

Beauty at High { Precision Sensitivity

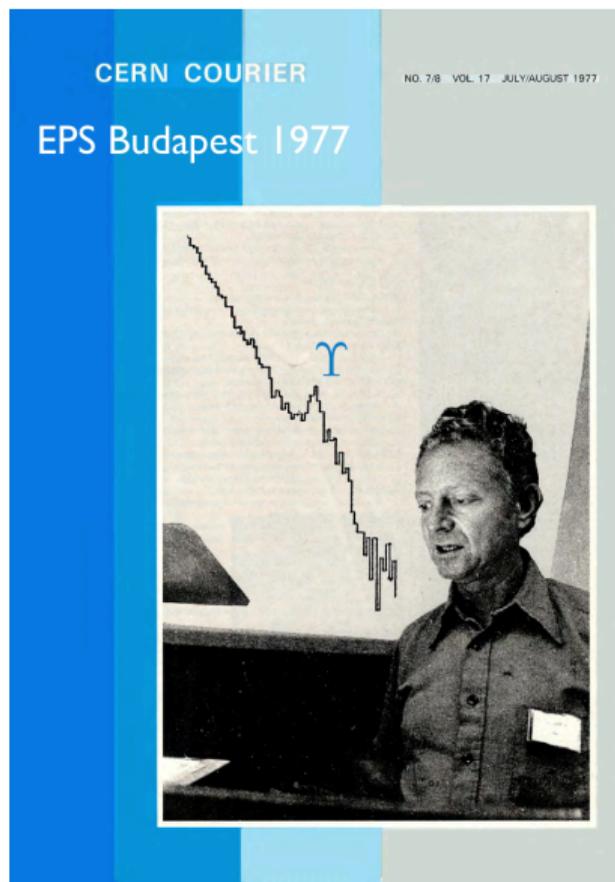
Chris Quigg
Fermilab

Beauty 2019 · Ljubljana · September 30, 2019

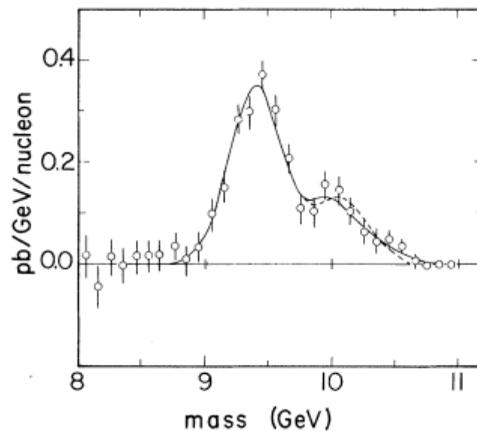
See also “Dream Machines” [1808.06036](#)

“Perspectives and Questions” [zenodo.3376597](#)

Origin Story ...



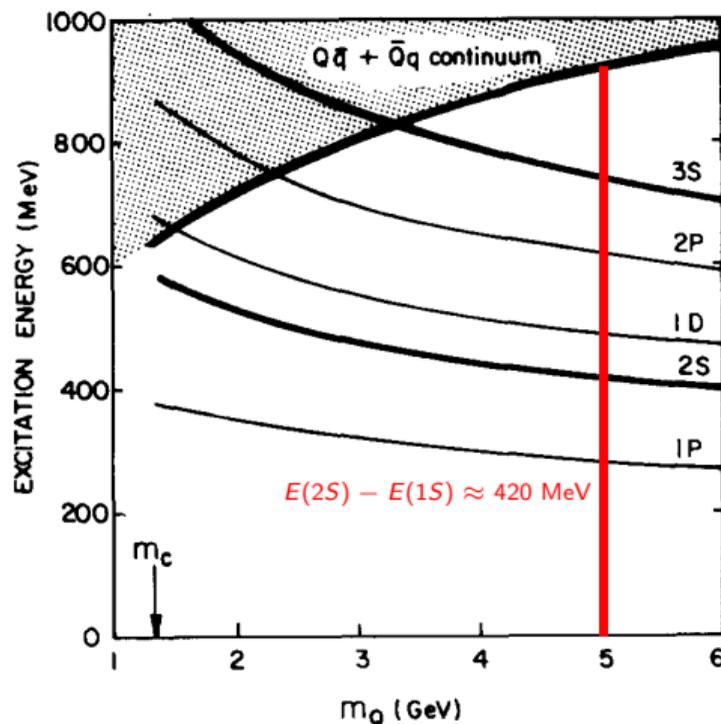
400-GeV $pN \rightarrow \mu^+ \mu^- + X$



E288	$M(\Upsilon') - M(\Upsilon)$	$M(\psi'') - M(\Upsilon')$
Two-level fit	650 ± 30 MeV	
Three-level fit	610 ± 40 MeV	1000 ± 120 MeV
$M(\psi') - M(J/\psi)$	≈ 590 MeV	

General motivation: J/ψ , τ discoveries
Kobayashi–Maskawa CPV insight

Eichten & Gottfried: CESR Proposal (November 1976)



General: # of narrow 3S_1 levels $\propto \sqrt{M_Q}$

Why choose $M_Q = 5 \text{ GeV}$?

Excess events at high inelasticity observed in $\bar{\nu}_\mu N \rightarrow \mu^+ + \text{anything}$

$$V - A: d\sigma(\nu q)/dy \propto 1 \quad d\sigma(\bar{\nu} q)/dy \propto (1 - y)^2$$

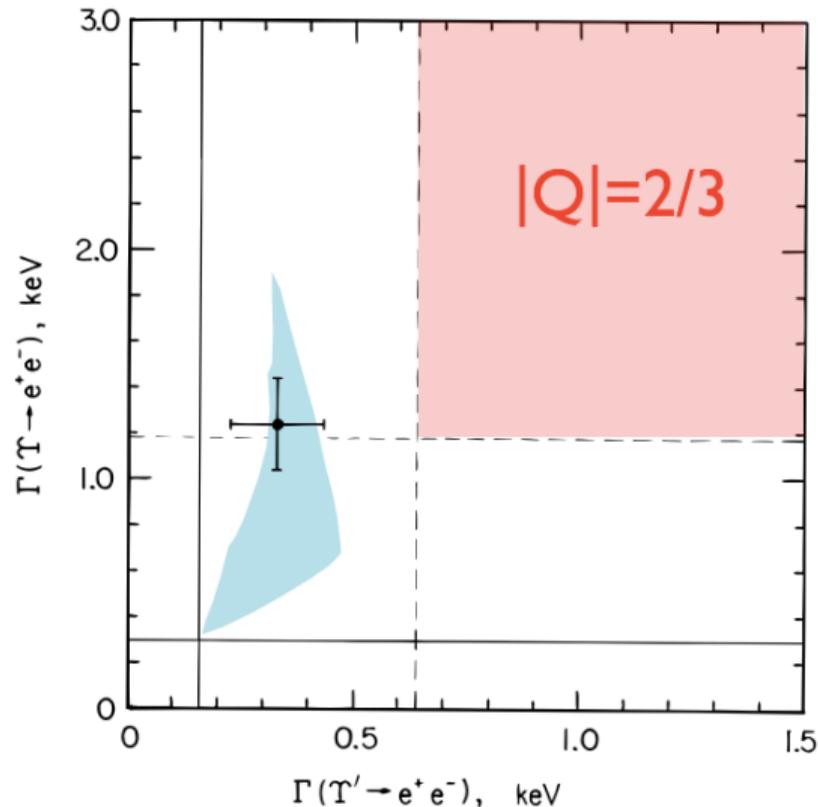
“high- y anomaly” could be explained by

$$\begin{pmatrix} u \\ b \end{pmatrix}_R \text{ with } m_b \approx 4 - 5 \text{ GeV}$$

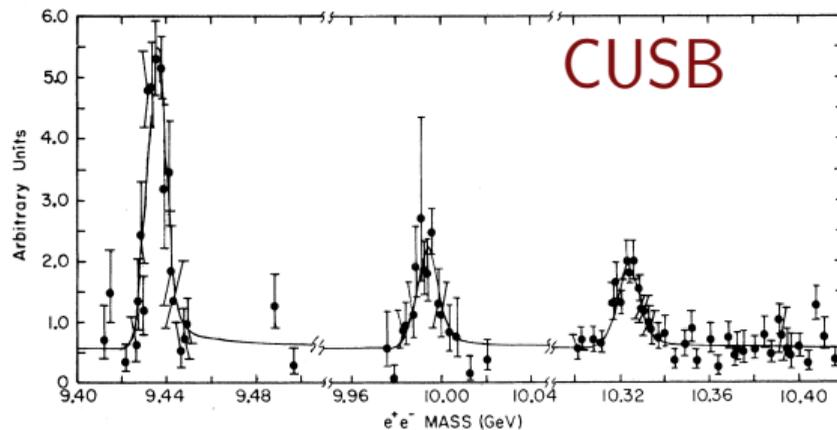
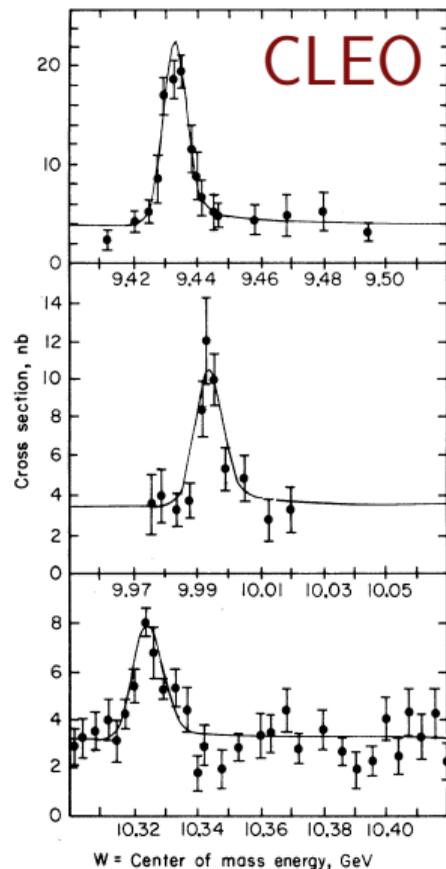
Also at Budapest 1977...

CDHS experiment ruled out the high- y anomaly

$\Upsilon(1S), \Upsilon(2S)$ leptonic widths $\rightsquigarrow Q_b = -\frac{1}{3}$ (DORIS, 1978)

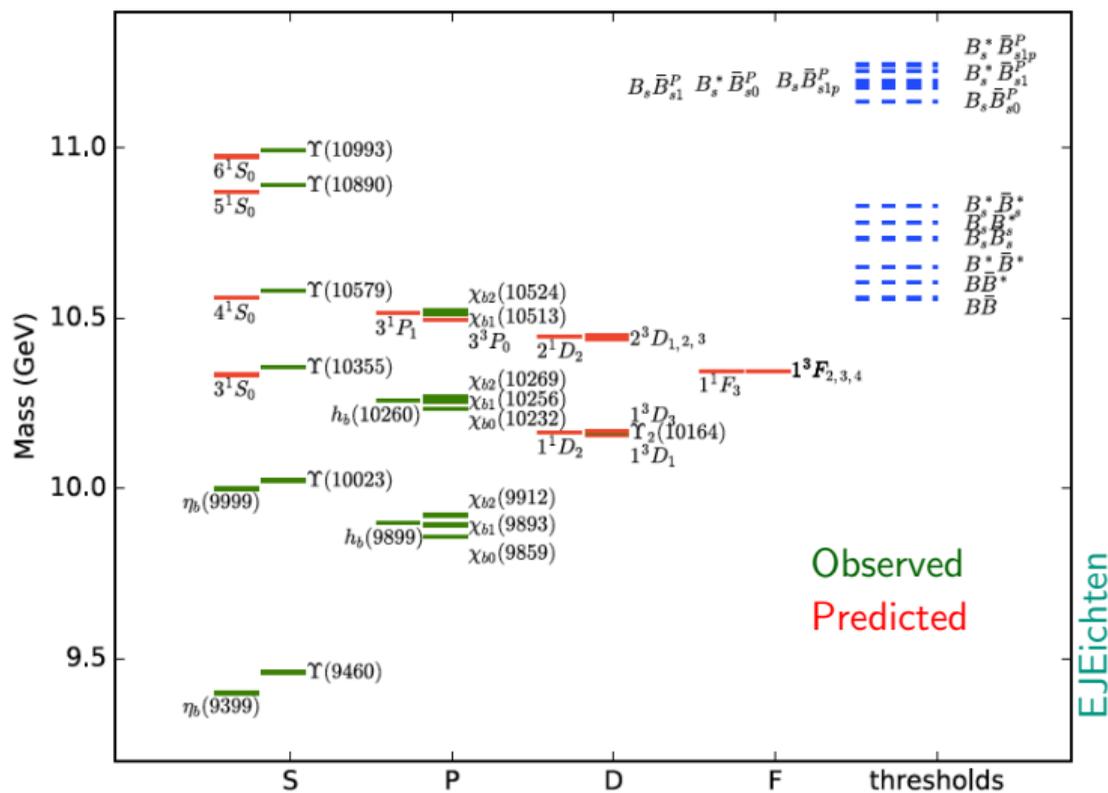


CESR resolves three narrow Υ states (1979–80)



$\Upsilon(4S)$ launches B physics (1980)

Rich spectrum of $(b\bar{b})$ levels



14 states below threshold still unobserved

Charmonium-associated states not pure charmonium

All these states near or above threshold

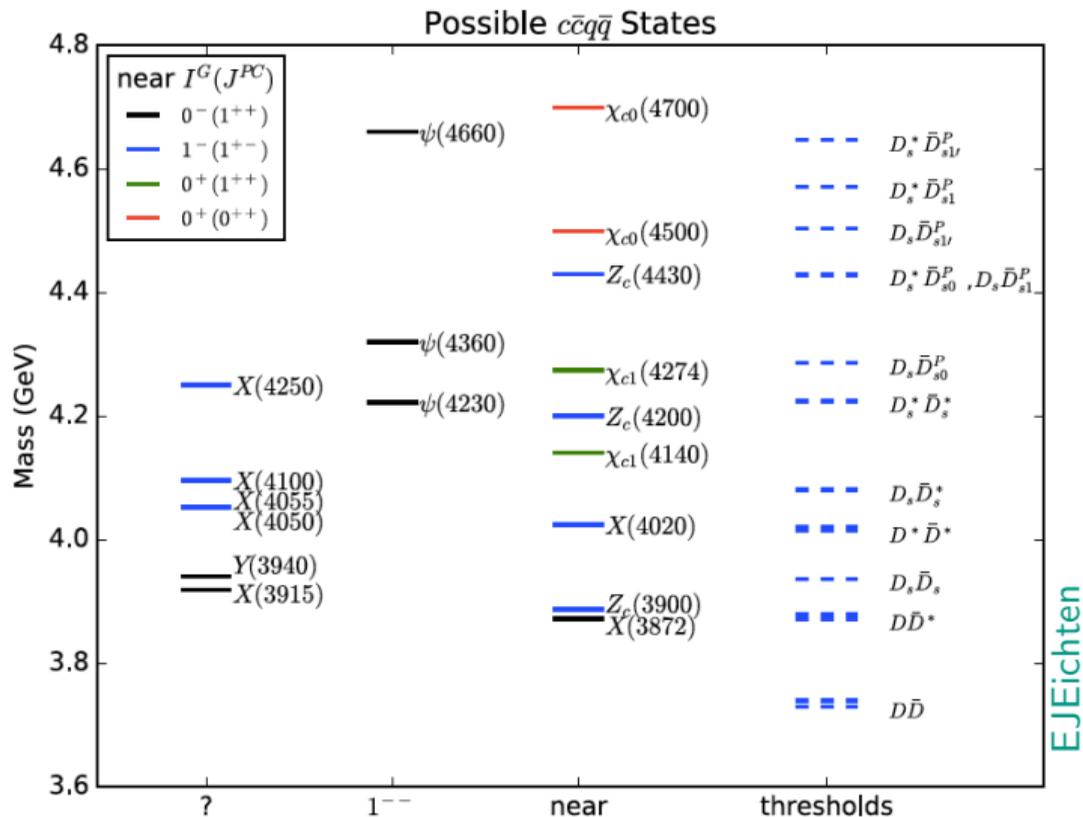
near threshold states have possible molecule component

“ $\zeta \dots ?$ ” need more info

if $J^{PC} = 0^{++}$, $\zeta X(3915)$? possible 2^3P_2

$\zeta \psi(4660)$? possible 5S

$\psi(4230)$, $\zeta \psi(4360)$? possible hybrids



When can we find ($b\bar{b}$) analogues?

Quarkonium-associated states: $M \gtrsim$ threshold: $X(3872)$ etc.

Mostly narrow, seen in hadronic transitions or decays

What are they?

Quarkonium (+ coupled-channels, thresholds)

Threshold effects

New body plans:

quarkonium hybrids ($q\bar{q}g$)

two-quark–two-antiquark states, including

dimeson “molecules”

tetraquarks

diquarkonium · hadroquarkonium

and superpositions!

(crypto)pentaquarks

CP violation might be large and observable (1980–81)

CP Nonconservation in Cascade Decays of B Mesons

Ashton B. Carter and A. I. Sanda
Rockefeller University, New York, New York 10021
(Received 2 June 1980)

General techniques are introduced to expose new CP -nonconserving effects in cascade decays of B mesons. These effects are computed in the Kobayashi-Maskawa model. The CP asymmetries so obtained range from 2% to 20% if the parameters are in the favorable range $s_3 < s_2 \lesssim 0.1$. Effects of this size should be observable in upcoming experiments.

NOTES ON THE OBSERVABILITY OF CP VIOLATIONS IN B DECAYS

I.I. BIGI

Institut für Theor. Physik der RWTH Aachen, D-5100 Aachen, FR Germany

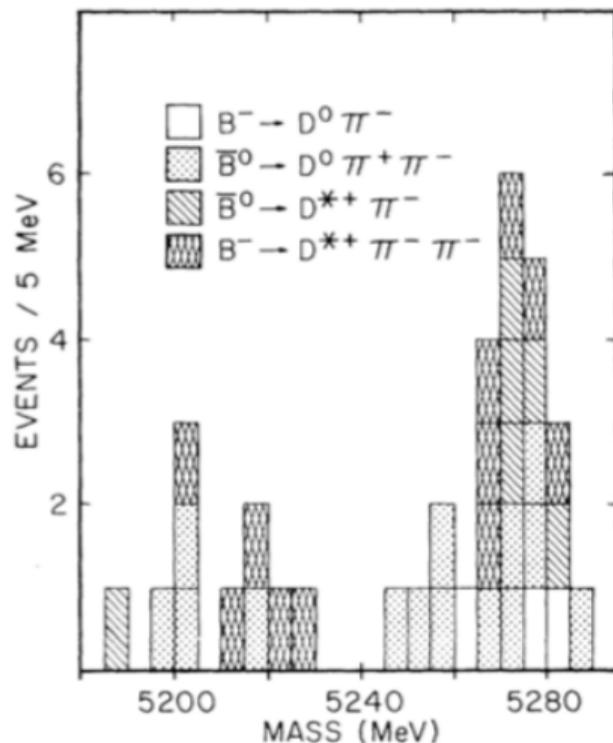
A.I. SANDA¹

Rockefeller University, New York 10021, USA

Received 16 June 1981

We describe a general method of exposing CP violations in on-shell transitions of B mesons. Such CP asymmetries can reach values of the order of up to 10% within the Kobayashi-Maskawa model for plausible values of the model parameters. Our discussion focuses on those (mainly non-leptonic) decay modes which carry the promise of exhibiting clean and relatively large CP asymmetries at the expense of a reduction in counting rates. Accordingly we address the complexities encountered when performing CP tests with a high statistics B meson factory like the Z^0 (and a toponium) resonance.

Reconstruction of B Mesons (CLEO, 1983)



PDG: I, J, P still need confirmation!

MAC & Mark II find unexpectedly long b -hadron lifetime (1983)

Charm lifetimes [fs]

$$D^+ : 1040 \pm 7$$

$$D^0 : 410.1 \pm 1.5$$

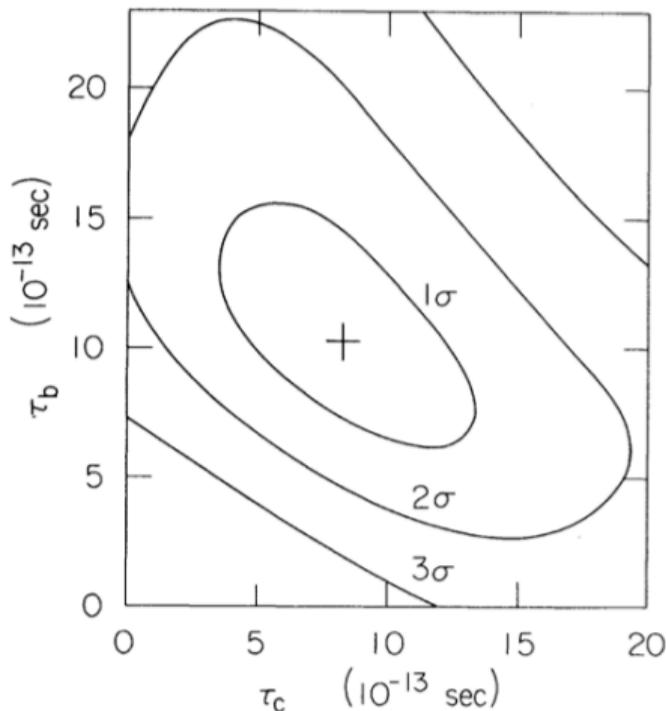
$$D_s : 504 \pm 4$$

$$\Lambda_c : 200 \pm 6$$

$$\Xi_c^+ : 442 \pm 26$$

$$\Xi_c^0 : 112^{+13}_{-10}$$

$$\Omega_c : 268^{+10}_{-26}$$



Beauty lifetimes [fs]

$$B^+ : 1638 \pm 4$$

$$B^0 : 1519 \pm 4$$

$$B_s : 1510 \pm 4$$

$$\Lambda_b : 1471 \pm 9$$

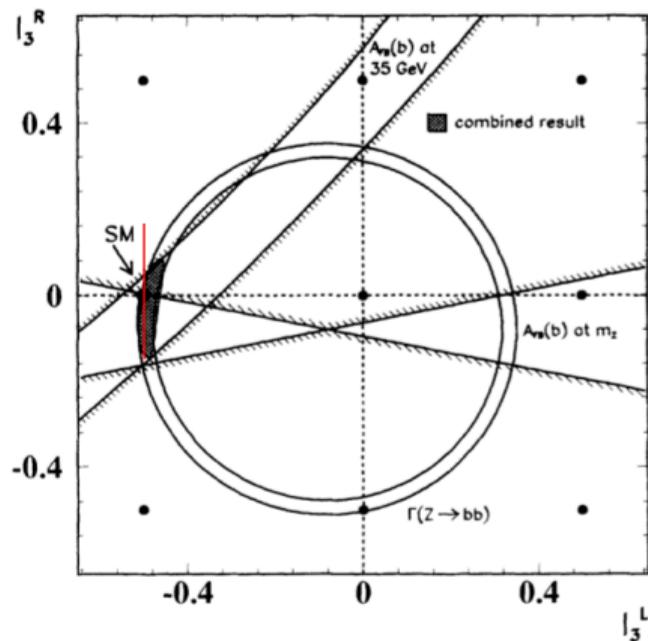
$$\Xi_b^- : 1572 \pm 40$$

$$\Xi_b^0 : 1480 \pm 30$$

$$\Omega_b : 1640^{+180}_{-170}$$

Evidence for small $|V_{cb}| \approx 0.05$

b properties imply top-quark partner must exist (1992)

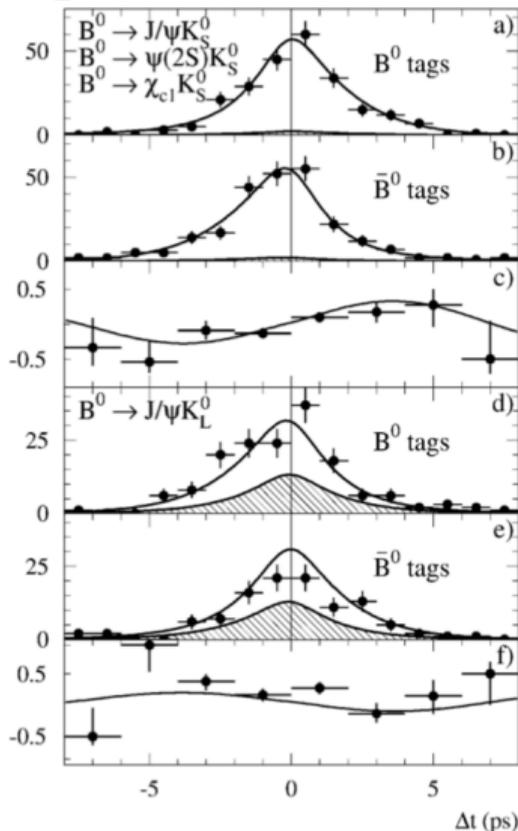


$$L_b \equiv 2I_{3L} - 2Q_b \sin^2 \theta_W, \quad R_b \equiv 2I_{3R} - 2Q_b \sin^2 \theta_W$$

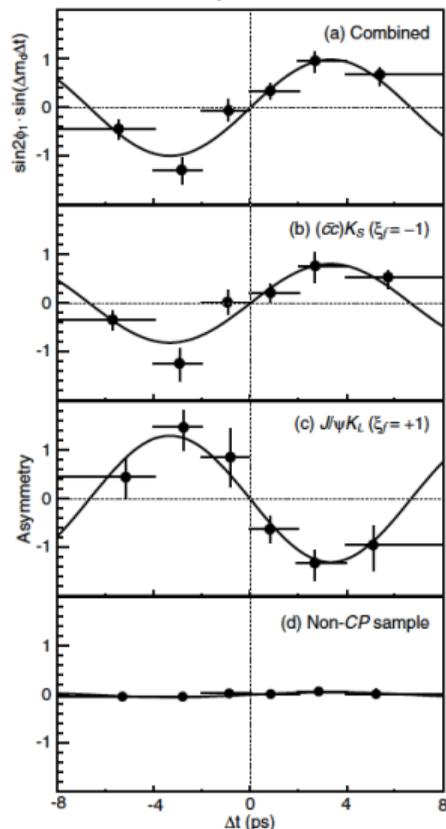
$\Gamma(Z^0 \rightarrow b\bar{b})$ measures $(L_b^2 + R_b^2)$, $A_{\text{peak}}^{(bb)} (L_b^2 - R_b^2)/(L_b^2 + R_b^2)$, LE FB asym $A(b\bar{b}) \propto (R_b - L_b)$

$$I_{3L} = -\frac{1}{2}; \quad I_{3R} = 0$$

Observation of *large* CP violation in B^0 decays (*BABAR* & Belle, 2001)

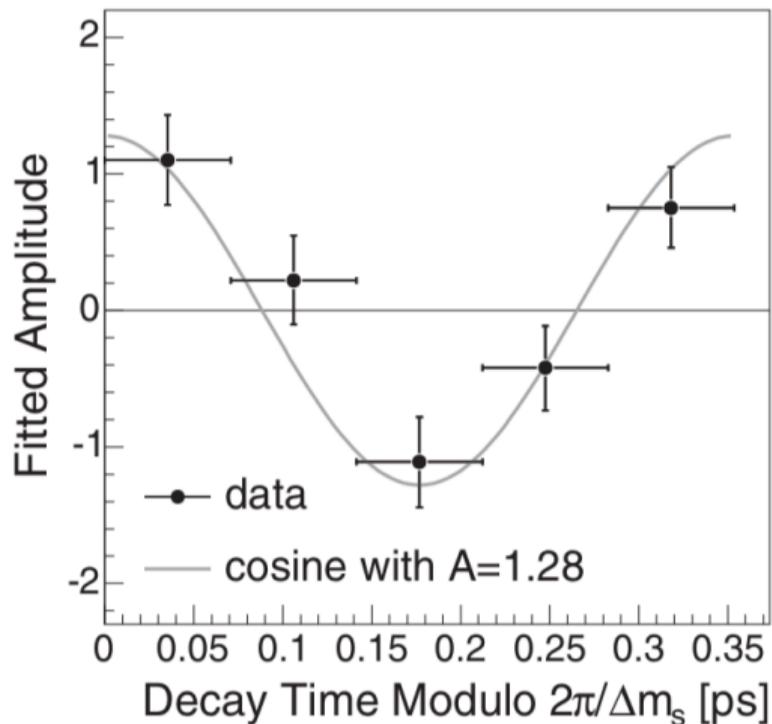


$$\sin 2\beta \approx 0.59$$



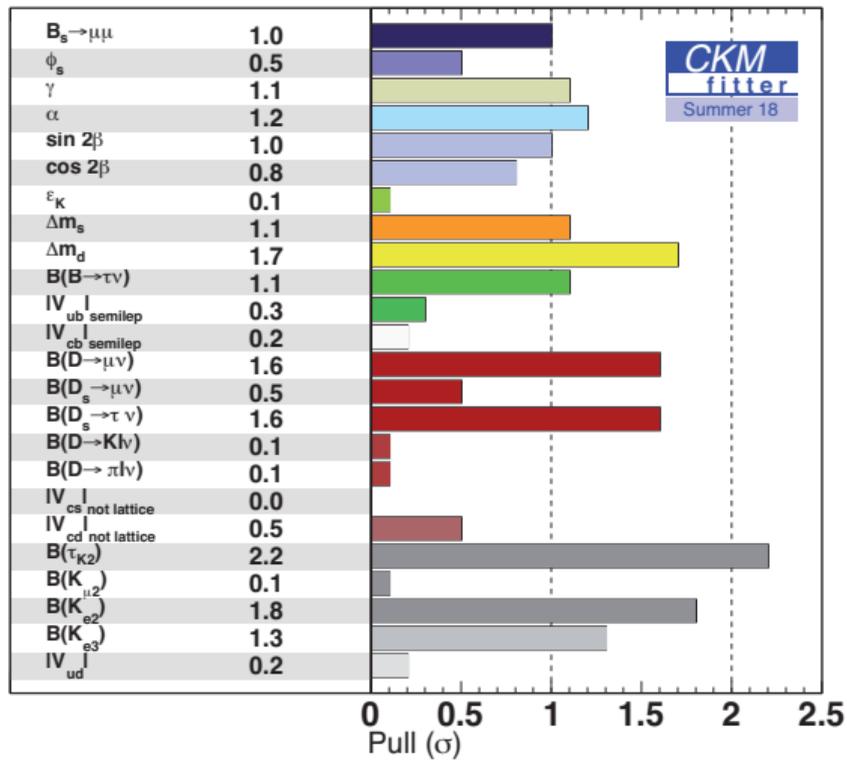
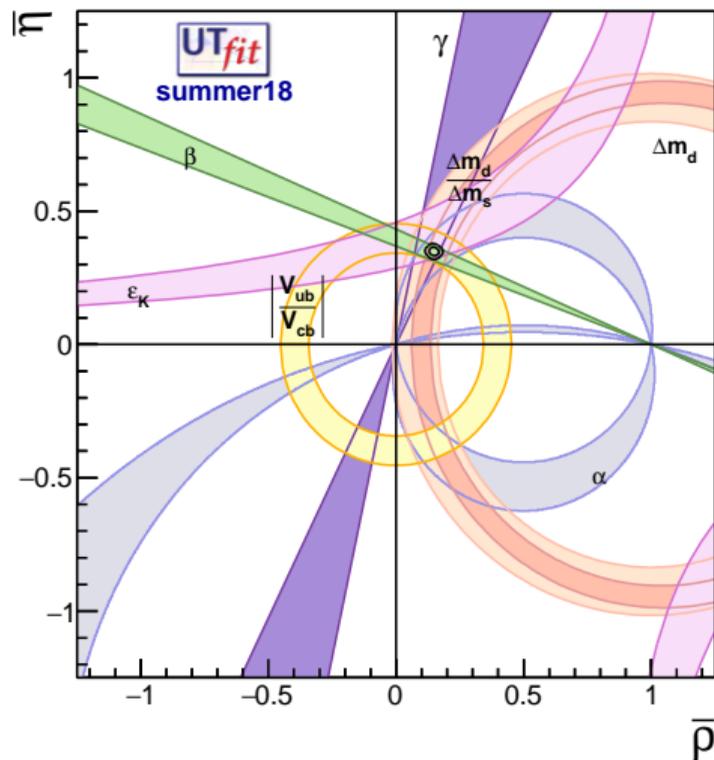
$$\sin 2\phi_1 \approx 0.99$$

Observation of $B_s^0 - \bar{B}_s^0$ Oscillations (CDF, 2006)

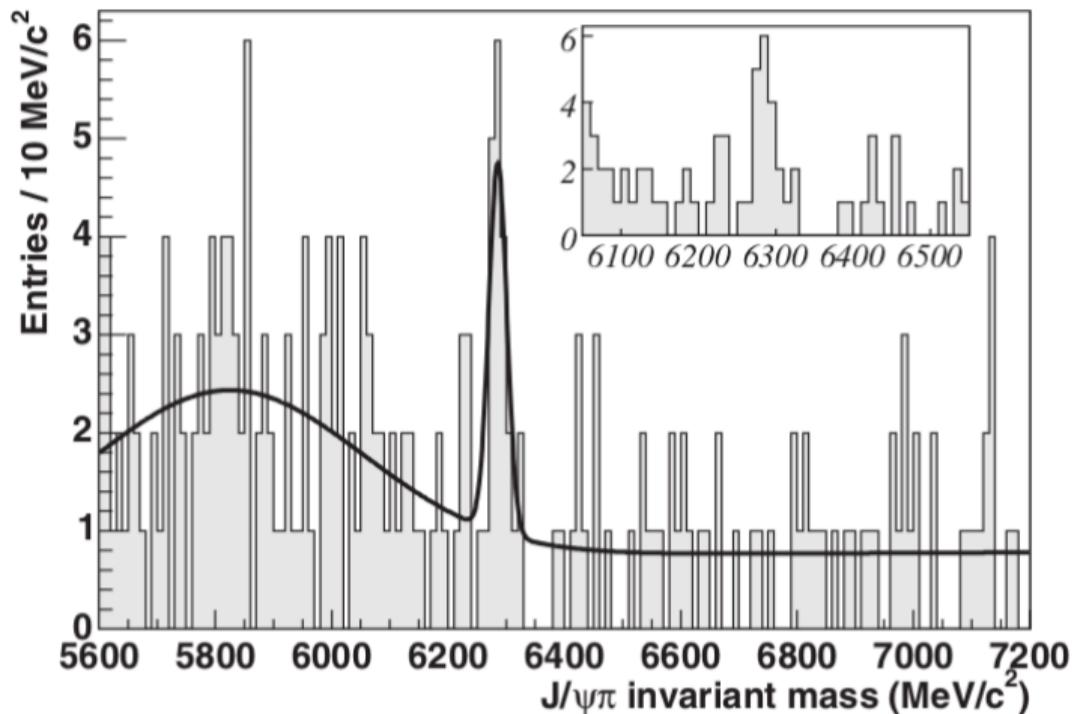


$$\Delta m_s \approx 17.77 \text{ ps}^{-1}$$

Precision tests of the CKM paradigm



Reconstruction of B_c meson (CDF, 2006)



$$M(B_c) = 6274.9 \pm 0.8 \text{ MeV} \quad (\text{Test of lattice QCD prediction})$$

Mesons with beauty and charm: stress test for NRQM, LQCD

B_c : weak decays only

$b \rightarrow c$ $c \rightarrow s$ $b\bar{c} \rightarrow W^-$

$B_c \rightarrow J/\psi\pi$: ($Q\bar{Q}$) transmutation

Rich ($b\bar{c}$) excitation spectrum;
interpolates J/ψ , Υ (\neq masses)

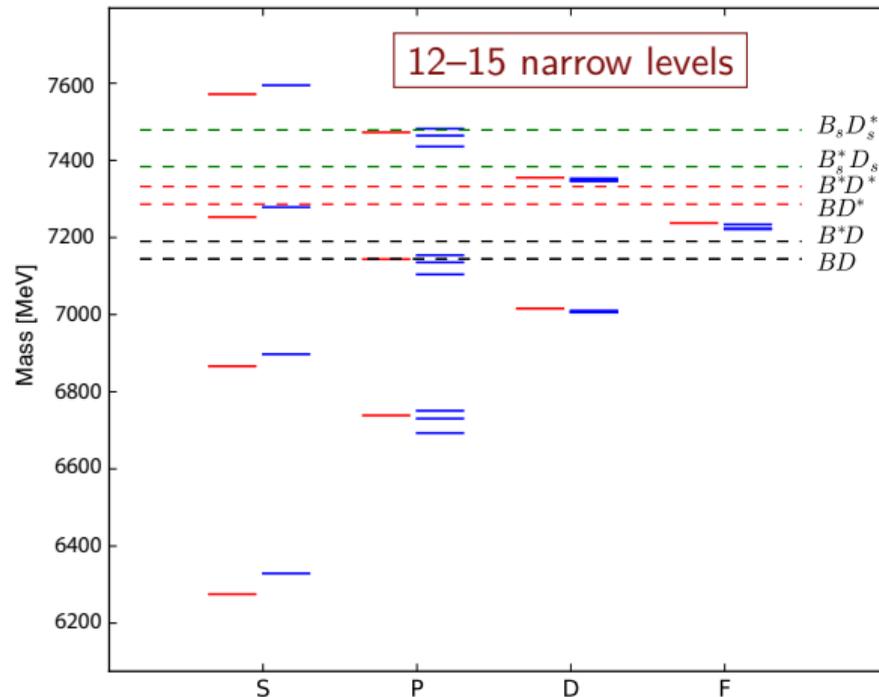
Excited states below $BD \rightarrow B_c + \dots$

$B_c(2S) \rightarrow B_c(1S) + \pi\pi$

P states: γ transitions

Many states observable at LHC, TeraZ

Update: Eichten & CQ (2019)
using “frozen- α_s ” potential, new
approach to spin splittings



Observing the B_c spectrum: $\pi\pi$ transitions

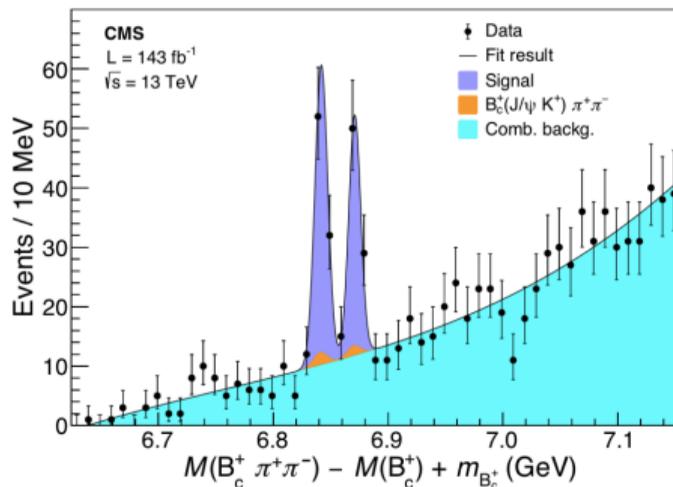
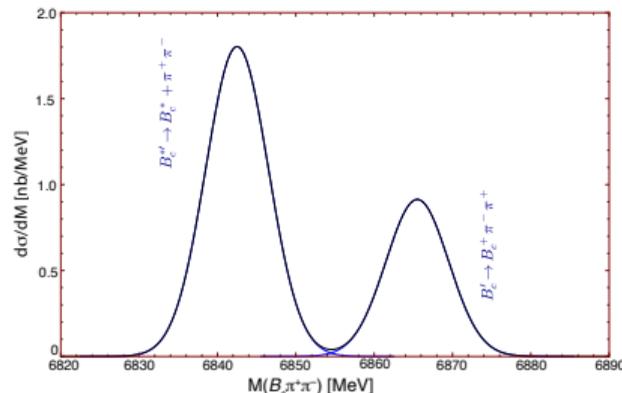
Combine predicted production rates (BCVEGPY2.2) with calculated branching fractions to obtain expectations for $\pi\pi$ transition rates
 \rightsquigarrow peak heights: $B_c^{*'} / B_c' \approx 2.5$

M1 $B_c^* \rightarrow \gamma B_c$ unobserved

$$[M(B_c^{*'}) - M(B_c')] - [M(B_c^*) - M(B_c)] \approx -23 \text{ MeV: } B_c^{*'} \text{ lower peak}$$

2S $\rightarrow \pi\pi +$ 1S transitions observed by ATLAS, CMS, LHCb

CMS separation: -29 MeV



Observing the B_c spectrum: E1 transitions

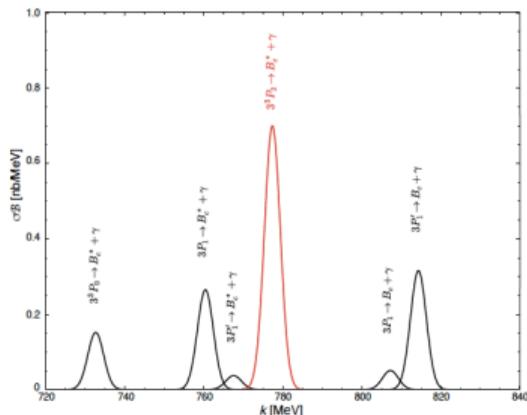
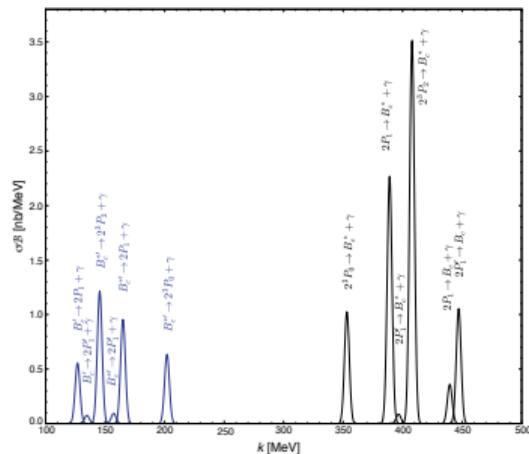
E1 spectroscopy in the $(b\bar{b})$ family:
LHC experiments discovered χ''_{b1}, χ''_{b2} .

Incentive for the search: $2S \rightarrow 2P$ and
 $2P \rightarrow 1S$ transitions, assuming missing
 $B_c^* \rightarrow B_c \gamma$ in the reconstruction.

$3S, 3P$ yields $\approx \frac{1}{4} \times 2P \rightarrow 1S$ lines, but
higher γ energies may aid detection.

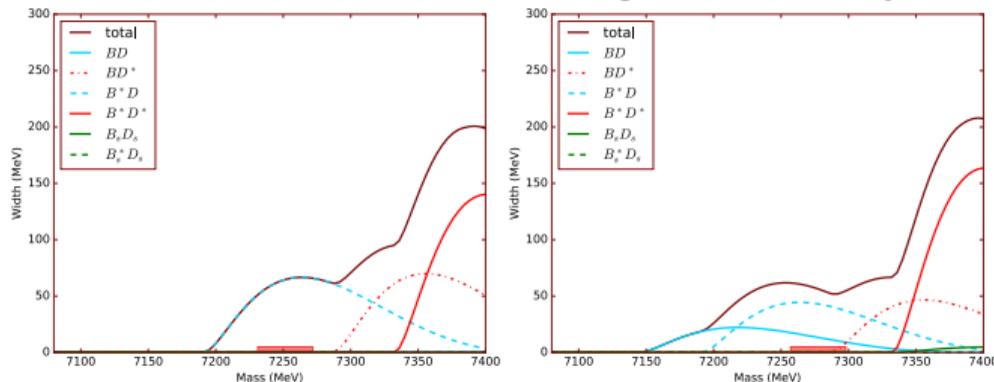
$$3^3P_2(7154) \rightarrow B_c^* \gamma(777 \text{ MeV})$$

Encourage search for $(3, 2)P(b\bar{c})$.

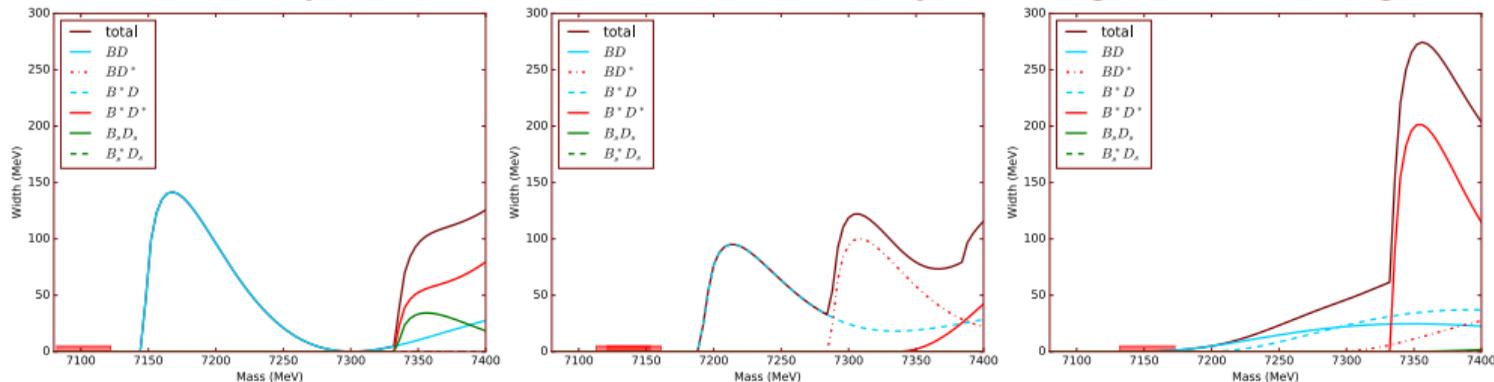


Mesons with beauty and charm: states above flavor threshold

3S states above threshold have significant decay widths



3P states just below threshold; $J = 1$ may have significant mixing



Strong dynamics greatly simplifies for $M_Q \gg \Lambda_{\text{QCD}}$

Symmetry independent of dynamics of light degrees of freedom

Heavy-light systems: $(c\bar{q}), (b\bar{q}), (cq), (bq), (ccq), (cbq), (bbq)$ ($q = u, d, s$)

HQET: systematic expansion in powers of Λ_{QCD}/M_Q

HQS relations among spectra in $[(c\bar{q}), (b\bar{q}), (ccq), (bcq), (bbq)]$ and $[(cq), (bq)]$

QED analogue: hydrogen atom ($e^- p^+$)

Nonrelativistic ($Q\bar{Q}$): bound-state masses $\mathcal{M} \approx 2M_Q$

NRQCD: systematic expansion in powers of v/c

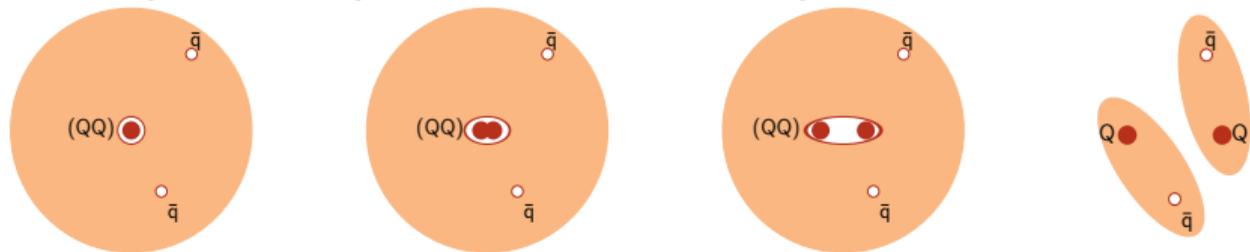
Quarkonium systems: $(c\bar{c}), (b\bar{b}), (b\bar{c})$

heavy quark velocity: $p_Q/M_Q \approx v/c \ll 1$

binding energy: $2M_Q - \mathcal{M} \approx M_Q v^2/c^2$

QED analogs: positronium ($e^+ e^-$), “true” muonium ($\mu^+ \mu^-$), muonium ($\mu^+ e^-$)

Heavy quark symmetry \Rightarrow stable heavy tetraquarks $Q_i Q_j \bar{q}_k \bar{q}_l$



HQS relates DHTQ mass to masses of QQq , Qqq , $Q\bar{q}$.

Lightest $bb\bar{u}\bar{d}$, $bb\bar{u}\bar{s}$, $bb\bar{d}\bar{s}$ states: (likely) no strong decays.

Heavier $bb\bar{q}_k\bar{q}_l$, $cc\bar{q}_k\bar{q}_l$, $bc\bar{q}_k\bar{q}_l \rightarrow Q\bar{q} + Q\bar{q}$ might be seen as “double-flavor” resonances near threshold.

Observing a weakly decaying double-beauty state would establish the existence of tetraquarks and illuminate the role of heavy color- $\bar{\mathbf{3}}$ diquarks as hadron constituents.

Eichten & CQ 1707.09575

HQS relations for ground-state tetraquark masses

$$m(Q_i Q_j \bar{q}_k \bar{q}_l) - m(Q_i Q_j q_m) = m(Q_x q_k q_l) - m(Q_x \bar{q}_m)$$

+ finite-mass corrections

RHS is determined from data

One doubly heavy baryon observed, Ξ_{cc} ; others from model calculations*

$$\text{LHCb: } M(\Xi_{cc}^{++}) = 3621.40 \pm 0.78 \text{ MeV}$$

*We adopt Karliner & Rosner, *PRD* **90**, 094007 (2014)

Strong decays $(Q_i Q_j \bar{q}_k \bar{q}_l) \not\rightarrow (Q_i Q_j q_m) + (\bar{q}_k \bar{q}_l \bar{q}_m) \forall$ ground states

Consider decays to pairs of heavy–light mesons case-by-case

Expectations for ground-state tetraquark masses, in MeV

State	J^P	$m(Q_i Q_j \bar{q}_k \bar{q}_l)$	Decay Channel	Q [MeV]
$\{cc\}[\bar{u}\bar{d}]$	1^+	3978	$D^+ D^{*0}$ 3876	102
$\{cc\}[\bar{q}_k \bar{s}]$	1^+	4156	$D^+ D_s^{*+}$ 3977	179
$\{cc\}\{\bar{q}_k \bar{q}_l\}$	$0^+, 1^+, 2^+$	4146, 4167, 4210	$D^+ D^0, D^+ D^{*0}$ 3734, 3876	412, 292, 476
$[bc][\bar{u}\bar{d}]$	0^+	7229	$B^- D^+ / B^0 D^0$ 7146	83
$[bc][\bar{q}_k \bar{s}]$	0^+	7406	$B_s D$ 7236	170
$[bc]\{\bar{q}_k \bar{q}_l\}$	1^+	7439	$B^* D / B D^*$ 7190/7290	249
$\{bc\}[\bar{u}\bar{d}]$	1^+	7272	$B^* D / B D^*$ 7190/7290	82
$\{bc\}[\bar{q}_k \bar{s}]$	1^+	7445	DB_s^* 7282	163
$\{bc\}\{\bar{q}_k \bar{q}_l\}$	$0^+, 1^+, 2^+$	7461, 7472, 7493	$BD / B^* D$ 7146/7190	317, 282, 349
$\{bb\}[\bar{u}\bar{d}]$	1^+	10482	$B^- \bar{B}^{*0}$ 10603	-121
$\{bb\}[\bar{q}_k \bar{s}]$	1^+	10643	$\bar{B} \bar{B}_s^* / \bar{B}_s \bar{B}^*$ 10695/10691	-48
$\{bb\}\{\bar{q}_k \bar{q}_l\}$	$0^+, 1^+, 2^+$	10674, 10681, 10695	$B^- B^0, B^- B^{*0}$ 10559, 10603	115, 78, 136

Cf. M. Karliner & J. L. Rosner model, Phys. Rev. Lett. **119**, 202001 (2017) [arXiv:1707.07666].
 Estimate deeper binding, so additional bc and cc candidates.

Real-world candidates for stable tetraquarks

$J^P = 1^+ \{bb\}[\bar{u}\bar{d}]$ meson, bound by 121 MeV

(77 MeV below $B^- \bar{B}^0 \gamma$)

$\mathcal{T}_{[\bar{u}\bar{d}]}^{\{bb\}}(10482)^- \rightarrow \Xi_{bc}^0 \bar{p}, B^- D^+ \pi^-,$ and $\underbrace{B^- D^+ \ell^- \bar{\nu}}_{\text{manifestly weak!}}$

$J^P = 1^+ \{bb\}[\bar{u}\bar{s}]$ and $\{bb\}[\bar{d}\bar{s}]$ mesons, bound by 48 MeV

(3 MeV below $BB_s \gamma$)

$\mathcal{T}_{[\bar{u}\bar{s}]}^{\{bb\}}(10643)^- \rightarrow \Xi_{bc}^0 \bar{\Sigma}^-$ $\mathcal{T}_{[\bar{d}\bar{s}]}^{\{bb\}}(10643)^0 \rightarrow \Xi_{bc}^0 (\bar{\Lambda}, \bar{\Sigma}^0)$

Unstable doubly heavy tetraquarks

Resonances in “wrong-sign” (double flavor) combinations $DD, DB, BB?$

$J^P = 1^+ \mathcal{T}_{[d\bar{s}]^{\{cc\}}^{++} (4156) \rightarrow D^+ D_s^{*+}$: *prima facie evidence* for non- $q\bar{q}$ level

Double charge / double charm

(New kind of resonance: no attractive force at the meson–meson level.)

Also, $1^+ \mathcal{T}_{\{\bar{q}_k \bar{q}_l\}^{\{bb\}}} (10681)^{0,-,-}, Q = +78 \text{ MeV}$ $1^+ \mathcal{T}_{[\bar{u}\bar{d}]^{\{bc\}}} (7272)^0, Q = +82 \text{ MeV}$

$0^+ \mathcal{T}_{[\bar{u}\bar{d}]^{\{bc\}}} (7229)^0, Q = +83 \text{ MeV}$ $1^+ \mathcal{T}_{[\bar{u}\bar{d}]^{\{cc\}}} (3978)^+, Q = +102 \text{ MeV}$

Aside: 3D_3 and 3F_4 $c\bar{c}$ mesons still to be found in $D\bar{D}$, etc.

Homework for experiment

- $\mathcal{T}1$. Look for double-flavor resonances near threshold.
- $\mathcal{T}2$. Measure cross sections for final states containing 4 heavies:
 $Q_i \bar{Q}_i Q_j \bar{Q}_j$.
- $\mathcal{T}3$. Discover and determine masses of doubly-heavy baryons.
needed to implement HQS calculation of tetraquark masses
intrinsic interest in these states:
compare heavy–light mesons, possible core excitations
Resolve Ξ_{cc} uncertainty (SELEX/LHCb)
- $\mathcal{T}4$. Find stable tetraquarks through weak decays. Lifetime: $\sim \frac{1}{3}$ ps ??

Homework for theory

- $\mathcal{T}5$. Develop expectations for production. A. Ali et al., “Prospects of discovering stable double-heavy tetraquarks at a Tera-Z factory,” arXiv:1805.02535 → PLB.
- $\mathcal{T}6$. Refine lifetime estimates for stable states.
- $\mathcal{T}7$. Understand how color configurations evolve with QQ (and $\bar{q}\bar{q}$) masses. J.-M. Richard, et al., “Few-body quark dynamics for doubly-heavy baryons and tetraquarks,” arXiv:1803.06155, Phys. Rev. C **97**, 035211 (2018).
- $\mathcal{T}8$. Investigate stability of different body plans in the heavy-quark limit.
... up to $(Q_i Q_j)(Q_k Q_l)(Q_m Q_n)$: $B = 2$, but $Q_p Q_q Q_r$ color structure?

Flavor: the problem of identity

What makes an electron an electron, a top quark a top quark, ... ?

We do not have a clear view of how to approach the diverse character of the constituents of matter

CKM paradigm: extraordinarily fruitful framework in hadron sector

BUT—many parameters: no clue what determines them, nor at what energy scale they are set

Even if Higgs mechanism explains *how* masses and mixing angles arise, we do not know *why* they have the values we observe

Physics beyond the standard model!

Flavor: the problem of identity (continued)

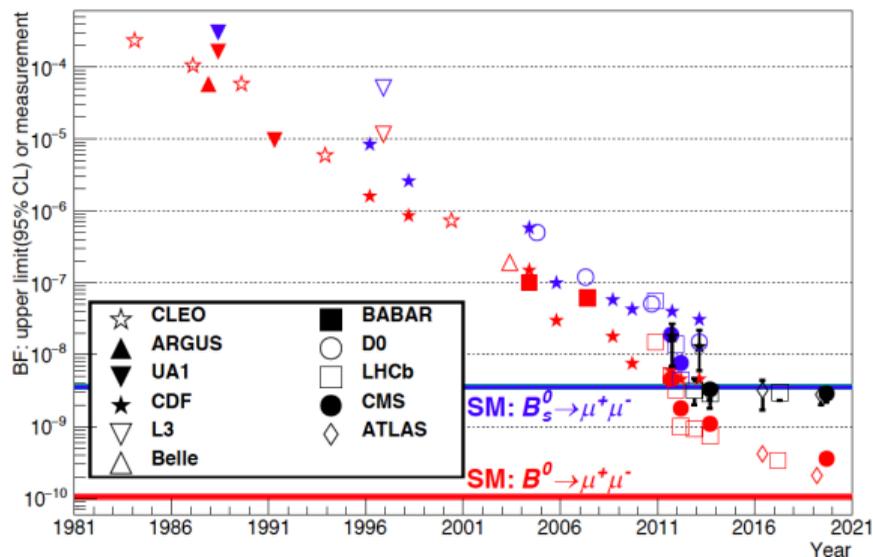
Parameters of the Standard Model

- 3 Coupling parameters, α_s , α_{em} , $\sin^2 \theta_W$
 - 2 Parameters of the Higgs potential
 - 1 Vacuum phase (QCD)
 - 6 Quark masses
 - 3 Quark mixing angles
 - 1 CP-violating phase
 - 3 Charged-lepton masses
 - 3 Neutrino masses
 - 3 Leptonic mixing angles
 - 1 Leptonic CP-violating phase (+ Majorana phases?)
-
- 26⁺ Arbitrary parameters
-

Questions concerning the problem of identity

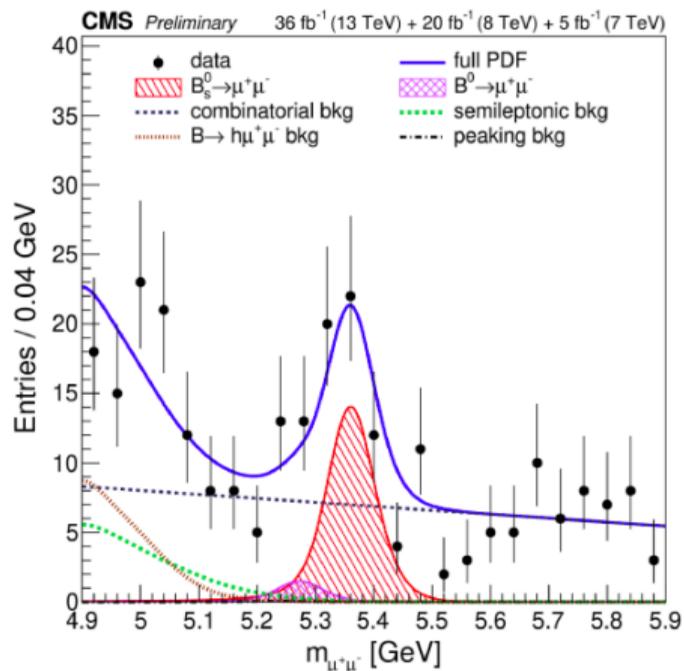
- F1. Can we find evidence of right-handed charged-current interactions?
Is nature built on a fundamentally asymmetrical plan, or are the right-handed weak interactions simply too feeble for us to have observed until now, reflecting an underlying hidden symmetry?
- F2. What is the relationship of left-handed and right-handed fermions?
- F3. Are there additional electroweak gauge bosons, beyond W^\pm and Z ?
- F4. Are there additional kinds of matter?
- F5. Is charged-current universality exact?
What about lepton-flavor universality?

$B_{(s,d)} \rightarrow \ell^+ \ell^-$ search and observation



$$\text{SM: } \mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = (3.66 \pm 0.23) \times 10^{-9}$$

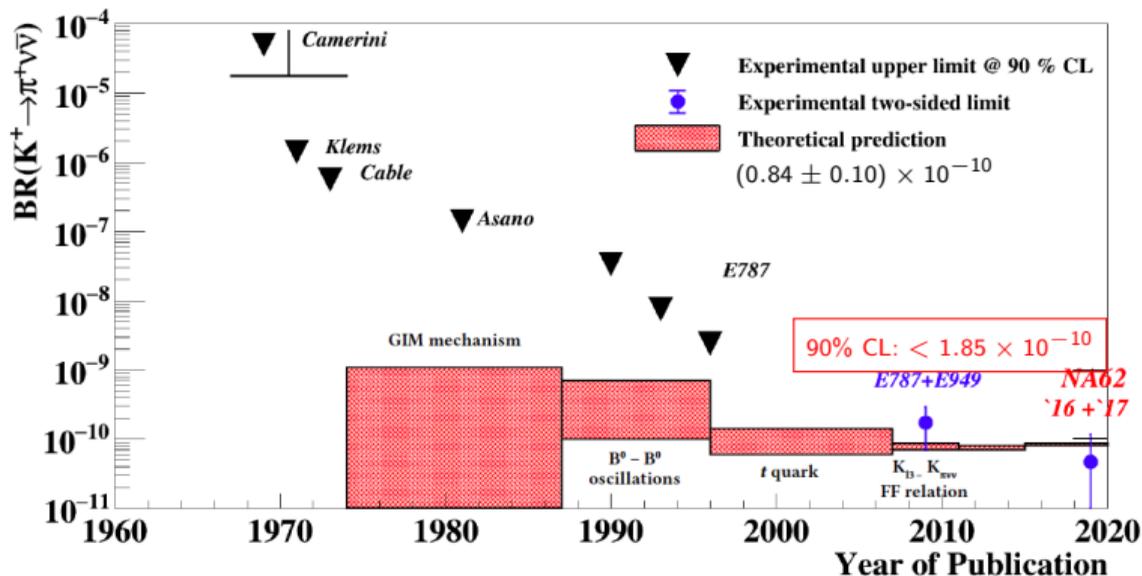
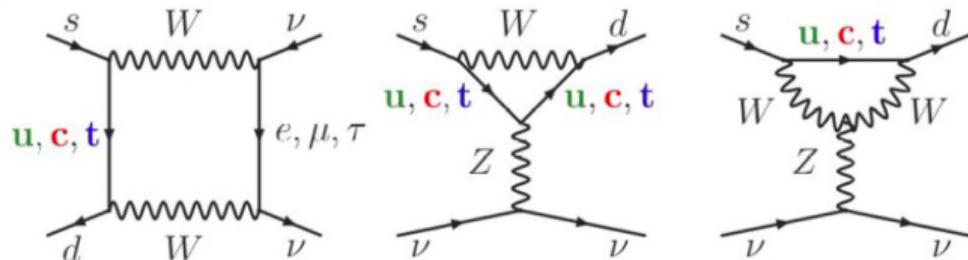
$$\mathcal{B}(B_d \rightarrow \mu^+ \mu^-) = (1.06 \pm 0.09) \times 10^{-10}$$



$$\text{Recent CMS: } \mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = [2.9_{-0.4}^{+0.7} \pm 0.2(f_s/f_d)] \times 10^{-9}$$

Coming: $\tau(B_s \rightarrow \mu^+ \mu^-)$, $B_{(d,s)} \rightarrow e^+ e^-$ searches

$K^+ \rightarrow \pi^+ \nu \bar{\nu}$ search and observation



Searches for flavor-changing neutral currents

- F6. Where are flavor-changing neutral currents in quark transitions? In the standard model, these are absent at tree level and highly suppressed by the Glashow–Iliopoulos–Maiani mechanism. They arise generically in proposals for physics beyond the standard model, and need to be controlled. And yet we have made no sightings!

Why not?

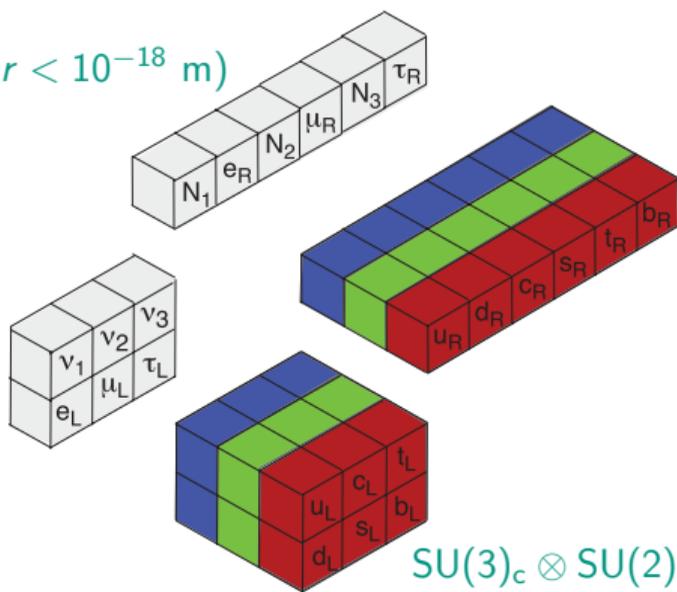
$$B_{s,d} \rightarrow \mu^+ \mu^-, K^+ \rightarrow \pi^+ \nu \bar{\nu}, \dots$$

- F7. Can we detect flavor-violating decays $H(125) \rightarrow \tau^\pm \mu^\mp, \dots$?

- F8. How well can we test the standard-model correlation among $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$, $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$, and the quark-mixing matrix parameter γ ?

Have we found the “periodic table” of elementary particles?

Pointlike spin-1/2 constituents ($r < 10^{-18}$ m)



F9. What do generations mean? Is there a family symmetry?

F10. Why are there three families of quarks and leptons? (Is it so?)

F11. Are there new species of quarks and leptons? exotic charges?

More questions concerning the problem of identity

- F12. Is there any link to a dark sector?
- F13. What will resolve the disparate values of $|V_{ub}|$ and $|V_{cb}|$ measured in inclusive and exclusive decays?
- F14. Is the 3×3 (CKM) quark-mixing matrix unitary?
- F15. Why is isospin a good symmetry? What does it mean?
- F16. Can we find evidence for charged-lepton flavor violation?
- F17. Will we establish and diagnose a break in the SM?
- F18. Do flavor parameters *mean* anything at all?
Contrast the landscape perspective.
- F19. If flavor parameters have meaning (beyond engineering information), what is the meta-question?

The top quark touches many topics in particle physics

- t*1. How well can we constrain V_{tb} in single-top production, ...?
- t*2. How well can we constrain the top-quark lifetime? How free is *t*?
Recent ATLAS: $\Gamma(t) = 1.9 \pm 0.5 \text{ GeV}$ (SM 1.32 GeV)
- t*3. Are there $t\bar{t}$ resonances?
- t*4. Can we find evidence of flavor-changing top decays $t \rightarrow (Z, \gamma)(c, u)$?

Questions about EWSB and the Higgs Sector

- H1. Is $H(125)$ the only member of its clan? Might there be others—charged or neutral—at higher or lower masses?
- H2. Does $H(125)$ fully account for electroweak symmetry breaking? Does it match standard-model branching fractions to gauge bosons? Are absolute couplings to W and Z as expected in the standard model?
- H3. Are all production rates as expected? Any surprise sources of $H(125)$?
- H4. What accounts for the immense range of fermion masses?
- H5. Is the Higgs field the only source of fermion masses?
Are fermion couplings proportional to fermion masses? $\mu^+\mu^-$ soon?
How can we detect $H \rightarrow c\bar{c}$ $e^+e^-??$ (basis of chemistry)
- H6. What role does the Higgs field play in generating neutrino masses?

More questions about EWSB and the Higgs Sector

- H7. Can we establish or exclude decays to new particles? Does $H(125)$ act as a portal to hidden sectors? When can we measure Γ_H ?
- H8. Can we detect flavor-violating decays ($\tau^\pm \mu^\mp, \dots$)?
- H9. Do loop-induced decays ($gg, \gamma\gamma, \gamma Z$) occur at standard-model rates?
- H10. What can we learn from rare decays ($J/\psi \gamma, \Upsilon \gamma, \dots$)?
- H11. Does the EW vacuum seem stable, or suggest a new physics scale?
- H12. Can we find signs of new strong dynamics or (partial) compositeness?
- H13. Can we establish the HHH trilinear self-coupling?
- H14. How well can we test the notion that H regulates Higgs–Goldstone scattering, i.e., tames the high-energy behavior of WW scattering?
- H15. Is the electroweak phase transition first-order?

See Dawson, Englert, Plehn, arXiv:1808.01324 \rightsquigarrow *Phys. Rep.*

An exercise for all of us

How do *you* assess the scientific potential *for Beauty and in general of*

- (a) *The High-Luminosity LHC?*
- (b) *The High-Energy LHC?*
- (c) *A 100-TeV pp Collider (FCC-hh)?*
- (d) *A 250-GeV ILC?*
- (e) *A circular Higgs factory (FCC-ee or CEPC)?*
- (f) *A 380-GeV CLIC?*
- (g) *A $\mu^+\mu^- \rightarrow H$ Higgs factory?*
- (h) *LHeC / FCC-eh? (or an electron-ion collider?)*
- (i) *A muon-storage-ring neutrino factory?*
- (j) *A multi-TeV muon collider?*
- (k) *The instrument of your dreams?*