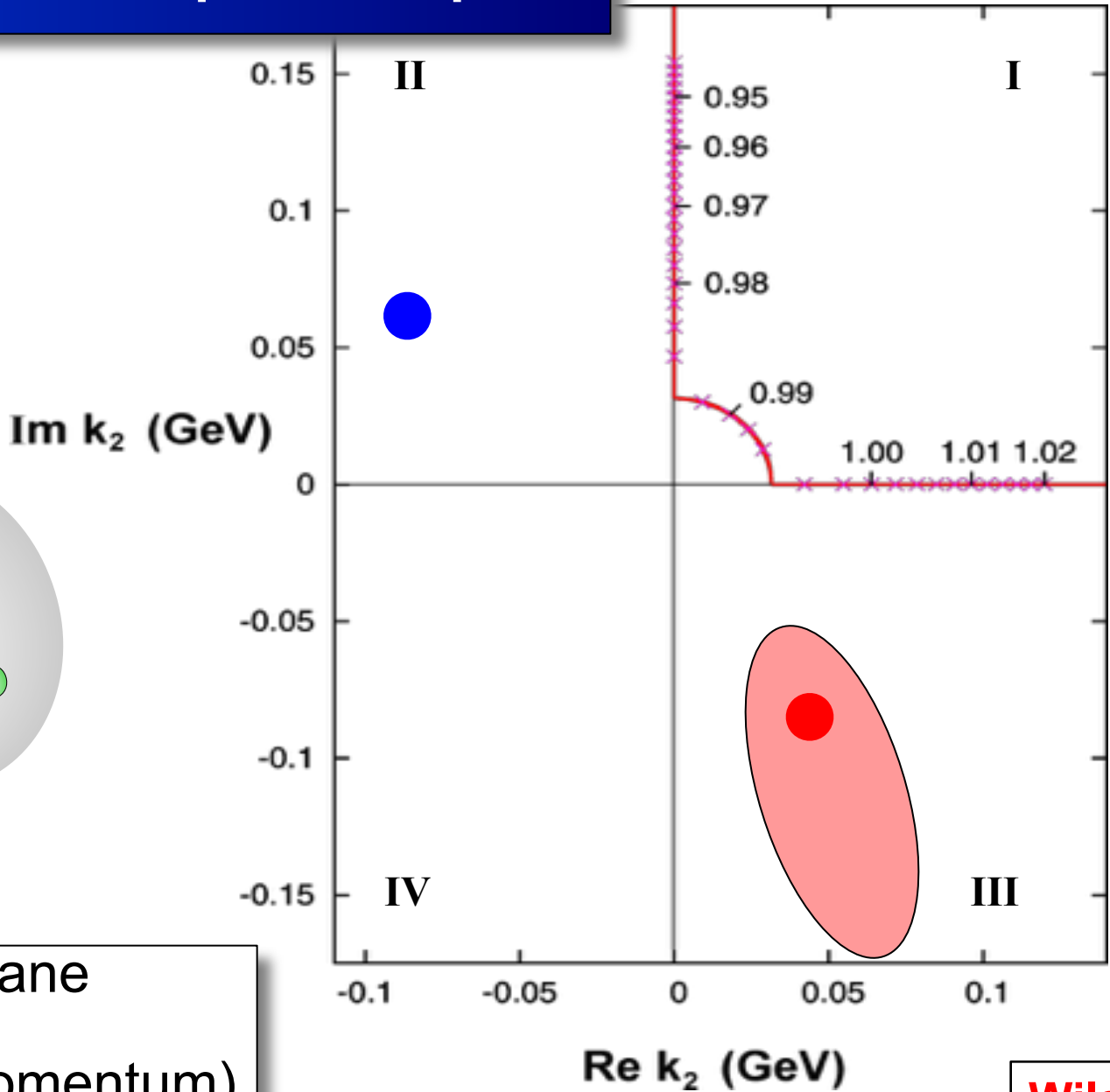
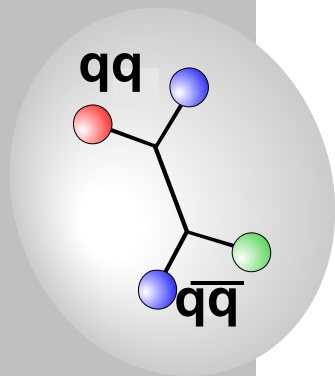
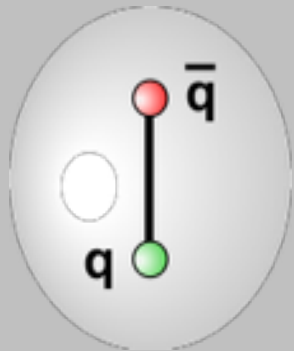
Im k_2 (GeV)



k_2 plane
($K\bar{K}$ c.m. momentum)

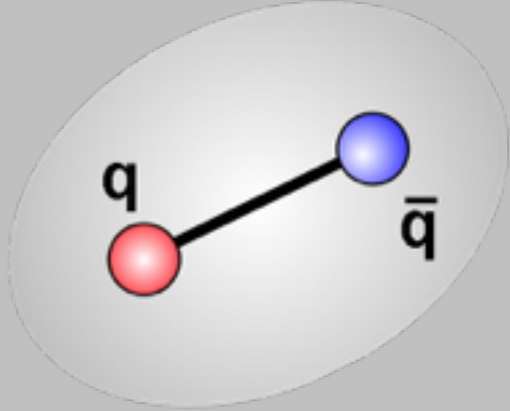
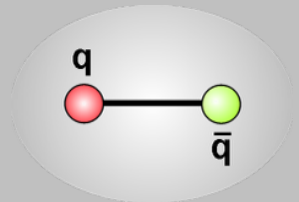
Wilson & P

Jost function: 1 pole v 2 pole

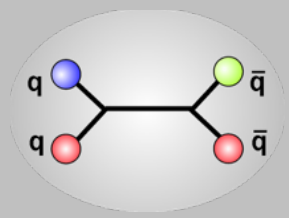


k_2 plane
($K\bar{K}$ c.m. momentum)

$f_0(980)$

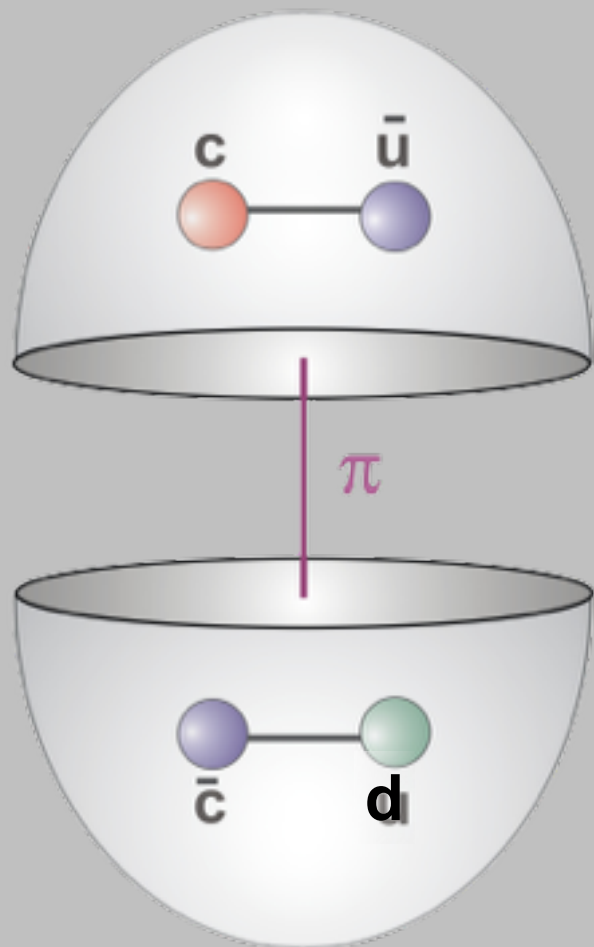


K

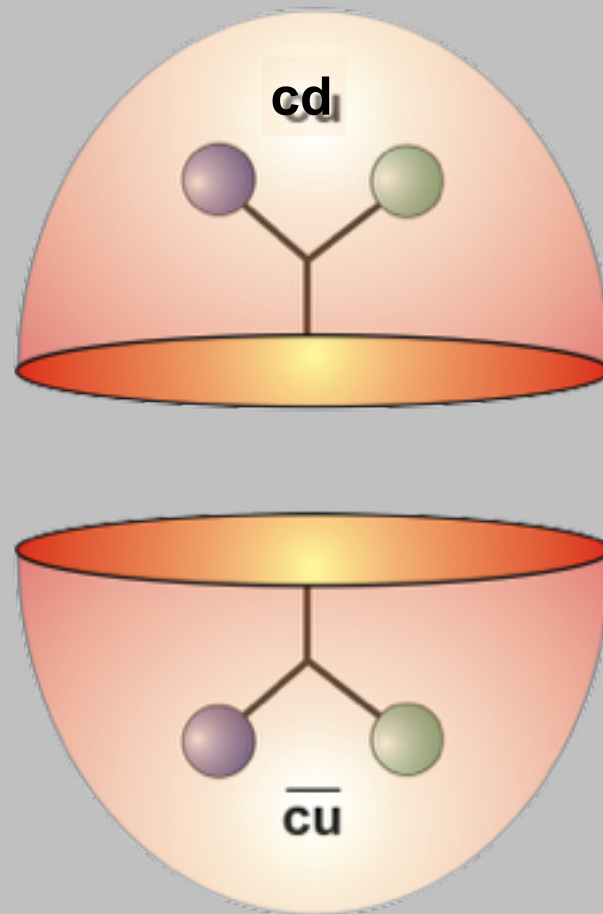


\bar{K}

molecule



tetraquark



Scalar meson multiplets

$q\bar{q}$

$q\bar{q}q\bar{q}$

$\bar{s}s$ ————— f_0

$\bar{s}n$ ————— K_0

$\bar{n}n$ ————— a_0/f_0

$\bar{s}s\bar{n}n$ ————— a_0/f_0

$\bar{s}n\bar{n}n$ ————— K_0 \mathbb{K}

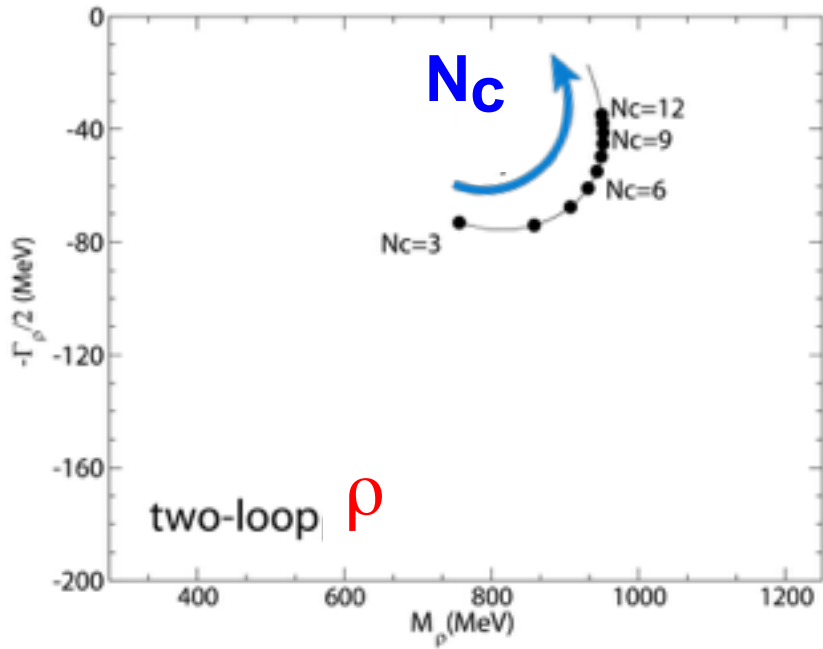
$\bar{n}n\bar{n}n$ ————— f_0 σ

N_c large \rightarrow stable

N_c large \rightarrow meson continuum

$1/N_c$ @ two loops

real axis



real axis

