

`Duality'

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In this case we know a lot about underlying dynamics - we are in the middle.

For good reasons we focus on semi-leptonic decays of beauty mesons & baryons (charm hadrons ??)

-- Misha, Kolya & me agreed there all the time;

-- for non-leptonic ones the situation was less clear

-- the situations are clearer for inclusive vs. exclusive decays

-- V_{xb} : V_{ub} vs. V_{cb} ;

Basics of Operator Product Expansion

$$\Gamma(H_Q \rightarrow f) = \sum_i c_i^{(f)}(KM, M_W, m_Q, \alpha_s, \mu) \langle H_Q | O_i | H_Q \rangle_{(\mu)}$$

- *short distance* dynamics \rightarrow coeff. $c_i^{(f)}$
- universal cast of **local** operators O_i
- $\langle H_Q | O_i | H_Q \rangle$ **inferred** from other **observables** or **LQCD!**
- expansion parameter

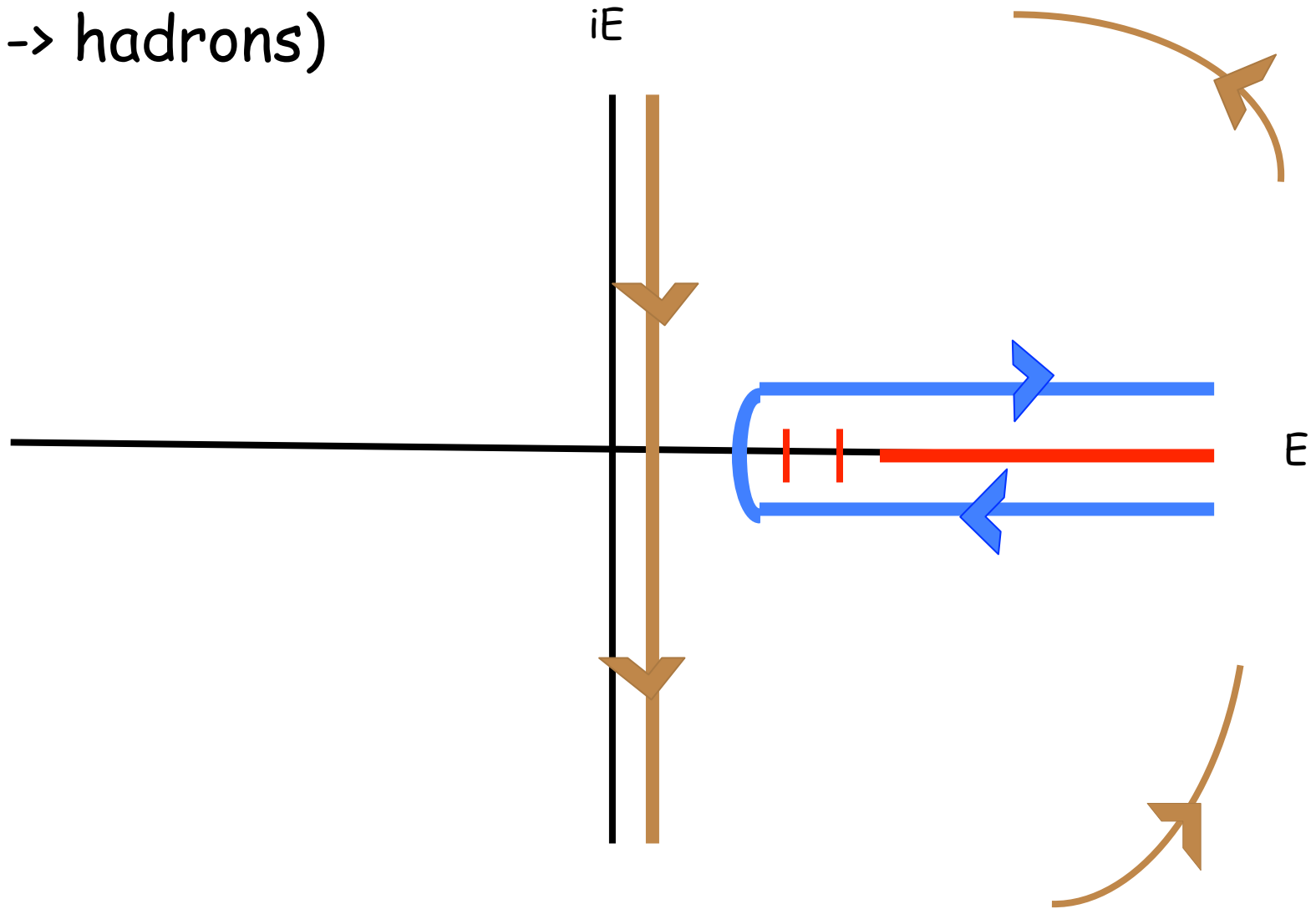
$$1/E_{\text{release}} \sim \begin{cases} 1/(m_b - m_c) & \text{for } b \rightarrow c \\ 1/m_b & \text{for } b \rightarrow u \end{cases}$$

- Wilson(ial) OPE: **auxiliary** scale μ s.t.

short distance $\langle \mu \rangle^{-1} <$ **long distance**

- $c_i \rightarrow$ **short distance** dynamics
- O_i active fields - **long distance** dynamics

$R(e^+e^- \rightarrow \text{hadrons})$



It needs some *judgment* where to apply
-- somewhat above thresholds etc. etc.

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👉 choose judiciously!

Scylla & Charybdis: $\Lambda_{\text{QCD}} \ll \mu \ll m_Q$ *

→ $\mu \ll m_Q$ → matrix elements calculable

→ $\alpha_S \ll 1$

→ $\mu \sim 1 \text{ GeV}$ okay for $Q = b!$ yet: $Q = c?$

leads to 'smart' pert. treatment

👉 treat as **physical** parameter (s. **sum rules**)

Novel **symbiosis** between different theoretical technologies for heavy flavour nonperturbative dynamics --

in particular between HQE and LQCD

$$\text{observables} = \sum_i c_i(\text{CKM}, m_Q, \alpha_S) \langle H_Q | O_i | H_Q \rangle$$

• it enhances the power of and confidence in both technologies by

- increasing the range of applications &
- providing more benchmarks

• duality \neq additional ad-hoc assumption

• duality violation in $\Gamma_{SL}(B) < 0.5\%$!

-- IB & N.Uraltsev, Int.J.Mod.Phys.A16(01)5201 (48 p!), arXiv: hep-ph/0106346

-- IB & Th. Mannel: arXiv: hep-ph/0212021v1 (13 p.) [it is easier to read]

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-- failure in $|V_{ub}|_{incl.}$ vs. $|V_{ub}|_{excl.}$?

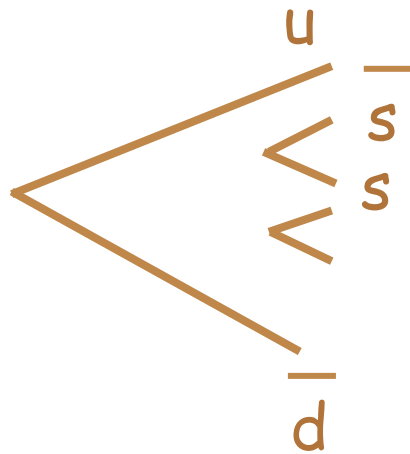
usually probed $B \rightarrow l \nu \pi$'s

but *not*

$B^- \rightarrow l^- \nu K^+ K^-, l^- \nu \overline{K^0} K^0, l^- \nu \overline{K} K \pi$

$B^0_d \rightarrow l^+ \nu K_S K^-, l^- \nu \overline{K} K \pi$

Real $|V_{ub}|_{incl.}$ might be smaller than thought before



due re-scattering!

at least novel lessons of non-perturb. QCD

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