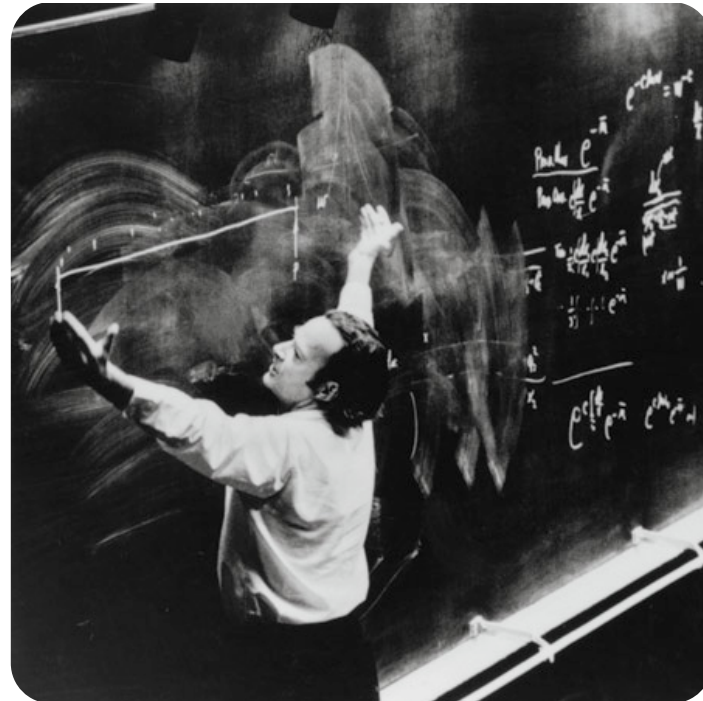


# Beyond the SM 3/4



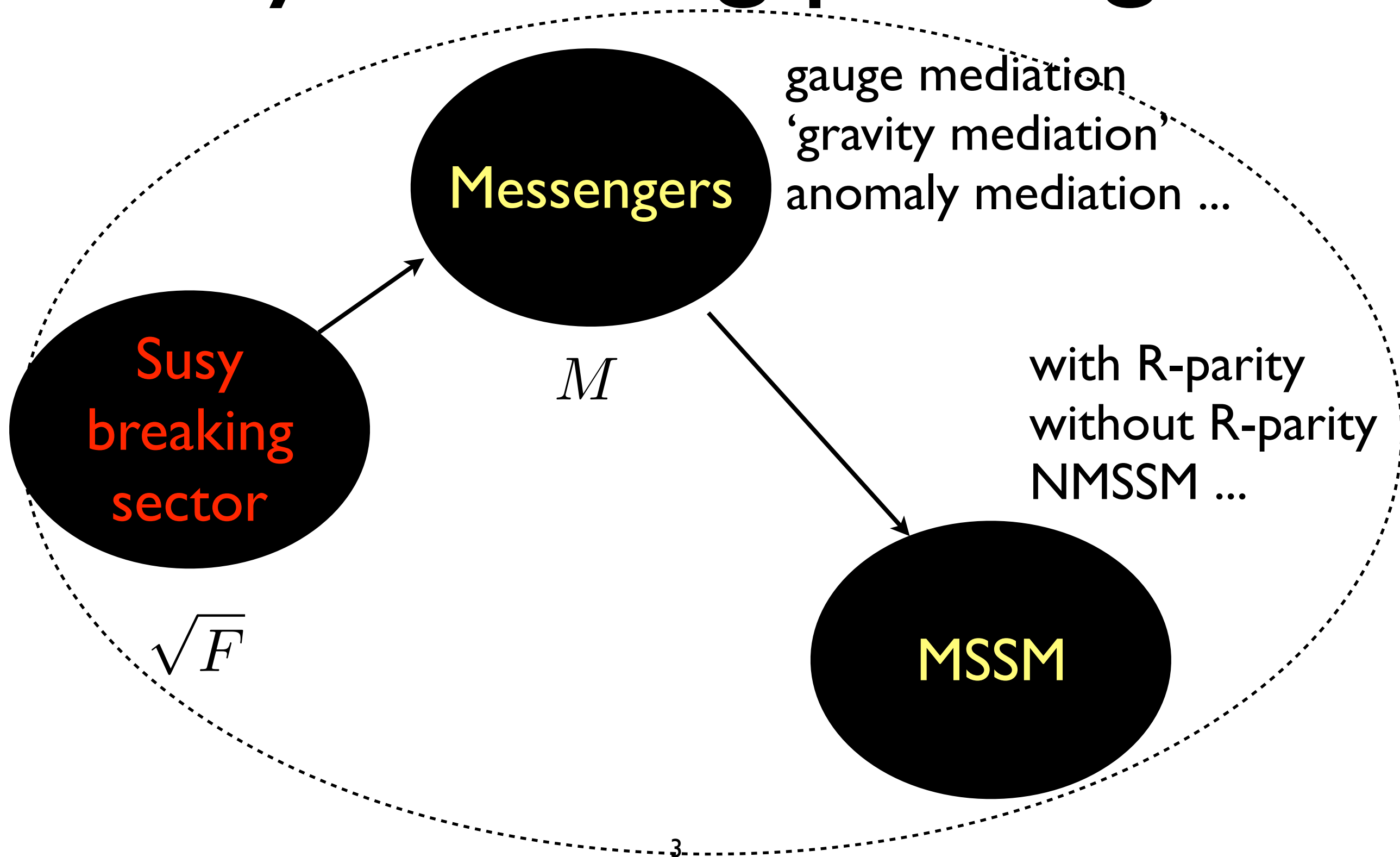
Andreas Weiler  
(TU Munich)

Summer school Slovenia  
2019-26-8

recap...

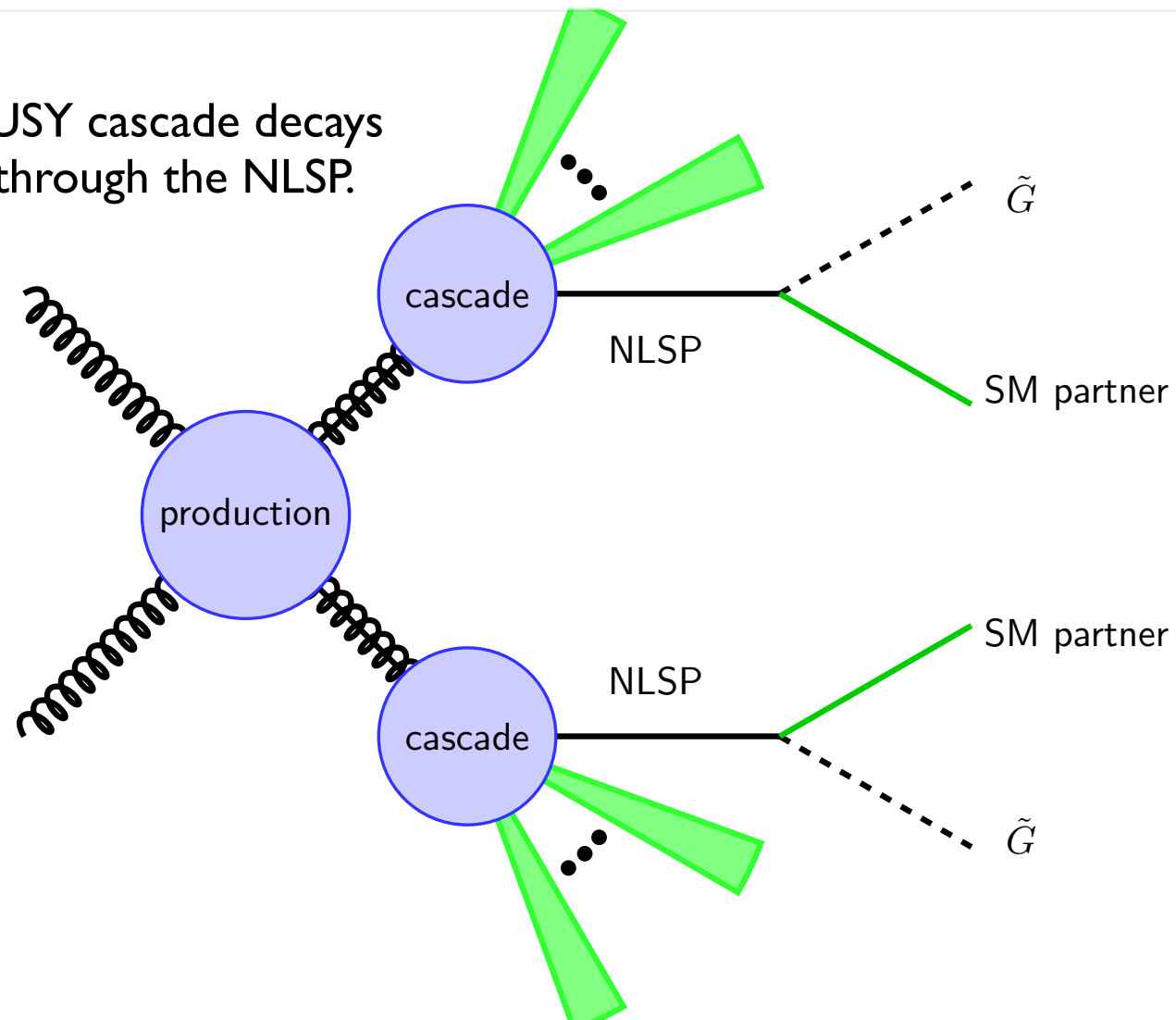


# Susy breaking paradigm



# Susy breaking paradigm

All SUSY cascade decays  
pass through the NLSP.



Susy  
breaking  
secto

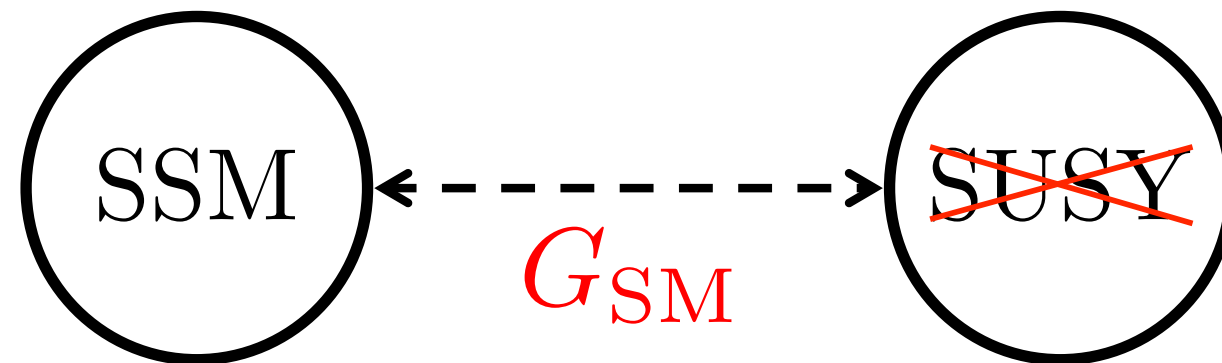
$\sqrt{F}$

on,  
tion ...

n R-parity  
hout R-parity  
SSM ...

# Gauge Mediation

see e.g. Giudice/Rattazzi review

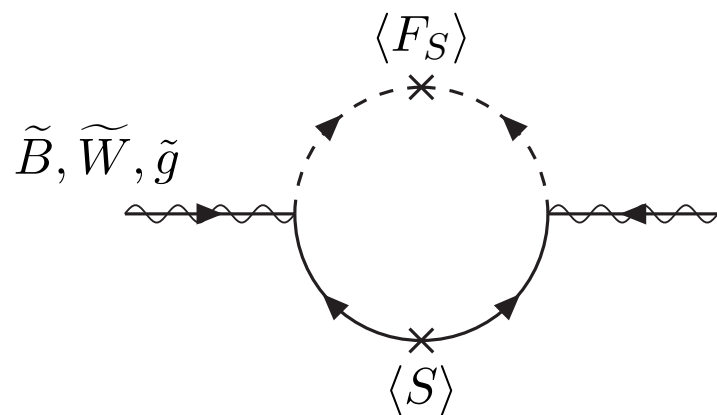


$$G_{SM} = SU(3) \times SU(2) \times U(1)$$

Degenerate quarks at the messenger scale, no flavor problem.

# Gauge mediation

*1 loop gaugino masses*



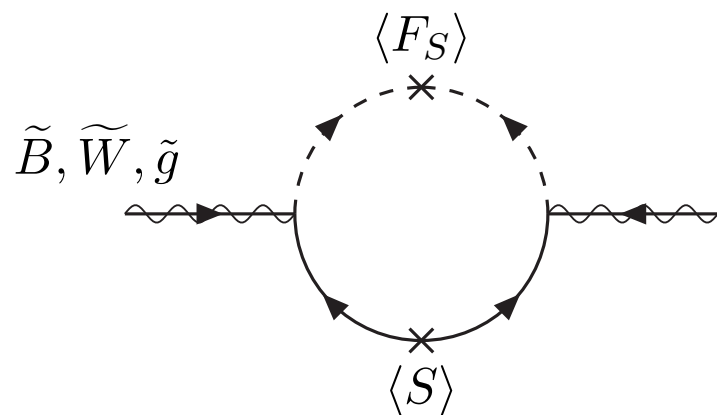
$$M_a = \frac{\alpha_a}{4\pi} M_S, \quad M_S = \frac{\langle F_S \rangle}{\langle S \rangle}$$

**Messengers (S)** feel SUSY breaking, charged under SM gauge symmetries.

$\sqrt{F}$  **Susy breaking order parameter**

# Gauge mediation

*1 loop gaugino masses*

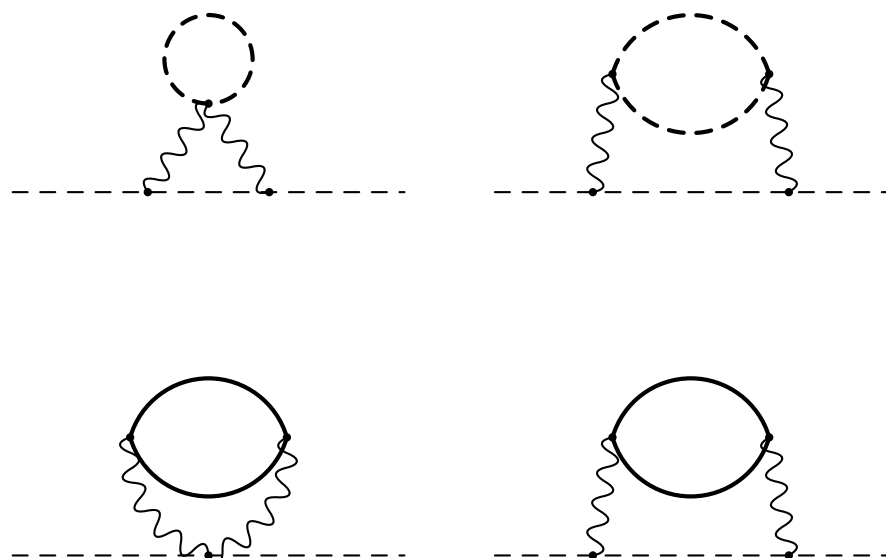


$$M_a = \frac{\alpha_a}{4\pi} M_S, \quad M_S = \frac{\langle F_S \rangle}{\langle S \rangle}$$

**Messengers (S)** feel SUSY breaking, charged under SM gauge symmetries.

$\sqrt{F}$  **Susy breaking order parameter**

*2 loop squark masses*



+ ....

$$m_{\text{scalar}}^2 = \left( \frac{\alpha}{4\pi} \right)^2 M_S^2$$

# Gravitino

- SUSY spontaneously broken: goldstino
- Fermionic component of super-field w/ vev
- Becomes longitudinal component of gravitino (spin 3/2)
- If  $\langle F \rangle \ll M_{\text{Pl}}$  (e.g gauge med., gravitino LSP): gravitino LSP & NLSP can be long lived

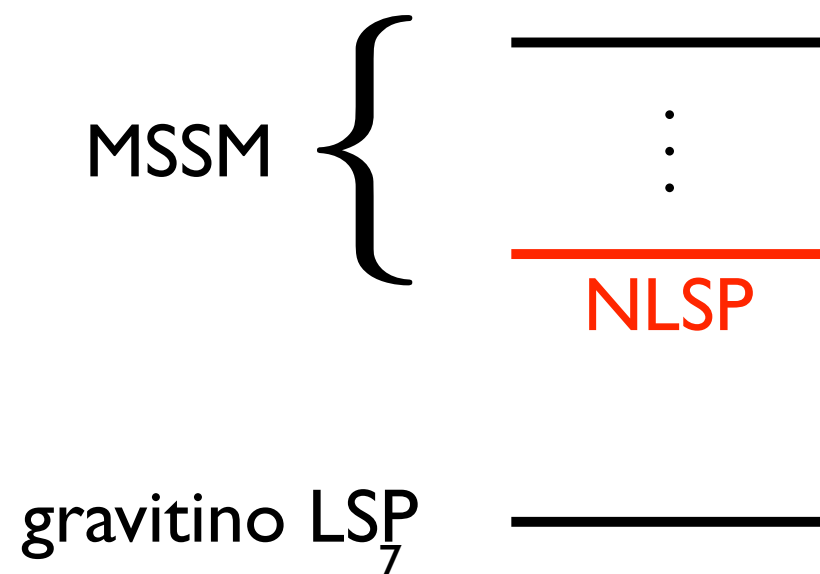
$$\Gamma(\overset{\text{sparticle}}{\tilde{X}} \rightarrow X \overset{\text{particle gravitino}}{\tilde{G}}) = \frac{m_{\tilde{X}}^5}{16\pi \langle F \rangle^2} \left( 1 - \frac{m_X^2}{m_{\tilde{X}}^2} \right)^4$$

# Gauge mediation

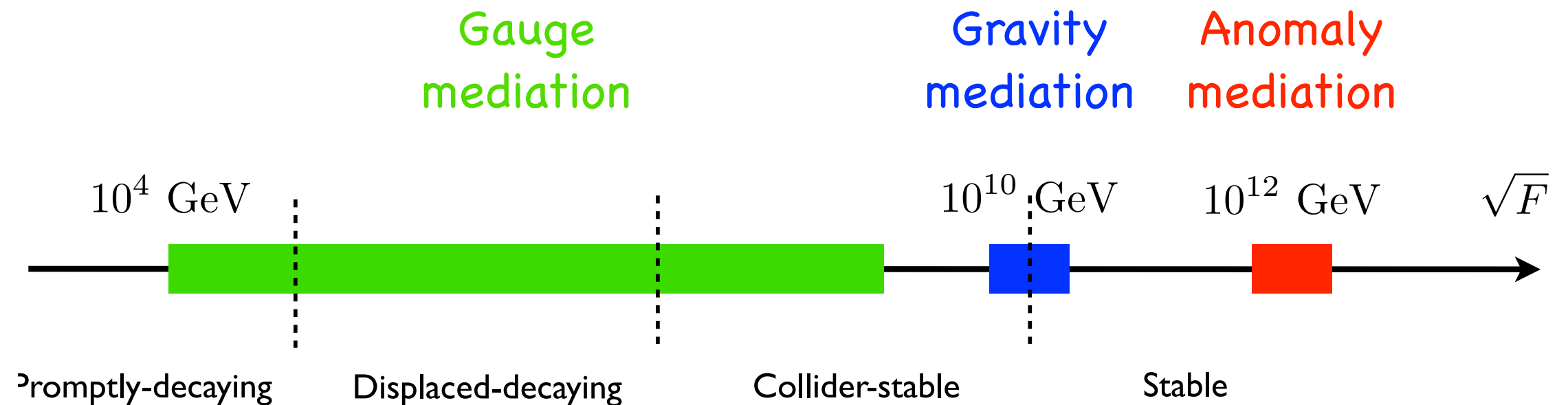
- Gravitino LSP is a universal prediction of gauge mediation models:

$$m_{3/2} = \frac{F}{\sqrt{3}M_{pl}} \quad (\sim \text{eV} - \text{GeV})$$

- Lightest MSSM sparticle becomes the **next-to-lightest superpartner (NLSP)**.



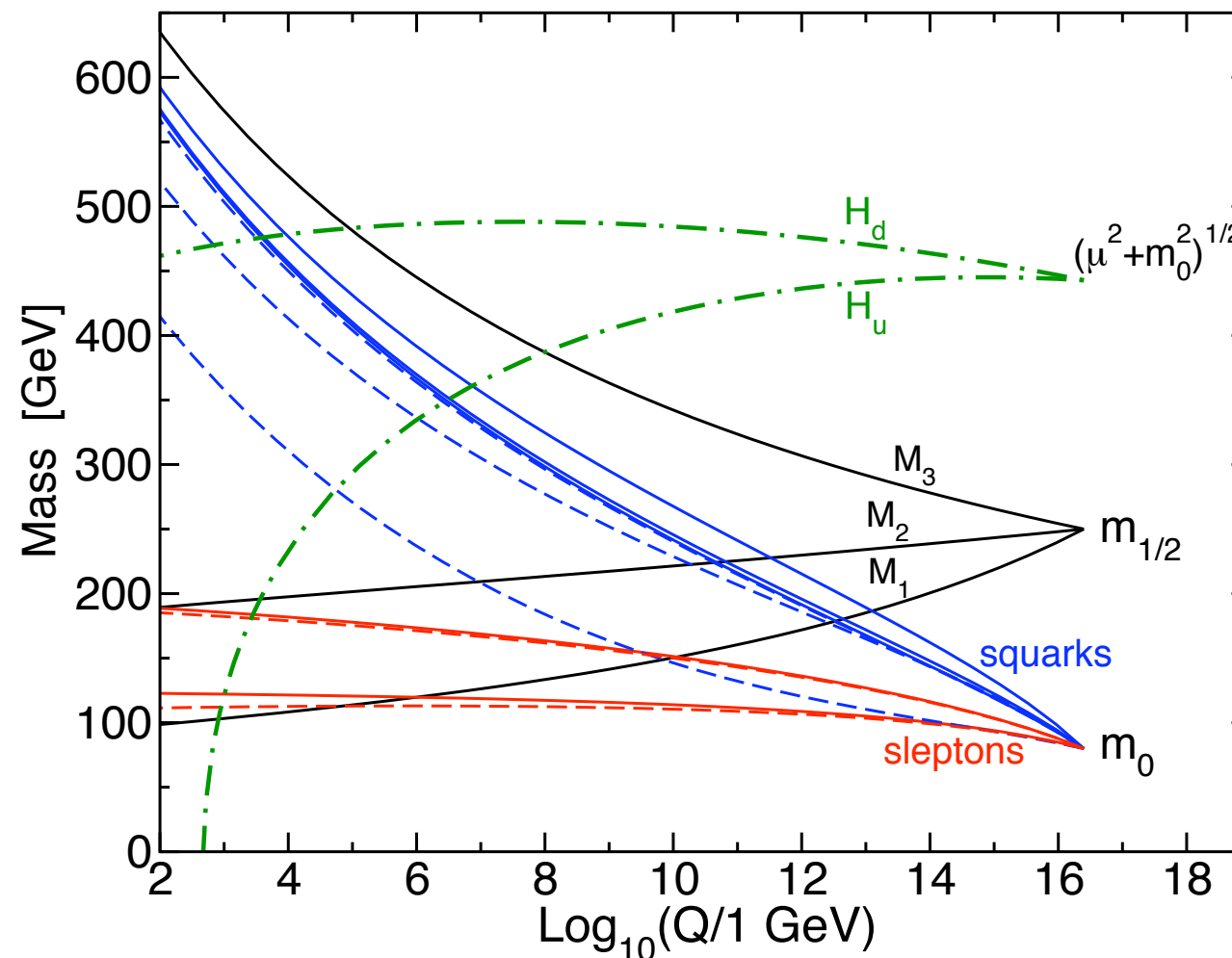
The scale of SUSY breaking determines the mediation mechanism.



It also determines the behavior of the lightest MSSM superpartner.



# RGE evolution



radiative  
EWSB

RGE evolution: masses evolve with scale  
colored particles 'run' faster, large  $\mathcal{O}(\text{several})$   
corrections

# Higgs potential

$$\begin{aligned} V_H = & (\mu^2 + m_{H_u}^2) |H_u|^2 + (\mu^2 + m_{H_d}^2) |H_d|^2 \\ & - B_\mu H_u \cdot H_d + \text{h.c.} + \frac{1}{2} g^2 |H_u^\dagger H_d|^2 \\ & + \frac{1}{8} (g^2 + g'^2) (|H_u|^2 - |H_d|^2)^2 \end{aligned}$$

# Neutral Higgs potential

$$V = (\mu_1^2 + m_{H_u}^2) |H_u^0|^2 + (\mu_2^2 + m_{H_d}^2) |H_d^0|^2 - B_\mu (H_u^0 H_d^0 + \text{h.c.}) + \frac{1}{8} (g^2 + g'^2) (|H_u^0|^2 - |H_d^0|^2)^2$$

quartic fixed by gauge interactions!

short digression →

# Super YM

So full Lagrangian:

$$\mathcal{L} = -\frac{1}{4g^2} \text{Tr} \left( W^\alpha W_\alpha \Big|_{\theta^2} + \bar{W}_{\dot{\alpha}} \bar{W}^{\dot{\alpha}} \Big|_{\bar{\theta}^2} \right) \\ + \phi^\dagger e^V \phi \Big|_{\theta^2 \bar{\theta}^2} + W(\phi) \Big|_{\theta^2} + \text{h.c.}$$

# Super YM

So full Lagrangian: <sup>gauge trace</sup>

$$\mathcal{L} = -\frac{1}{4g^2} \text{Tr} \left( W^\alpha W_\alpha|_{\theta^2} + \bar{W}_{\dot{\alpha}} \bar{W}^{\dot{\alpha}}|_{\bar{\theta}^2} \right) \\ + \phi^\dagger e^V \phi|_{\theta^2 \bar{\theta}^2} + W(\phi)|_{\theta^2} + \text{h.c.}$$

$$\mathcal{L} = \frac{1}{4g^2} \left( W^a{}_\alpha W^a{}^\alpha|_{\theta^2} + \bar{W}^a{}_{\dot{\alpha}} \bar{W}^a{}^{\dot{\alpha}}|_{\bar{\theta}^2} \right)$$

$$= -\frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} + i \bar{\lambda}^a D_\mu \bar{\sigma}^\mu \lambda^a + \frac{1}{2} D^a D^a$$

# Super YM

So full Lagrangian:

$$\mathcal{L} = -\frac{1}{4g^2} \text{Tr} \left( W^\alpha W_\alpha \Big|_{\theta^2} + \bar{W}_{\dot{\alpha}} \bar{W}^{\dot{\alpha}} \Big|_{\bar{\theta}^2} \right) + \phi^\dagger e^V \phi \Big|_{\theta^2 \bar{\theta}^2} + W(\phi) \Big|_{\theta^2} + \text{h.c.}$$

← gauge trace

$$\mathcal{L} = \frac{1}{4g^2} \left( W^a{}_\alpha W^{\alpha}{}_a \Big|_{\theta^2} + \bar{W}^{\dot{a}}{}_{\dot{\alpha}} \bar{W}^{\dot{\alpha}}{}_{\dot{a}} \Big|_{\bar{\theta}^2} \right) = -\frac{1}{4} F^a_{\mu\nu} F^{a\mu\nu} + i \bar{\lambda}^a D_\mu \bar{\sigma}^\mu \lambda^a + \frac{1}{2} D^a D^a$$

$$\phi^\dagger e^V \phi \Big|_{\theta^2 \bar{\theta}^2} = |D_\mu \psi|^2 + i \bar{\psi} D_\mu \bar{\sigma}^\mu \psi + F^* F + i \sqrt{2} (\psi^* T^a \lambda^a \psi + \text{h.c.}) + \frac{1}{2} \psi^* T^a D^a \psi$$

Need to integrate out  $P^a$   $\downarrow$  new source for  
Scalar potential.

Full scalar potential

$$V_D = \frac{1}{2} g^2 \sum_a \left| \sum_{\psi} \psi_i^* T^a \psi_i \right|^2$$

$$V_F = \sum_i \left| \frac{\partial W}{\partial \psi_i} \right|^2$$

$V(\psi) \geq 0$  as expected...

# Neutral Higgs potential

$$V = (\mu_1^2 + m_{H_u}^2) |H_u^0|^2 + (\mu_2^2 + m_{H_d}^2) |H_d^0|^2 - B_\mu (H_u^0 H_d^0 + \text{h.c.}) + \frac{1}{8} (g^2 + g'^2) (|H_u^0|^2 - |H_d^0|^2)^2$$

quartic fixed by gauge interactions!



# Higgs spectrum

$$V(H_u^0, H_d^0) = (|\mu|^2 + m_{H_u}^2)|H_u^0|^2 + (|\mu|^2 + m_{H_d}^2)|H_d^0|^2 - (b H_u^0 H_d^0 + h.c.) + \frac{1}{8}(g^2 + g'^2)(|H_u^0|^2 - |H_d^0|^2)^2.$$

- Supersymmetry: gauge interactions always come with quartic scalar interactions ( $D$ -term potential)

$$\frac{1}{8} (g^2 + g'^2) \left( |H_u^0|^2 - |H_d^0|^2 \right)^2$$

- Implication: Higgs quartic related to gauge couplings, which also determine  $W, Z$  masses: tree-level bound

$$m_h \leq m_Z \cos(2\beta)$$

# Higgs spectrum

$$V(H_u^0, H_d^0) = (|\mu|^2 + m_{H_u}^2)|H_u^0|^2 + (|\mu|^2 + m_{H_d}^2)|H_d^0|^2 - (b H_u^0 H_d^0 + h.c.) + \frac{1}{8}(g^2 + g'^2)(|H_u^0|^2 - |H_d^0|^2)^2.$$

- Supersymmetry: gauge interactions always come with quartic scalar interactions ( $D$ -term potential)

$$\frac{1}{8} (g^2 + g'^2) \left( |H_u^0|^2 - |H_d^0|^2 \right)^2$$

- Implication: Higgs also determine  $W$

**Higgs mass maximized at large  $\tan \beta$ .**

$$m_h \leq m_Z \cos(2\beta)$$

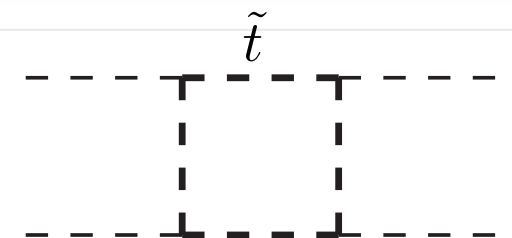
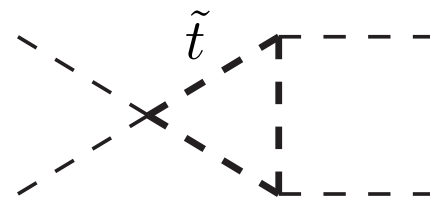
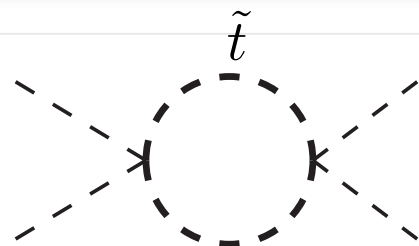
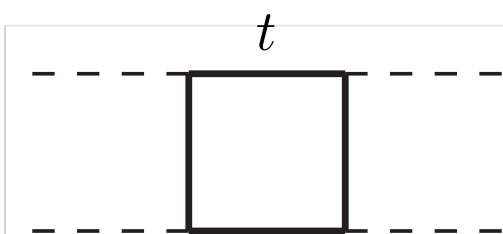
# Susy and the 125 GeV Higgs

MSSM:

$$m_h^2 = m_Z^2 c_{2\beta}^2$$

Haber, Hempfling '91

$$+ \frac{3m_t^4}{4\pi^2 v^2} \left( \log \left( \frac{M_S^2}{m_t^2} \right) + \frac{X_t^2}{M_S^2} \left( 1 - \frac{X_t^2}{12M_S^2} \right) \right)$$



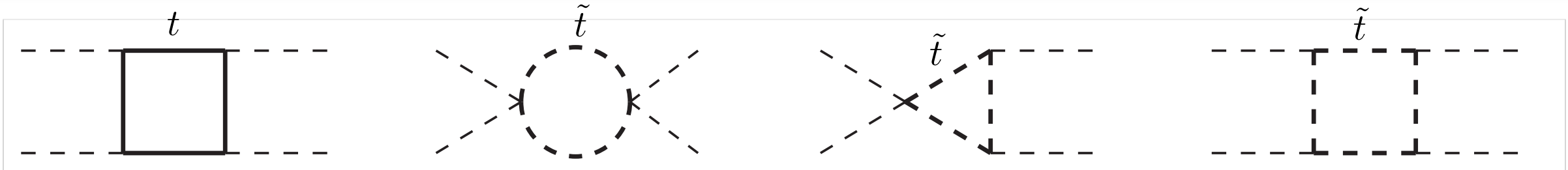
# Susy and the 125 GeV Higgs

MSSM:

tree-level bound  $< M_Z$

$$m_h^2 = m_Z^2 c_{2\beta}^2 + \frac{3m_t^4}{4\pi^2 v^2} \left( \log \left( \frac{M_S^2}{m_t^2} \right) + \frac{X_t^2}{M_S^2} \left( 1 - \frac{X_t^2}{12M_S^2} \right) \right)$$

Haber, Hempfling '91



# Susy and the 125 GeV Higgs

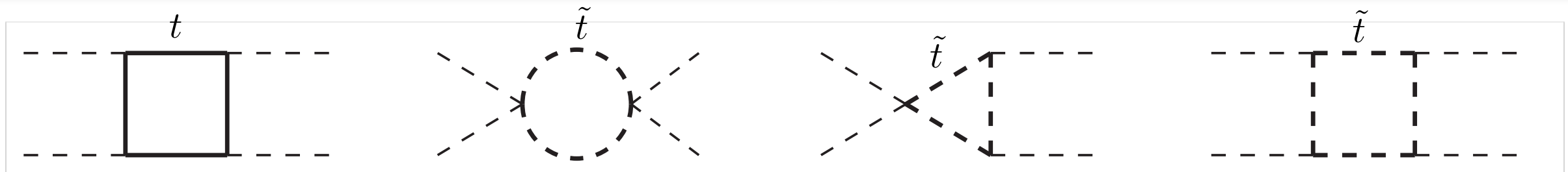
MSSM:

$$m_h^2 = m_Z^2 c_{2\beta}^2$$

$$+ \frac{3m_t^4}{4\pi^2 v^2} \left( \log \left( \frac{M_S^2}{m_t^2} \right) + \frac{X_t^2}{M_S^2} \left( 1 - \frac{X_t^2}{12M_S^2} \right) \right)$$

**Logarithmic** growth with  $M_{\text{SUSY}}$

91





# Susy and the 125 GeV Higgs

MSSM:

$$m_h^2 = m_Z^2 c_{2\beta}^2$$

$$+ \frac{3m_t^4}{4\pi^2 v^2} \left( \log \left( \frac{M_S^2}{m_t^2} \right) + \frac{X_t^2}{M_S^2} \left( 1 - \frac{X_t^2}{12M_S^2} \right) \right)$$

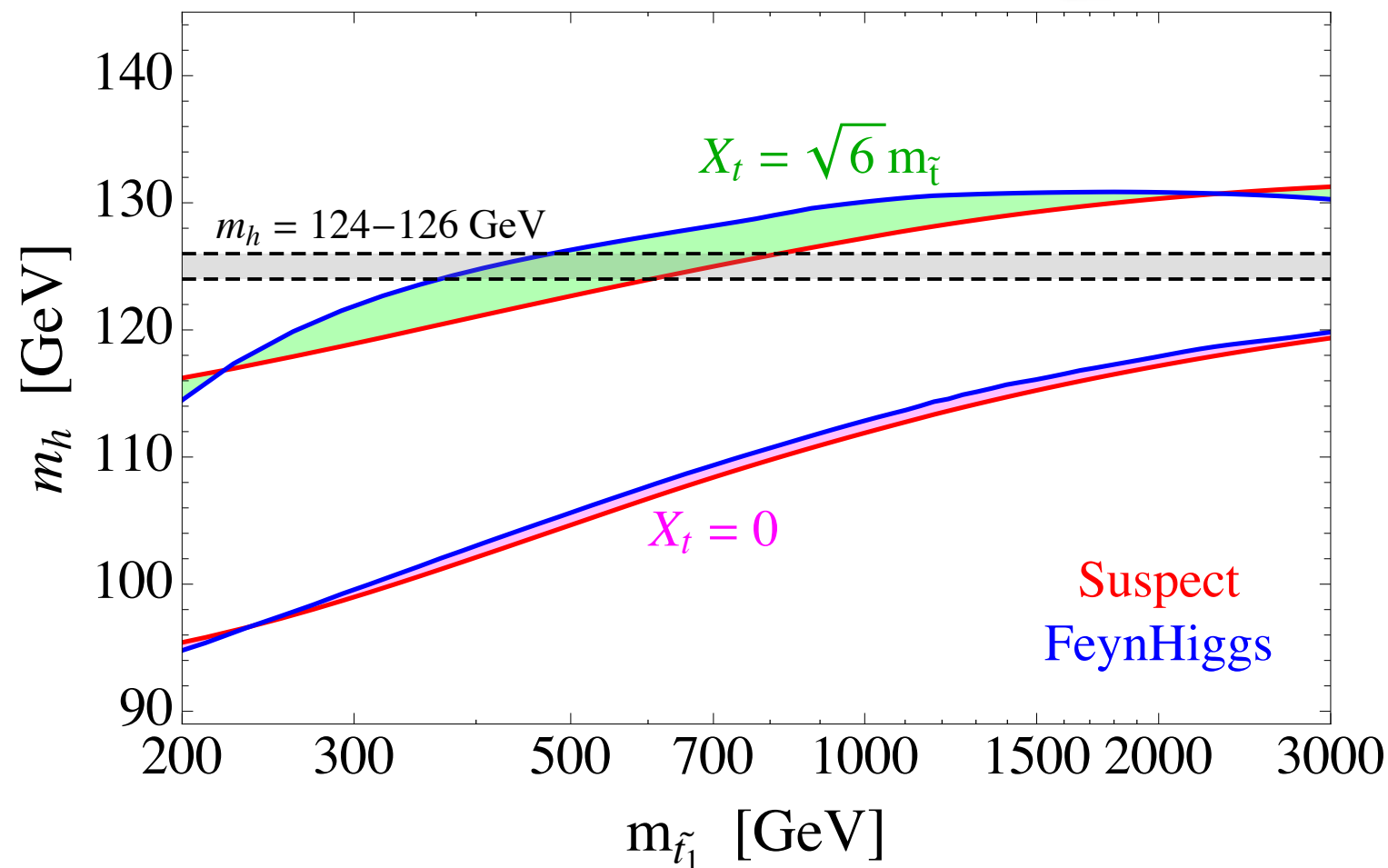
**Quadratic** term from stop mixing

more: Haber, Hempfling, Hoang, Ellis, Ridolfi, Zwirner, Casas, Espinosa, Quiros, Riotto, Carena, Wagner, Degrandi, Heinemeyer, Hollik, Slavich, Weiglein

# MSSM vs. the 125 GeV Higgs

$$X_t = A_t - \mu \cot \beta$$

MSSM Higgs Mass



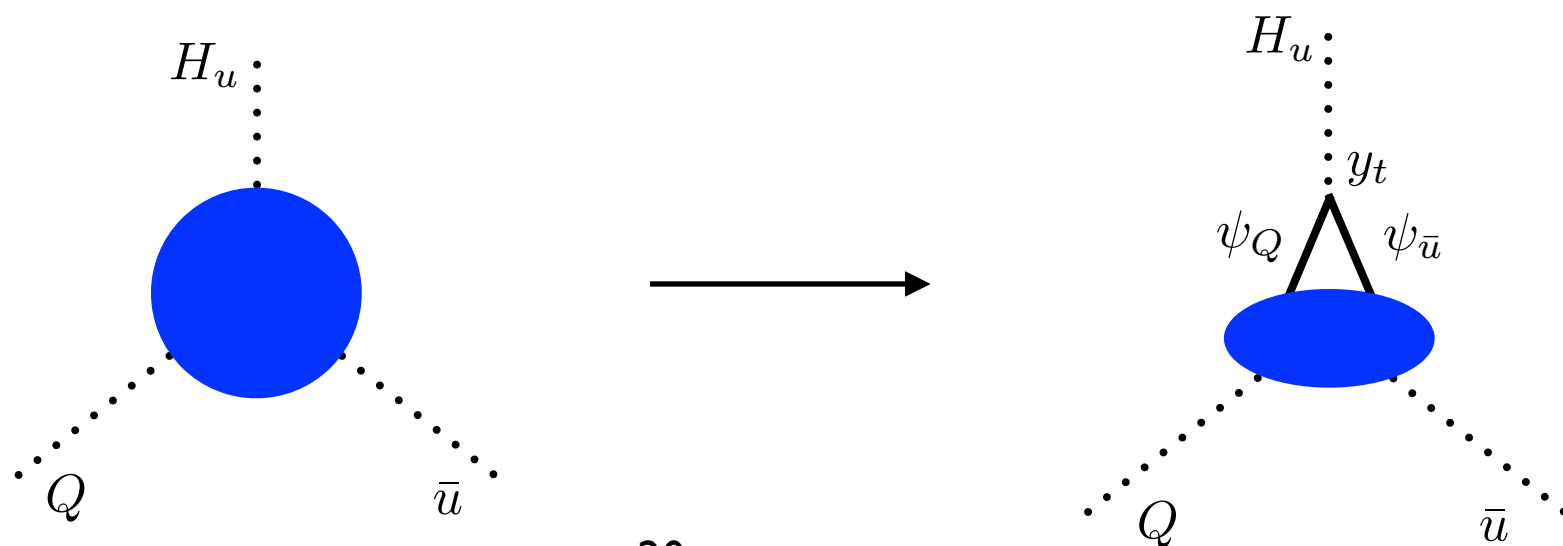
$$\mathcal{L} \supset A_t Q \bar{u} H_u + c.c.$$

# A terms in gauge mediation?

$$\mathcal{L} \supset A_t Q \bar{u} H_u + c.c.$$

Like Yukawa couplings, break chiral (flavor) symmetries

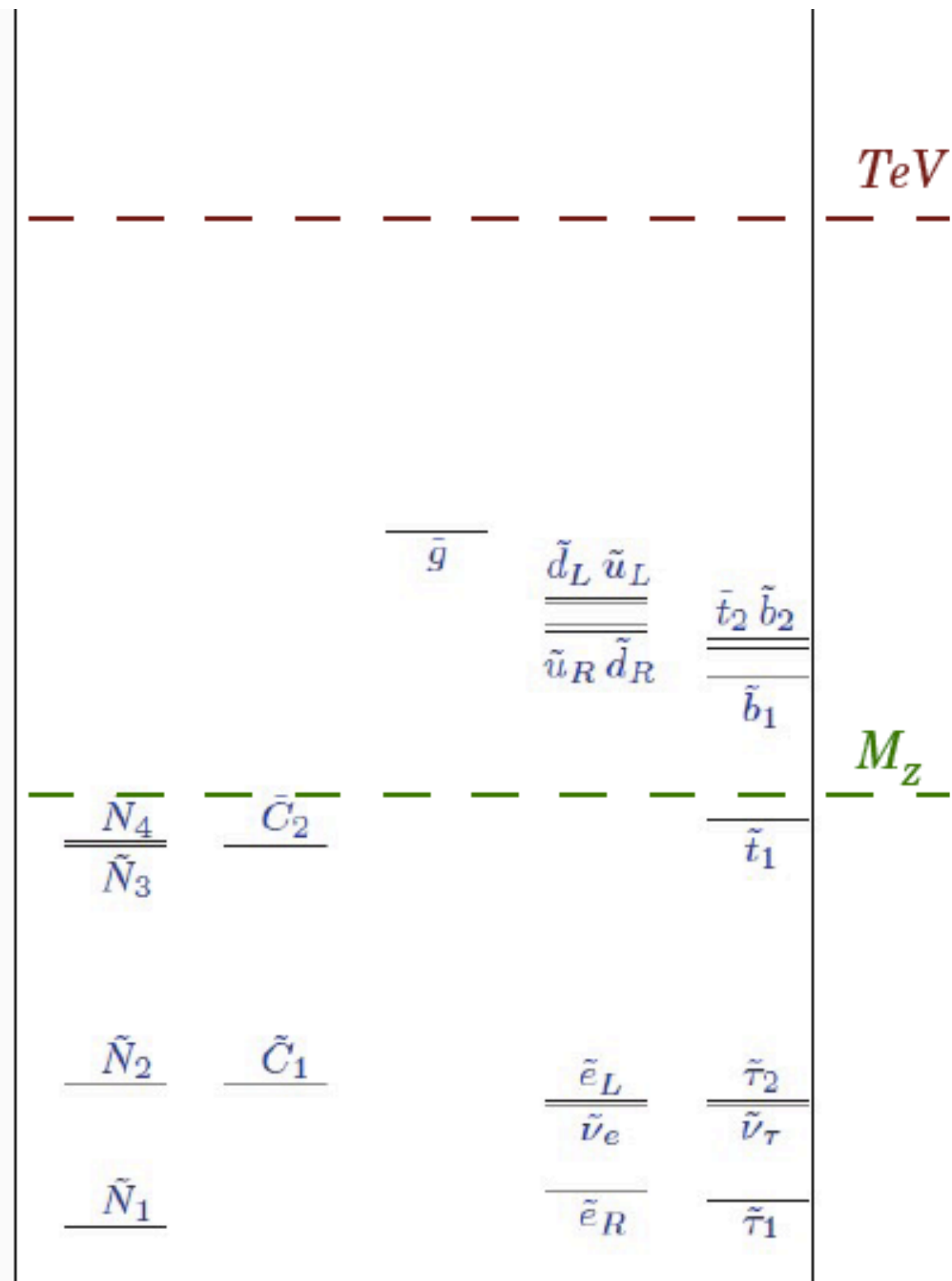
Can not be induced by gauge interactions alone (those leave chiral symmetries intact)  $\rightarrow$





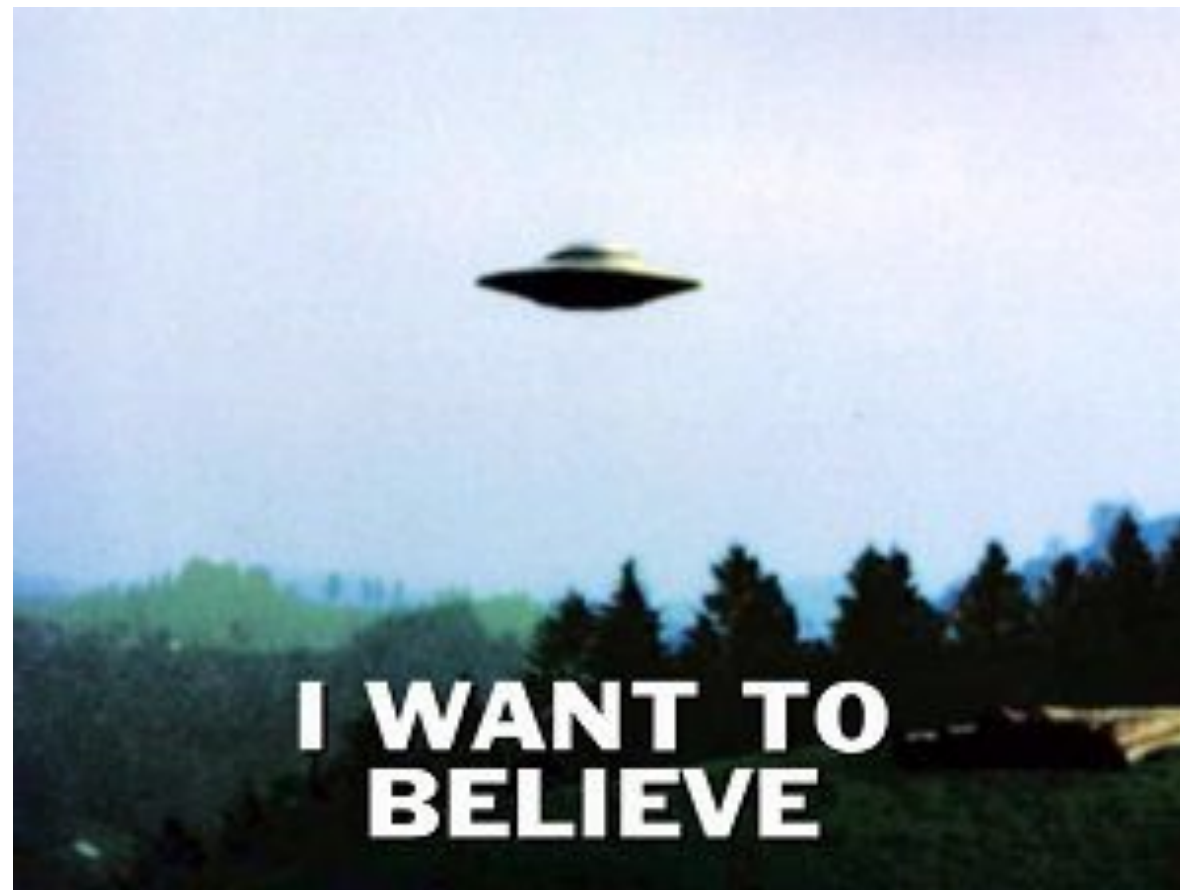
# Direct Searches for Supersymmetry

# Pre LEP





# Where is everybody?



# ATLAS SUSY Searches\* - 95% CL Lower Limits

July 2019

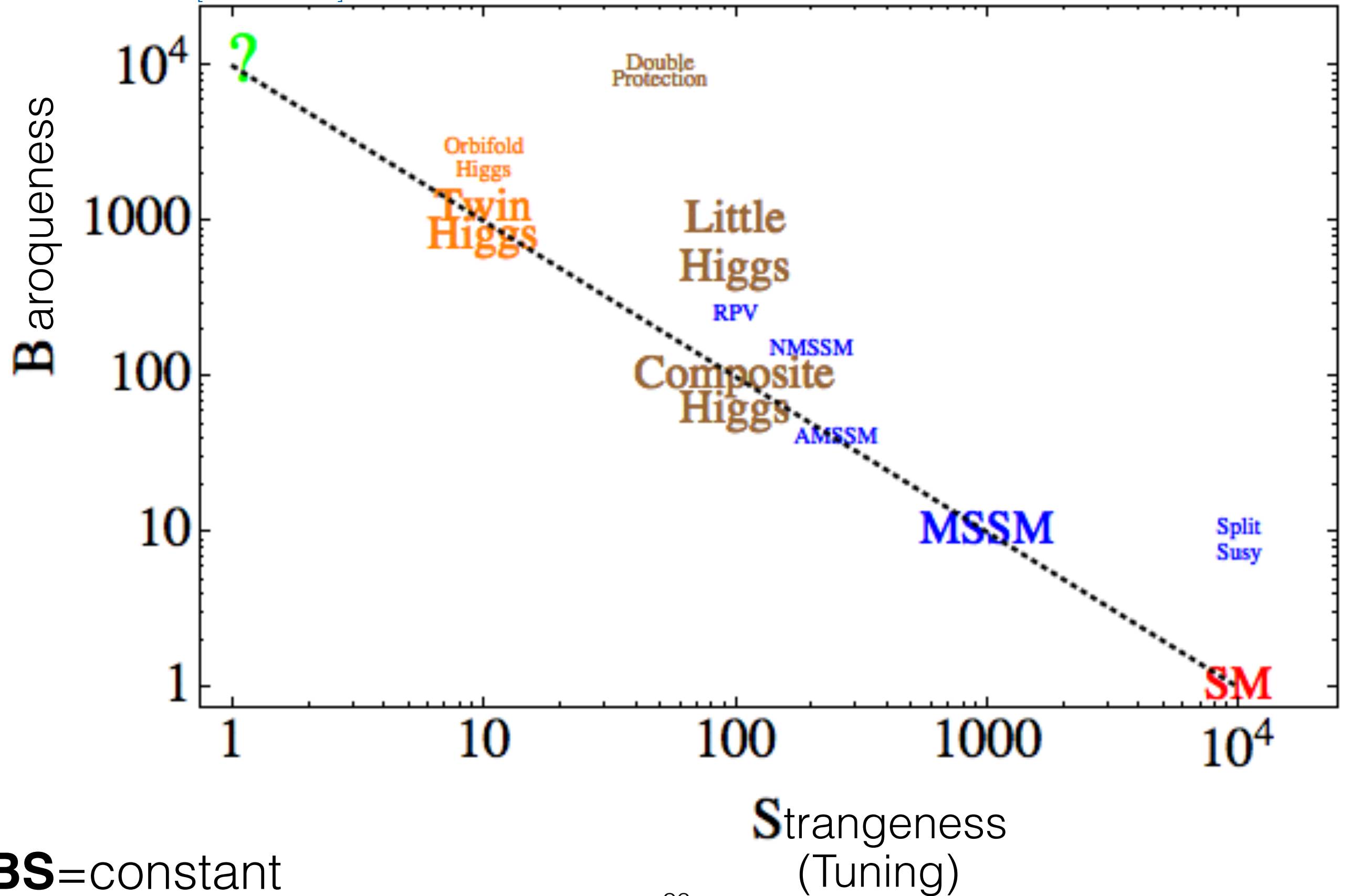
ATLAS Preliminary

$\sqrt{s} = 13$  TeV

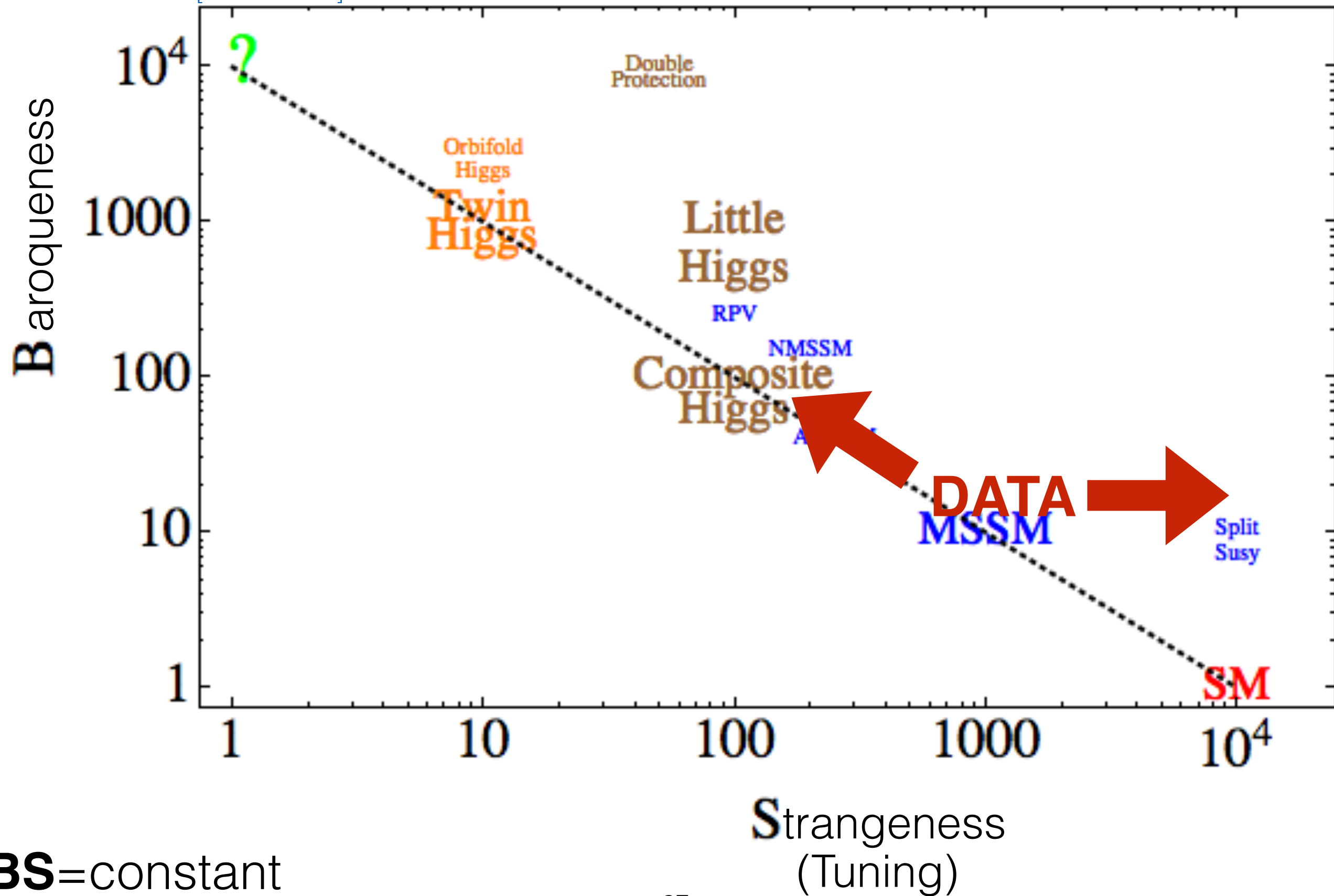
Model	Signature	$\int \mathcal{L} dt$ [fb <sup>-1</sup> ]	Mass limit	Reference
Inclusive Searches	$\tilde{q}\tilde{q}, \tilde{q} \rightarrow q\tilde{\chi}_1^0$	0 $e, \mu$	2-6 jets	$E_T^{\text{miss}}$ 36.1
	mono-jet	1-3 jets	$E_T^{\text{miss}}$ 36.1	
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{q}\tilde{\chi}_1^0$	0 $e, \mu$	2-6 jets	$E_T^{\text{miss}}$ 36.1
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{q}(\ell\ell)\tilde{\chi}_1^0$	3 $e, \mu$	4 jets	$E_T^{\text{miss}}$ 36.1
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{q}\mu\mu$	2 jets	$E_T^{\text{miss}}$ 36.1	
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow qqWZ\tilde{\chi}_1^0$	0 $e, \mu$	7-11 jets	$E_T^{\text{miss}}$ 36.1
3 <sup>rd</sup> gen. squarks direct production	$\tilde{b}_1\tilde{b}_1, \tilde{b}_1 \rightarrow b\tilde{\chi}_1^0/\tilde{\chi}_1^\pm$	Multiple	Multiple	Multiple
	$\tilde{b}_1\tilde{b}_1, \tilde{b}_1 \rightarrow b\tilde{\chi}_2^0 \rightarrow bh\tilde{\chi}_1^0$	0 $e, \mu$	6 $b$	$E_T^{\text{miss}}$ 139
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow Wb\tilde{\chi}_1^0$ or $\tilde{t}\tilde{\chi}_1^0$	0-2 $e, \mu$	0-2 jets/1-2 $b$	$E_T^{\text{miss}}$ 36.1
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow Wb\tilde{\chi}_1^0$	1 $e, \mu$	3 jets/1 $b$	$E_T^{\text{miss}}$ 139
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow \tilde{\tau}_1 b\nu, \tilde{\tau}_1 \rightarrow \tau\tilde{G}$	1 $\tau + 1 e, \mu, \tau$	2 jets/1 $b$	$E_T^{\text{miss}}$ 36.1
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow c\tilde{\chi}_1^0 / \tilde{c}\tilde{c}, \tilde{c} \rightarrow c\tilde{\chi}_1^0$	0 $e, \mu$	2 $c$	$E_T^{\text{miss}}$ 36.1
EW direct	$\tilde{\chi}_1^\pm\tilde{\chi}_2^0$ via WZ	2-3 $e, \mu$	$\geq 1$	$E_T^{\text{miss}}$ 36.1
	$\tilde{\chi}_1^\pm\tilde{\chi}_1^\mp$ via WW	2 $e, \mu$		$E_T^{\text{miss}}$ 139
	$\tilde{\chi}_1^\pm\tilde{\chi}_2^0$ via Wh	0-1 $e, \mu$	2 $b/2 \gamma$	$E_T^{\text{miss}}$ 139
	$\tilde{\chi}_1^\pm\tilde{\chi}_1^\mp$ via $\tilde{\ell}_L/\tilde{\nu}$	2 $e, \mu$		$E_T^{\text{miss}}$ 139
	$\tilde{\tau}\tilde{\tau}, \tilde{\tau} \rightarrow \tau\tilde{\chi}_1^0$	2 $\tau$		$E_T^{\text{miss}}$ 139
	$\tilde{\ell}_{L,R}\tilde{\ell}_{L,R}, \tilde{\ell} \rightarrow \ell\tilde{\chi}_1^0$	2 $e, \mu$	0 jets	$E_T^{\text{miss}}$ 139
Long-lived particles	$\tilde{H}\tilde{H}, \tilde{H} \rightarrow h\tilde{G}/Z\tilde{G}$	0 $e, \mu$	$\geq 3 b$	$E_T^{\text{miss}}$ 36.1
		4 $e, \mu$	0 jets	$E_T^{\text{miss}}$ 36.1
	Direct $\tilde{\chi}_1^+\tilde{\chi}_1^-$ prod., long-lived $\tilde{\chi}_1^\pm$	Disapp. trk	1 jet	$E_T^{\text{miss}}$ 36.1
	Stable $\tilde{g}$ R-hadron	Multiple		36.1
	Metastable $\tilde{g}$ R-hadron, $\tilde{g} \rightarrow qq\tilde{\chi}_1^0$	Multiple		36.1
RPV	LFV $pp \rightarrow \tilde{\nu}_\tau + X, \tilde{\nu}_\tau \rightarrow e\mu/\tau\mu/\tau\tau$	$e\mu, e\tau, \mu\tau$		3.2
	$\tilde{\chi}_1^\pm\tilde{\chi}_1^\mp/\tilde{\chi}_2^0 \rightarrow WW/Z\ell\ell\ell\nu$	4 $e, \mu$	0 jets	$E_T^{\text{miss}}$ 36.1
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow qq\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow qq\tilde{q}$	4-5 large- $R$ jets		36.1
		Multiple		36.1
	$\tilde{t}\tilde{t}, \tilde{t} \rightarrow t\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow tbs$	Multiple		36.1
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow bs$	2 jets + 2 $b$		36.7
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow q\ell$	2 $e, \mu$	2 $b$	36.1
		1 $\mu$	DV	136

\*Only a selection of the available mass limits on new states or phenomena is shown. Many of the limits are based on simplified models, c.f. refs. for the assumptions made.

[Falkowski '15]



[Falkowski '15]



# Comment on 'beauty'

- We adapt our notation to make established physics as simple as possible, the SM is economical but not minimal

original form (1865)

$e + \frac{df}{dx} + \frac{dg}{dy} + \frac{dh}{dz} = 0$	(1) Gauss' Law
$\mu\alpha = \frac{dH}{dy} - \frac{dG}{dz}$ $\mu\beta = \frac{dF}{dz} - \frac{dH}{dx}$ $\mu\gamma = \frac{dG}{dx} - \frac{dF}{dy}$	(2) Equivalent to Gauss' Law for magnetism
$P = \mu \left( \gamma \frac{dy}{dt} - \beta \frac{dz}{dt} \right) - \frac{dF}{dt} - \frac{d\Psi}{dz}$ $Q = \mu \left( \alpha \frac{dz}{dt} - \gamma \frac{dx}{dt} \right) - \frac{dG}{dt} - \frac{d\Psi}{dy}$ $R = \mu \left( \beta \frac{dx}{dt} - \alpha \frac{dy}{dt} \right) - \frac{dH}{dt} - \frac{d\Psi}{dx}$	(3) Faraday's Law (with the Lorentz Force and Poisson's Law)
$\frac{d\gamma}{dy} - \frac{d\beta}{dz} = 4\pi\varphi'$ $p' = p + \frac{df}{dt}$ $\frac{d\alpha}{dz} - \frac{d\gamma}{dx} = 4\pi\eta'$ $q' = q + \frac{dg}{dt}$ $\frac{d\beta}{dx} - \frac{d\alpha}{dy} = 4\pi\tau'$ $r' = r + \frac{dh}{dt}$	(4) Ampère-Maxwell Law
$P = -\xi p \quad Q = -\xi q \quad R = -\xi r$	Ohm's Law
$P = kf \quad Q = kg \quad R = kh$	The electric elasticity equation ( $\mathbf{E} = \mathbf{D}/\epsilon$ )
$\frac{de}{dt} + \frac{dp}{dx} + \frac{dq}{dy} + \frac{dr}{dz} = 0$	Continuity of charge

covariant form

$$\partial_\mu F^{\mu\nu} = \frac{1}{c} J^\nu \quad \text{and} \quad \partial_\mu {}^*F^{\mu\nu} = 0,$$



# An analogy

# An analogy

- Problem: Weak interactions

# An analogy

- Problem: Weak interactions
- Framework: Gauge theory

# An analogy

- Problem: Weak interactions
- Framework: Gauge theory
- Simple theory:  $O(3)$  Schwinger Model (1957)

# An analogy

- Problem: Weak interactions
- Framework: Gauge theory
- Simple theory:  $O(3)$  Schwinger Model (1957)
- Problems: no  $Z$ , not V-A.

# An analogy

- Problem: Weak interactions
- Framework: Gauge theory
- Simple theory:  $O(3)$  Schwinger Model (1957)
- Problems: no  $Z$ , not  $V-A$ .
- More baroque theory:  $SU(2) \times U(1)$  Glashow Model (1961)

# An analogy

- Problem: Weak interactions
- Framework: Gauge theory
- Simple theory:  $O(3)$  Schwinger Model (1957)
- Problems: no  $Z$ , not V-A.
- More baroque theory:  $SU(2) \times U(1)$  Glashow Model (1961)
- *Framework correct! Actual realization in nature not really minimal.*

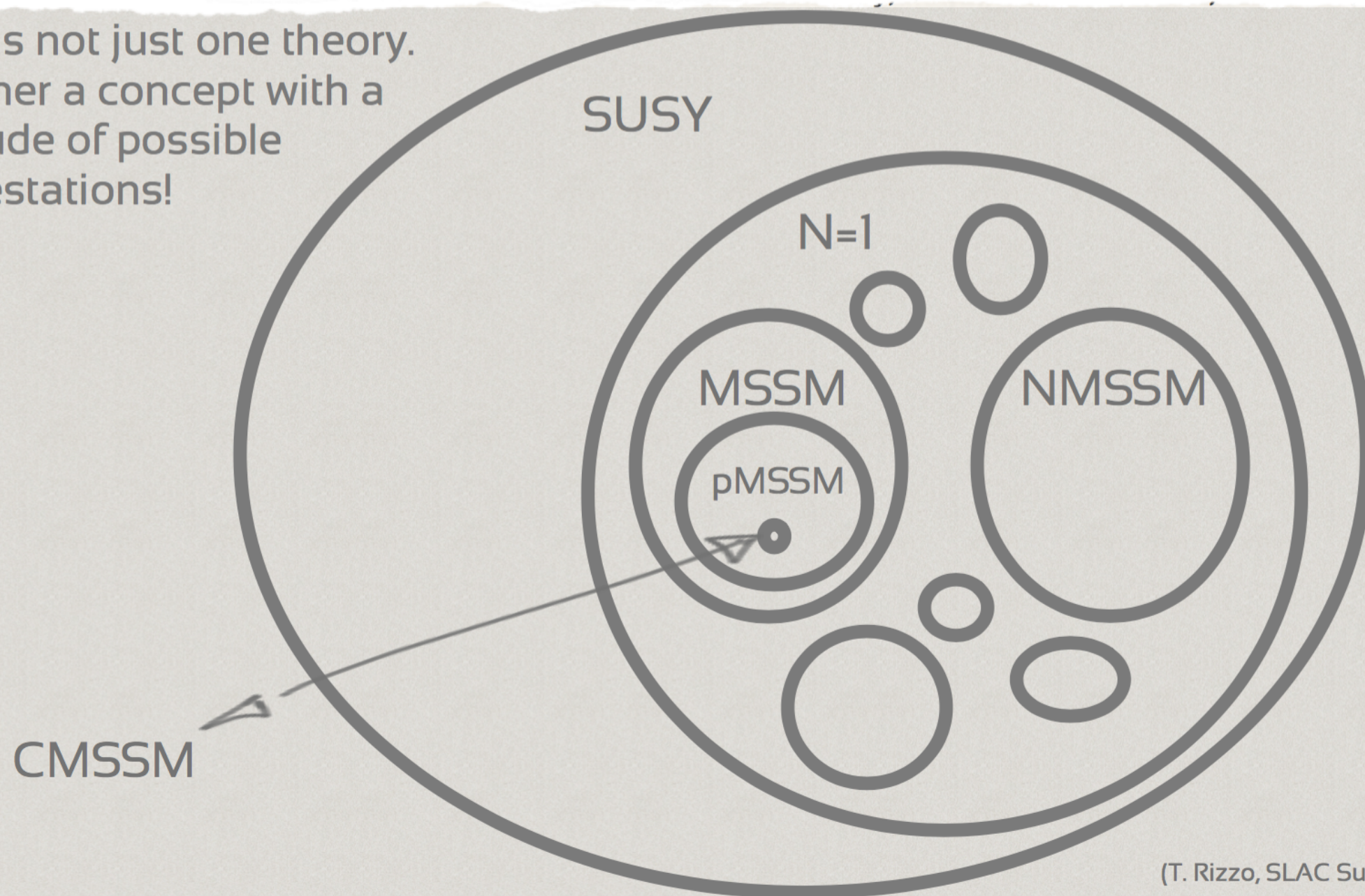
# An analogy

- Problem: Weak interactions
- Framework: Gauge theory
- Simple theory:  $O(3)$  Schwinger Model (1957)
- Problems: no  $Z$ , not V-A.
- More baroque theory:  $SU(2) \times U(1)$  Glashow Model (1961)
- *Framework correct! Actual realization in nature not really minimal.*



# SUSY contains multitudes!

SUSY is not just one theory.  
It's rather a concept with a  
multitude of possible  
manifestations!



(T. Rizzo, SLAC Summer Institute, 2012)

# Natural EWSB & MSSM

Fine-tuning of (Higgs mass)<sup>2</sup>

$$\begin{aligned}\frac{m_Z^2}{2} &= -|\mu|^2 - \frac{m_{H_u}^2 \tan^2 \beta - m_{H_d}^2}{\tan^2 \beta - 1} \\ &\approx -|\mu|^2 - m_{H_u}^2 - \delta m_{H_u}^2\end{aligned}$$

# Natural EWSB & SUSY

Fine-tuning of (Higgs mass)<sup>2</sup>

$$\frac{m_{Higgs}^2}{2} = -|\mu|^2 + \dots + \delta m_H^2$$

# Natural EWSB & SUSY

Fine-tuning of (Higgs mass)<sup>2</sup>

$$\frac{m_{Higgs}^2}{2} = -|\mu|^2 + \dots + \delta m_H^2$$

Higgsinos

# Natural EWSB & SUSY

Fine-tuning of (Higgs mass)<sup>2</sup>

$$\frac{m_{Higgs}^2}{2} = -|\mu|^2 + \dots + \delta m_H^2$$

Higgsinos

1 loop

$$\delta m_H^2|_{stop} = -\frac{3}{8\pi^2} y_t^2 \left( m_{U_3}^2 + m_{Q_3}^2 + |A_t|^2 \right) \log \left( \frac{\Lambda}{\text{TeV}} \right)$$

stops, sbottoms

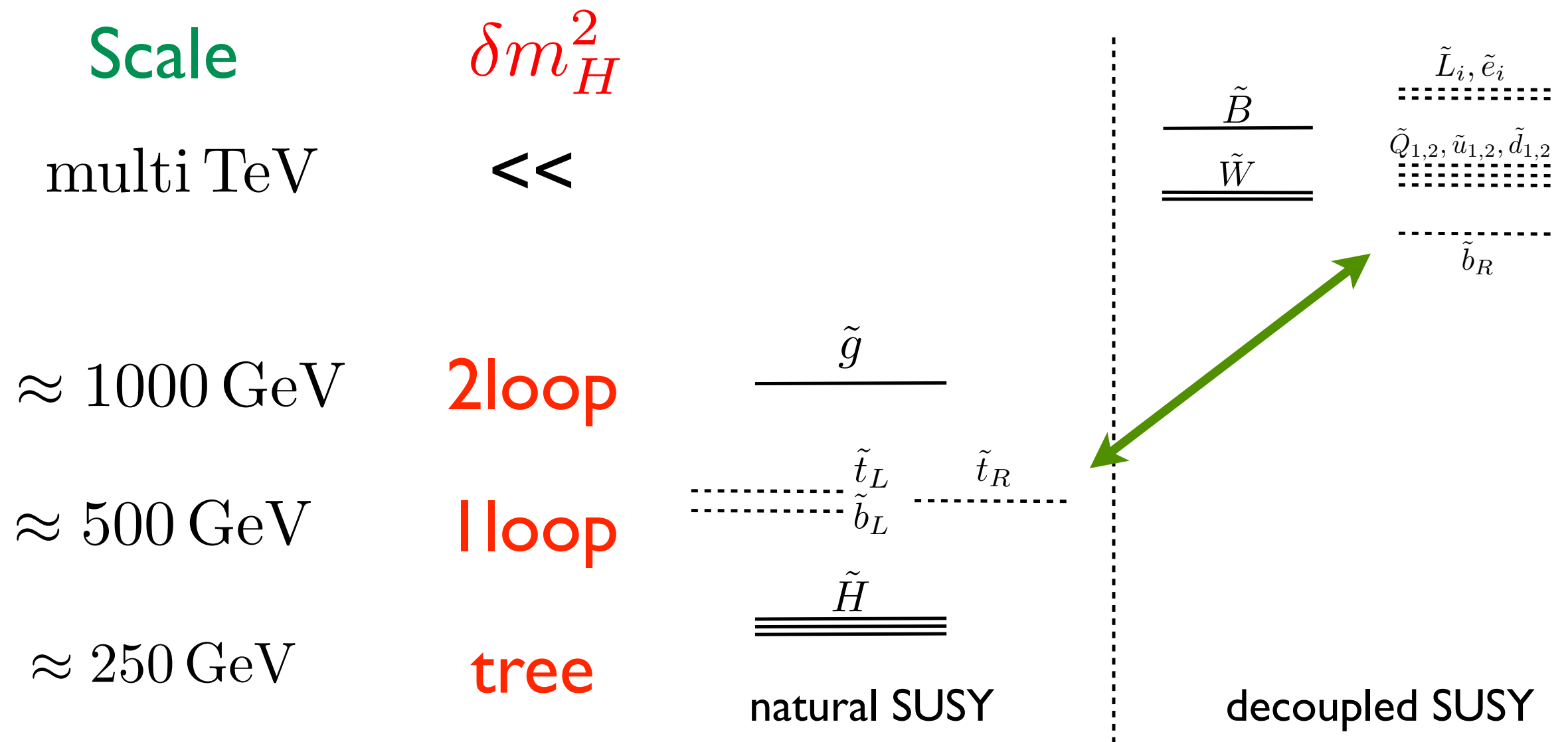
2 loop

$$\delta m_H^2|_{gluino} = -\frac{2}{\pi^2} y_t^2 \left( \frac{\alpha_s}{\pi} \right) |M_3|^2 \log^2 \left( \frac{\Lambda}{\text{TeV}} \right)$$

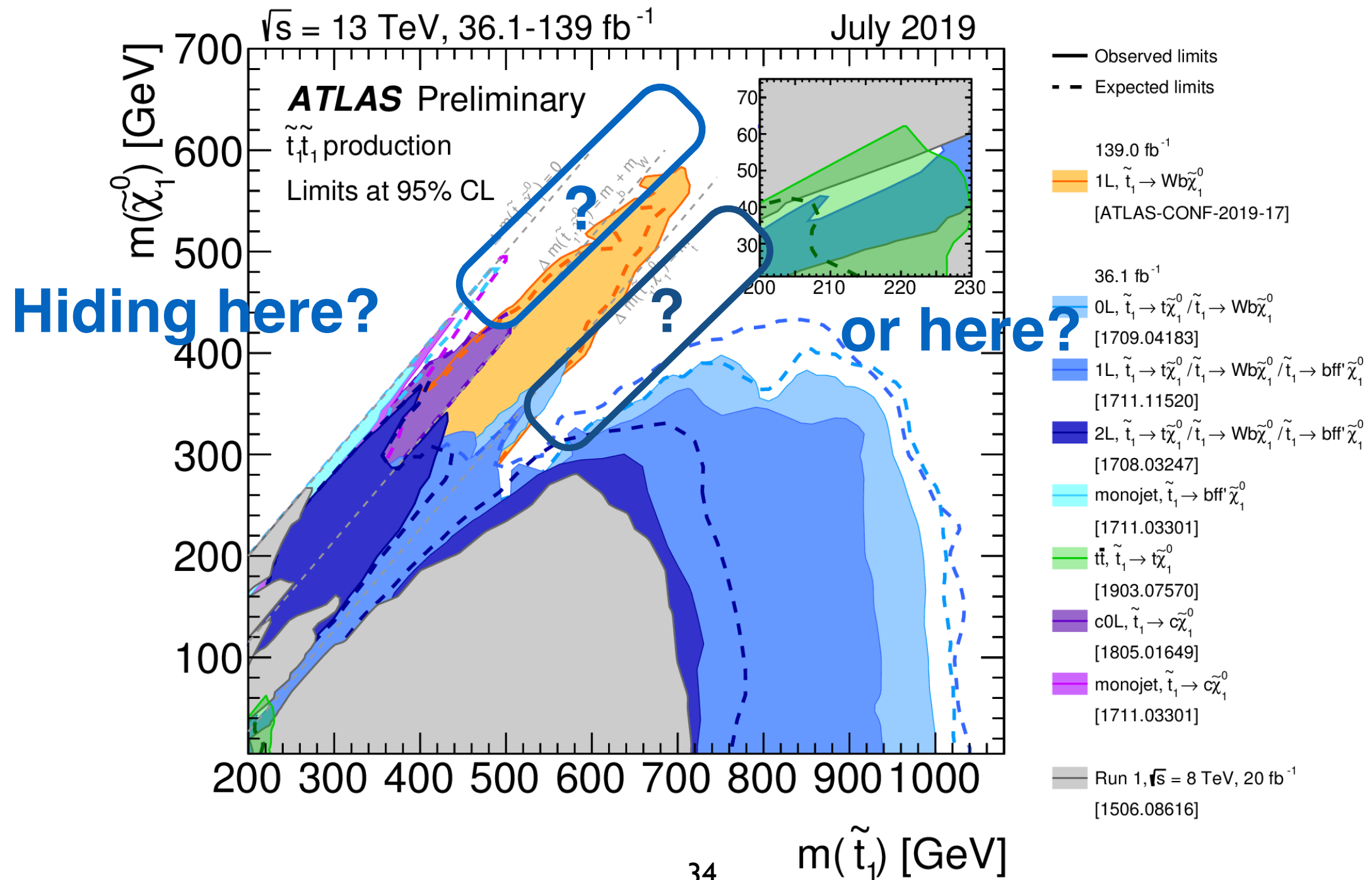
gluino



# Reason for some optimism: natural susy



# Stop searches



# The other symmetric approach

## Composite/Goldstone Higgs



Supersymmetry is a **weakly coupled** solution to the hierarchy problem. We can extrapolate physics to the Planck scale, complete the MSSM into a GUT.

There is another way. Nature already employs a **strongly coupled** mechanism to explain:

$$\Lambda_{\text{QCD}} \ll M_{\text{Planck}}$$
$$\sim 1 \text{ GeV} \quad 10^{19} \text{ GeV}$$

# QCD



David J. Gross



H. David Politzer



Frank Wilczek

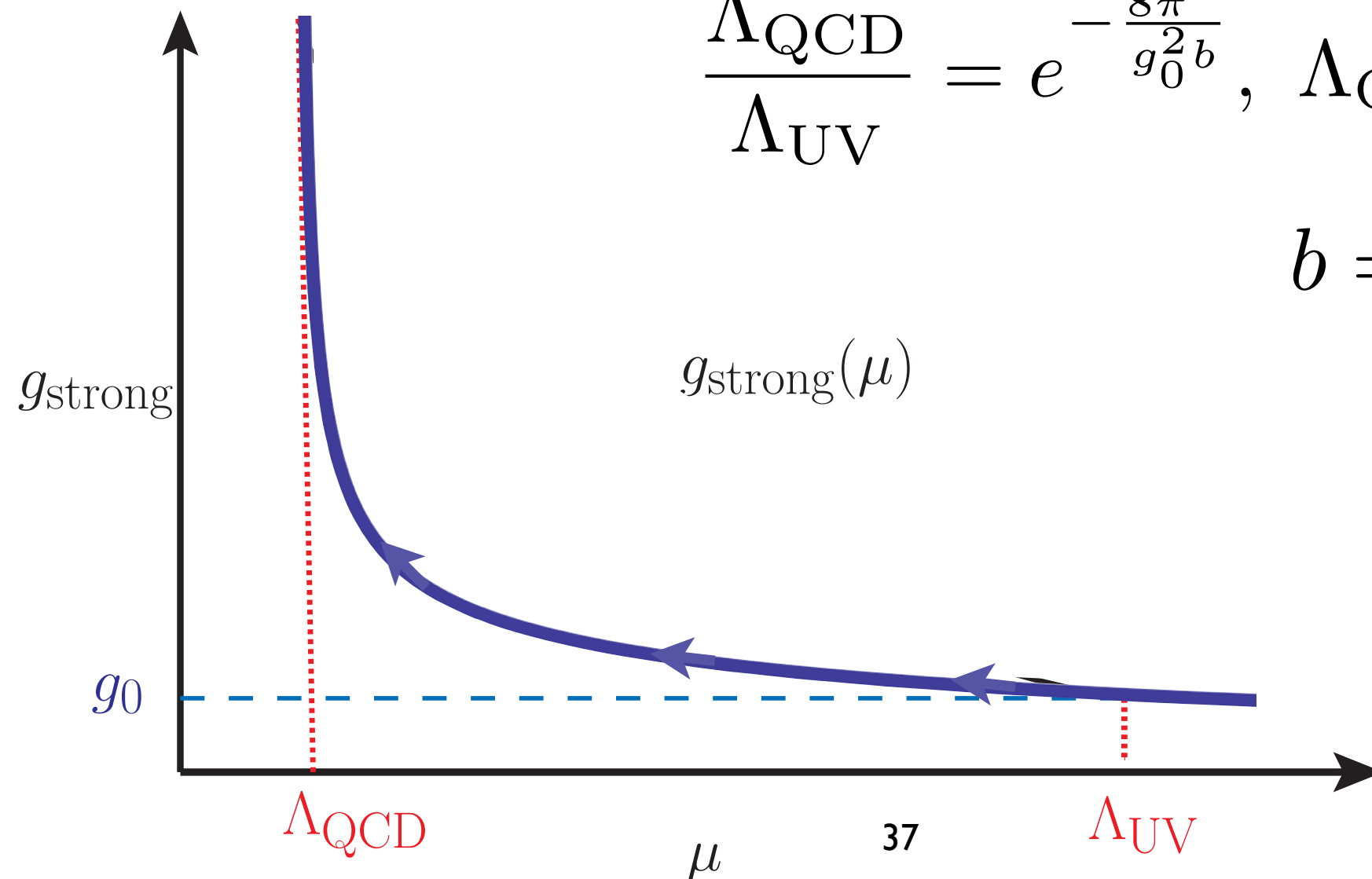


Fix QCD coupling at some high scale

→ exponential hierarchy generated dynamically

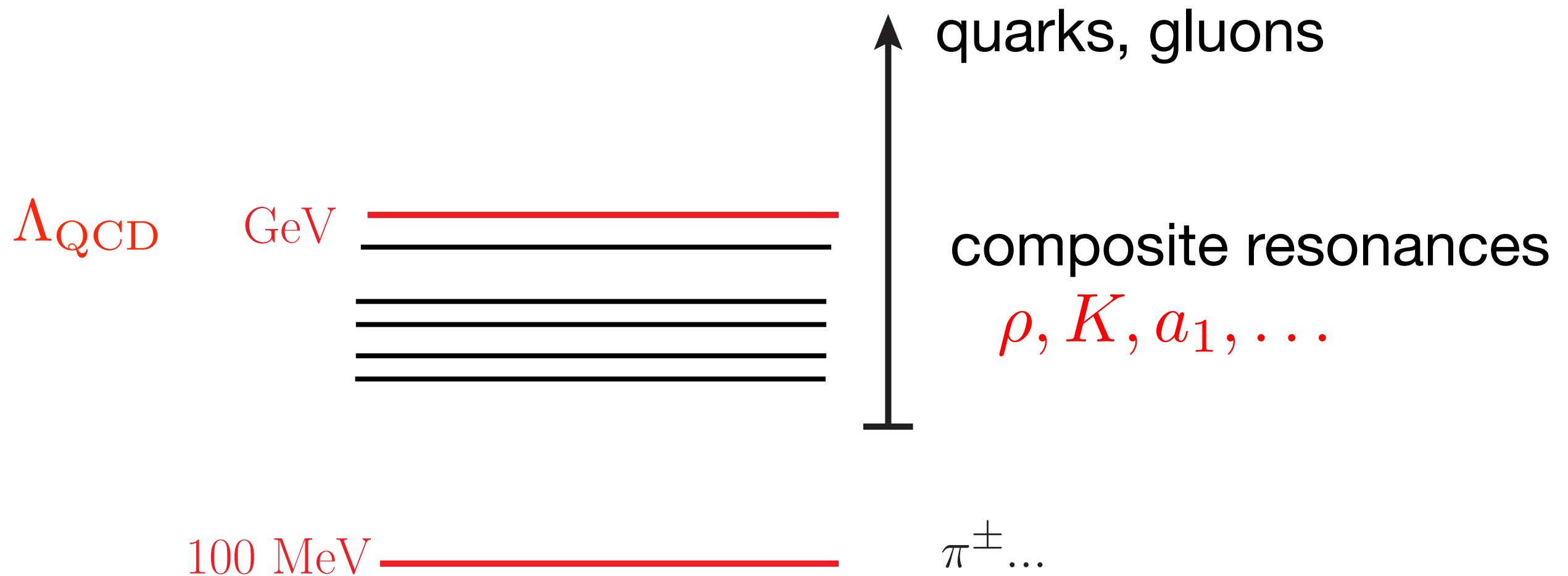
$$\frac{\Lambda_{\text{QCD}}}{\Lambda_{\text{UV}}} = e^{-\frac{8\pi^2}{g_0^2 b}}, \quad \Lambda_{\text{QCD}} \leq \text{GeV}$$

$$b = 7$$



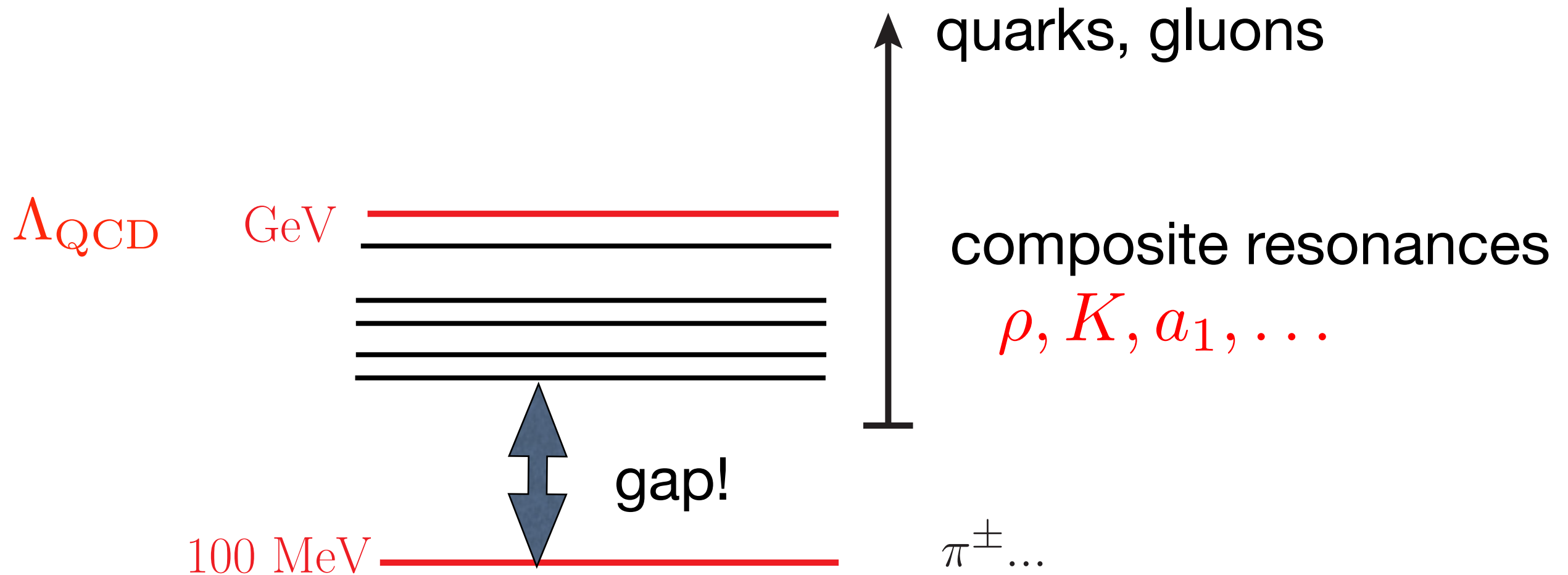
Asymptotic  
freedom

# QCD: composite bound states



At strong coupling, new resonances are generated

# QCD: composite bound states



At strong coupling, new resonances are generated

# QCD vs. EWSB

QCD dynamically breaks SM gauge symmetry

$$SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$$

$$\langle \bar{q}_L q_R \rangle \simeq \Lambda_{\text{QCD}}^3 \sim (\text{GeV})^3$$

# QCD vs. EWSB

QCD dynamically breaks SM gauge symmetry

$$SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$$

$$\langle \bar{q}_L q_R \rangle \simeq \Lambda_{\text{QCD}}^3 \sim (\text{GeV})^3$$

The QCD masses of W/Z are small

$$m_{W,Z} \sim \frac{g}{4\pi} \Lambda_{\text{QCD}} \sim 100 \text{ MeV}$$

Longitudinal components of W & Z have tiny admixture of pions...

# Technicolor

Scaled up version of QCD mechanism

$$\langle \bar{q}'_L q'_R \rangle \sim \Lambda_{\text{TC}}^3, \quad \Lambda_{\text{TC}} \sim \text{TeV}$$

Technicolor, doesn't have a Higgs ...  
(or if there is one, it would look  
very different from the SM)



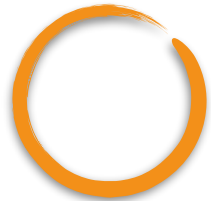
\* the Higgs as the dilaton  
as the last bastion ...

# Composite Higgs

- Want to copy QCD, but extend pion sector (QCD:  $\pi^0, \pi^\pm$ )
- Higgs as a (pseudo) Goldstone boson



# Goal

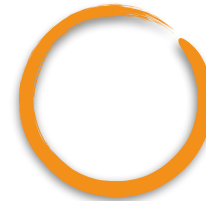


## SUPERSYMMETRY

$$\begin{aligned}\phi &\rightarrow \phi + \epsilon\psi \\ \psi &\rightarrow \psi - i(\sigma^\nu \epsilon^\dagger)_\alpha \partial_\nu \phi\end{aligned}$$

OPPOSITE-STATISTICS PARTNER  
FOR EVERY SM PARTICLE

CONTRIBUTE TO THE HIGGS MASS:



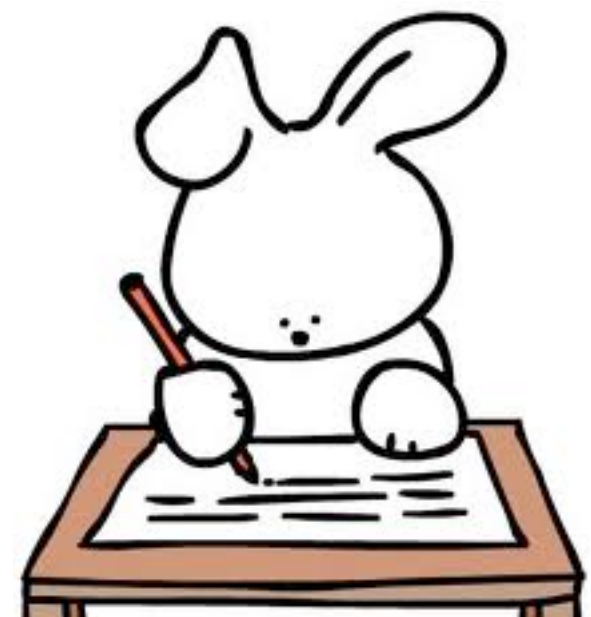
## GLOBAL SYMMETRY

$$\Phi \rightarrow (1 + i\alpha T)\Phi$$

SAME-STATISTICS PARTNER  
FOR EVERY SM PARTICLE

$$m_h^2 \sim \frac{3y_t^2}{4\pi^2} \tilde{m}^2 \log(\Lambda^2 / \tilde{m}^2)$$

Need to learn about  
goldstone bosons...



# Quantum Protection

Symmetries can soften quantum behaviour

$$\mathcal{L} = |\partial_\mu \phi|^2 + \boxed{\mu^2 |\phi|^2} - \lambda |\phi|^4 + \dots$$

breaks susy  $\rightarrow$  corrections must be  
proportional to susy breaking

# Shift symmetry

Higgs mass term can be forbidden

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

$$\phi \rightarrow e^{i\alpha} \phi$$

# Shift symmetry

Higgs mass term can be forbidden

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

$$\phi \rightarrow e^{i\alpha} \phi$$

does not forbid the mass<sup>2</sup>

# Shift symmetry

Higgs mass term can be forbidden

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

$$\phi \rightarrow e^{i\alpha} \phi$$

does not forbid the mass<sup>2</sup>

$$\phi \rightarrow \phi + \alpha$$

works!

# Shift symmetry

Higgs mass term can be forbidden

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

$$\phi \rightarrow e^{i\alpha} \phi$$

does not forbid the mass<sup>2</sup>

$$\phi \rightarrow \phi + \alpha$$

works!

Can we make the Higgs transform this way?

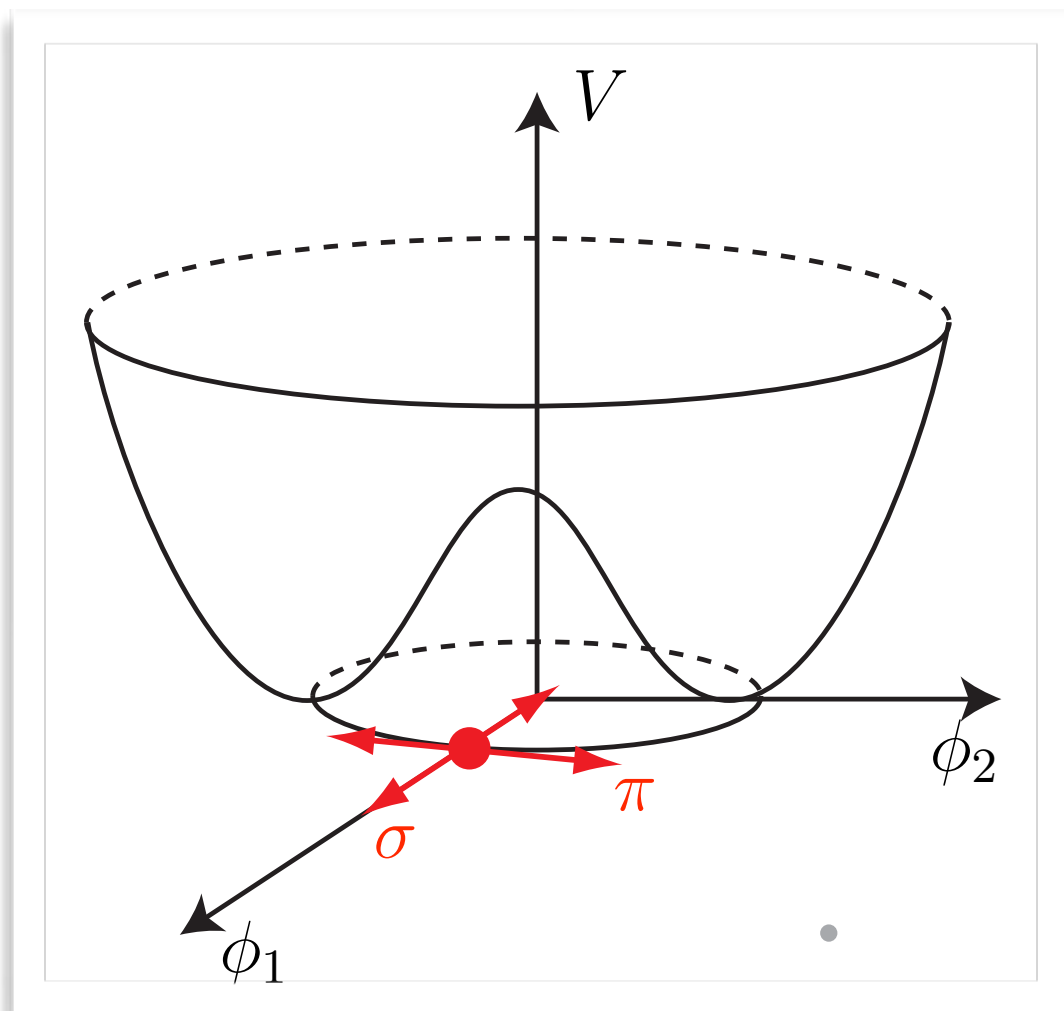
# Spontaneous breaking of U(1)

$$\langle \Phi \rangle = \frac{f}{\sqrt{2}}$$

Instead using complex field

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

$$\phi = \phi_1 + i\phi_2$$



‘phase’

‘modulos’



# Spontaneous breaking of U(1)

$$\langle \Phi \rangle = \frac{f}{\sqrt{2}}$$

Instead using complex field

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

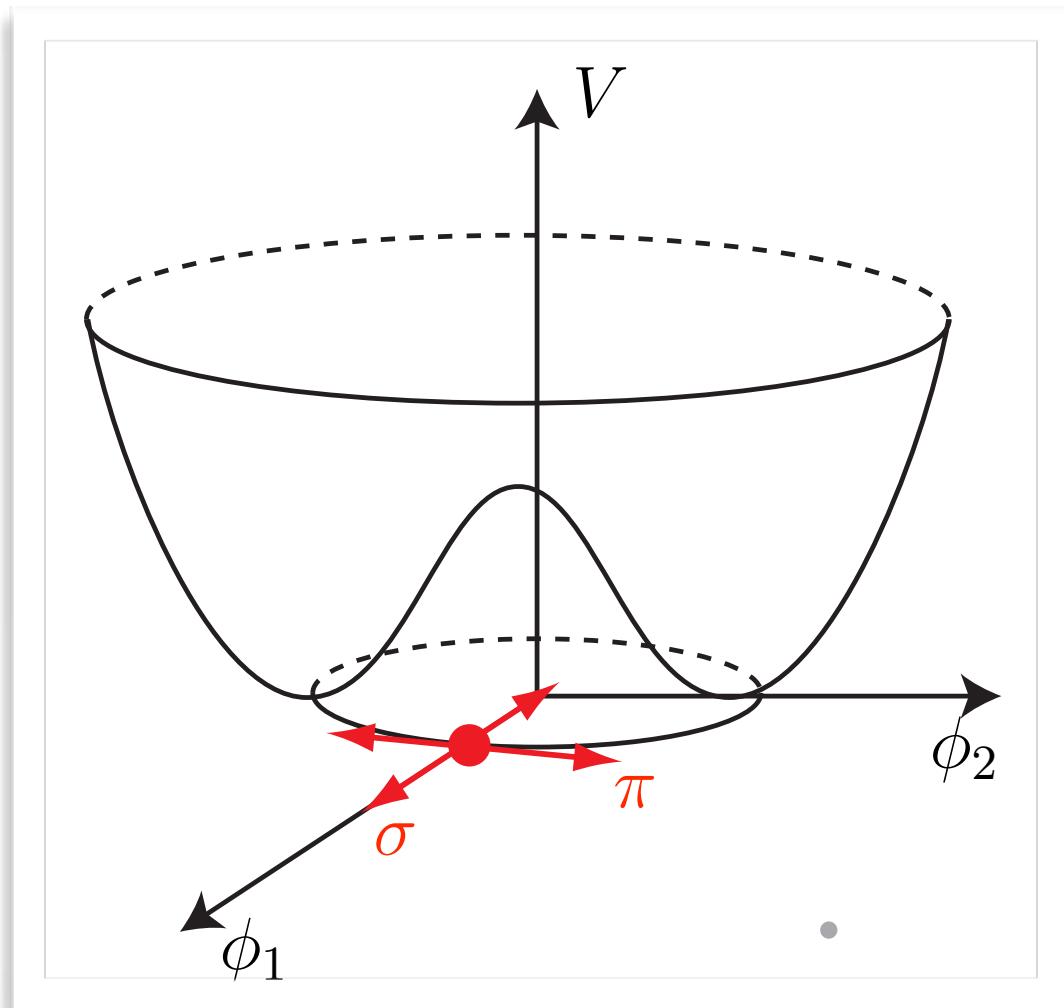
$$\phi = \phi_1 + i\phi_2$$

use real parametrisation

$$\phi(x) = \frac{1}{2} e^{i\pi(x)/f} (f + \sigma(x))$$

‘phase’

‘modulos’



$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

**use**  $\phi(x) = \frac{1}{2} e^{i\pi(x)/f} (f + \sigma(x))$

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

**use**  $\phi(x) = \frac{1}{2} e^{i\pi(x)/f} (f + \sigma(x))$

$$\partial^\mu \phi^\dagger \partial_\mu \phi = \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma + \frac{1}{2} (1 + \sigma/f)^2 \frac{1}{2} \partial^\mu \pi \partial_\mu \pi$$

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots \quad V(|\phi(x)|^2)$$

use  $\phi(x) = \frac{1}{2} e^{i\pi(x)/f} (f + \sigma(x))$

$$\partial^\mu \phi^\dagger \partial_\mu \phi = \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma + \frac{1}{2} (1 + \sigma/f)^2 \frac{1}{2} \partial^\mu \pi \partial_\mu \pi$$

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots \quad V(|\phi(x)|^2)$$

use  $\phi(x) = \frac{1}{2} e^{i\pi(x)/f} (f + \sigma(x))$

$$\partial^\mu \phi^\dagger \partial_\mu \phi = \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma + \frac{1}{2} (1 + \sigma/f)^2 \frac{1}{2} \partial^\mu \pi \partial_\mu \pi$$

$$V(|\phi(x)|^2) = V(\sigma(x))$$

no dependence on  $\pi(x)$

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots \quad V(|\phi(x)|^2)$$

use  $\phi(x) = \frac{1}{2} e^{i\pi(x)/f} (f + \sigma(x))$

$$\partial^\mu \phi^\dagger \partial_\mu \phi = \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma + \frac{1}{2} (1 + \sigma/f)^2 \frac{1}{2} \partial^\mu \pi \partial_\mu \pi$$

$$V(|\phi(x)|^2) = V(\sigma(x))$$

no mass term

no dependence on  $\pi(x)$

$$\frac{1}{2} (1 + \sigma(x)/f)^2 \frac{1}{2} \partial^\mu \pi \partial_\mu \pi + \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma - V(\sigma(x))$$

Using this parameterization a new symmetry is visible:

$$\pi(x) \rightarrow \pi(x) + \alpha$$

because  $\pi(x)$  has only ‘derivative interactions’

$$\partial_\mu (\pi(x) + \alpha) = \partial_\mu \pi(x)$$

$$\pi(x), \sigma(x)$$

$$\frac{1}{2} (1 + \sigma(x)/f)^2 \frac{1}{2} \partial^\mu \pi \partial_\mu \pi + \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma - V(\sigma(x))$$

Using this parameterization a new symmetry is visible:

$$\pi(x) \rightarrow \pi(x) + \alpha$$

because  $\pi(x)$  has only ‘derivative interactions’

$$\partial_\mu (\pi(x) + \alpha) = \partial_\mu \pi(x)$$

But what happened to the U(1) symmetry ?

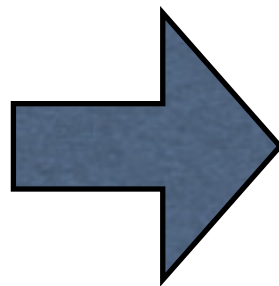
$\pi(x), \sigma(x)$  are real...



But what happened to the  $U(1)$  symmetry ?

$$\phi \rightarrow e^{i\alpha} \phi$$

$$e^{i\pi(x)/f} (f + \sigma(x)) \rightarrow e^{i\alpha} e^{i\pi(x)/f} (f + \sigma(x))$$



$$\sigma(x) \rightarrow \sigma(x)$$

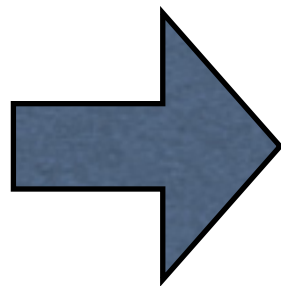
$$\pi(x) \rightarrow \pi(x) + \alpha$$

Phase rotation becomes shift symmetry

But what happened to the U(1) symmetry ?

$$\phi \rightarrow e^{i\alpha} \phi$$

$$e^{i\pi(x)/f} (f + \sigma(x)) \rightarrow e^{i\alpha} e^{i\pi(x)/f} (f + \sigma(x))$$



$$\sigma(x) \rightarrow \sigma(x)$$

$$\pi(x) \rightarrow \pi(x) + \alpha$$

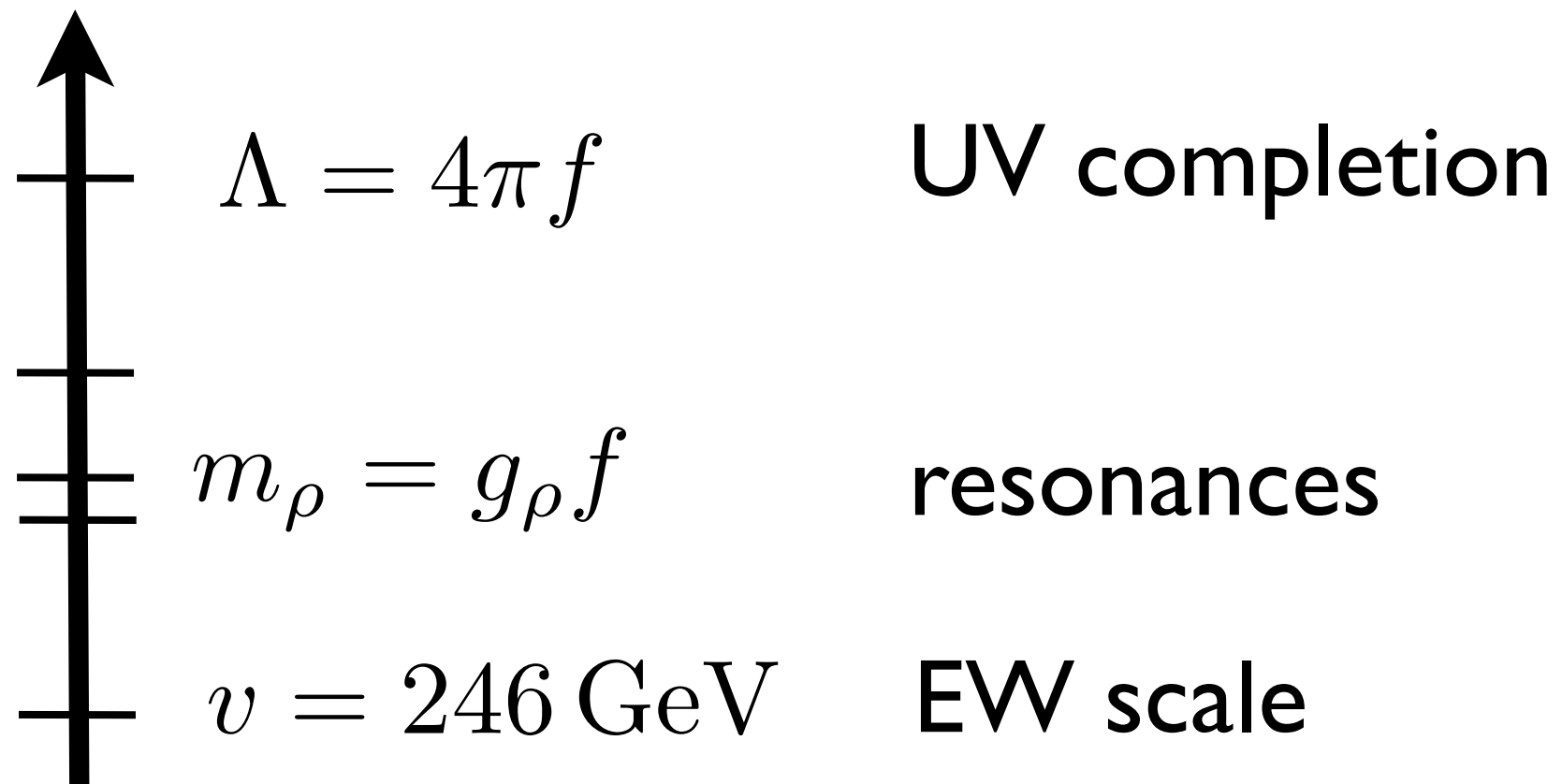
Phase rotation becomes shift symmetry

$\pi(x)$  is **massless** **but** also no

- gauge couplings
- potential
- yukawas

# Semi-realistic model





# pGB Higgs

$$SU(3) \rightarrow SU(2)$$

Break symmetry using  $\langle \Phi \rangle = \begin{pmatrix} 0 \\ 0 \\ f \end{pmatrix}$

# Goldstone bosons = # broken generators

$$\Phi = \frac{1}{\sqrt{2}} e^{i\Pi/f} \begin{pmatrix} 0 \\ 0 \\ f + \sigma \end{pmatrix} \quad \Pi = \frac{1}{\sqrt{2}} \begin{pmatrix} \eta/\sqrt{3} & 0 & H_1 \\ 0 & \eta/\sqrt{3} & H_2 \\ H_1^* & H_2^* & -2\eta/\sqrt{3} \end{pmatrix}$$

$$\Phi = \frac{1}{\sqrt{2}} e^{i\Pi/f} \begin{pmatrix} 0 \\ 0 \\ f + \sigma \end{pmatrix} \quad \Pi = \frac{1}{\sqrt{2}} \begin{pmatrix} \eta/\sqrt{3} & 0 & H_1 \\ 0 & \eta/\sqrt{3} & H_2 \\ H_1^* & H_2^* & -2\eta/\sqrt{3} \end{pmatrix}$$

**Expand**

$$\Phi(x) = \begin{pmatrix} H_1(x) \\ H_2(x) \\ -\frac{2}{\sqrt{2}}\eta(x) \end{pmatrix} + \dots$$

**Contains a Higgs:**  $H = \begin{pmatrix} H_1 \\ H_2 \end{pmatrix} = SU(2) \text{ doublet}$

kinetic term:

$$\partial_\mu \Phi \partial^\mu \Phi^\dagger = \partial_\mu H \partial^\mu H^\dagger + \frac{(\partial_\mu H \partial^\mu H^\dagger) H^\dagger H}{f^2} + \dots$$

Nonlinear corrections

$$SU(3) \rightarrow SU(2)$$

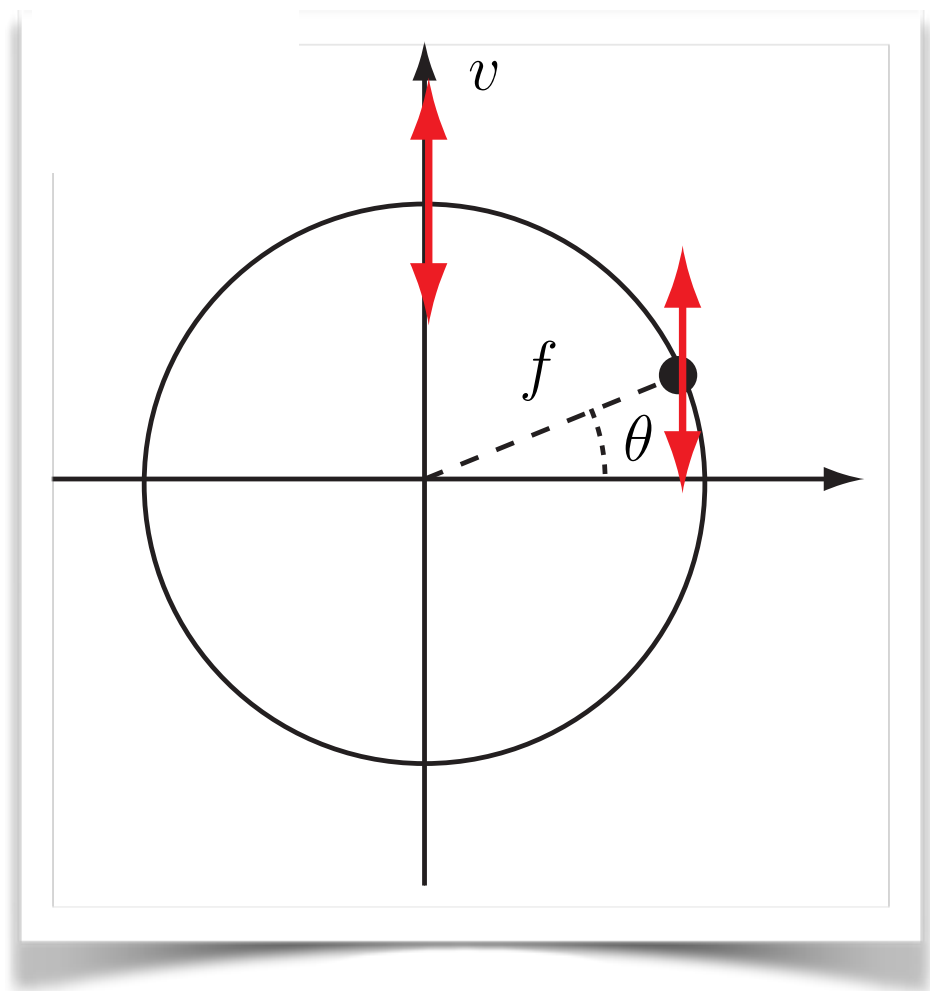
# pGB Higgs

Unbroken gauge symmetry in global  $SU(2)$ ,  
dynamics generates ‘**vacuum misalignment**’

$SU(2)_L$  vs.  $SU(2)$

$$\langle \Phi \rangle = \frac{f}{\sqrt{2}} \begin{pmatrix} 0 \\ \sin \theta \\ \cos \theta \end{pmatrix} \quad SU(2)_L$$

EW symmetry broken



# pGB Higgs

$$\langle \Phi \rangle = \frac{f}{\sqrt{2}} \begin{pmatrix} 0 \\ \sin \theta \\ \cos \theta \end{pmatrix} \text{SU}(2)_L$$

Electro-weak scale  $v = f \sin \theta$

$f \sim$  scale of new physics

$\sin \theta \ll 1 \Leftrightarrow f \gg v$  (SM limit)

$$\Rightarrow \langle H \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}$$



# Collective Breaking

We now want to add a yukawa coupling to give mass to the top quark

$$\lambda_t \bar{Q}_i H_i^c t_R \quad i: \text{sum over SU(2)}$$

Fundamental field is a triplet

$$\phi = \exp \left\{ i \begin{pmatrix} h_1 & h_2 \\ h_1^* & h_2^* \end{pmatrix} \right\} \begin{pmatrix} f \end{pmatrix}$$

# Top yukawa: 1st try

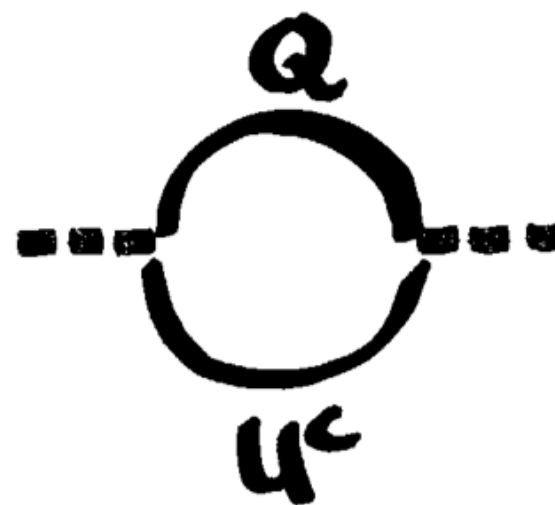
$$\sum_i^2 \lambda_t \phi_i^c \bar{Q}_i t_R \quad \text{works, gives mass to the top}$$

... but breaks **SU(3)** structure explicitly, does not respect Goldstone symmetry protecting the Higgs mass:

# Top yukawa: 1st try

$$\sum_i^2 \lambda_t \phi_i^c \bar{Q}_i t_R \quad \text{works, gives mass to the top}$$

... but breaks **SU(3)** structure explicitly, does not respect Goldstone symmetry protecting the Higgs mass:



$$\sim \frac{\lambda_t^2}{16\pi^2} \Lambda_{UV}^2$$

we've accomplished nothing...

# 2nd try: “collective breaking”

Example:  $SU(3) \rightarrow SU(2)$  (ignore  $U(1)_Y$  again)

$$\langle \Phi_1 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ f_1 \end{pmatrix} \quad \langle \Phi_2 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ f_2 \end{pmatrix} \quad \text{two scalar fields!}$$

Gauge full  $SU(3) \Rightarrow$  exact symmetry

$$\Psi_L = \begin{pmatrix} t_L \\ b_L \\ T_L \end{pmatrix} \quad t_{1R}, t_{2R}, b_R$$

Global rotations ( $SU(3)_1 \times SU(3)_2$ ):

$$\Phi_1 \rightarrow U_1 \Phi_1$$

$$\Phi_2 \rightarrow U_2 \Phi_2$$

Gauge symmetry ( $SU(3)_{1+2}$ ):

$$\Psi_L \rightarrow U_{1+2}(x) \Psi_L$$

$$y_1 = 0, \quad y_2 \neq 0$$

$$\text{SU}(3)_{1+2}$$

$$\text{SU}(3)_2$$

$$y_1 \neq 0, \quad y_2 = 0$$

$$\text{SU}(3)_1$$

$$\text{SU}(3)_{1+2}$$

$$y_1 \neq 0, \quad y_2 \neq 0$$

$$\text{SU}(3)_{1+2}$$

If **only one**  $y_1$  or  $y_2$  is present, then two  $\text{SU}(3)$ 's survive, one for the gauge bosons (eating the goldstones of one  $\Phi_i$ ) and one global  $\text{SU}(3)$  guaranteeing that the Yukawa does not contribute to Goldstone mass.

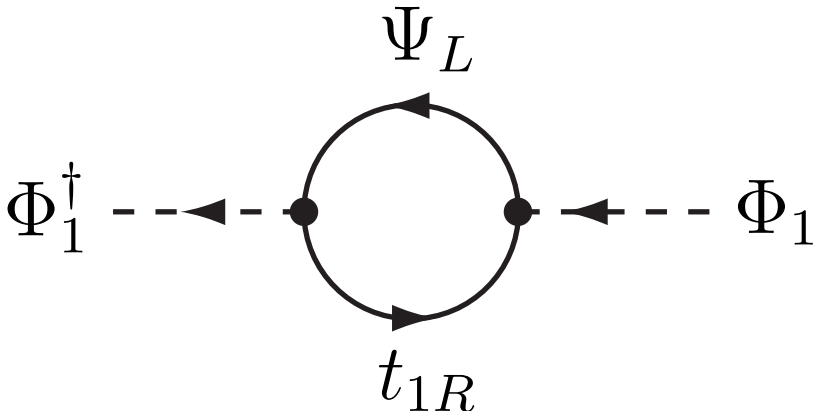
If **both**  $y_1$  and  $y_2$  present, then only one  $\text{SU}(3)$  present, and the goldstones of one combination of  $\Phi_1$  and  $\Phi_2$  are eaten, the other combination gets a mass from the Yukawa.

$$\mathcal{L}_{\text{Yukawa}} = y_1 \bar{\Psi}_L \Phi_1 t_{1R} + y_2 \bar{\Psi}_L \Phi_2 t_{2R}$$

$y_1 = 0, y_2 \neq 0$	$\text{SU}(3)_{1+2}$	$\text{SU}(3)_2$
$y_1 \neq 0, y_2 = 0$	$\text{SU}(3)_1$	$\text{SU}(3)_{1+2}$
$y_1 \neq 0, y_2 \neq 0$	$\text{SU}(3)_{1+2}$	

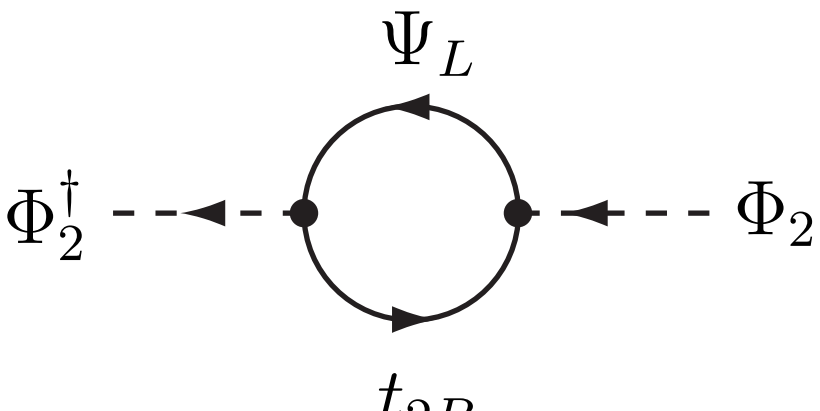
If **only one**  $y_1$  or  $y_2$  is present, then two  $\text{SU}(3)$ 's survive, one for the gauge bosons (eating the goldstones of one  $\Phi_i$ ) and one global  $\text{SU}(3)$  guaranteeing that the Yukawa does not contribute to Goldstone mass.

If **both**  $y_1$  and  $y_2$  present, then only one  $\text{SU}(3)$  present, and the goldstones of one combination of  $\Phi_1$  and  $\Phi_2$  are eaten, the other combination gets a mass from the Yukawa.



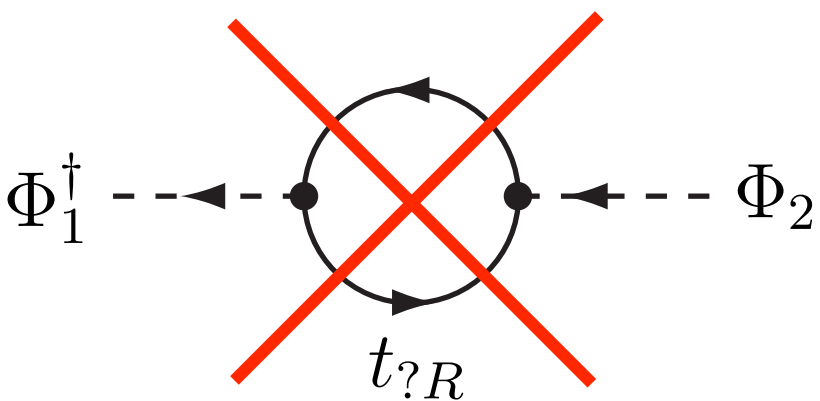
$$\Phi_1^\dagger \text{---}\blacktriangleleft\text{---}\bullet\text{---}\bigcirc\text{---}\blacktriangleleft\text{---}\Phi_1 \sim \underbrace{\frac{y_1^2}{16\pi^2}} \Lambda^2$$

preserves  $SU(3)_2 \rightarrow SU(2)_2$   
 $\Rightarrow$  no PNGB Higgs mass



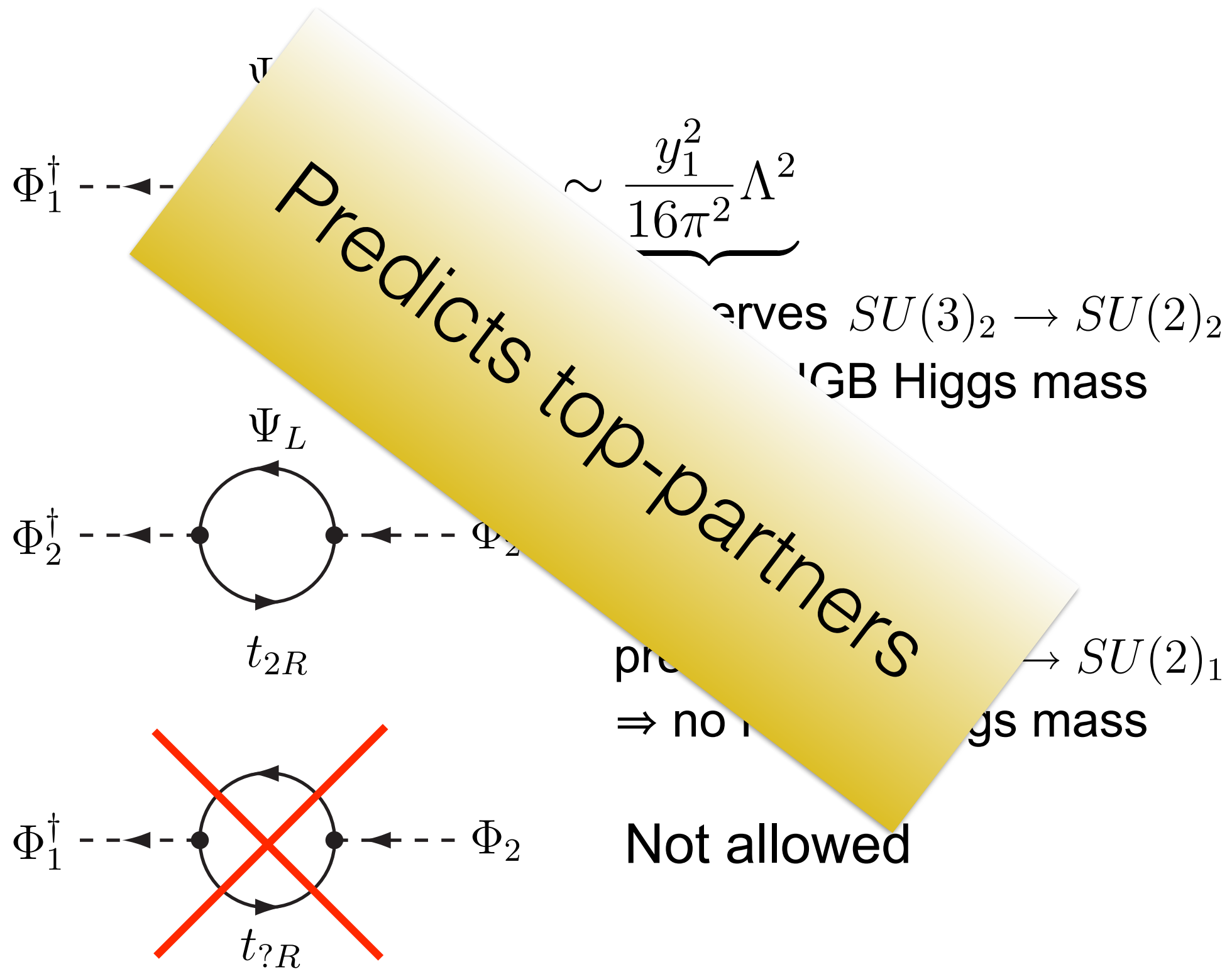
$$\Phi_2^\dagger \text{---}\blacktriangleleft\text{---}\bullet\text{---}\bigcirc\text{---}\blacktriangleleft\text{---}\Phi_2 \sim \underbrace{\frac{y_2^2}{16\pi^2}} \Lambda^2$$

preserves  $SU(3)_1 \rightarrow SU(2)_1$   
 $\Rightarrow$  no PNGB Higgs mass



$$\Phi_1^\dagger \text{---}\blacktriangleleft\text{---}\bullet\text{---}\bigcirc\text{---}\blacktriangleleft\text{---}\Phi_2$$

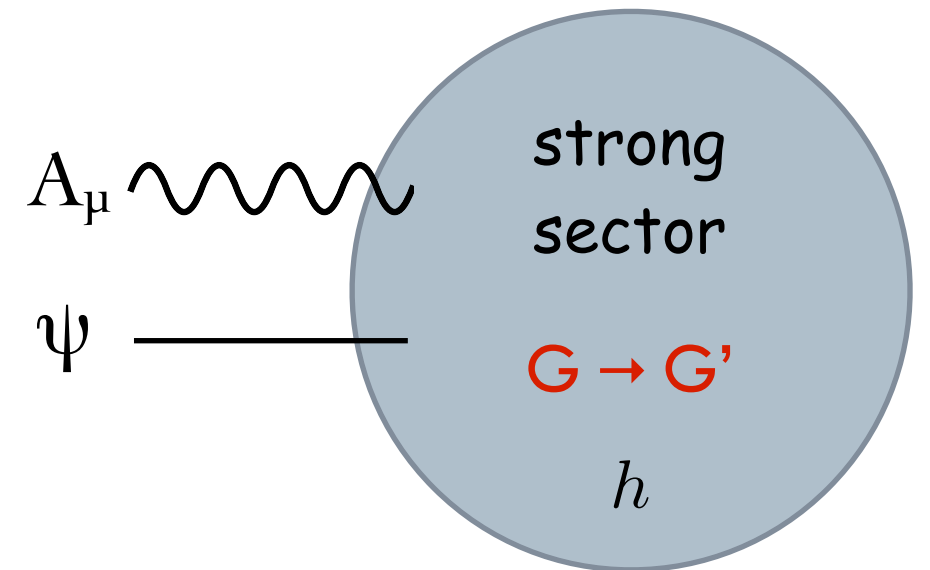
Not allowed





# Minimal composite Higgs

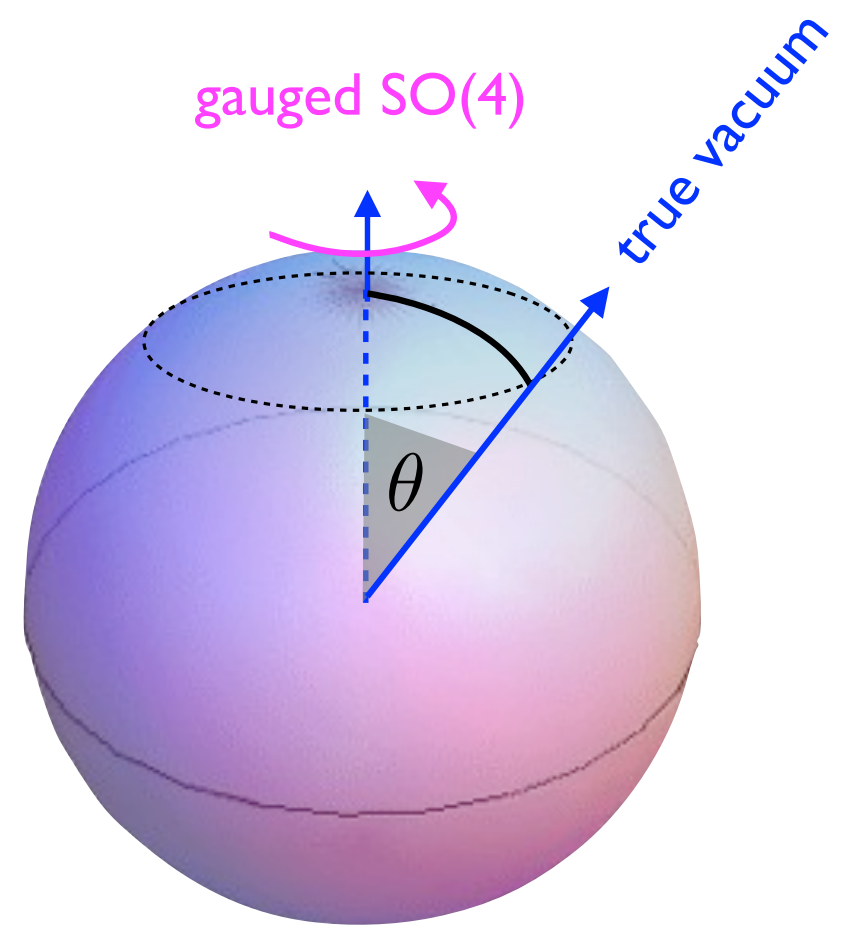
Agashe et. al



Minimal bottom up construction

$$SO(5) \rightarrow SO(4) \sim SU(2)_L \times SU(2)_R$$

$$SO(5)/SO(4)$$



Tree level: gauge  $SO(4)$  aligned

Higgs

$$\phi = e^{i\pi^{\hat{a}} T^{\hat{a}} / f} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} \sin(\pi/f) \times \begin{pmatrix} \hat{\pi}^1 \\ \hat{\pi}^2 \\ \hat{\pi}^3 \\ \hat{\pi}^4 \end{pmatrix} \\ \cos(\pi/f) \end{pmatrix} \stackrel{\text{I-loop } \langle \phi(x) \rangle = \theta \cdot f}{=} \begin{pmatrix} \sin(\theta + \underbrace{h(x)/f}_{\text{Higgs}}) \underbrace{e^{i\chi^i(x) A^i / v}}_{\text{eaten by } W_L, Z_L} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} \\ \cos(\theta + h(x)/f) \end{pmatrix}$$

# Implications of $m_H = 125 \text{ GeV}$

Agashe et. al

Potential is fully radiatively generated

$$V_{gauge}(h) = \frac{9}{2} \int \frac{d^4 p}{(2\pi)^4} \log \left( \Pi_0(p) + \frac{s_h^2}{4} \Pi_1(p) \right) \quad s_h \equiv \sin h/f$$

$$\Pi_0(p) = \frac{p^2}{g^2} + \Pi_a(p) \ , \quad \Pi_1(p) = 2[\Pi_{\hat{a}}(p) - \Pi_a(p)]$$

# Implications of $m_H = 125 \text{ GeV}$

Agashe et. al

Potential is fully radiatively generated

$$V_{gauge}(h) = \frac{9}{2} \int \frac{d^4 p}{(2\pi)^4} \log \left( \Pi_0(p) + \frac{s_h^2}{4} \Pi_1(p) \right) \quad s_h \equiv \sin h/f$$

$$\Pi_0(p) = \frac{p^2}{g^2} + \Pi_a(p) \quad , \quad \Pi_1(p) = 2[\Pi_{\hat{a}}(p) - \Pi_a(p)]$$

$$\int d^4 p \Pi_1(p)/\Pi_0(p) < \infty \quad \text{Higgs dependent term UV finite}$$

# Implications of $m_H = 125 \text{ GeV}$

Agashe et. al

Potential is fully radiatively generated

$$V_{gauge}(h) = \frac{9}{2} \int \frac{d^4 p}{(2\pi)^4} \log \left( \Pi_0(p) + \frac{s_h^2}{4} \Pi_1(p) \right) \quad s_h \equiv \sin h/f$$

$$\Pi_0(p) = \frac{p^2}{g^2} + \Pi_a(p) \ , \quad \Pi_1(p) = 2[\Pi_{\hat{a}}(p) - \Pi_a(p)]$$

$$\int d^4 p \Pi_1(p)/\Pi_0(p) < \infty \quad \text{Higgs dependent term UV finite}$$

→ ‘Weinberg sum rules’

$$\lim_{p^2 \rightarrow \infty} \Pi_1(p) = 0 \ ,$$

$$\lim_{p^2 \rightarrow \infty} p^2 \Pi_1(p) = 0$$

UV finiteness requires at least two resonances

$$\Pi_1(p) = \frac{f^2 m_\rho^2 m_{a_1}^2}{(p^2 + m_\rho^2)(p^2 + m_{a_1}^2)} \quad \text{spin 1}$$

UV finiteness requires at least two resonances

$$\Pi_1(p) = \frac{f^2 m_\rho^2 m_{a_1}^2}{(p^2 + m_\rho^2)(p^2 + m_{a_1}^2)} \quad \text{spin 1}$$

Similarly for SO(5) fermionic contribution

Pomarol et al; Marzocca

$$m_h^2 \simeq \frac{N_c}{\pi^2} \left[ \frac{m_t^2}{f^2} \frac{m_{Q_4}^2 m_{Q_1}^2}{m_{Q_1}^2 - m_{Q_4}^2} \log \left( \frac{m_{Q_1}^2}{m_{Q_4}^2} \right) \right]$$

similar result in deconstruction:  
Matsedonskyi et al; Redi et al

5 = 4 + 1      with EM charges 5/3, 2/3, -1/3  
Q<sub>4</sub>   Q<sub>1</sub>

64 → solve for  $m_h = 125 \text{ GeV}$

# Light Higgs implies light fermionic top partners

$$m_h^2 \simeq \frac{N_c}{\pi^2} \left[ \frac{m_t^2}{f^2} \frac{m_{Q_4}^2 m_{Q_1}^2}{m_{Q_1}^2 - m_{Q_4}^2} \log \left( \frac{m_{Q_1}^2}{m_{Q_4}^2} \right) \right]$$

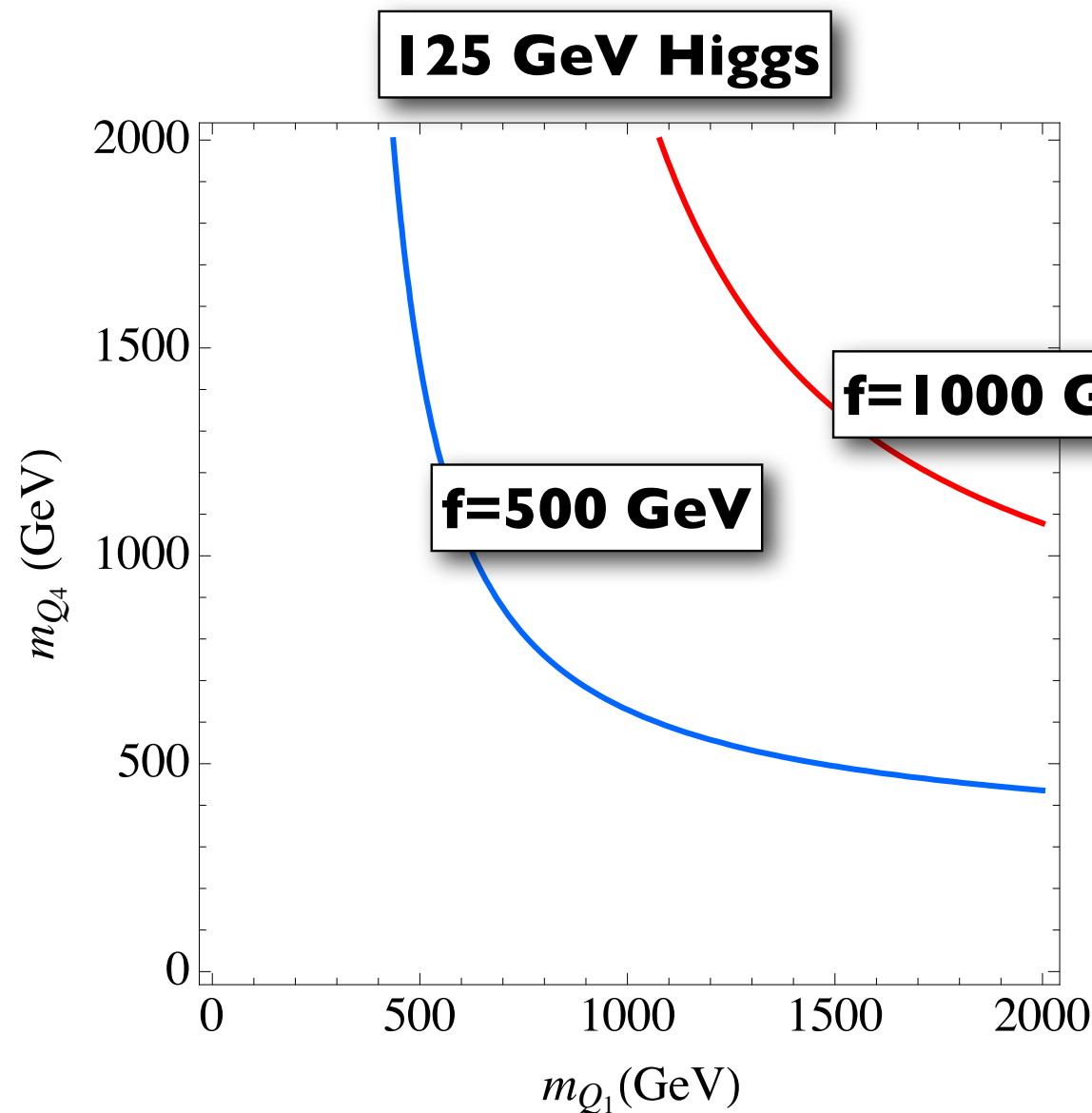
Pomarol et al; Marzocca



# Light Higgs implies light fermionic top partners

$$m_h^2 \simeq \frac{N_c}{\pi^2} \left[ \frac{m_t^2}{f^2} \frac{m_{Q_4}^2 m_{Q_1}^2}{m_{Q_1}^2 - m_{Q_4}^2} \log \left( \frac{m_{Q_1}^2}{m_{Q_4}^2} \right) \right]$$

Pomarol et al; Marzocca



$$5 = 4 + 1$$

$Q_4 \quad Q_1$

with EM charges 5/3, 2/3, -1/3

Contino et al; Pomarol, Riva;  
Matsedonskyi, Panico, Wulzer; Redi, Tesi;  
Marzocca, Serone, Shu;

# Light Higgs implies light fermionic top partners

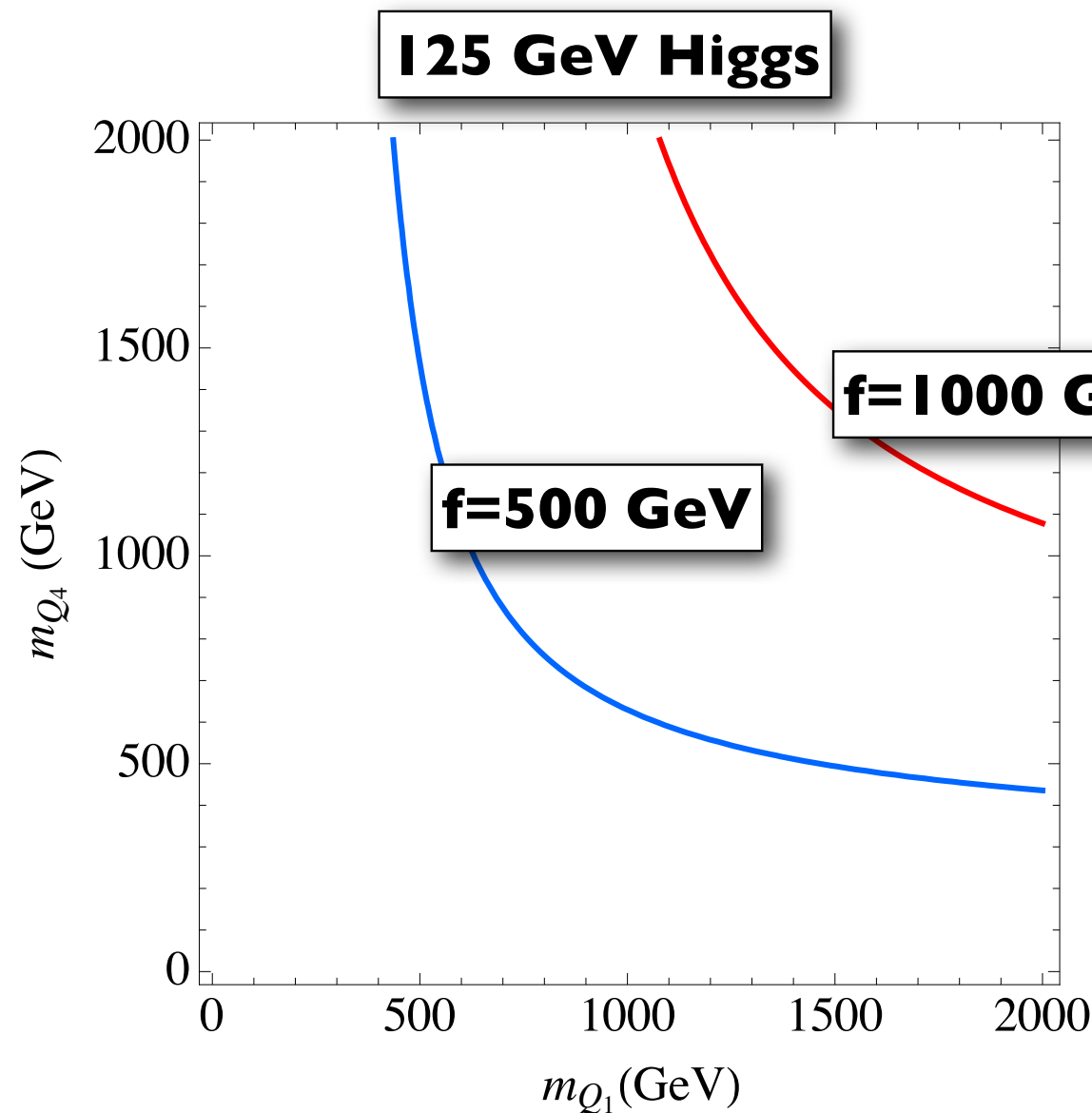
$$m_h^2 \simeq \frac{N_c}{\pi^2} \left[ \frac{m_t^2}{f^2} \frac{m_{Q_4}^2 m_{Q_1}^2}{m_{Q_1}^2 - m_{Q_4}^2} \log \left( \frac{m_{Q_1}^2}{m_{Q_4}^2} \right) \right]$$

Pomarol et al; Marzocca

# Light Higgs implies light fermionic top partners

$$m_h^2 \simeq \frac{N_c}{\pi^2} \left[ \frac{m_t^2}{f^2} \frac{m_{Q_4}^2 m_{Q_1}^2}{m_{Q_1}^2 - m_{Q_4}^2} \log \left( \frac{m_{Q_1}^2}{m_{Q_4}^2} \right) \right]$$

Pomarol et al; Marzocca



$$5 = 4 + 1$$

$Q_4 \quad Q_1$

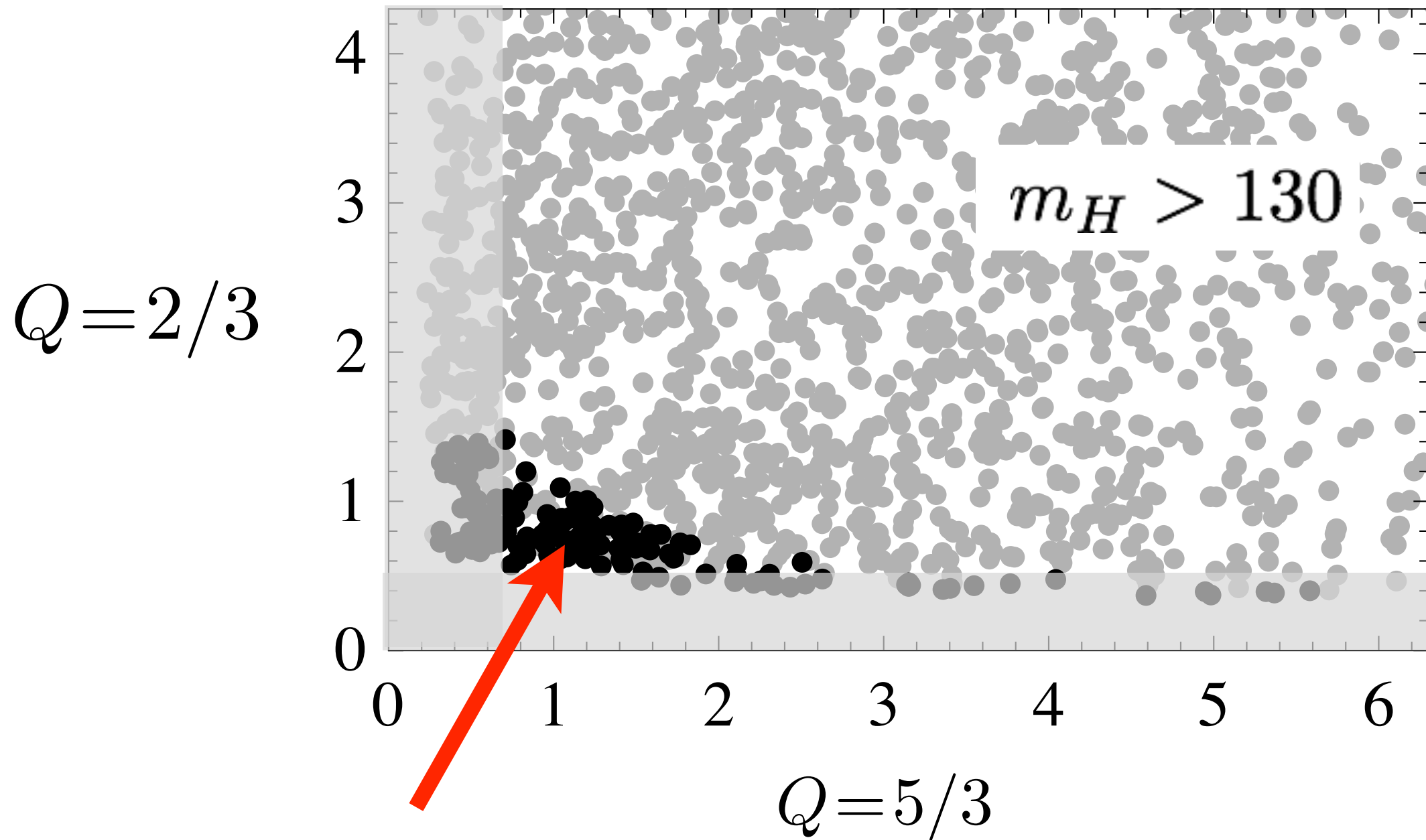
with EM charges 5/3, 2/3, -1/3

Contino et al; Pomarol, Riva;  
Matsedonskyi, Panico, Wulzer; Redi, Tesi;  
Marzocca, Serone, Shu;

# Scan over composite Higgs parameter space

$$\xi = 0.2$$

from 1204.6333



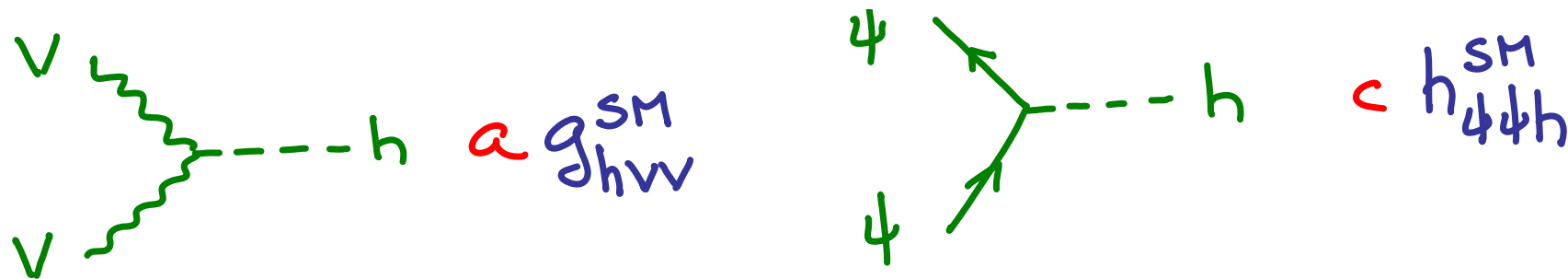
$$m_H = 115 \dots 130 \text{ GeV}$$

# Deviations from SM Higgs

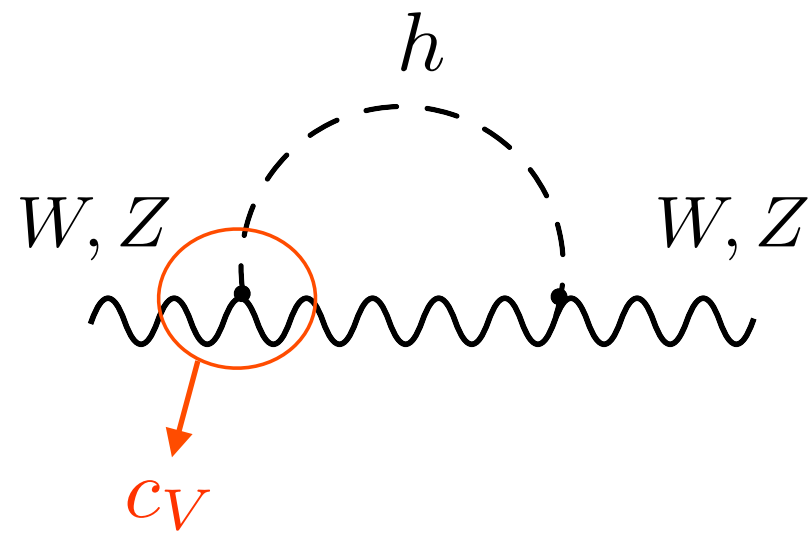
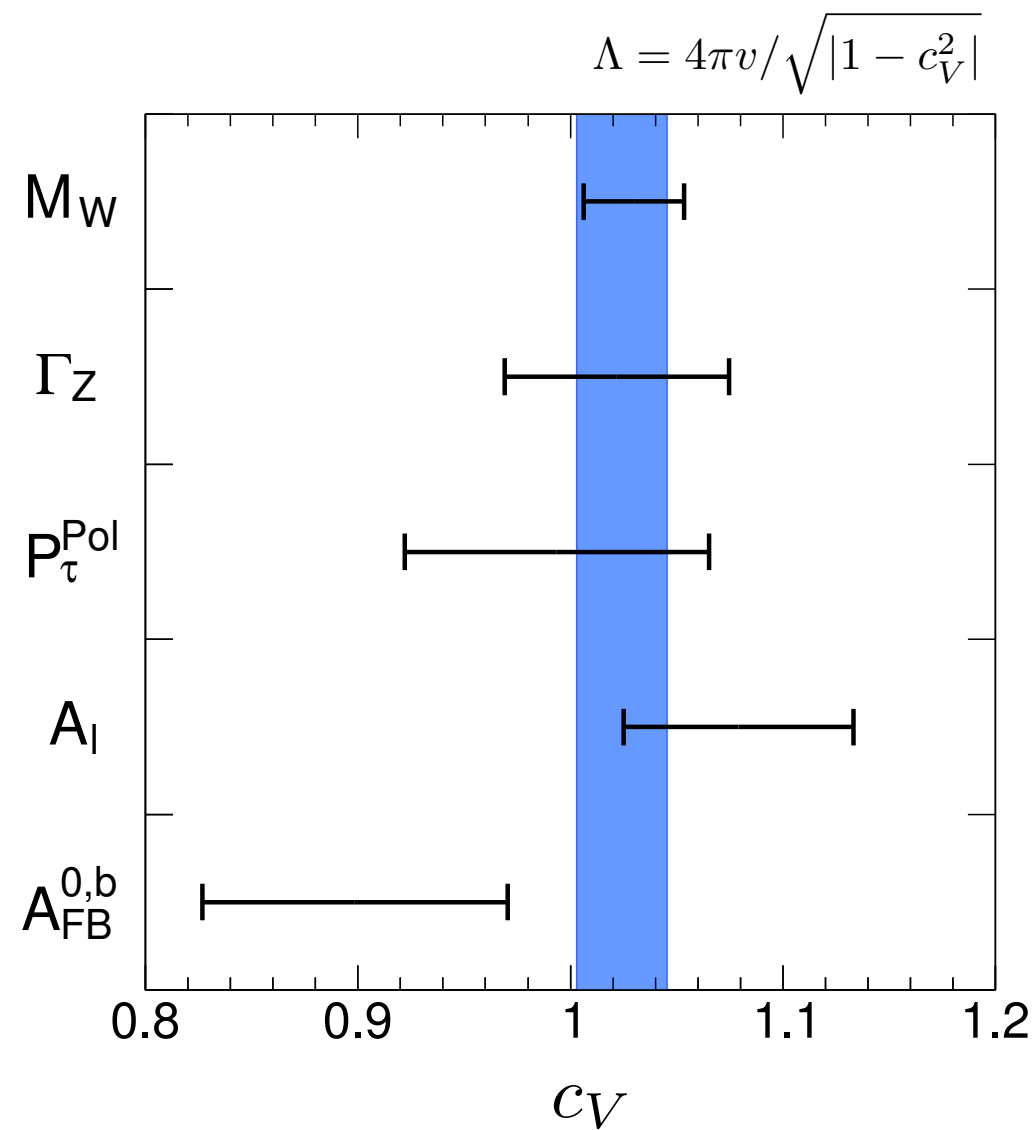
## Goldstone boson nature

$$f^2 \left| \partial_\mu e^{i\pi/f} \right|^2 = |D_\mu H|^2 + \frac{c_H}{2f^2} [\partial_\mu (H^\dagger H)]^2 + \frac{c'_H}{2f^4} (H^\dagger H) [\partial_\mu (H^\dagger H)]^2 + \dots$$

Giudice et al. JHEP 0706 (2007) 045



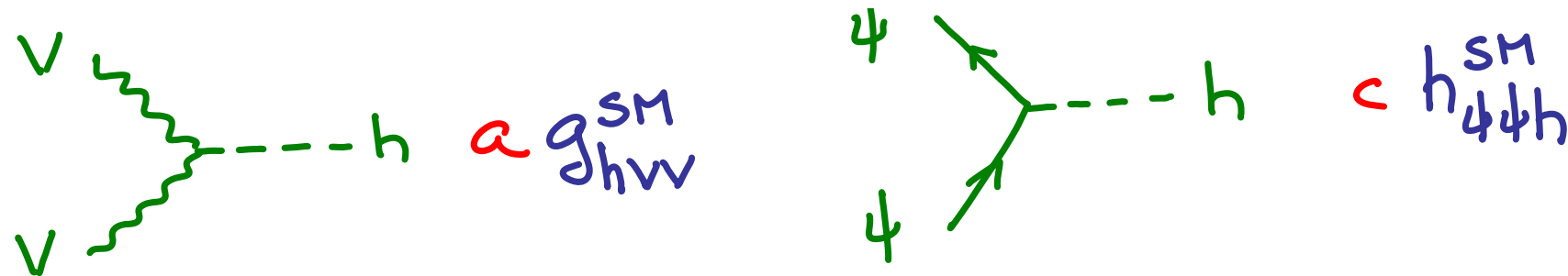
# EW precision tests



Ciuchini, Franco, Silvestrini, Mishima, arXiv:1306.4644

# Higgs couplings

Have been measured to 20-30% precision



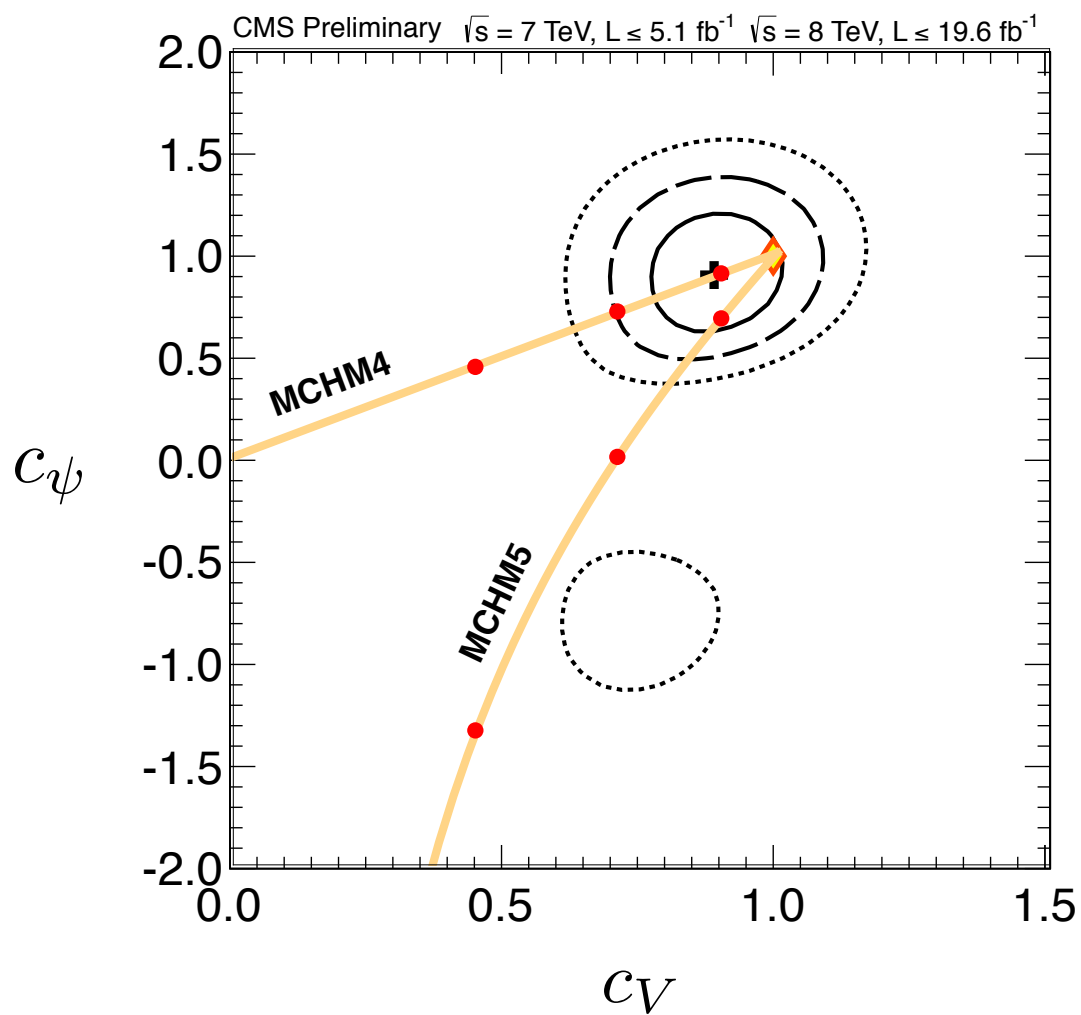
Expect deviations  $\sim (v/f)^2$

$$\xi \equiv \frac{v^2}{f^2}$$

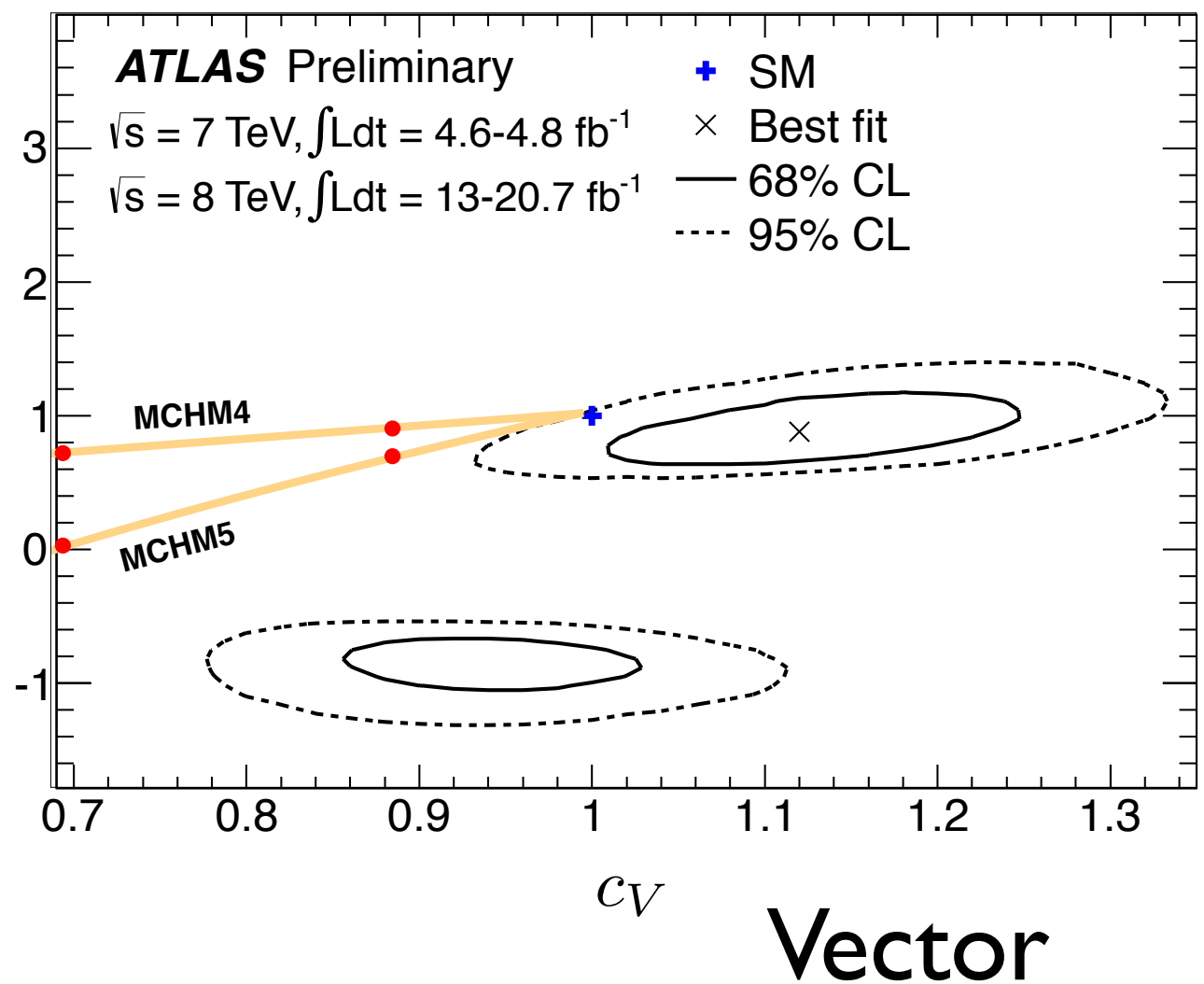
$$a = \sqrt{1 - \xi}$$

$$c_f = \frac{1 - (1 + n)\xi}{1 - \xi}$$

# Higgs couplings



Fermion

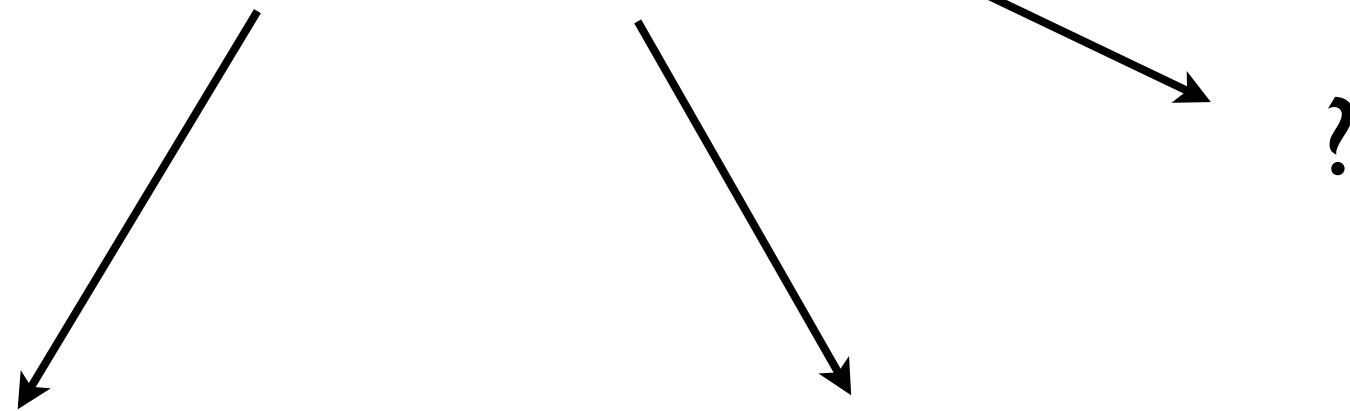


Red points at  $\xi \equiv (v/f)^2 = 0.2, 0.5, 0.8$



# New physics & naturalness

## Light Higgs



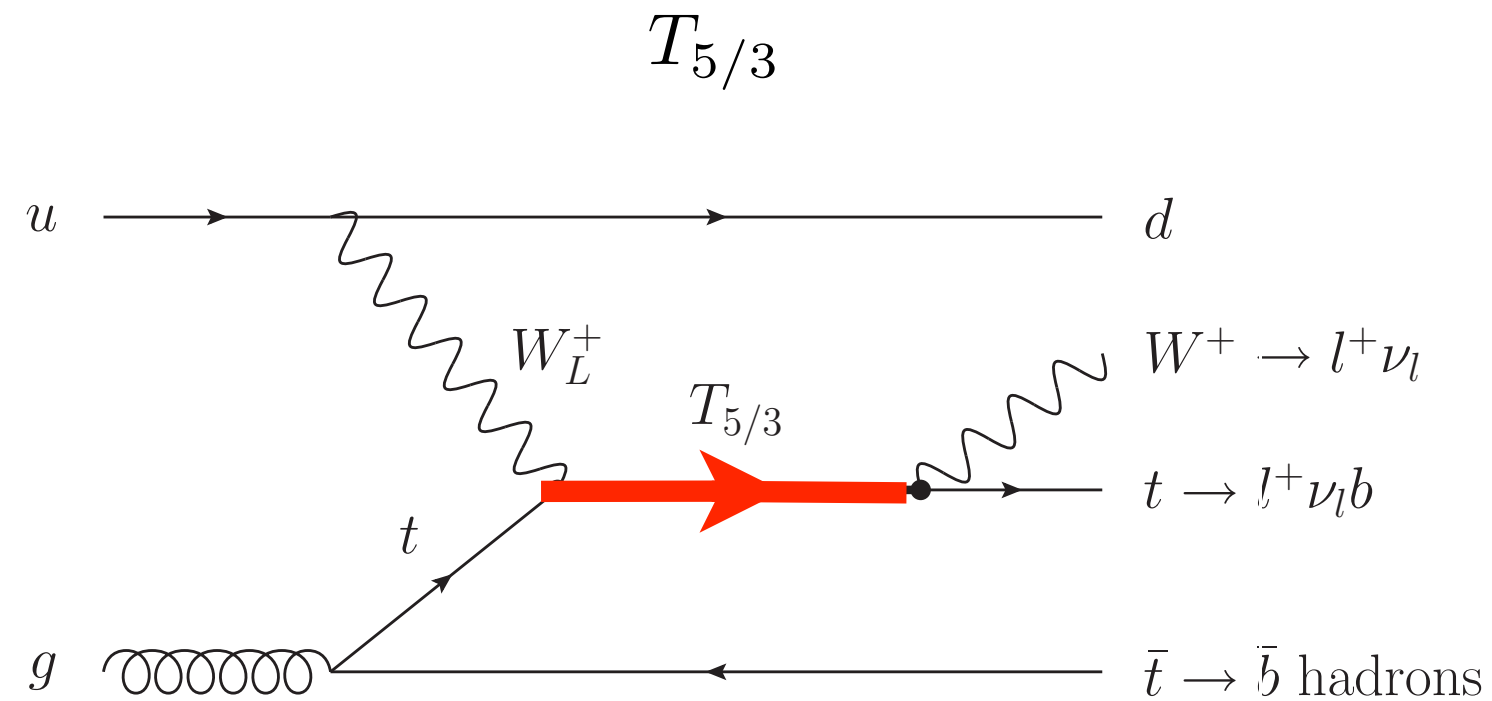
light stops<sub>1,2</sub>, sbottom<sub>L</sub>,  
higgsinos, gluinos, ...

supersymmetry

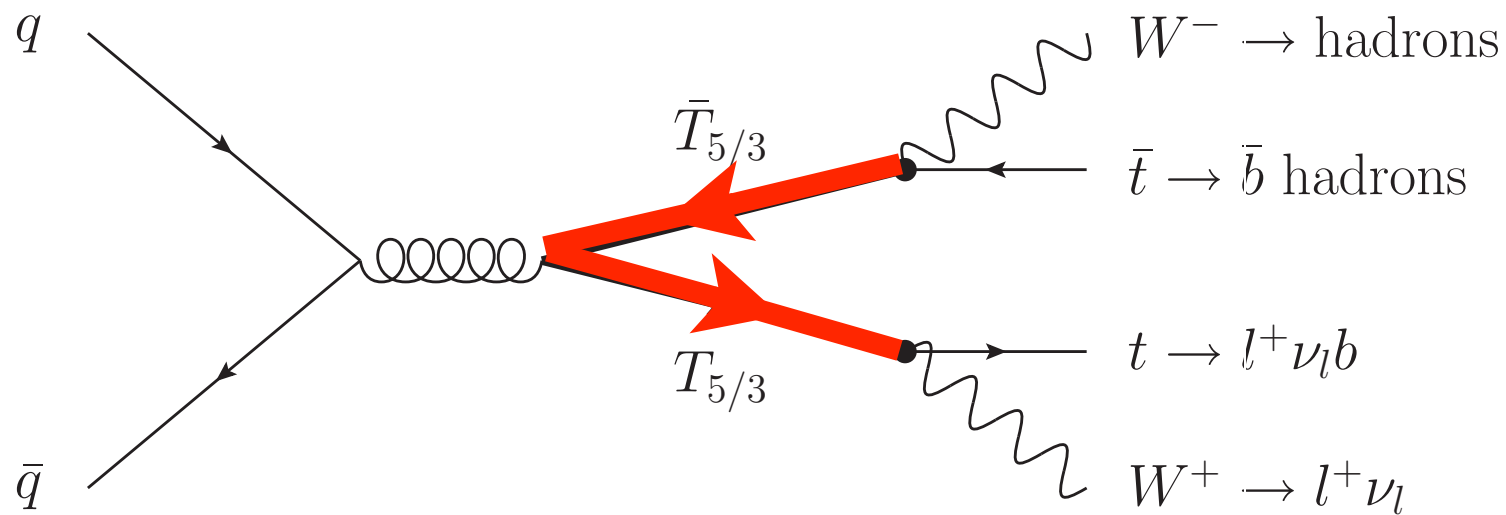
light top partners  
( $Q=5/3, 2/3, 1/3$ ),  
anything else ?

composite Higgs

e.g. Perelstein, Pierce, Peskin  
 Contino, Servant; Mrazek, Wulzer;  
 De Simone, Matsedonkyi, Rattazzi, Wulzer



Single



Double

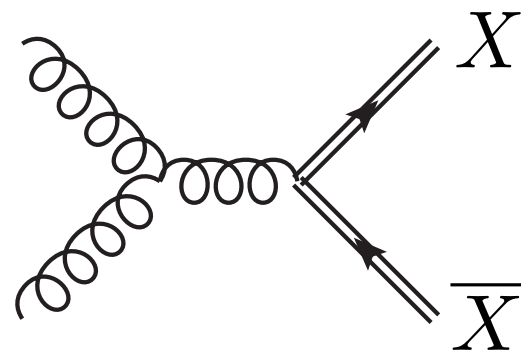
Spectrum:

$\text{---} B$   
 $\text{---} T$

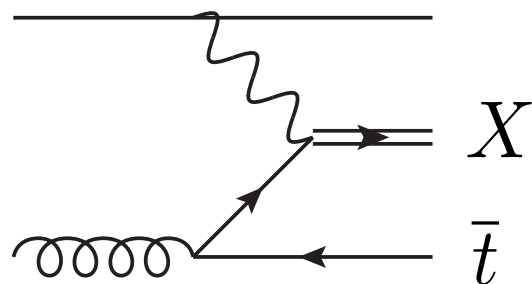
$\text{==} X_{2/3}$   
 $\text{==} X_{5/3}$

# Phenomenology

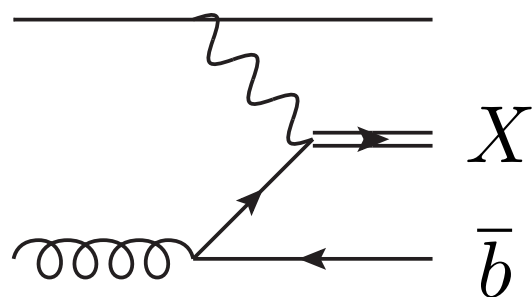
## Three possible production mechanisms



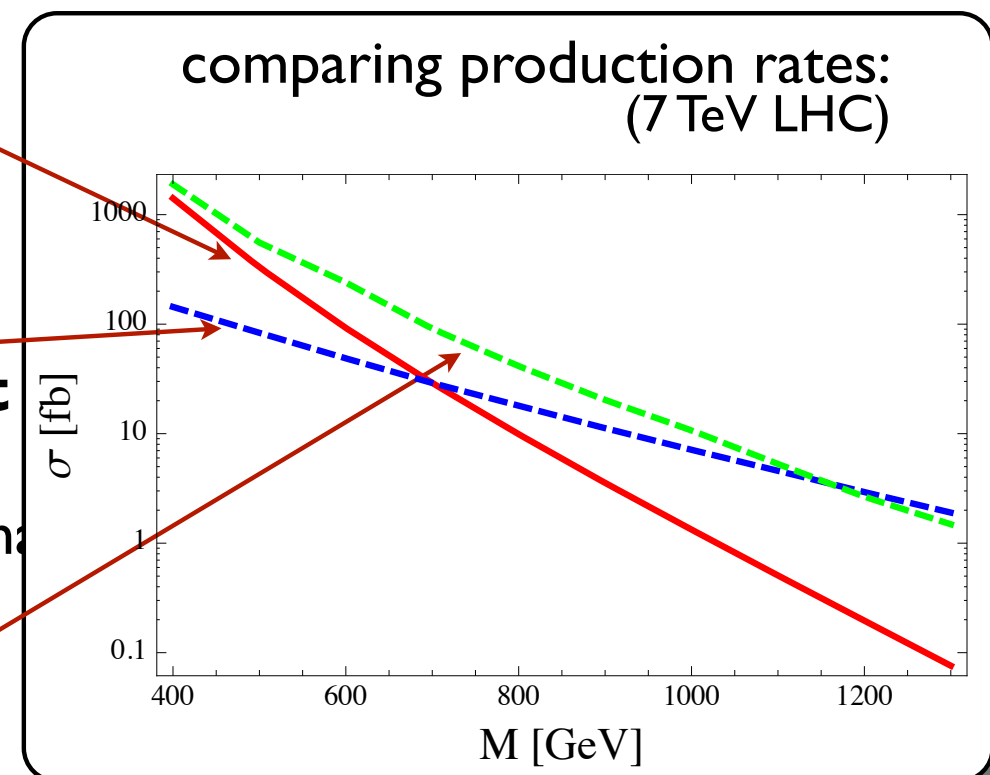
**QCD pair prod.**  
model indep.,  
relevant at low mass



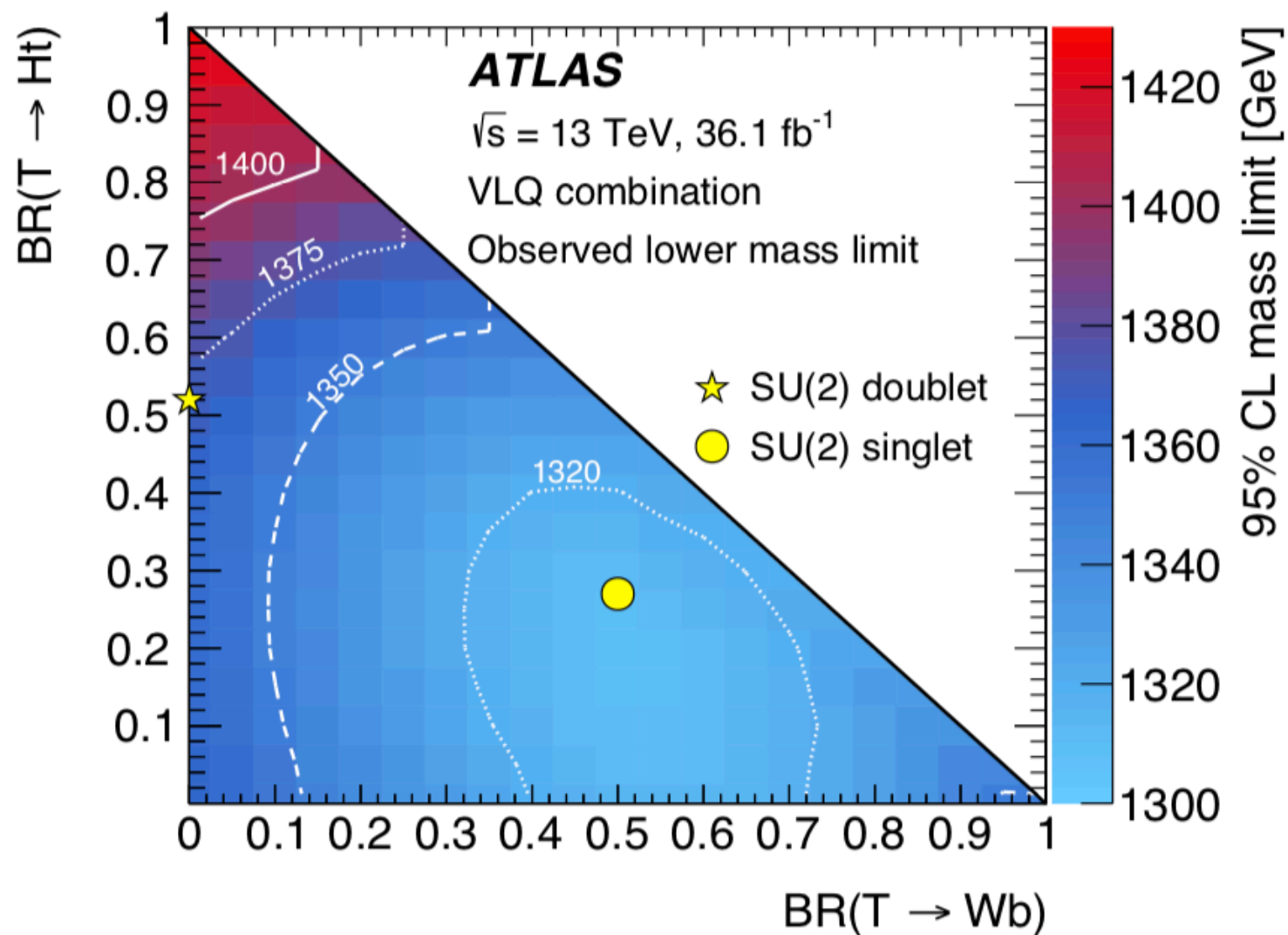
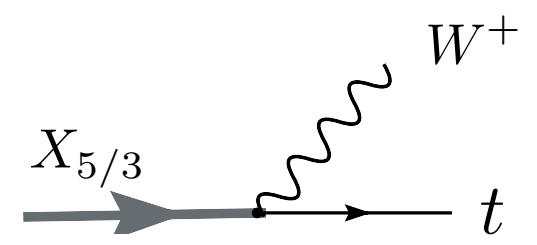
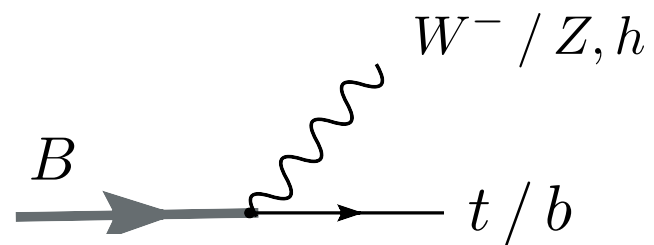
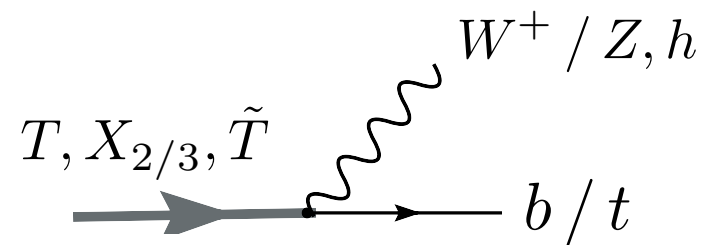
**single prod. with  $t$**   
model dep. coupling  
pdf-favored at high mass



**single prod. with  $b$**   
favored by small  $b$  mass  
**dominant** when allowed

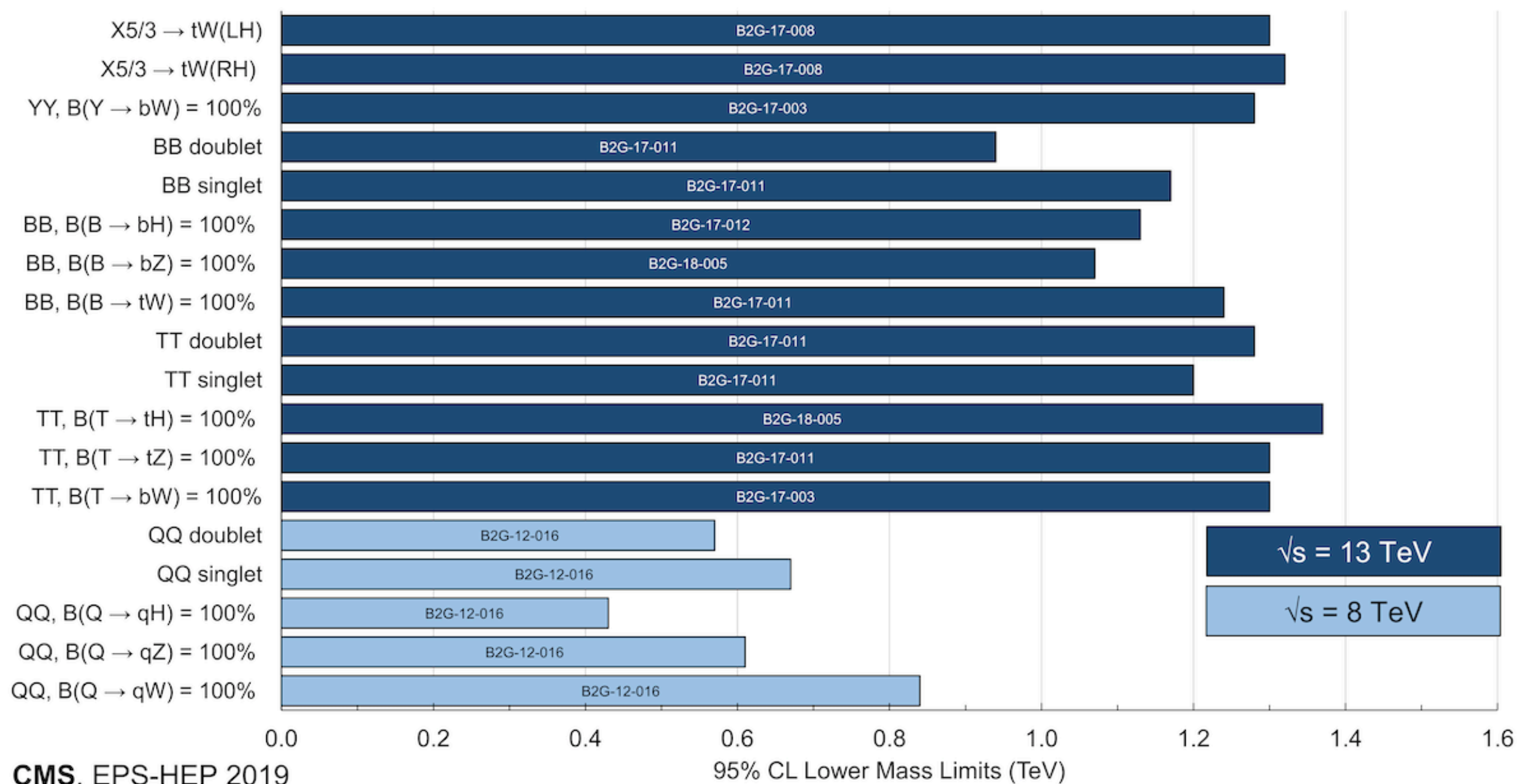


# Decay modes



Current limits  
 $> 1300 \text{ GeV}$

## Vector-like quark pair production



# New ideas

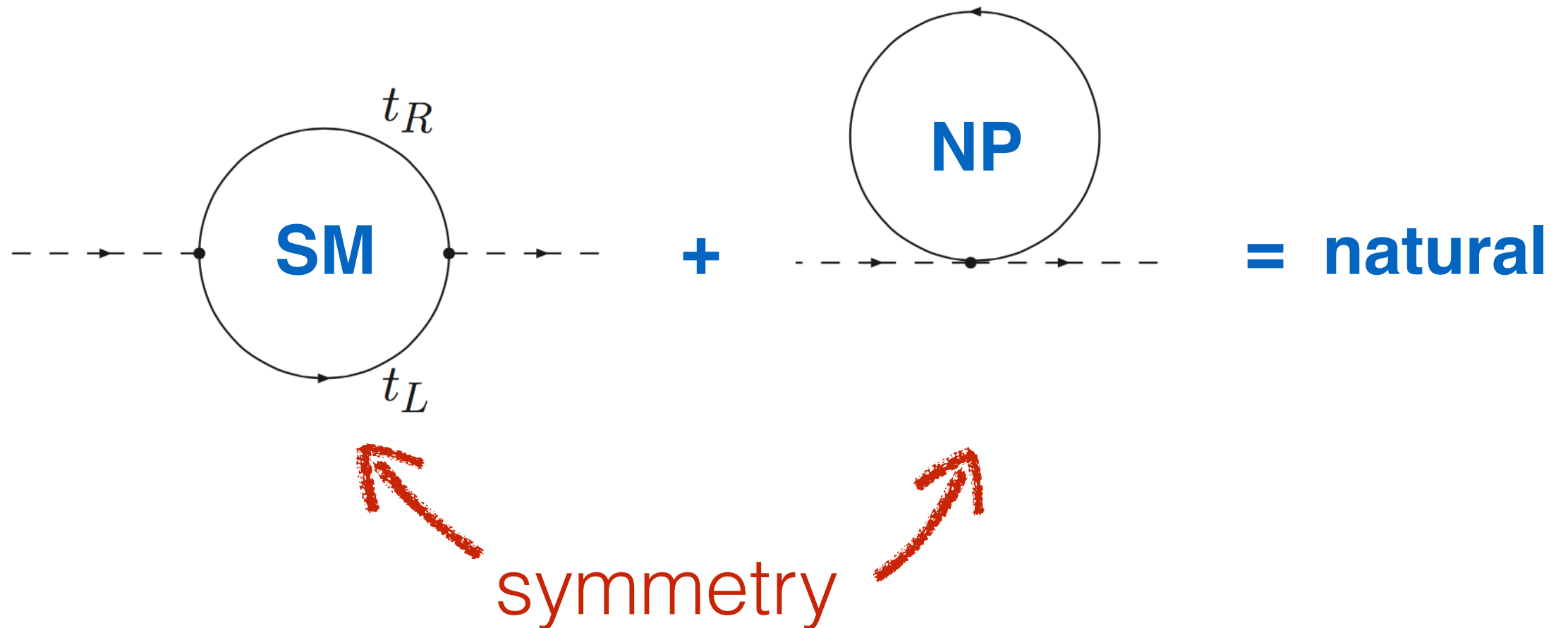
twin Higgs



Relaxion

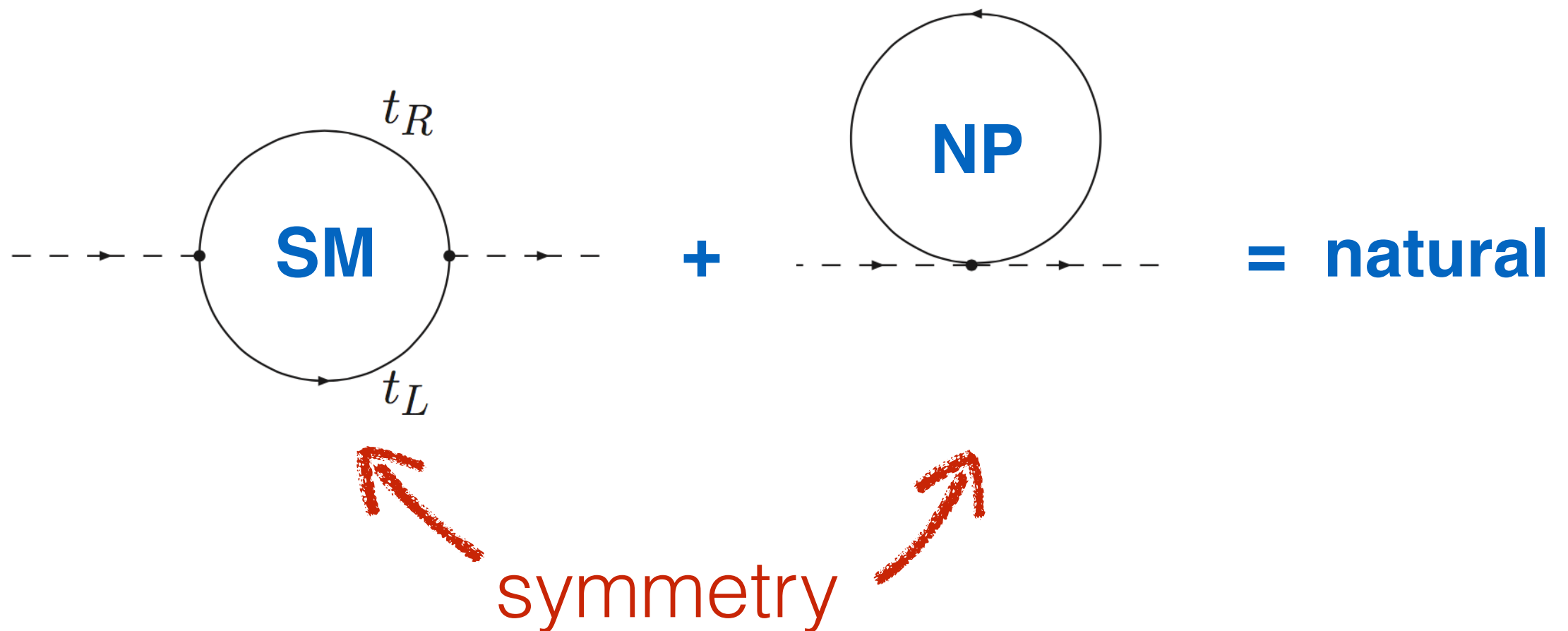


# No lose for naturalness?





# No lose for naturalness?

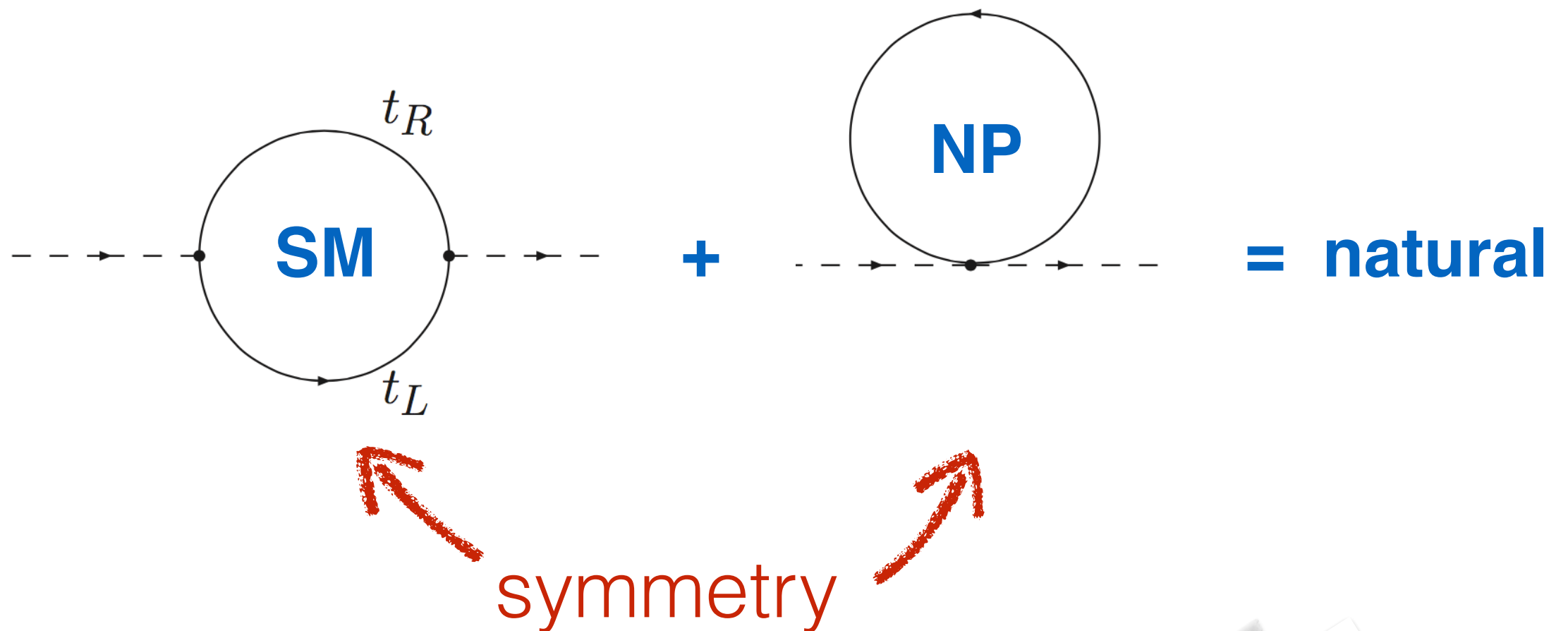


NP is related to the top by a symmetry, natural new particle mass around TeV

Symmetry commutes with color: will be produced copiously at the LHC!



# No lose for naturalness?

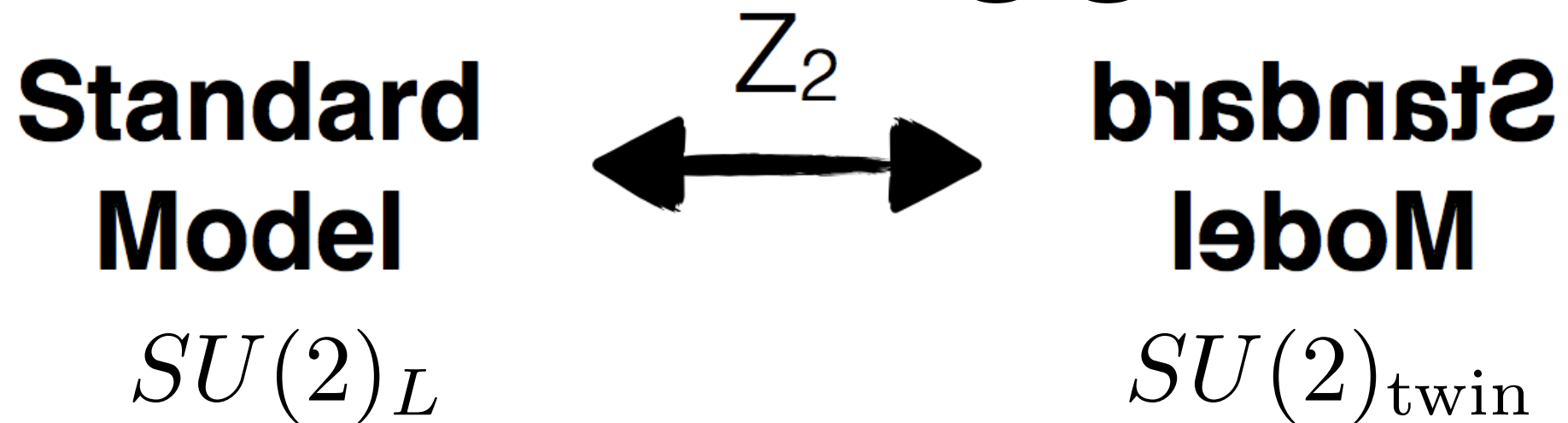


NP is related to the top by a symmetry, natural new particle mass around TeV

Symmetry broken with color: produced copiously at the LHC!

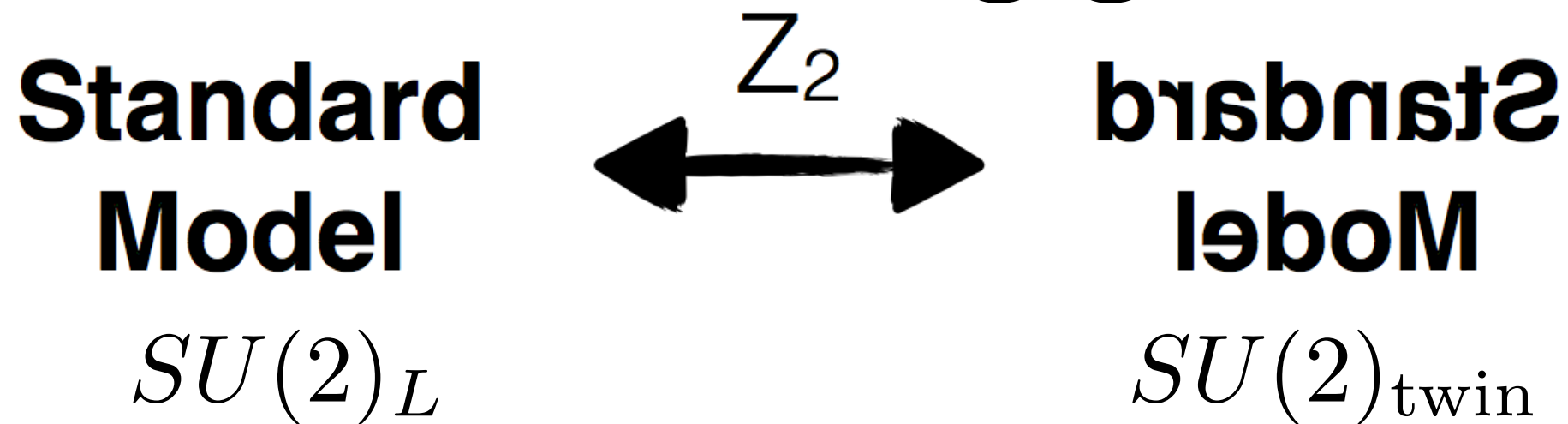
**Not true!**

# Twin Higgs

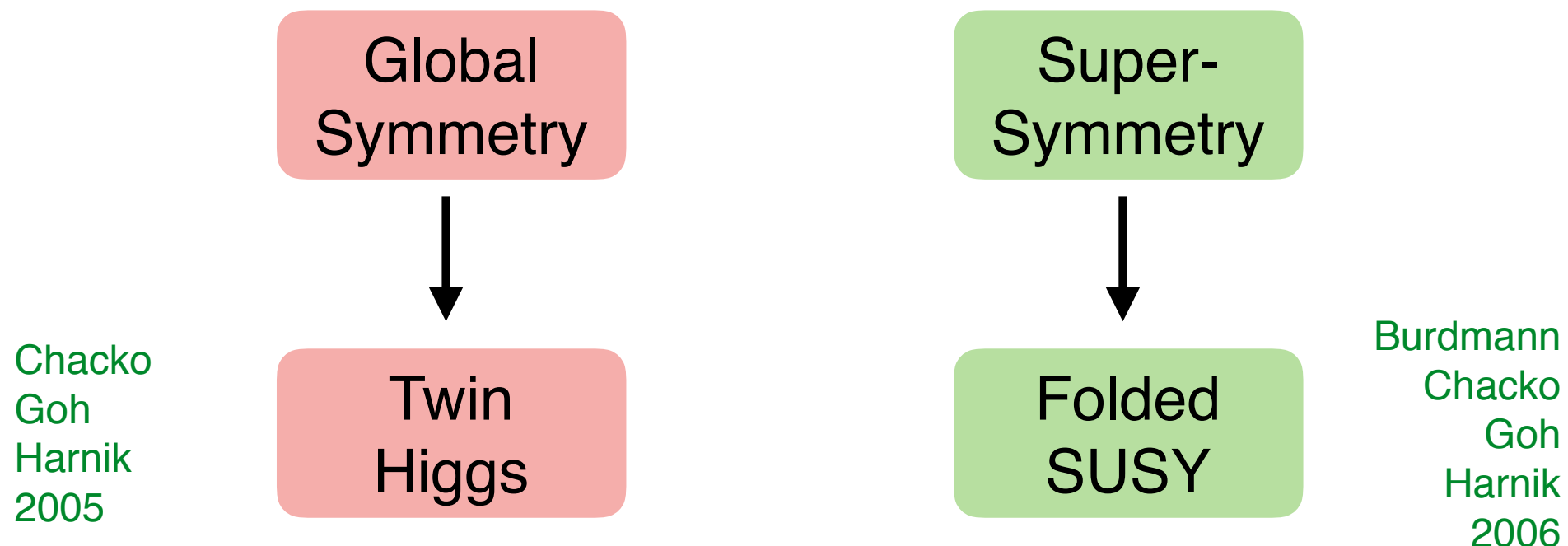


Quadratic divergences from SM top quark loops cancelled by loops of “Twin” top quarks.

# Twin Higgs



Quadratic divergences from SM top quark loops cancelled by loops of “Twin” top quarks.



**Under the gauge symmetry,**

$$H = \begin{pmatrix} H_A \\ H_B \end{pmatrix}$$

**where  $H_A$  will eventually be identified with the Standard Model Higgs, while  $H_B$  is its 'twin partner'.**

**Now the Higgs potential receives radiative corrections from gauge fields**

$$\Delta V(H) = \frac{9g_A^2\Lambda^2}{64\pi^2} H_A^\dagger H_A + \frac{9g_B^2\Lambda^2}{64\pi^2} H_B^\dagger H_B$$

**Impose a  $Z_2$  'twin' symmetry under which  $A \leftrightarrow B$ . Then  $g_A = g_B = g$ . Then the radiative corrections take the form**

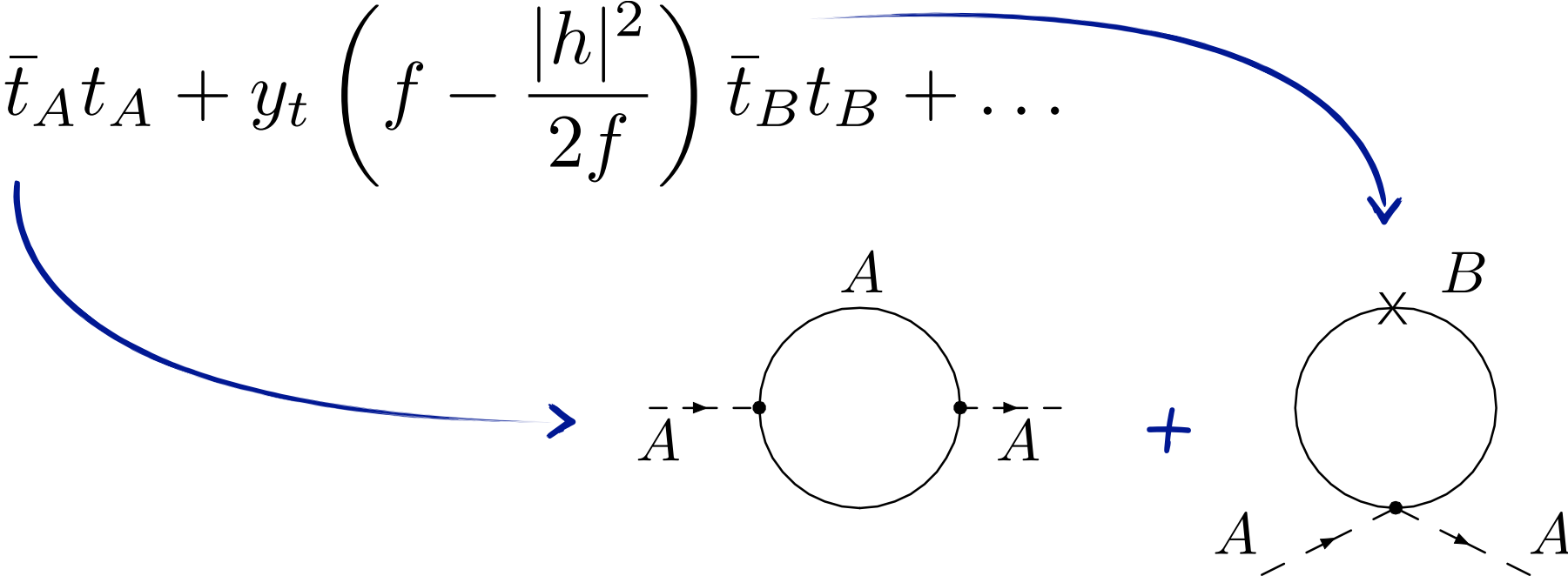
$$\Delta V = \frac{9g^2\Lambda^2}{64\pi^2} (H_A^\dagger H_A + H_B^\dagger H_B)$$

**This is U(4) invariant and cannot give a mass to the Goldstones!**

Parity symmetry enforces  $y_t$  same

$$\mathcal{L} \supset y_t H_A \bar{t}_A t_A + y_t H_B \bar{t}_B t_B$$

$$= y_t h \bar{t}_A t_A + y_t \left( f - \frac{|h|^2}{2f} \right) \bar{t}_B t_B + \dots$$

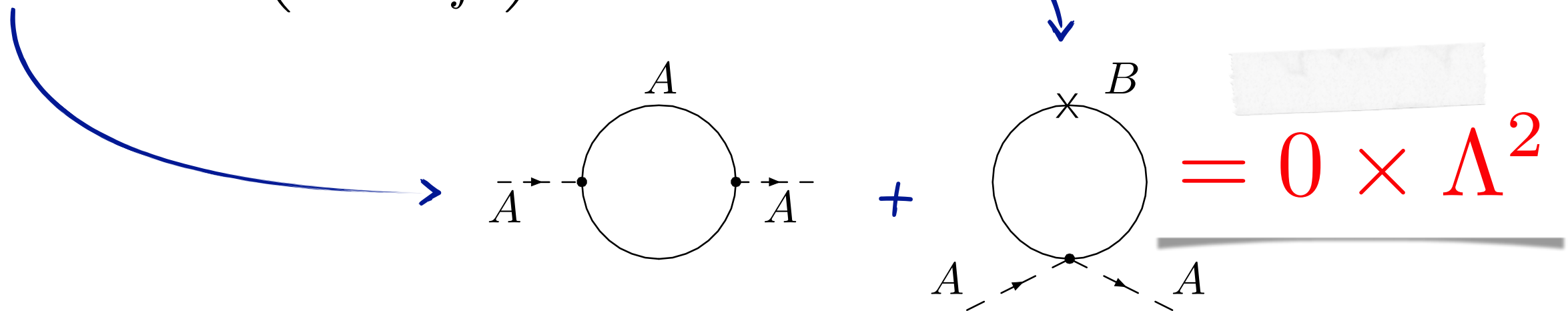


Same coupling, but not same colour group for top and top partner! Still: little Higgs like cancellation.

Parity symmetry enforces  $y_t$  same

$$\mathcal{L} \supset y_t H_A \bar{t}_A t_A + y_t H_B \bar{t}_B t_B$$

$$= y_t h \bar{t}_A t_A + y_t \left( f - \frac{|h|^2}{2f} \right) \bar{t}_B t_B + \dots$$



Same coupling, but not same colour group for top and top partner! Still: little Higgs like cancellation.

- Mirror sector is copy of SM, completely neutral under SM interactions
- Allowed interaction terms:

$$\lambda_{AB} |H_A|^2 |H_B|^2$$

Higgs portal

$$\epsilon_{AB} F_{\mu\nu,A} F_B^{\mu\nu}$$

kinetic mixing portal



- Mirror sector is copy of SM, ~~completely neutral~~ under SM interactions
- Allowed interaction terms:

# Hypercharged Naturalness

Javi Serra<sup>a</sup>, Stefan Stelzl<sup>a</sup>, Riccardo Torre<sup>b,c</sup>, and Andreas Weiler<sup>a</sup>

<sup>a</sup> *Physik-Department, Technische Universität München, 85748 Garching, Germany*

<sup>b</sup> *Theoretical Physics Department, CERN, 1211 Geneva 23, Switzerland*

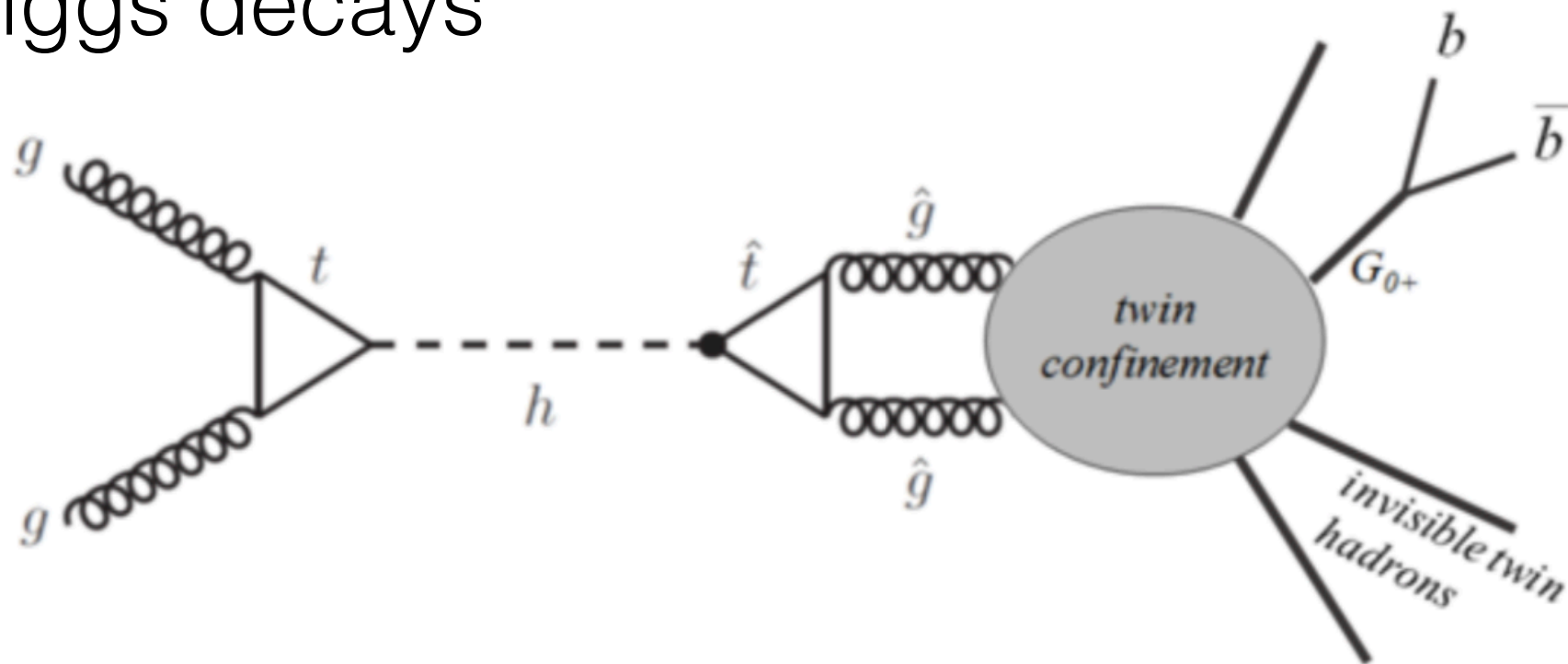
<sup>c</sup> *INFN, Sezione di Genova, Via Dodecaneso 33, 16146 Genova, Italy*

## Abstract

We present an exceptional twin-Higgs model with the minimal symmetry structure for an exact implementation of twin parity along with custodial symmetry. Twin particles are mirrors of the Standard Model yet they carry hypercharge, while the photon is identified with its twin. We thoroughly explore the phenomenological signatures of hypercharged naturalness: long-lived charged particles, a colorless twin top with elec-

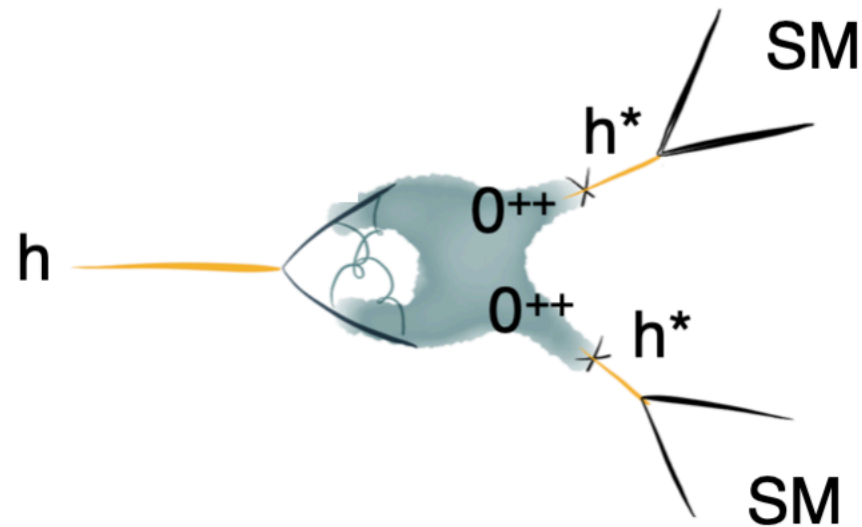
# Twin Higgs consequences

- $SU(3)_B$  confines at  $\Lambda_B > \Lambda_{QCD}$
- Dark sector QCD-like with dark-pions, dark kaons, ...
- Exotic Higgs decays



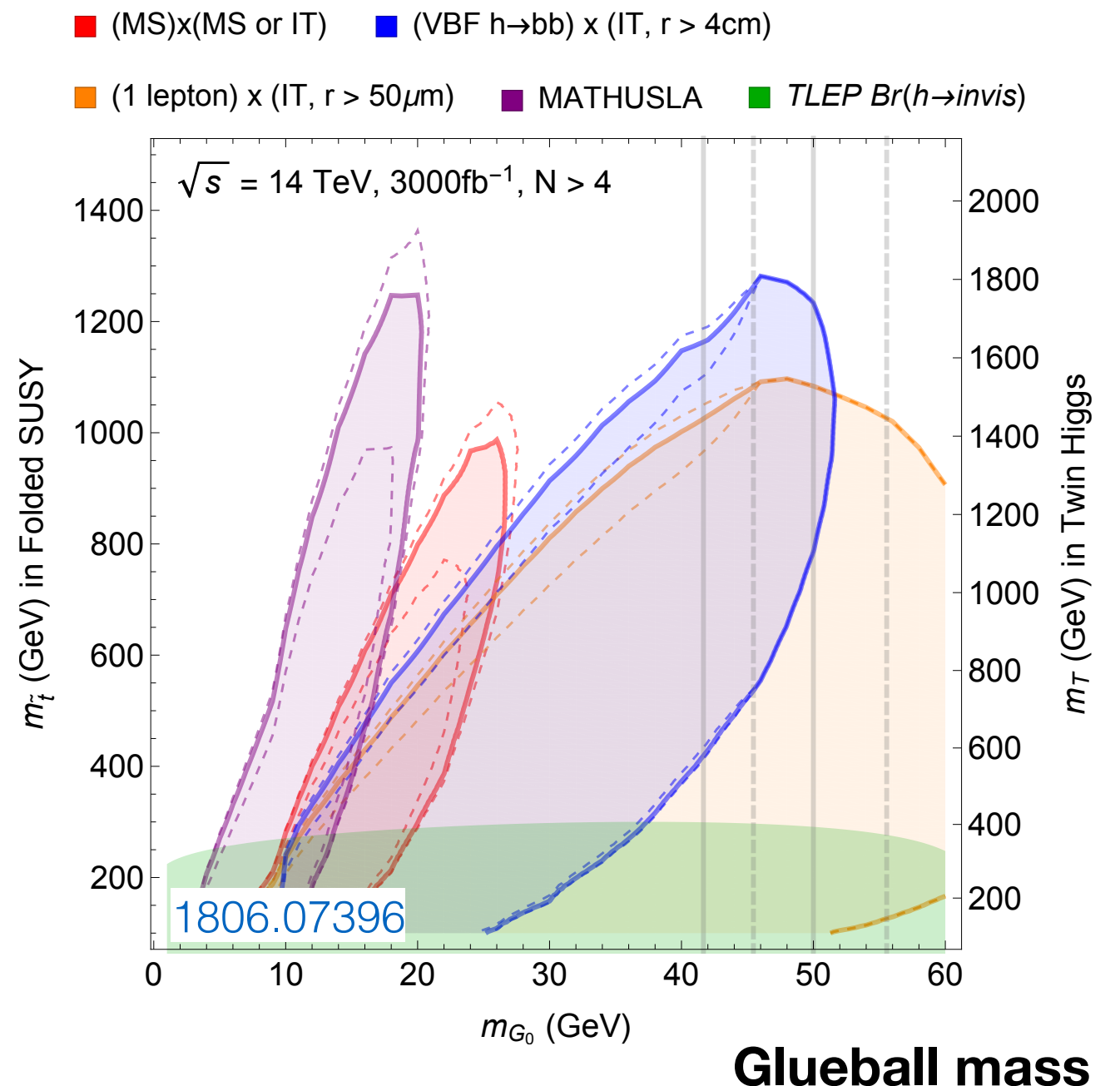
Craig, Katz, Sundrum, Strassler, 2015

# New signature: exotic Higgs decays

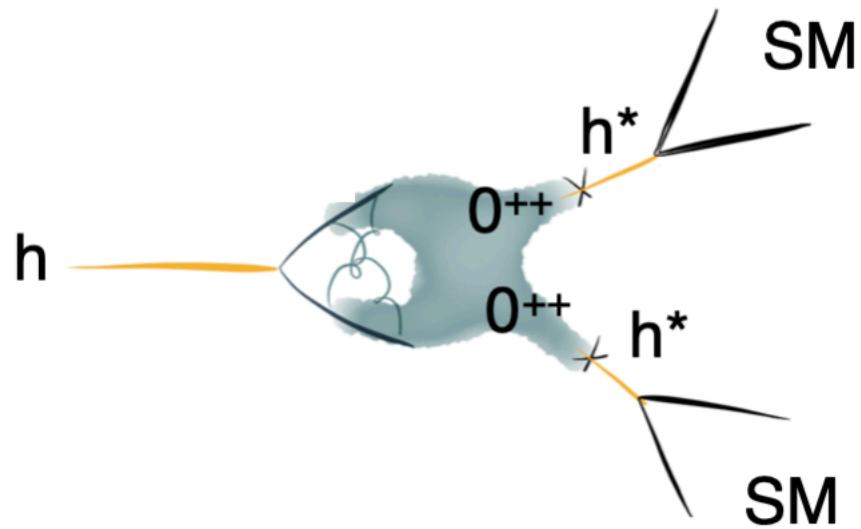


Long-lived Glueballs;  
lightest have same  
quantum # as Higgs

$$\mathcal{L} \supset -\frac{\alpha'_3}{6\pi} \frac{v}{f} \frac{h}{f} G'_{\mu\nu} G'^{\mu\nu}_a$$

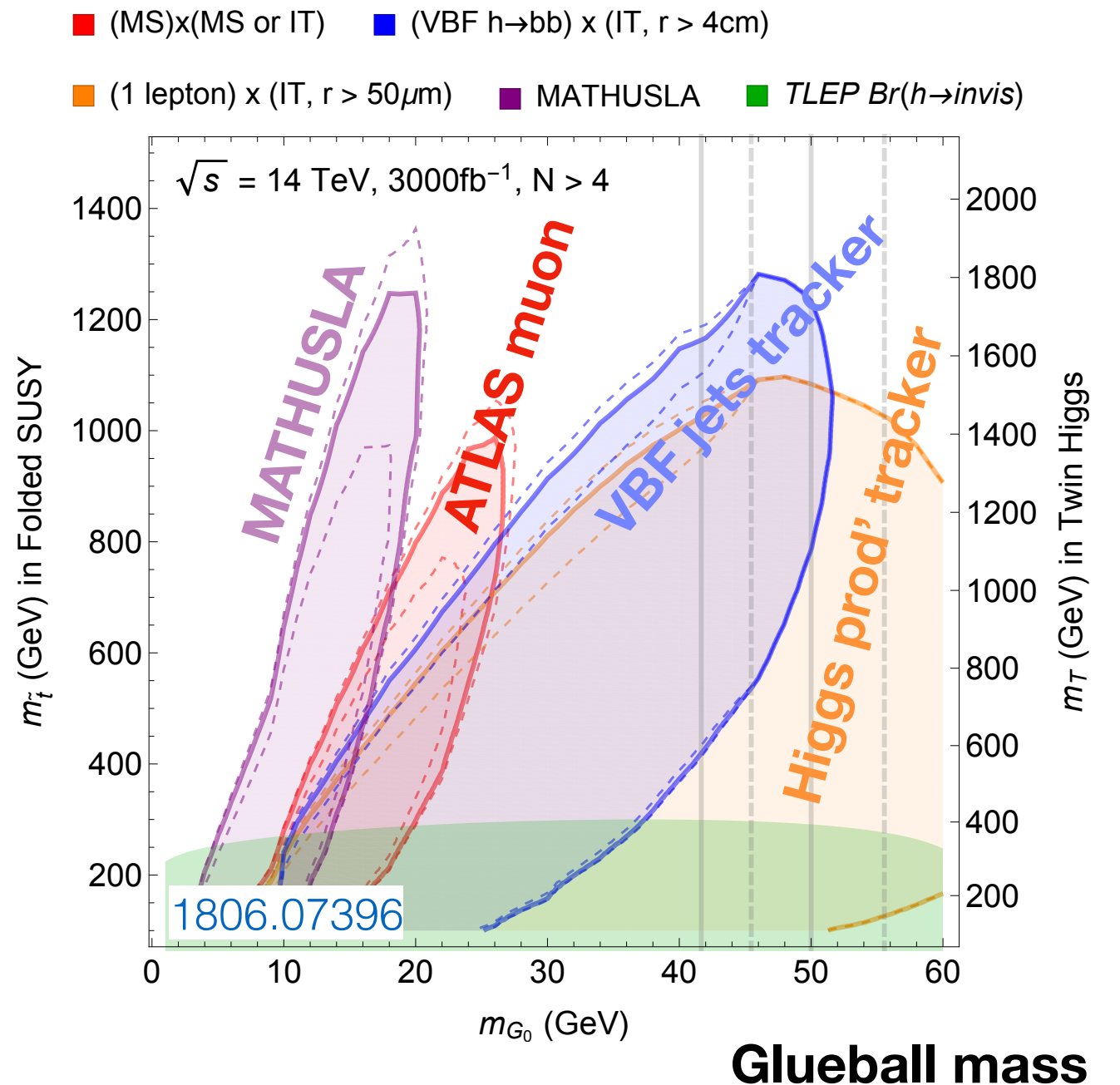


# New signature: exotic Higgs decays



Long-lived Glueballs;  
lightest have same  
quantum # as Higgs

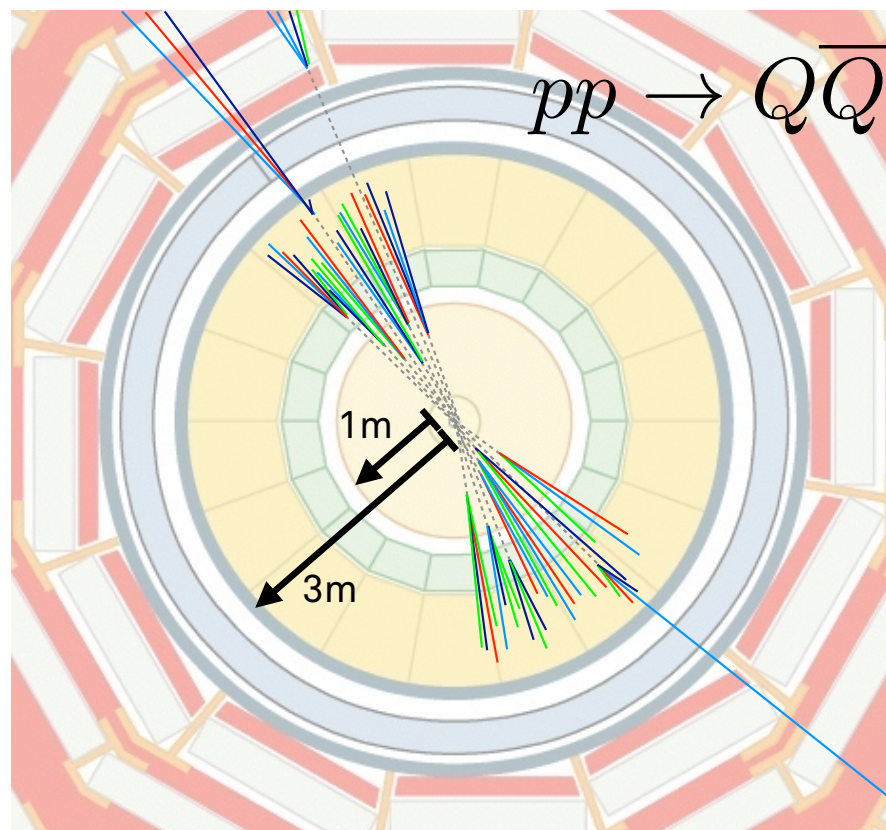
$$\mathcal{L} \supset -\frac{\alpha'_3}{6\pi} \frac{v}{f} \frac{h}{f} G'_{\mu\nu} G'^{\mu\nu}_a$$



# Twin Higgs pheno

Schwaller, Stolarski, AW '15

- Twin parton shower -> Emerging Jets
- Signature of dark sector with long lived states



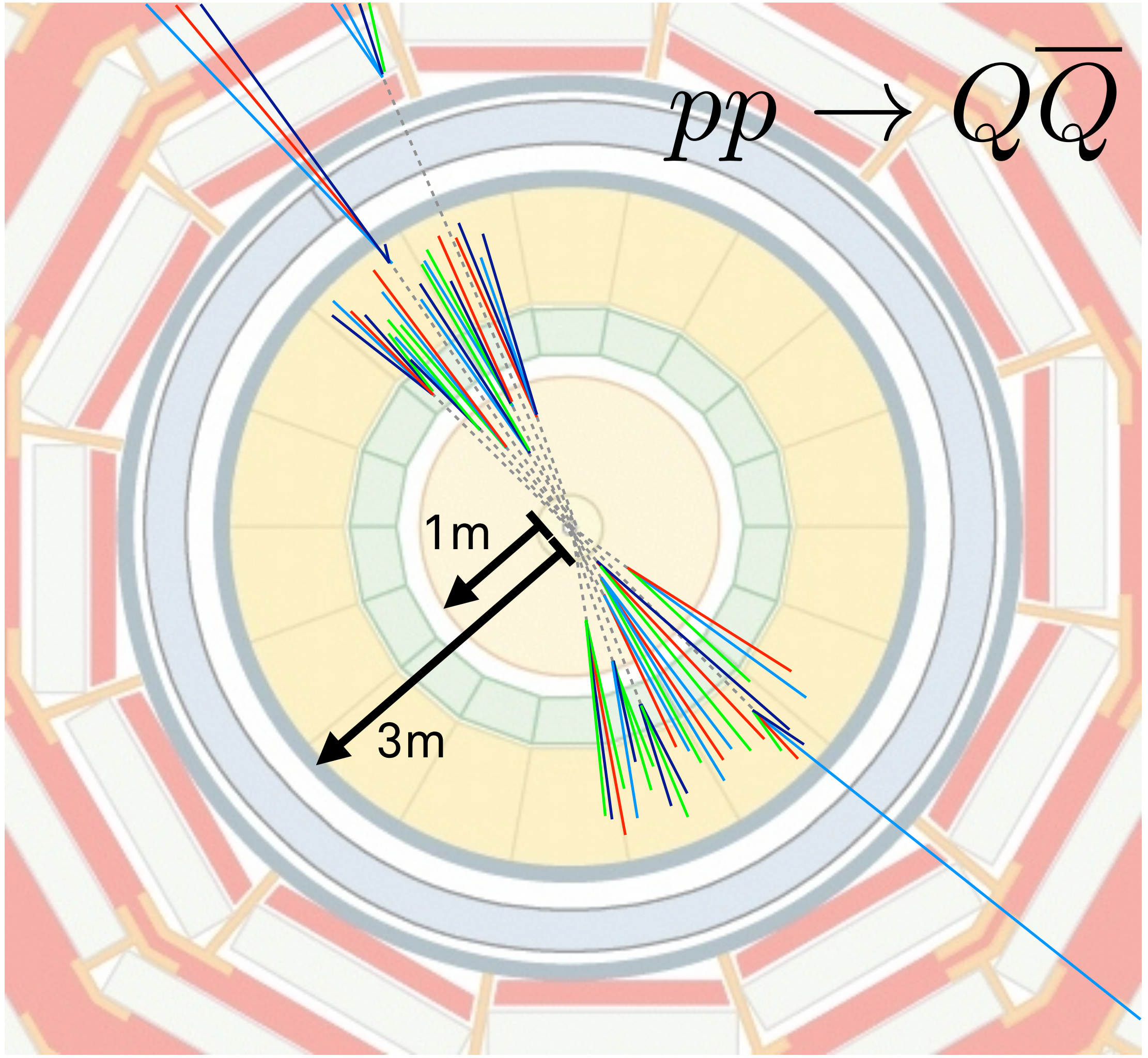


$$pp \rightarrow q_d q_d$$

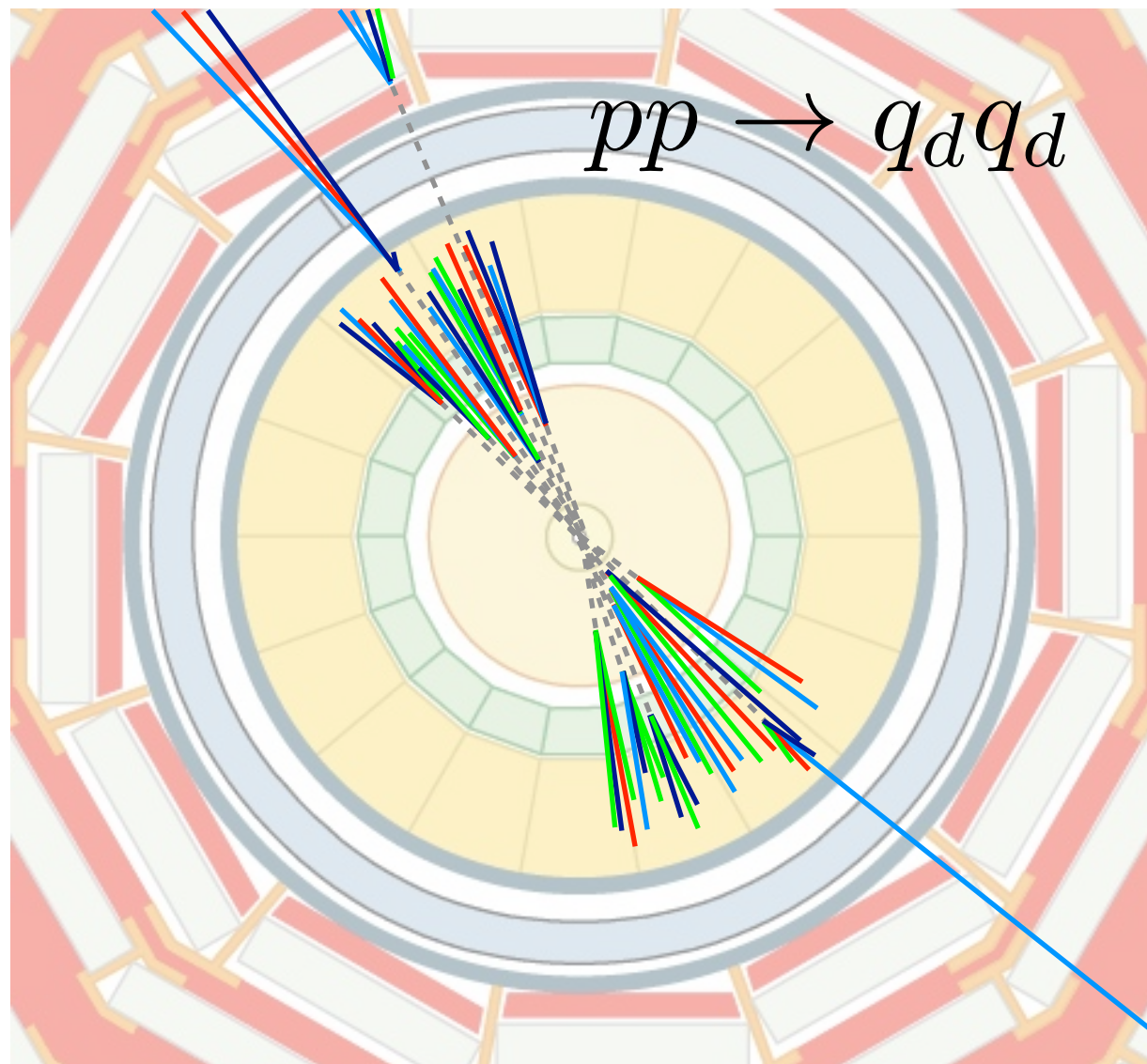


$$pp \rightarrow Q\bar{Q}$$

1m  
3m





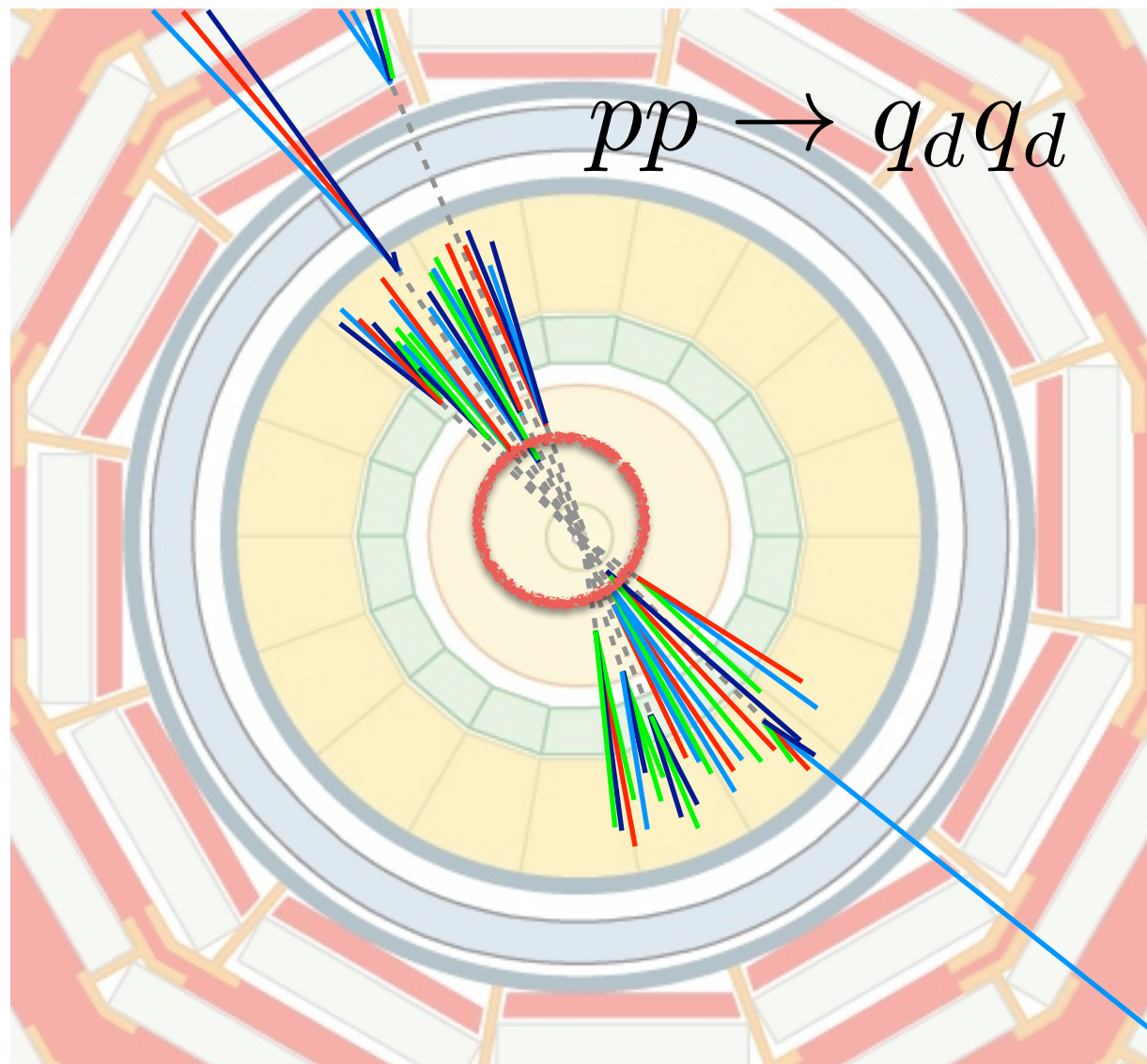


Decay lifetime of  $\sim \text{cm}$

Exponential decay profile: Several displaced vertices inside a jet “cone” (or calo-jet)

No/few tracks originating from interaction point

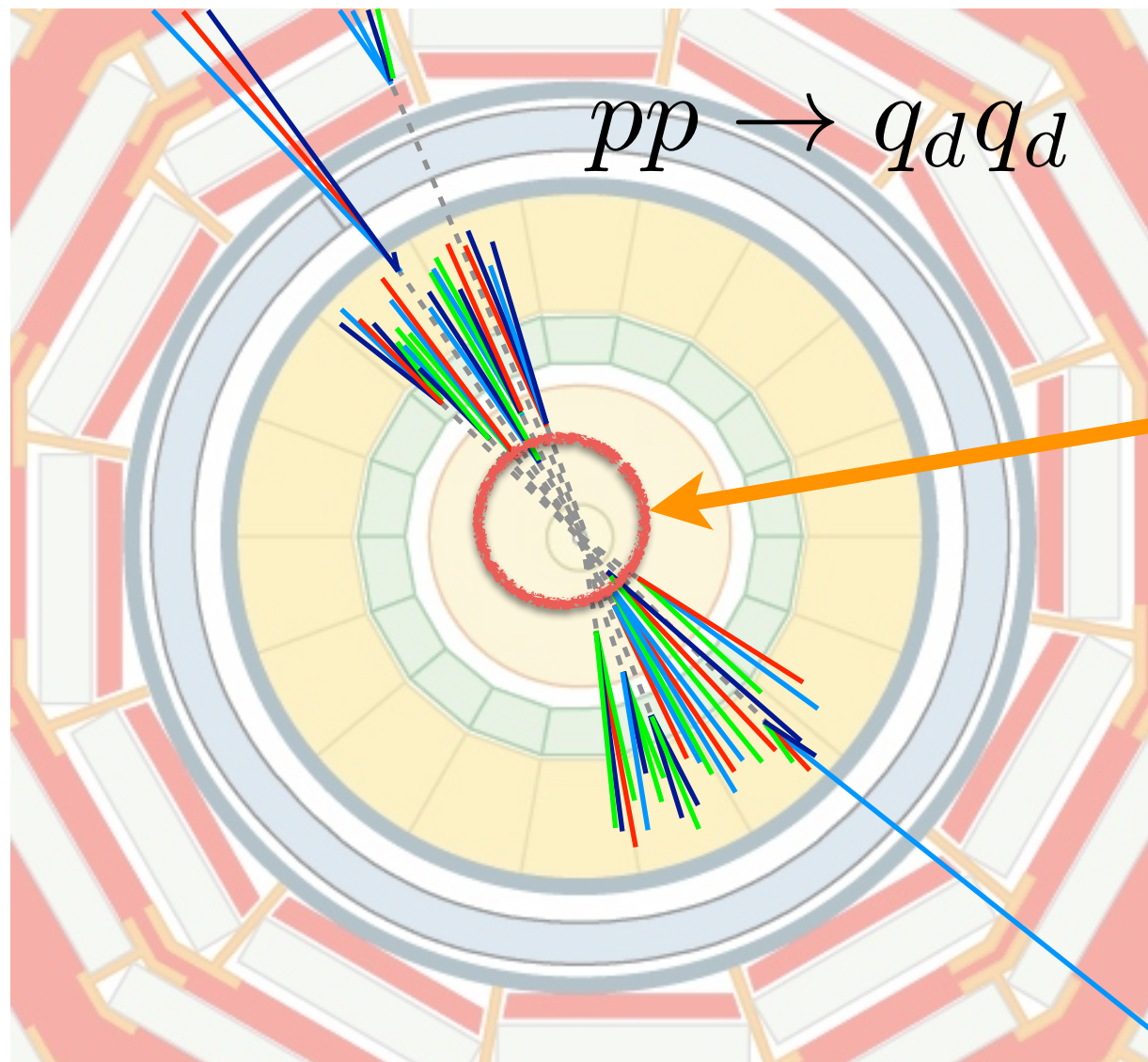




Look for Hcal-jets with no/few tracks below distance to interaction point (inside **circle**)

New '**track-less**' signature

Universal for a large class of displaced physics



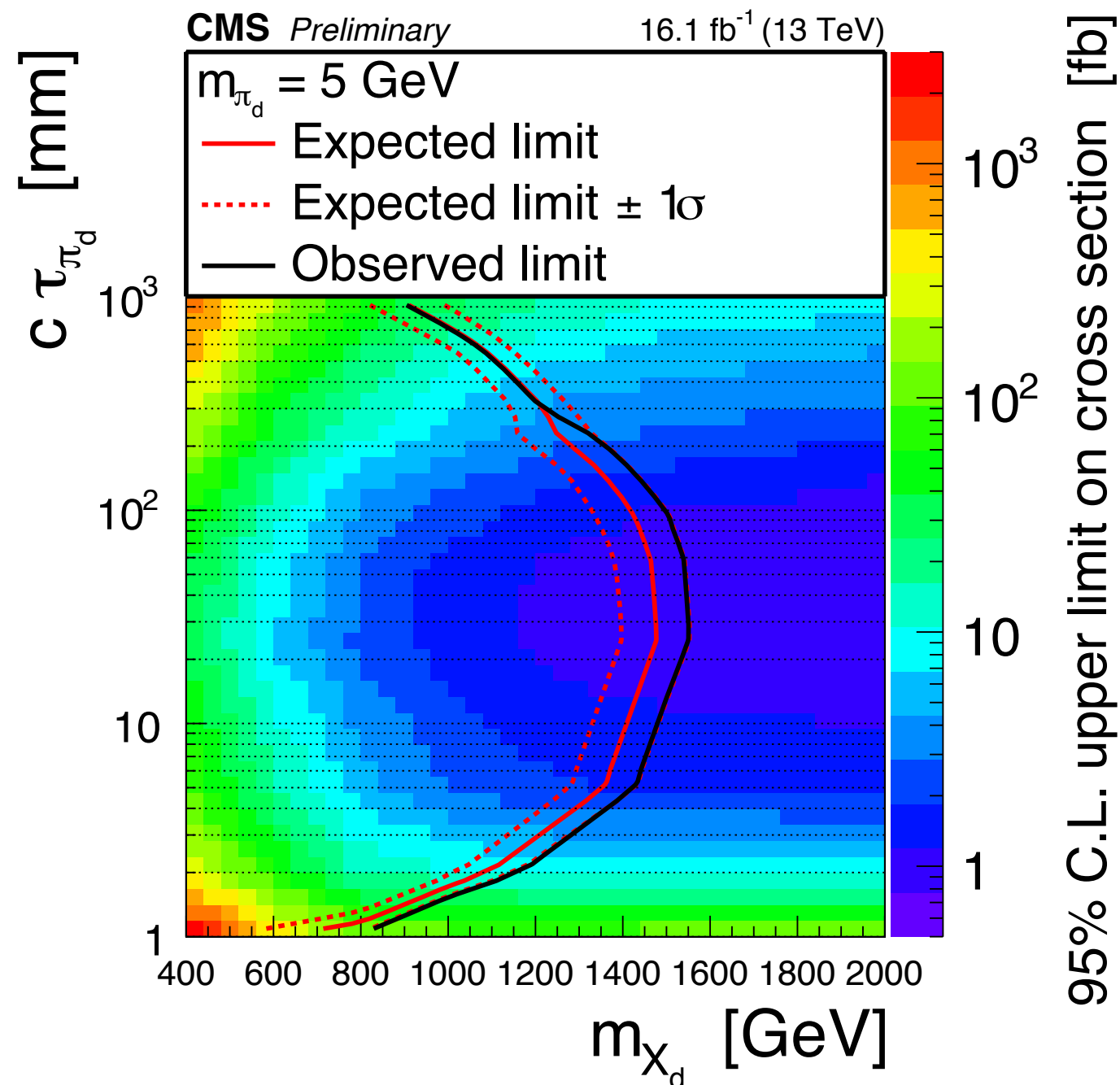
Look for Hcal-jets with no/few tracks below distance to interaction point (inside **circle**)

New '**track-less**' signature

Universal for a large class of displaced physics

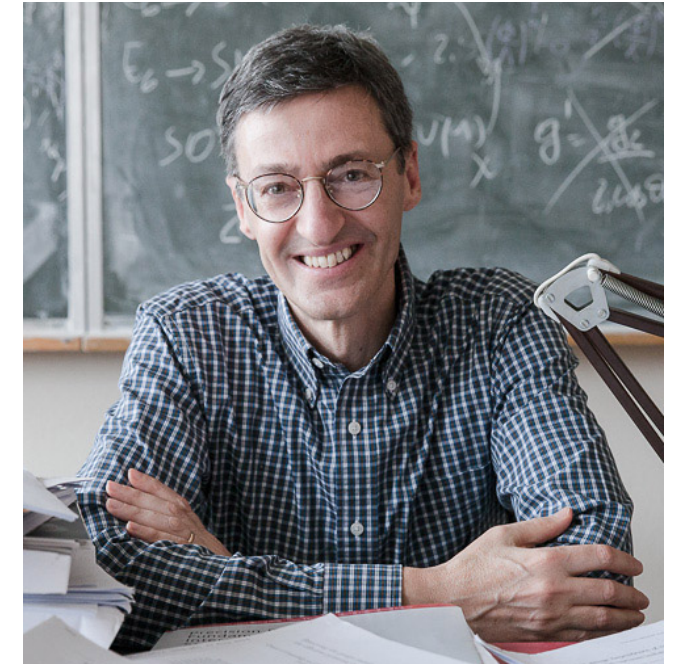
# Emerging jets search

“Mediator particles with masses between 400 and 1250 GeV are excluded for dark hadron decay lengths between 5 and 225 mm.”



[CMS PAS EXO-18-001]

Amazing work by UMD CMS team (Belloni, Eno, Jeng, ...)



G. Giudice

“Is neutral naturalness the beautiful reason we haven’t seen anything, or the last desperate hope of theorists?”

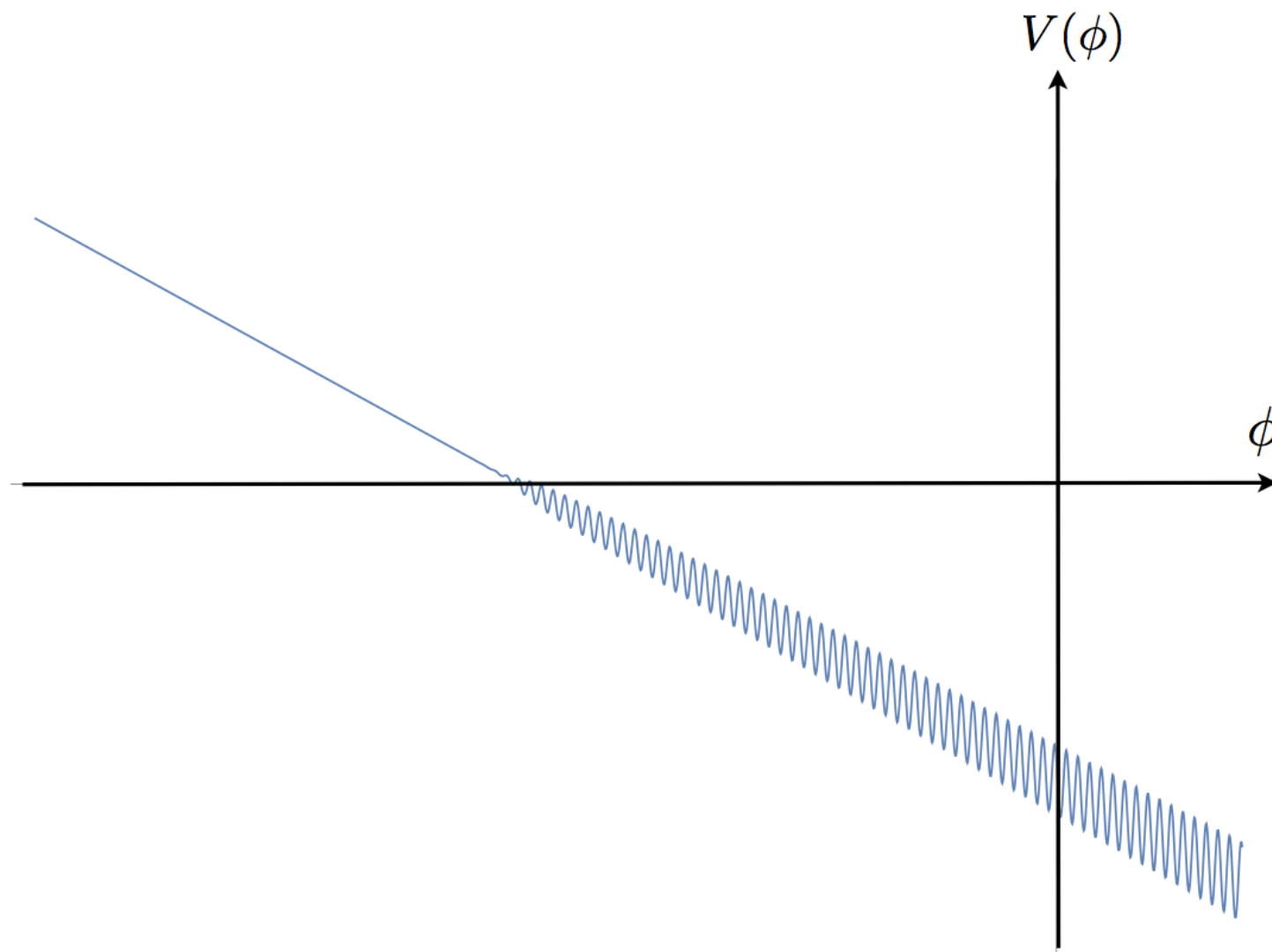


# Relaxion



# Relaxing towards the Fermi scale

SM + axion +  $m_{\text{Higgs}}^2(\text{axion-field}) + \text{driver}$



# Relaxion paradigm

P.W. Graham, D.E. Kaplan, S.Rajendran '15  
(earlier work by Abbott 85, G.Dvali, A.Vilenkin 04, G.Dvali 06)

A **technically natural** solution to the hierarchy problem

Uses dynamics, not symmetries

Still at the drafting stage, but a very interesting framework

# Relaxion paradigm

P.W. Graham, D.E. Kaplan, S.Rajendran '15  
(earlier work by Abbott 85, G.Dvali, A.Vilenkin 04, G.Dvali 06)

A **technically natural** solution to the hierarchy problem

Uses dynamics, not symmetries

Still at the drafting stage, but a very interesting framework

$$m^2 |H|^2$$

Higgs mass



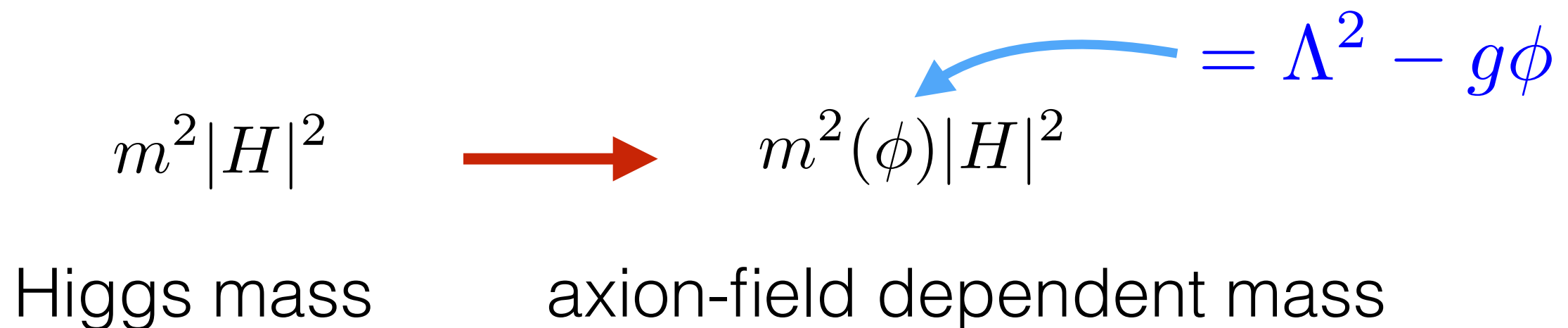
# Relaxion paradigm

P.W. Graham, D.E. Kaplan, S.Rajendran '15  
(earlier work by Abbott 85, G.Dvali, A.Vilenkin 04, G.Dvali 06)

A **technically natural** solution to the hierarchy problem

Uses dynamics, not symmetries

Still at the drafting stage, but a very interesting framework



# Relaxion paradigm

P.W. Graham, D.E. Kaplan, S.Rajendran '15  
(earlier work by Abbott 85, G.Dvali, A.Vilenkin 04, G.Dvali 06)

A **technically natural** solution to the hierarchy problem

Uses dynamics, not symmetries

Still at the drafting stage, but a very interesting framework

$$m^2 |H|^2 \quad \longrightarrow \quad m^2(\phi) |H|^2 \quad \overset{= \Lambda^2 - g\phi}{\curvearrowright}$$

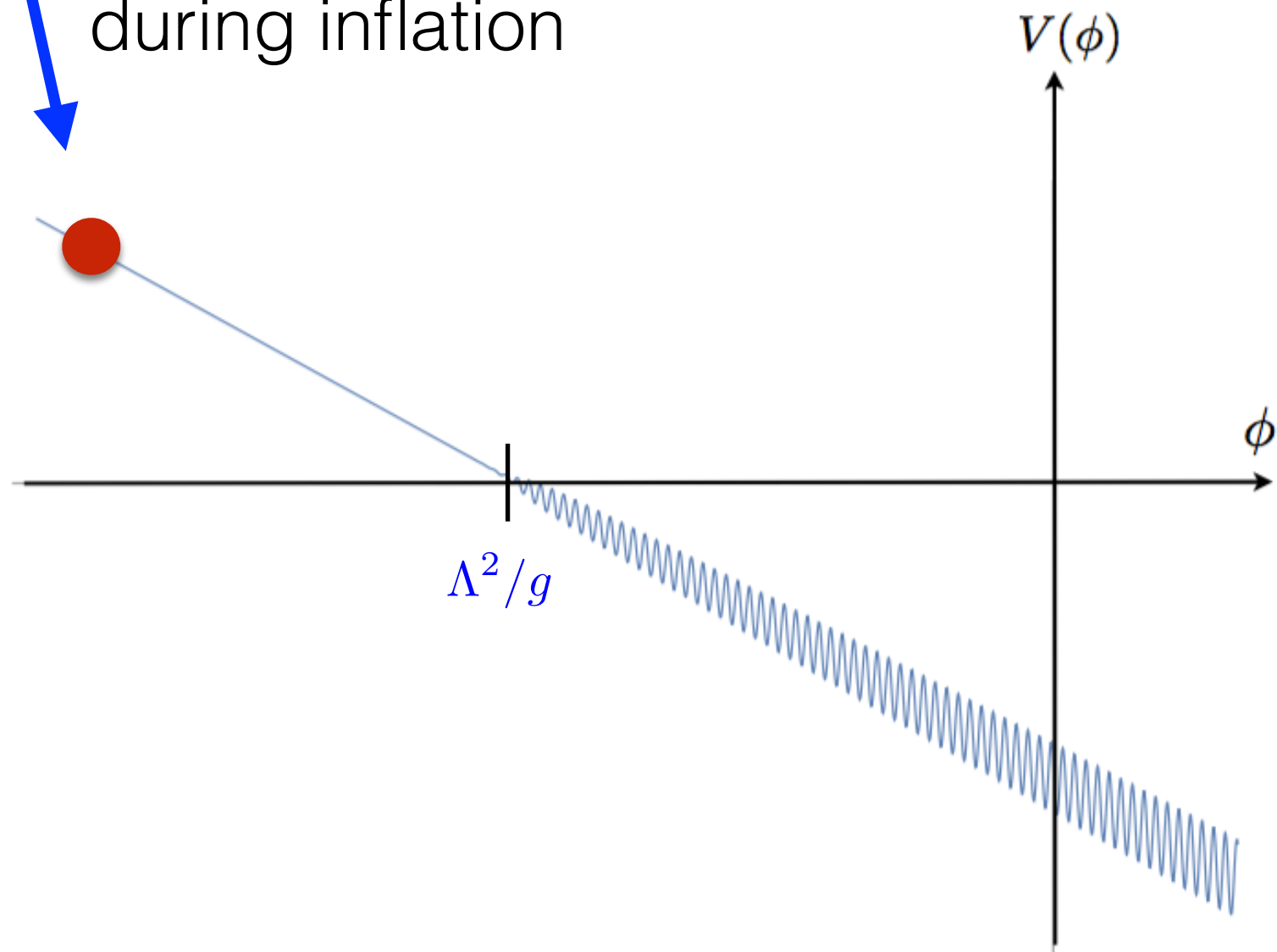
Higgs mass

axion-field dependent mass

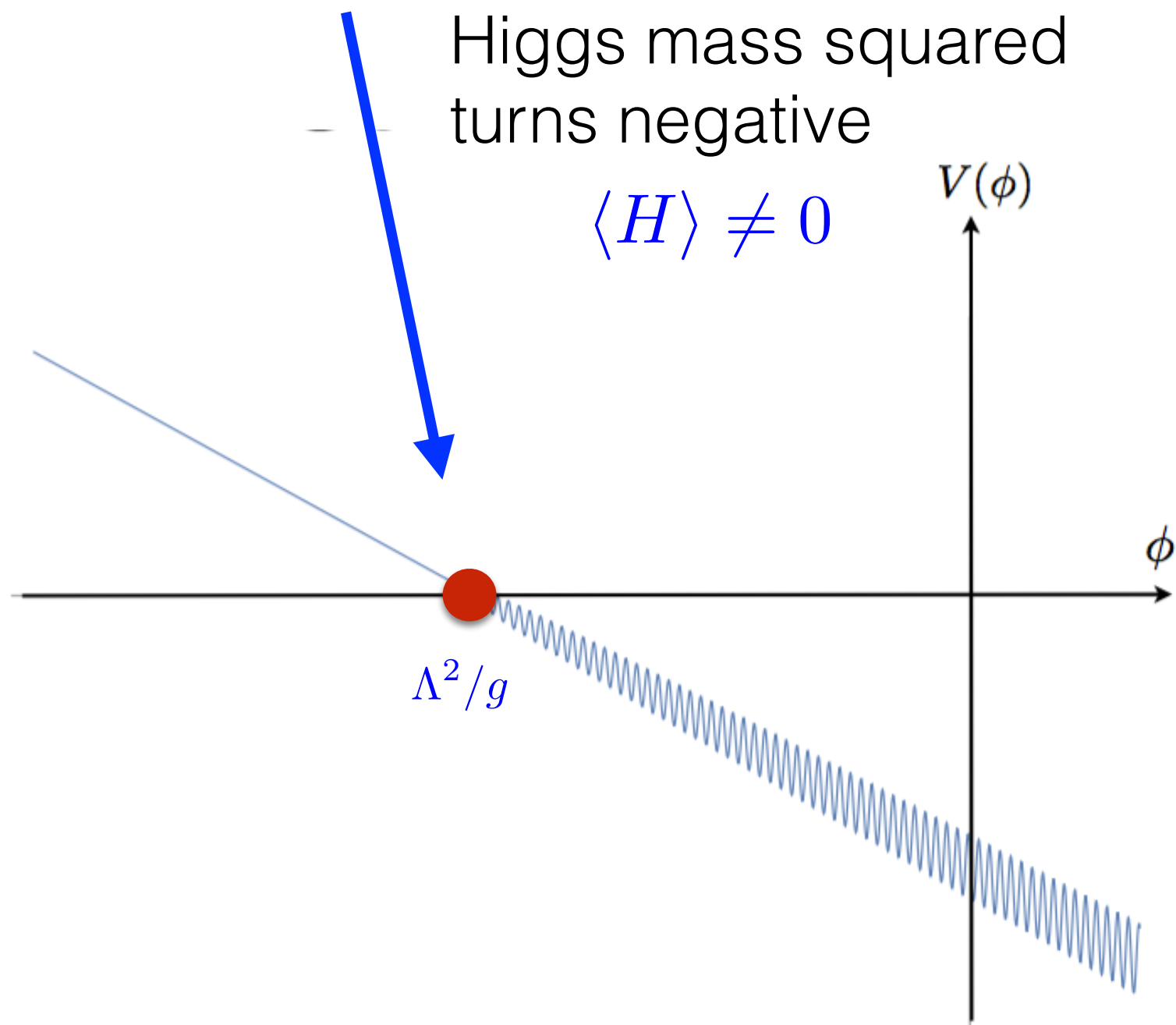
Clever dynamics stabilizes  $\phi$  at values:  $m^2(\phi) \ll \Lambda^2$

$$V(g\phi) + (\Lambda^2 - g\phi)|H|^2 + \epsilon\Lambda_{QCD}^3 h \cos \frac{\phi}{f}$$

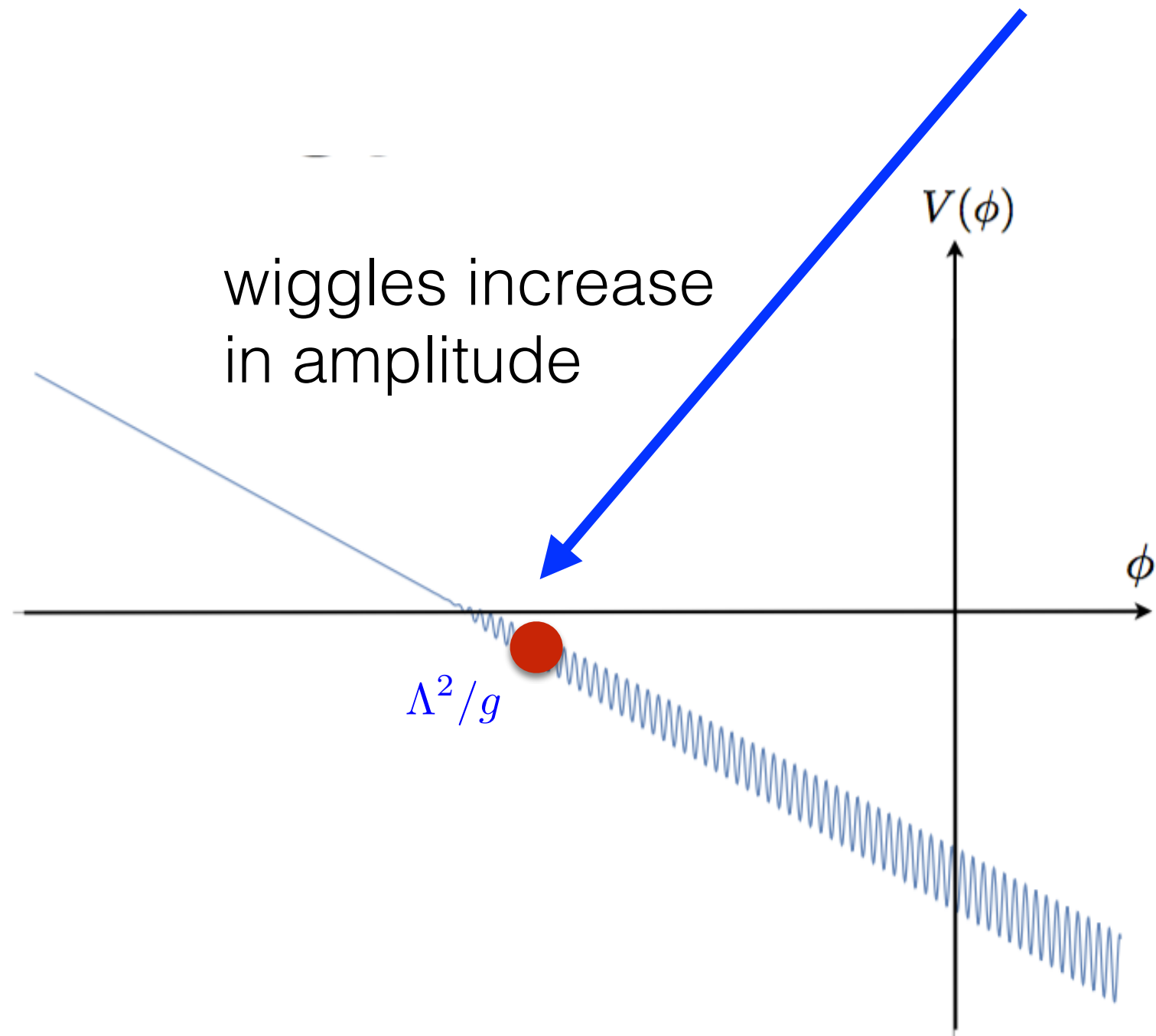
potential to slow-roll  $\phi$   
during inflation



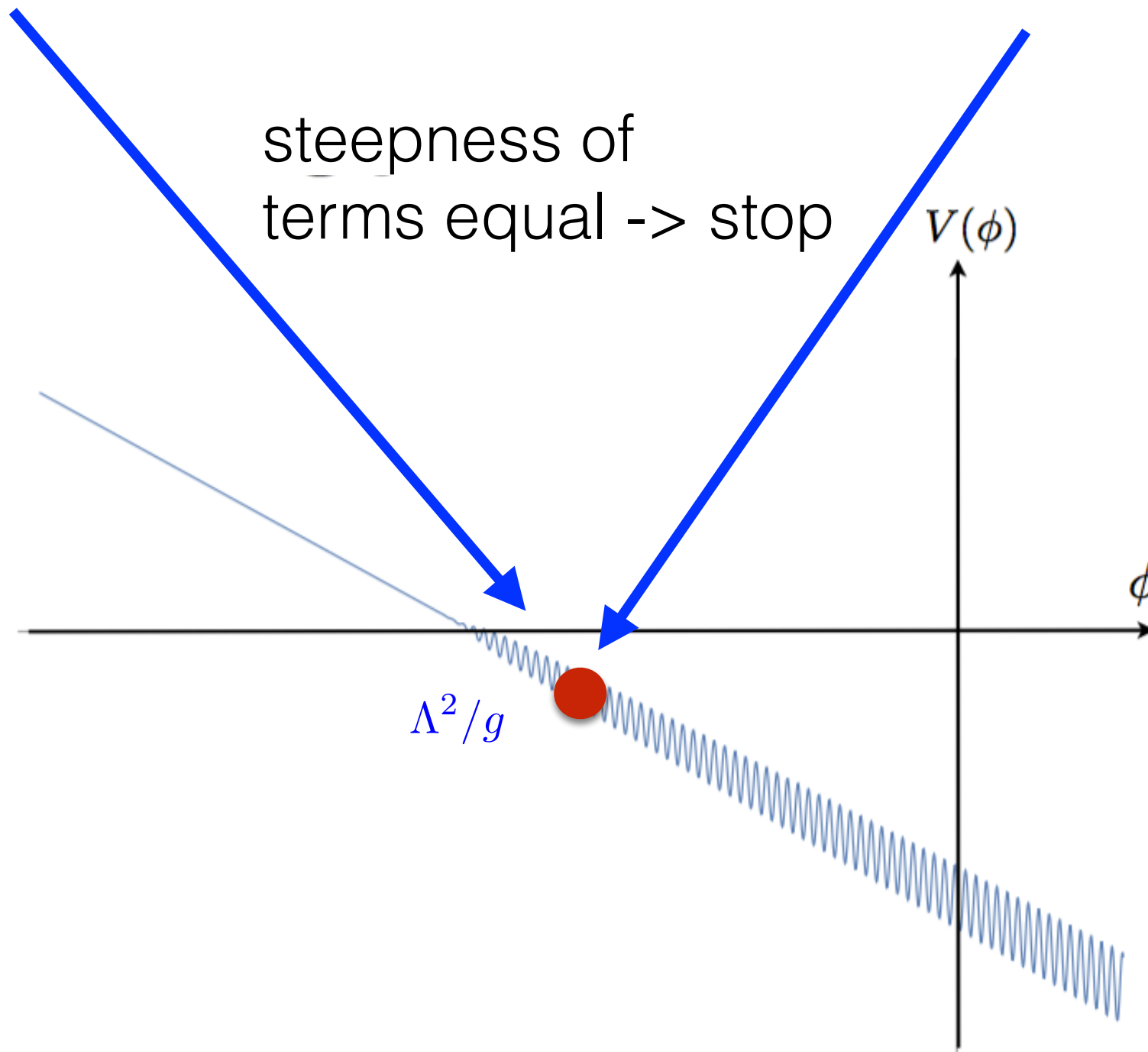
$$V(g\phi) + (\Lambda^2 - g\phi)|H|^2 + \epsilon\Lambda_{QCD}^3 h \cos \frac{\phi}{f}$$



$$V(g\phi) + (\Lambda^2 - g\phi)|H|^2 + \epsilon\Lambda_{QCD}^3 h \cos \frac{\phi}{f}$$



$$V(g\phi) + (\Lambda^2 - g\phi)|H|^2 + \epsilon\Lambda_{QCD}^3 h \cos \frac{\phi}{f}$$



$$V(g\phi) + (\Lambda^2 - g\phi)|H|^2 + \epsilon\Lambda_{QCD}^3 h \cos \frac{\phi}{f}$$

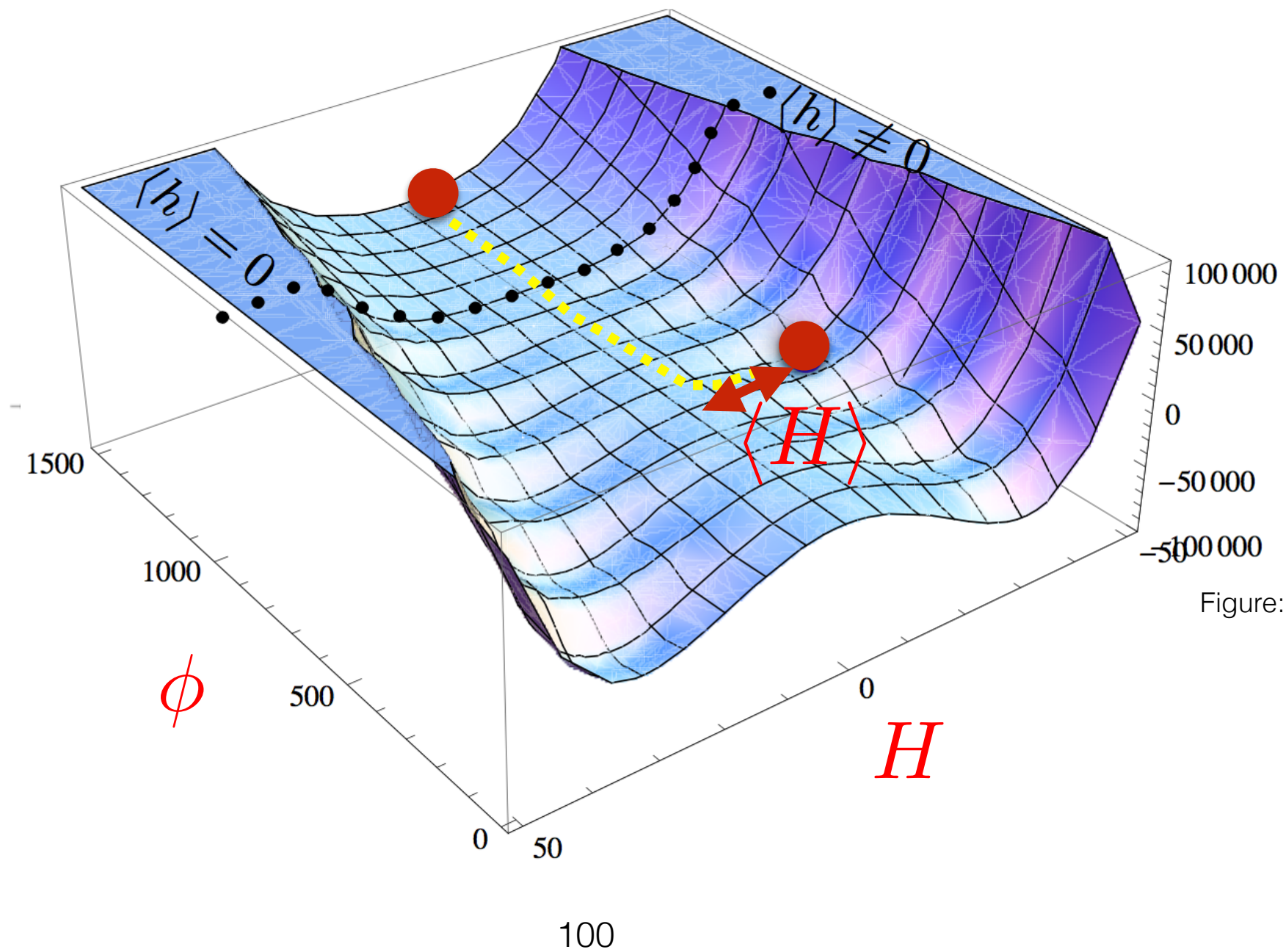


Figure: C. Grojean

- \* QCD axion doesn't work:  $\theta_{QCD} \sim 1$  due to tilt
- \* Add new QCD' group => new weak-scale signals!
- \* Add additional scanning field => **no** collider signals!

Espinosa, Grojean, Panico, Pomarol, Pujolas, Servant '15

## Some points of concern:

$$g \sim 10^{-27} \text{ GeV}$$

UV completion ?

$$N > H^2 / g^2 \sim 10^{45}$$

inflation ?

$$\Delta\Phi \simeq 10^{41} \text{ GeV}$$

large field excursions



# The future



Or ...



# How far can we go?

Can I get an App for that?



# Collider-Reach Projections

$$\frac{N_{\text{signal-events}}(M_{\text{high}}^2, 14 \text{ TeV}, \text{Lumi})}{N_{\text{signal-events}}(M_{\text{low}}^2, 8 \text{ TeV}, 19\text{fb}^{-1})} = 1$$

Coupling constants & other prefactors mostly cancel in the ratio.

Dependence on  $M$  and on  $\sqrt{s}$  mostly comes about through parton distribution functions (PDFs) & simple dimensions.

G. Salam, AW [cern.ch/collider-reach](http://cern.ch/collider-reach)

# Z' example

$$\hat{\sigma}_0(\hat{s}) = C \frac{\hat{s}}{(\hat{s} - M_{Z'}^2)^2 + \Gamma_{Z'}^2 M_{Z'}^2}$$

---

$\mathcal{L}_{ij}$

narrow width approx.

---

$$\rightsquigarrow \frac{1}{M^2} \times \text{parton-luminosity}$$

# Z' example

$$\frac{d\sigma}{dm^2} = \int dx_1 dx_2 [f_1(x_1) f_2(x_2)] \hat{\sigma}_0(\hat{s}) \delta(m^2 - \hat{s}^2), \quad \hat{\sigma}_0(\hat{s}) = C \frac{\hat{s}}{(\hat{s} - M_{Z'}^2)^2 + \Gamma_{Z'}^2 M_{Z'}^2},$$

$$= \sum_{ij} \underbrace{\left[ \tau \int \frac{dx}{x} f_i(x) f_j(\tau/x) \right]}_{\mathcal{L}_{ij}} \underbrace{\frac{C}{(m^2 - M_{Z'}^2)^2 + \Gamma_{Z'}^2 M_{Z'}^2}}_{\text{narrow width approx.}}$$

$\mathcal{L}_{ij}$

narrow width approx.

$$\rightsquigarrow \frac{1}{M^2} \times \text{parton-luminosity}$$

# Z' example

$$\frac{d\sigma}{dm^2} = \int dx_1 dx_2 [f_1(x_1) f_2(x_2)] \hat{\sigma}_0(\hat{s}) \delta(m^2 - \hat{s}^2), \quad \hat{\sigma}_0(\hat{s}) = C \frac{\hat{s}}{(\hat{s} - M_{Z'}^2)^2 + \Gamma_{Z'}^2 M_{Z'}^2},$$

$$= \sum_{ij} \left[ \tau \int \frac{dx}{x} f_i(x) f_j(\tau/x) \right] \frac{C}{(m^2 - M_{Z'}^2)^2 + \Gamma_{Z'}^2 M_{Z'}^2}$$

$\mathcal{L}_{ij}$

narrow width approx.

$$\sigma \approx \int dm^2 \sum_{ij} \mathcal{L}_{ij}(m^2, s) C \frac{\pi}{\Gamma_{Z'} M_{Z'}} \delta(m^2 - M_{Z'}^2) \quad \Gamma_{Z'} \propto M_{Z'}$$

$$= \frac{1}{M_{Z'}^2} \sum_{ij} C' \mathcal{L}_{ij}(M_{Z'}^2, s)$$

$$= N(M_{Z'}, s)$$

$$\rightsquigarrow \frac{1}{M^2} \times \text{parton-luminosity}$$



Instead of cross section ratio, use **parton luminosity ratio**

Equation we solve to find  $M_{\text{high}}$  is then

$$\frac{\mathcal{L}_{ij}(M_{\text{high}}^2, s_{\text{high}})}{\mathcal{L}_{ij}(M_{\text{low}}^2, s_{\text{low}})} \times \frac{\text{lumi}_{\text{high}}}{\text{lumi}_{\text{low}}} = \frac{M_{\text{high}}^2}{M_{\text{low}}^2}$$

The tools we use for this are  
LHAPDF and HOPPET  
most plots with MSTW2008 NNLO PDFs

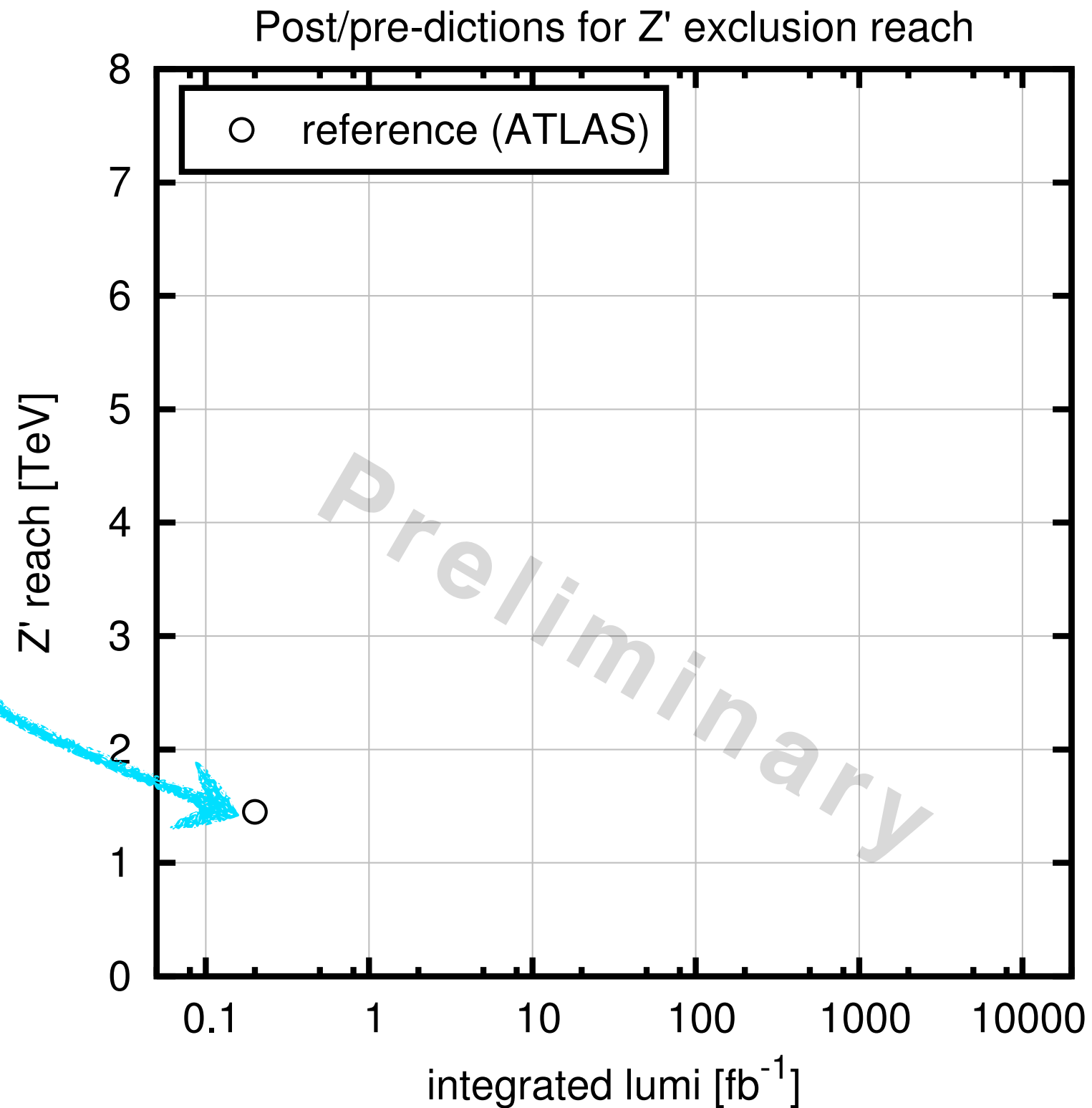
$$\mathcal{L}_{ij}(M^2, s) = \int_{\tau}^1 \frac{dx}{x} x f_i(x, M^2) \frac{\tau}{x} f_j\left(\frac{\tau}{x}, M^2\right) \quad \tau \equiv \frac{M^2}{s}$$

i & j parton

Does it work?

Try a  $Z'$  search. Take a baseline analysis:

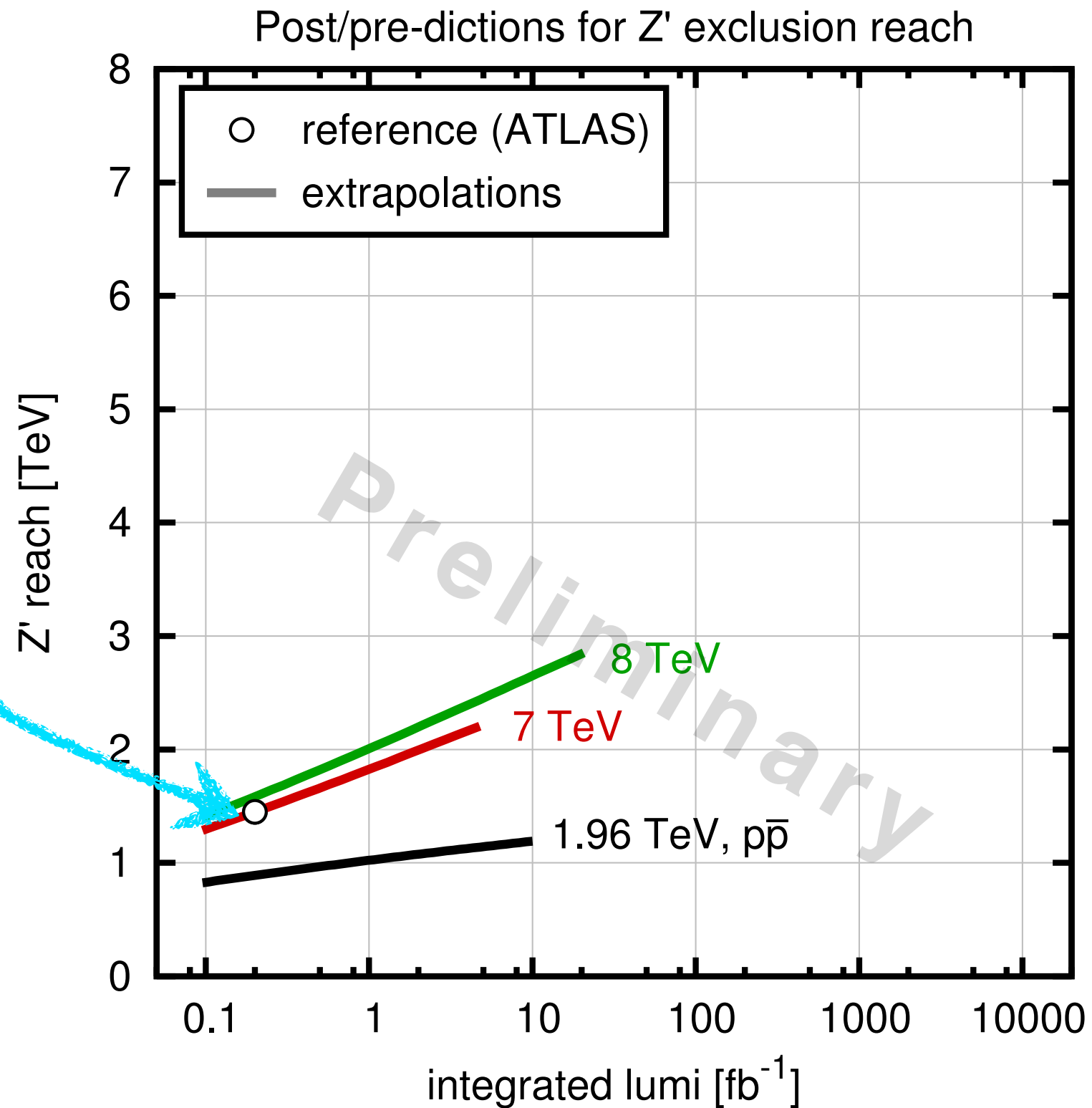
ATLAS,  
 $0.2 \text{ fb}^{-1}$  @ 7 TeV  
excludes  $M < 1450 \text{ GeV}$



Try a  $Z'$  search. Take a baseline analysis:

ATLAS,  
 $0.2 \text{ fb}^{-1}$  @ 7 TeV  
excludes  $M < 1450 \text{ GeV}$

“Predict” exclusions  
at other lumis &  
energies (assume  $q\bar{q}$ )

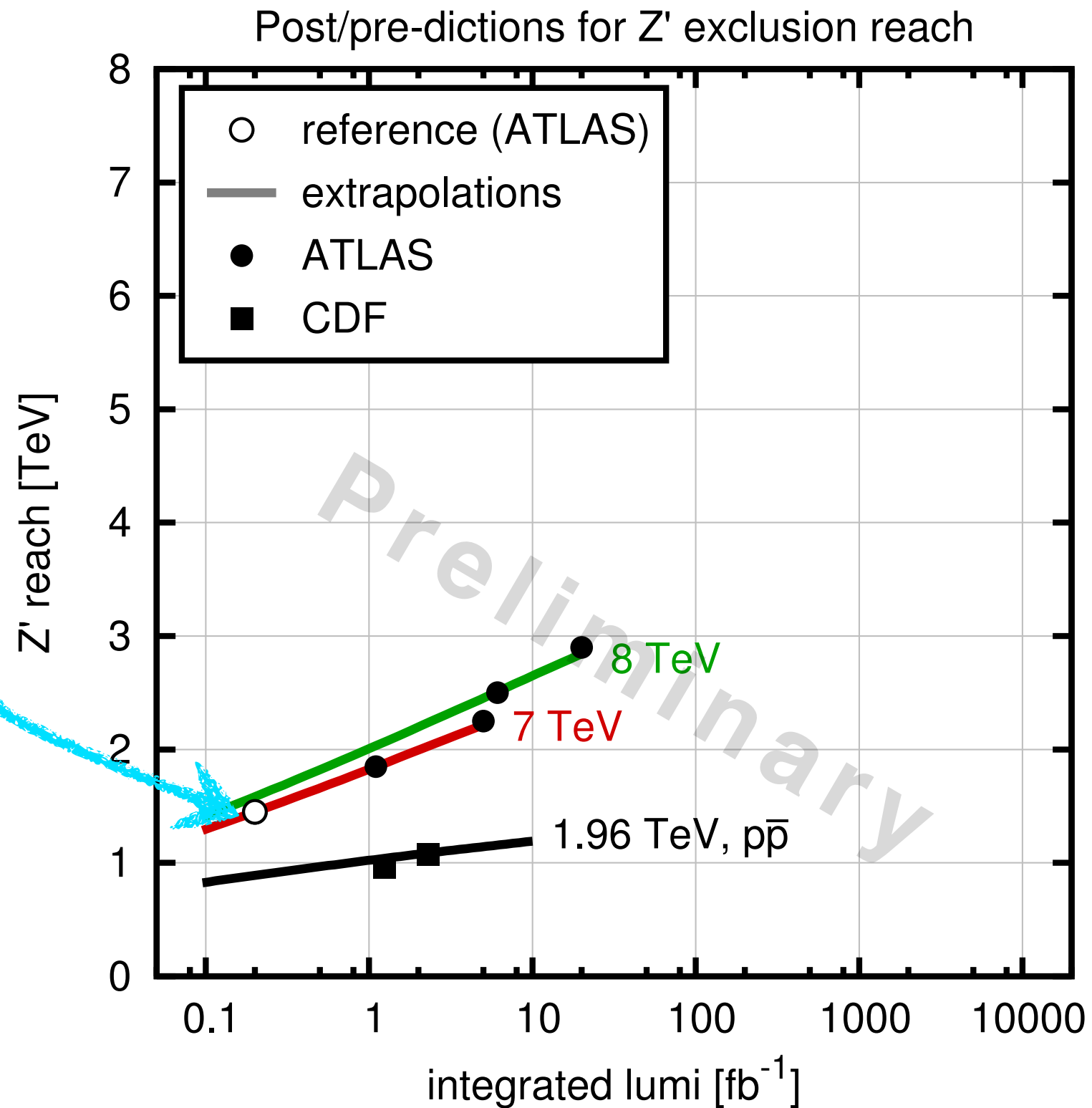


Try a  $Z'$  search. Take a baseline analysis:

ATLAS,  
 $0.2 \text{ fb}^{-1}$  @ 7 TeV  
excludes  $M < 1450 \text{ GeV}$

“Predict” exclusions  
at other lumis &  
energies (assume  $q\bar{q}$ )

Compare to actual  
exclusions

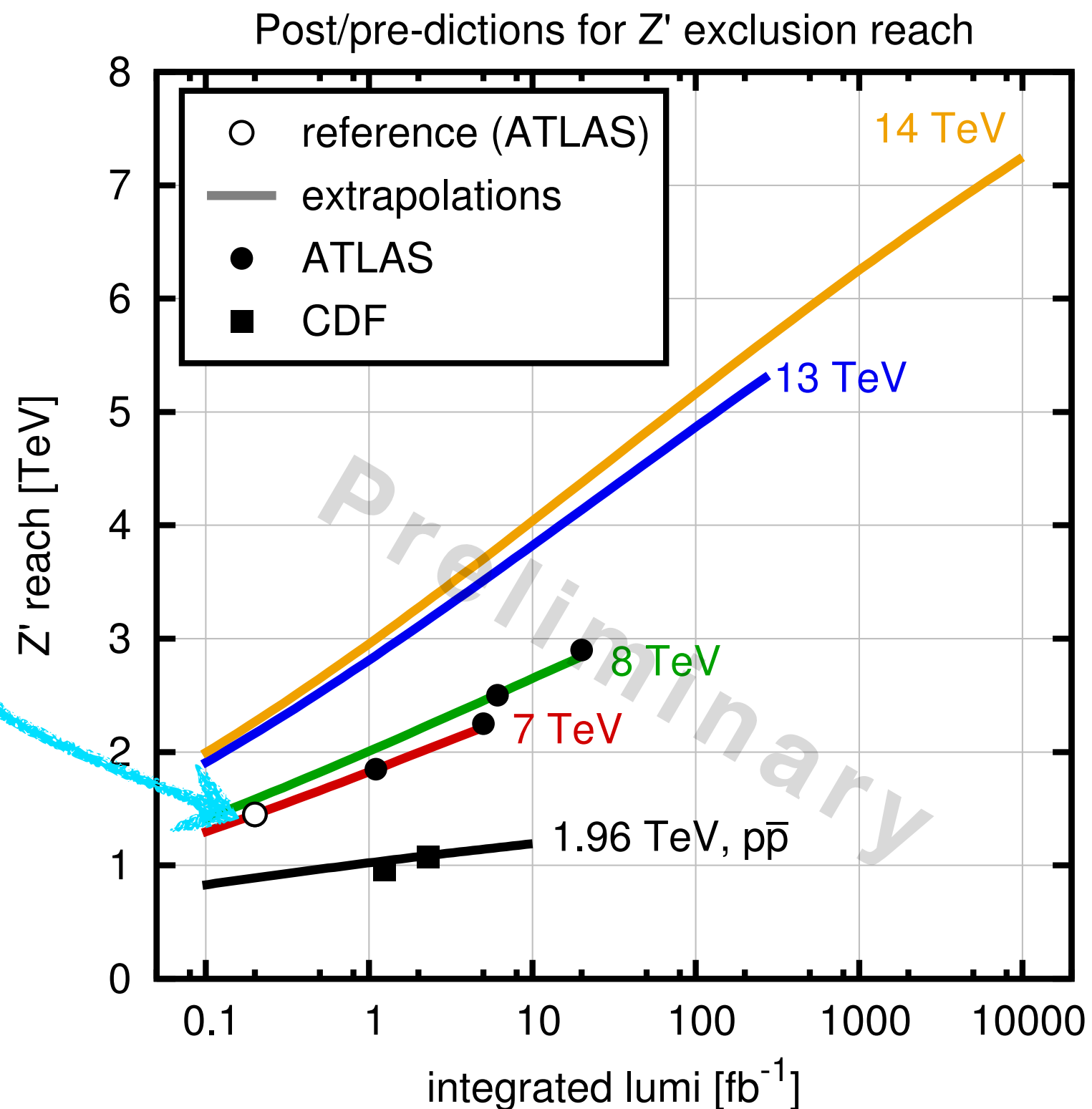


Try a  $Z'$  search. Take a baseline analysis:

ATLAS,  
 $0.2 \text{ fb}^{-1}$  @ 7 TeV  
excludes  $M < 1450 \text{ GeV}$

“Predict” exclusions  
at other lumis &  
energies (assume  $q\bar{q}$ )

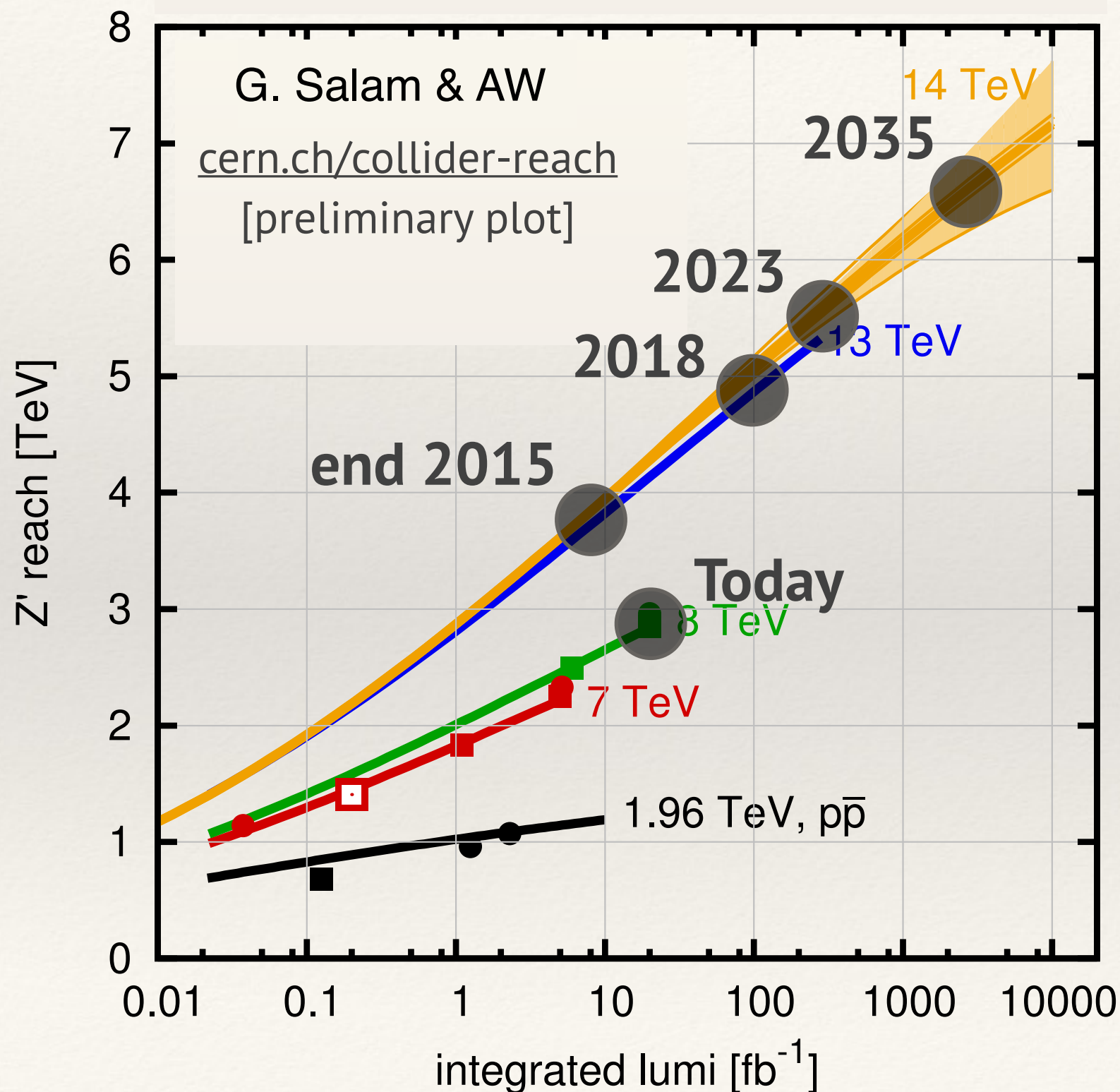
Compare to actual  
exclusions



Maybe it only works so well because it's a simple search?  
(Signal & Bkgd are both  $q\bar{q}$  driven)

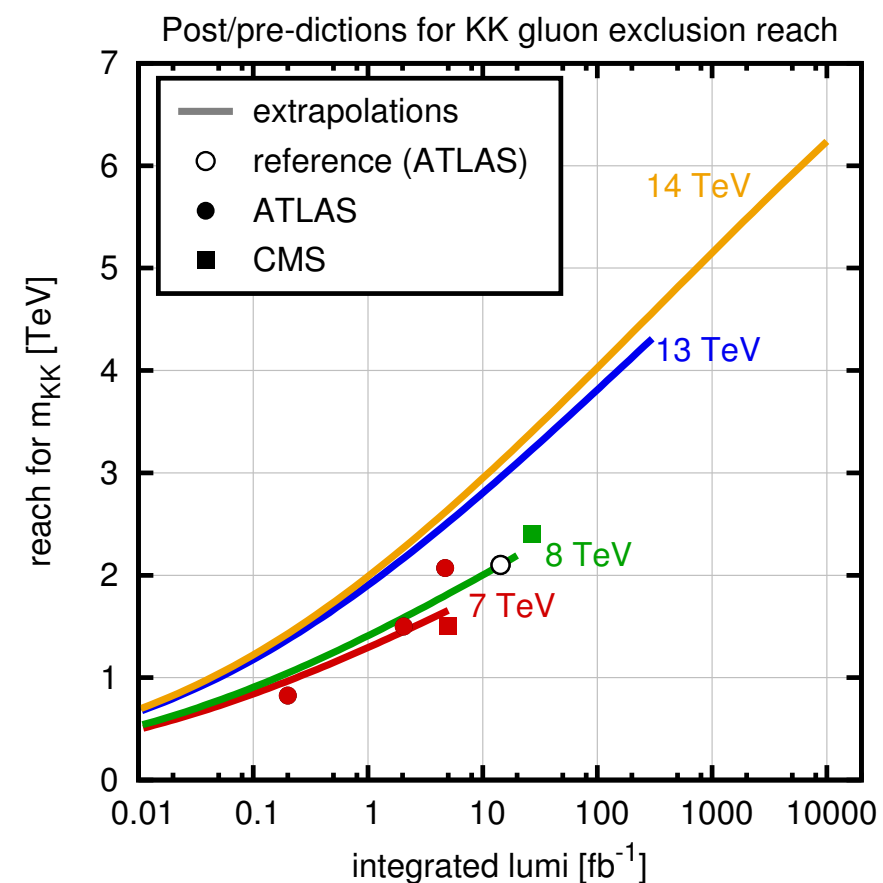
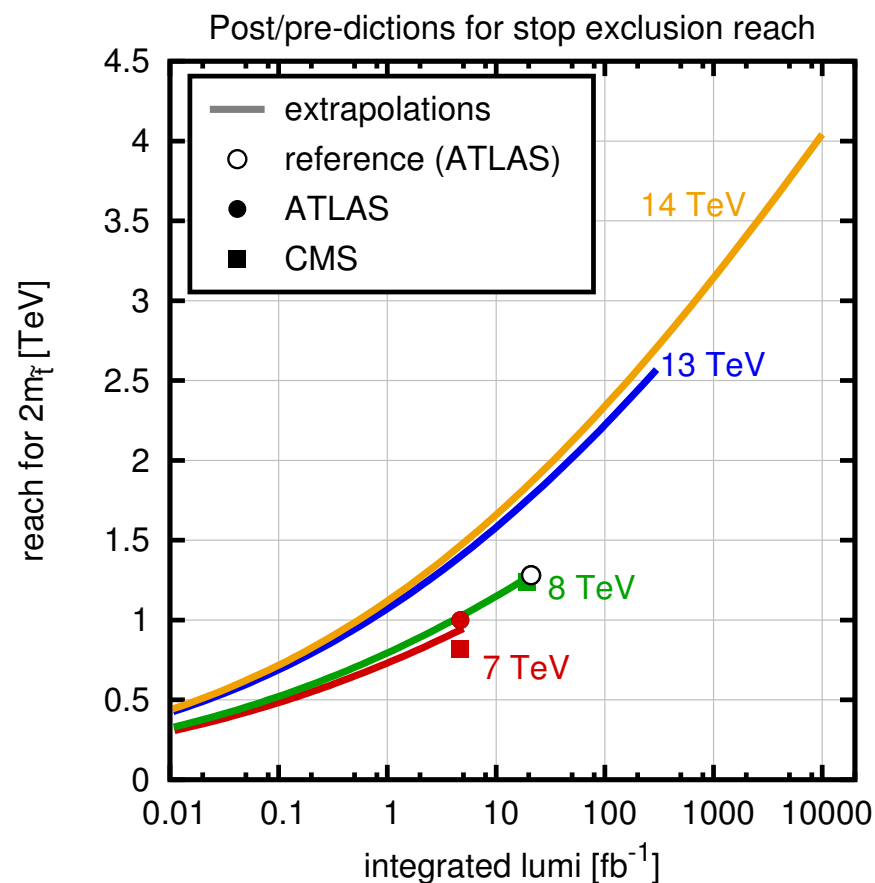
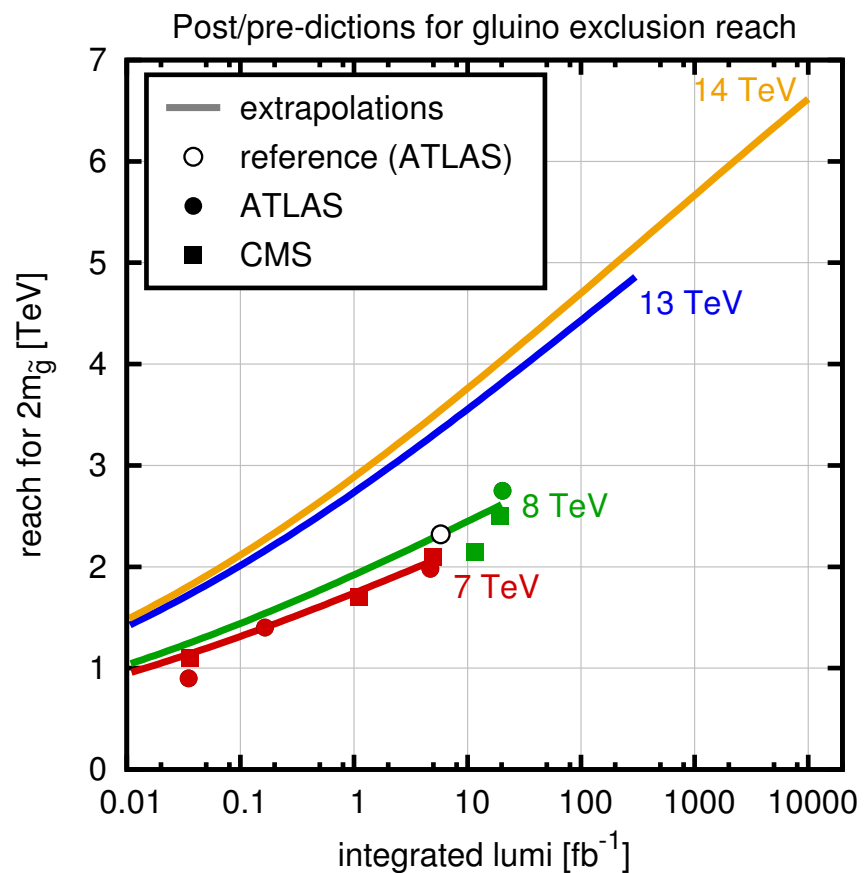
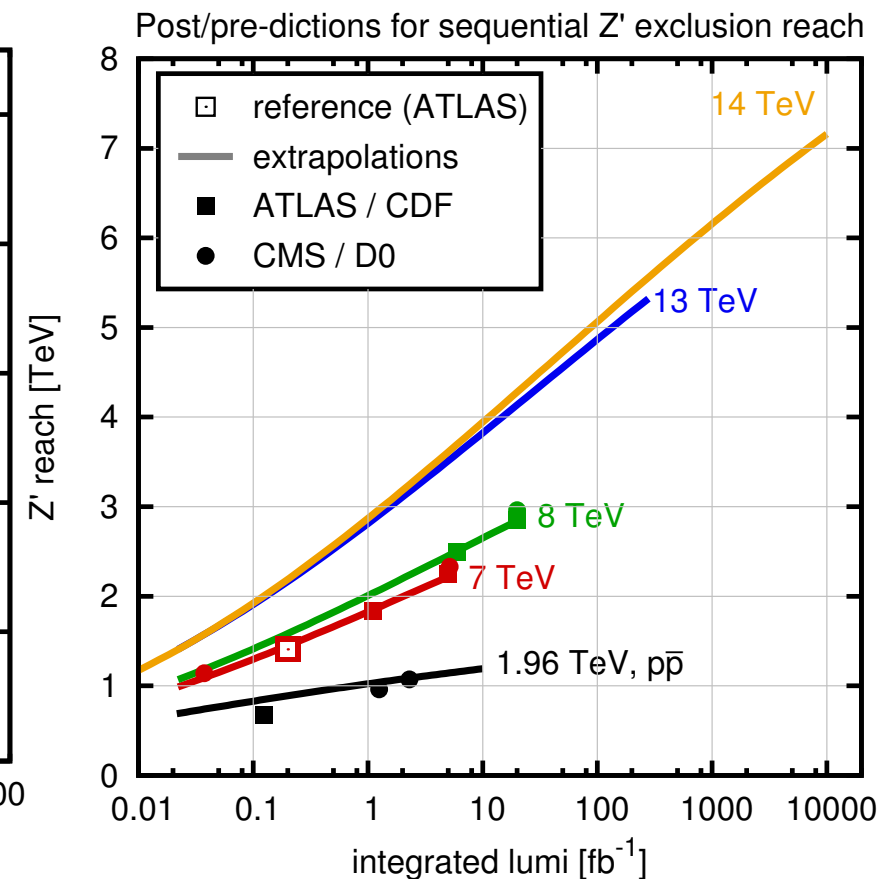
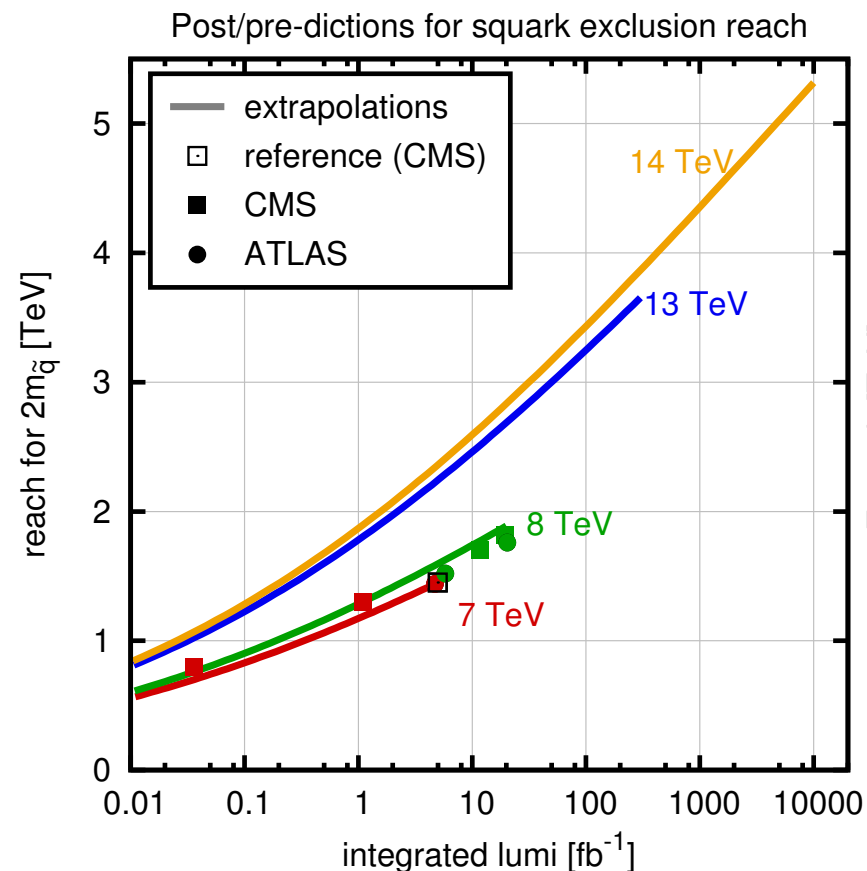
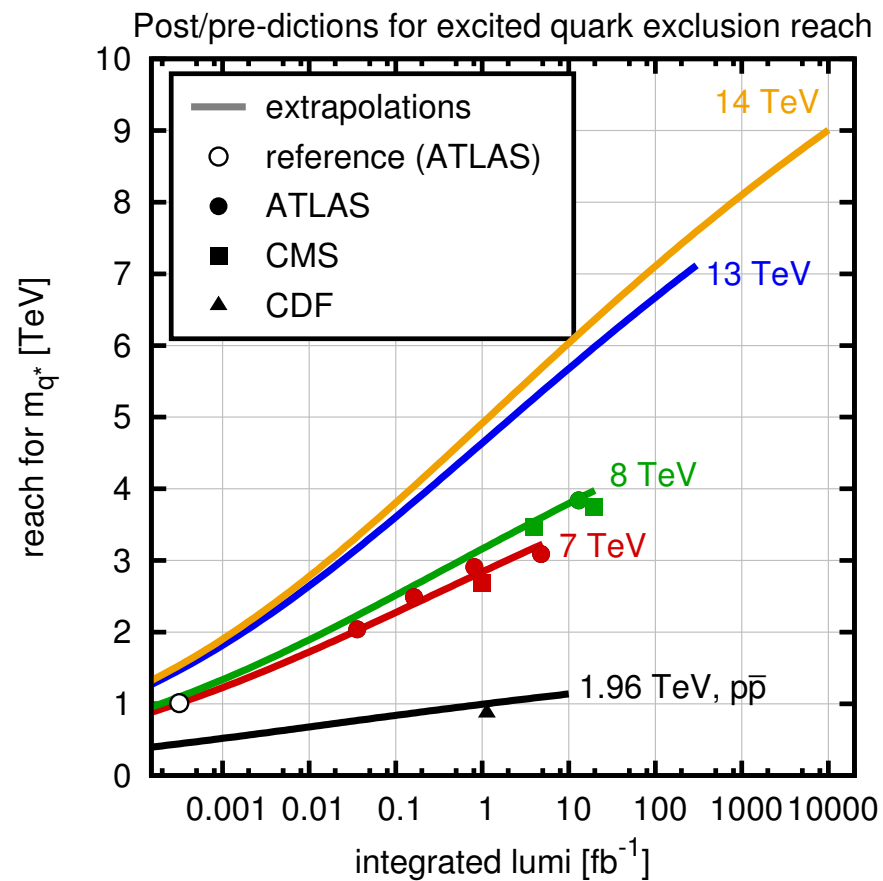


# Z' exclusion reach v. lumi



By the end of the year, most searches will beat 8 TeV results

[Some, e.g. excited quarks, will surpass 8 TeV with just  $0.2 \text{ fb}^{-1}$ ]





From your iPhone/Android  
(or a generic browser)  
[cern.ch/collider-reach](http://cern.ch/collider-reach)

Collider 1: CoM energy

8

TeV, integrated luminosity

20

$\text{fb}^{-1}$

Collider 2: CoM energy

14

TeV, integrated luminosity

300

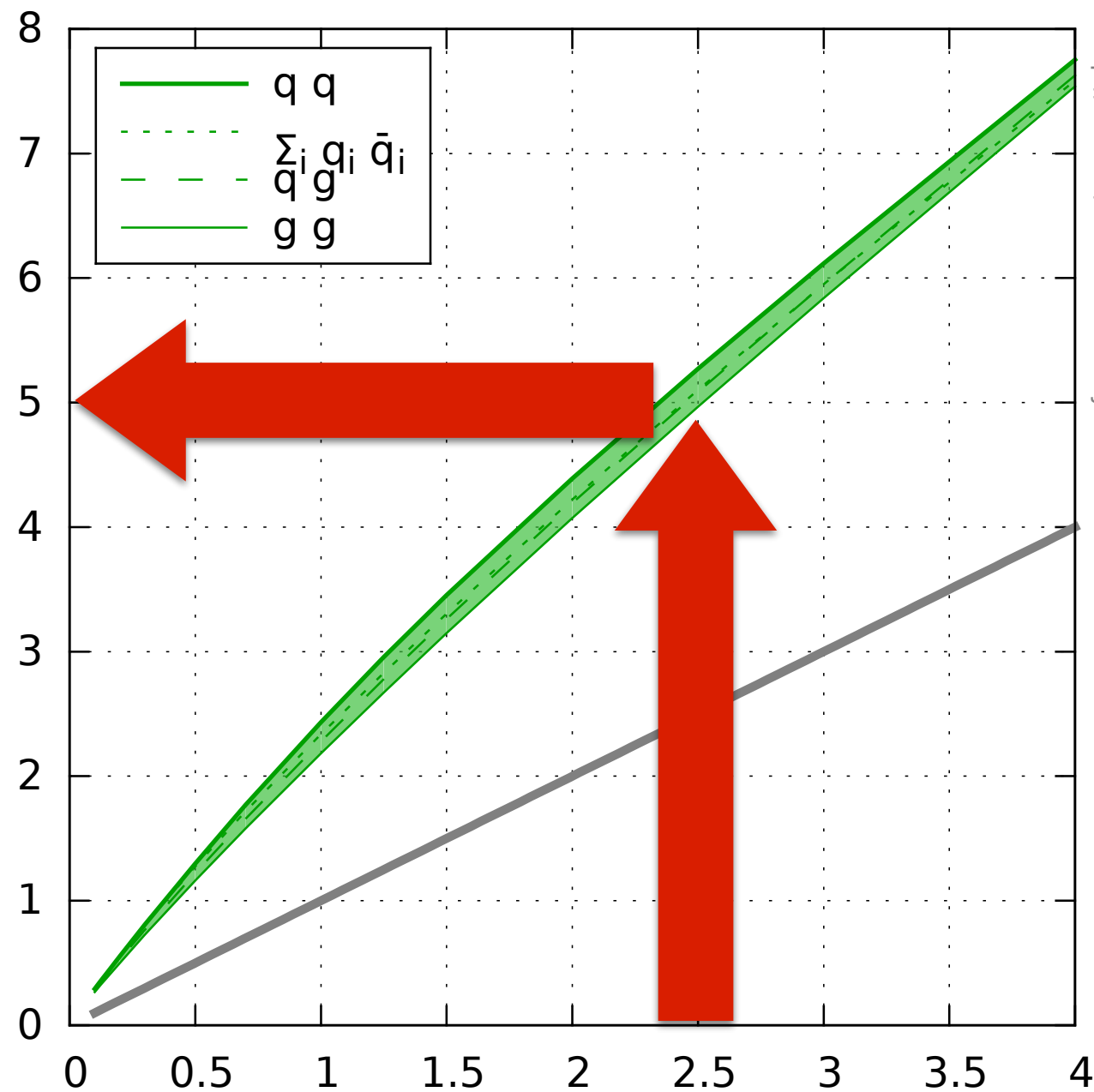
$\text{fb}^{-1}$

PDF:

MSTW2008nnlo68cl



Mass [TeV] at  
collider #2



Mass [TeV] at collider #1

8

TeV, integrated luminosity

20

 $fb^{-1}$ 

## Collider 2: CoM energy

14

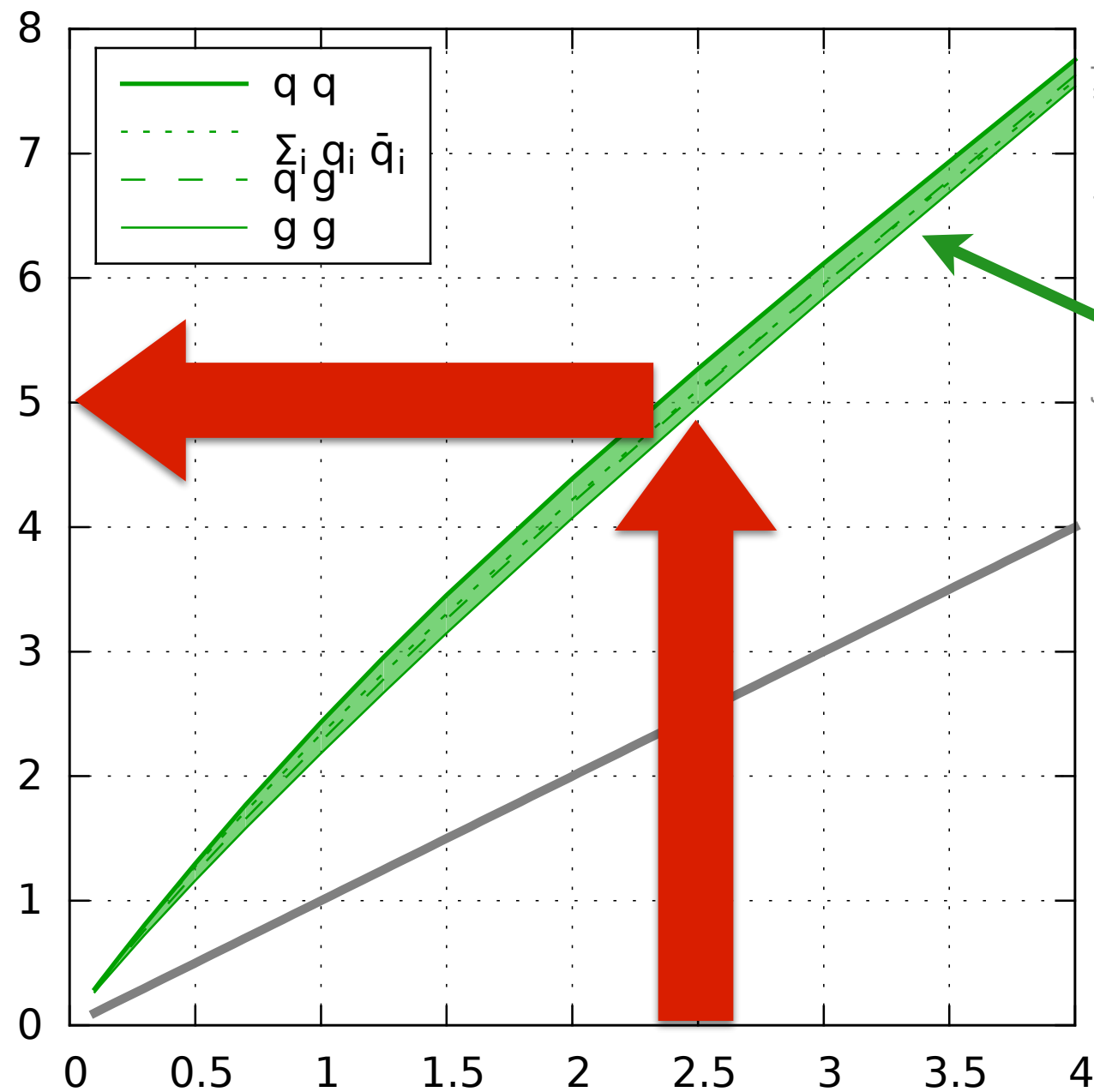
TeV, integrated luminosity

300

 $fb^{-1}$ 

PDF:

MSTW2008nnlo68cl



**Mass [TeV] at  
collider #2**

**Spread of  
partonic  
channels  
(assume same  
channel for  
S & B)**

## Mass [TeV] at collider #1

The Collider Reach tool gives you a quick (and dirty) estimate of the relation between the mass reaches of different proton-proton collider setups.

Collider 1: CoM energy  TeV, integrated luminosity  fb<sup>-1</sup>

Collider 2: CoM energy  TeV, integrated luminosity  fb<sup>-1</sup>

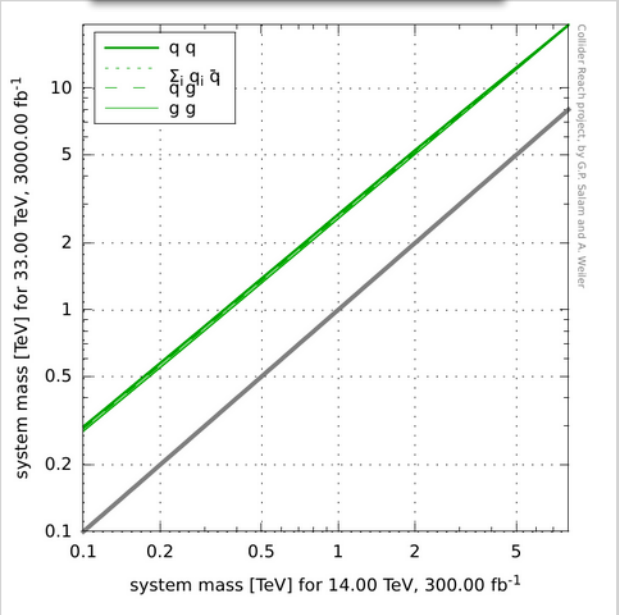
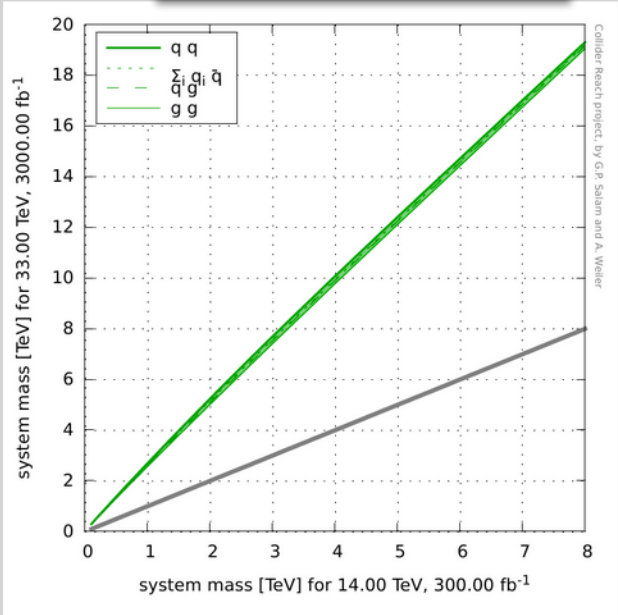
PDF:

Submit

Plots

linear plot

log-log plot

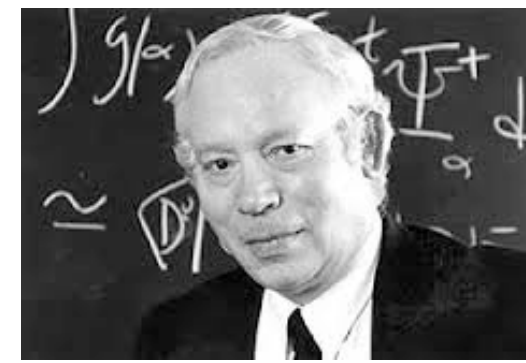


Download: [collider.pdf](#), [colliderloglog.pdf](#), plot generation [log file](#)  
The PDF choice was CT10nlo.LHgrid

Original mass	gg	qg	allqq	qqbar
100.	283.	291.	298.	297.
125.	350.	359.	368.	367.
150.	416.	427.	438.	437.
200.	547.	562.	576.	575.
300.	806.	827.	848.	847.
500.	1317.	1350.	1386.	1382.
700.	1822.	1866.	1916.	1907.
1000.	2570.	2628.	2702.	2680.
1250.	3188.	3256.	3349.	3314.
1500.	3802.	3879.	3990.	3939.
2000.	5018.	5110.	5251.	5169.
2500.	6223.	6327.	6488.	6380.
3000.	7417.	7530.	7703.	7578.
4000.	9782.	9904.	10082.	9945.
5000.	12120.	12246.	12417.	12284.
6000.	14439.	14565.	14726.	14601.
7000.	16748.	16871.	17021.	16905.
8000.	19053.	19169.	19310.	19206.

the last word...

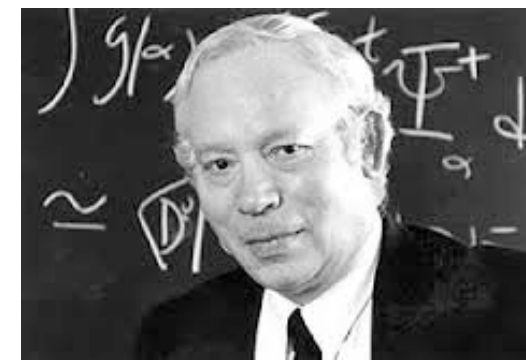
# Four Lessons



1) How could I do anything without knowing everything that had already been done? [...] **pick up what I needed to know as I went along.** It was sink or swim. [...] But I did learn one big thing: **that no one knows everything, and you don't have to.**

2) While you are swimming and not sinking you should aim for rough water. [...] **My advice is to go for the messes — that's where the action is.**

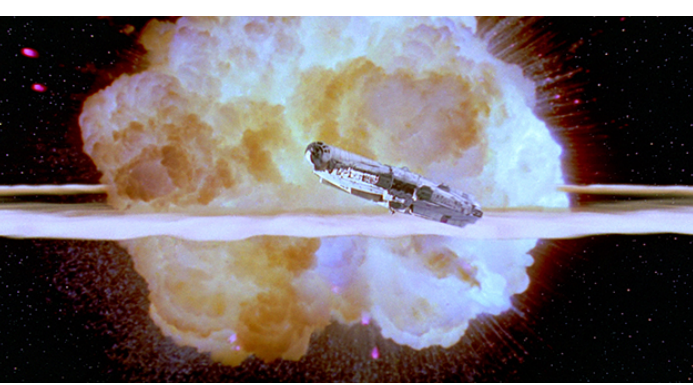
# Four Lessons



3) Forgive yourself for wasting time. [...] in the real world, it's **very hard to know which problems are important, and you never know whether at a given moment in history a problem is solvable** [...] get used [...] to being becalmed on the ocean of scientific knowledge.



4) **Learn something about the history of science** [...] As a scientist, you're probably not going to get rich. [...] But you can get great satisfaction by recognizing that your work in science is a part of history.



- No signs of new physics have appeared so far.
- The Higgs fine-tuning puzzle is as puzzling as ever. Do we simply live in a (mildly?) fine-tuned universe? Or is there a subtle solution?
- Themes of recent years: search for electroweak or neutral new particles at colliders to exhaust possibilities; intriguing possibilities for connections of the weak scale with cosmology.
- Amazing landscape of experiments: LHC, dark matter, EDMs, flavor physics. New physics discovery could come at any time!