

# Results and Future Prospects from NA62 and Other Kaon Experiments

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On behalf of the NA62 Collaboration

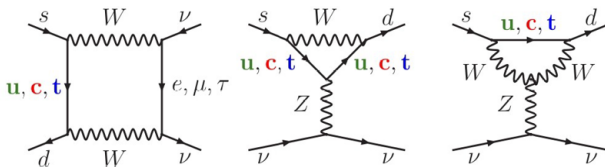
01/10/2019

BEAUTY 2019, Ljubljana, Slovenia



Type	Decay mode
<b>Main goal:</b>	$K^+ \rightarrow \pi^+ \nu \bar{\nu}$
<b>Exotic searches:</b> Heavy neutral lepton Dark photon $A'$ others	$K^+ \rightarrow l^+ N$ $K^+ \rightarrow \pi^+ \pi^0, \pi^0 \rightarrow A' \gamma$
<b>Forbidden decays:</b>	$K^+ \rightarrow \pi^- e^+ e^+$ $K^+ \rightarrow \pi^- \mu^+ \mu^+$ others
<b>Rare decays:</b>	$K^+ \rightarrow \pi^+ \mu^+ \mu^-$ $K^+ \rightarrow \pi^+ \gamma \gamma$ others

# $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ in Standard Model



- FCNC loop process - rare meson decay naturally suppressed by the GIM mech.
- Theoretically very clean (no hadronic uncertainties)
- Sensitive to contributions of physics BSM
  - **MSSM** [Blazek, Matak, Int.J.Mod.Phys. A29 (2014) no.27], [Isidori et al. JHEP 0608 (2006) 064]
  - **Custodial Randall-Sundrum** [Blanke, Buras, Duling, Gemmler, Gori, JHEP 0903 (2009) 108]
  - **Simplified Z, Z' models** [Buras, A.J., Buttazzo, D. & Kneijens, R. J. High Energ. Phys. (2015) 2015: 166]
  - **Littlest Higgs with T-parity** [Blanke, Buras, Recksiegel, Eur.Phys.J. C76 (2016) 182]
  - **LFU violation models** [Bordone, M., Buttazzo, D., Isidori, G. et al. Eur. Phys. J. C (2017) 77: 618]

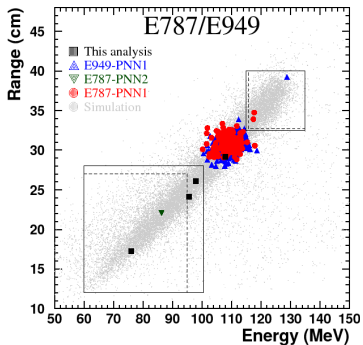
- SM prediction

[Brod, Gorbahn, Stamou, Phys.Rev.D 83, 034030(2011)], [Buras et al., JHEP11(2015) 033]:

$$\mathcal{B}_{SM}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.4 \pm 1.0) \times 10^{-11}$$

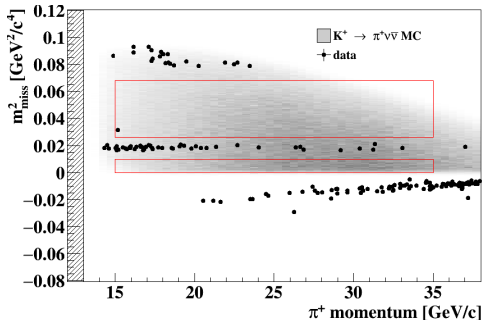
- Uncertainty coming mostly from CKM parameters ( $\gamma, |V_{cb}|$ )

## E787/E949 (BNL), $K^+$ decays at rest



- [Phys.Rev.D 79, 092004(2009)]
- $\mathcal{B}_{\text{exp.}} = (1.73_{-1.05}^{+1.15}) \times 10^{-10}$

## NA62 (CERN), $K^+$ decays in flight



- [Phys.Lett.B 791, 156-166(2019)]
- $\mathcal{B}_{\text{exp.}} < 14 \times 10^{-10}$  @ 95% CL

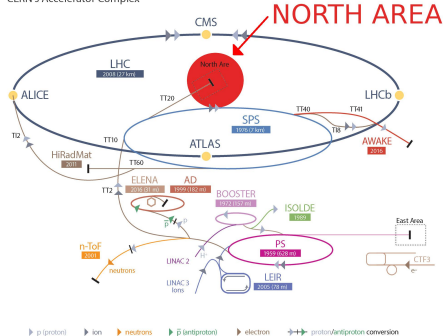
# NA62 Experiment at CERN

**MAIN GOAL:** measure  $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$  with precision better than 10%

Requirements:  $10^{13} K$  decays, Signal acceptance  $\mathcal{O}(10\%)$ , Bckg rejection  $\mathcal{O}(10^{12})$

Other physics program: LFV/LNV searches, Exotic searches, Rare decays,  $\pi^0$  decays

CERN's Accelerator Complex

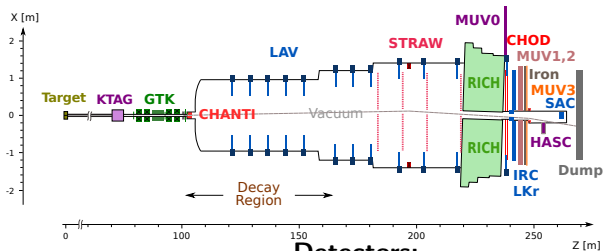


## NA62:

- 2014: Pilot run
- 2015: Commissioning run
- September 2016: full detector installation completed
- September-October 2016: first physics run
- **May-October 2017: second physics run**
- April-November 2018: third physics run

- ~200 participants, 31 institutes

# NA62 Beam and Detector



## Beam:

- Primary (SPS) proton beam with momentum 400 GeV/c
- $2 \times 10^{12}$  protons per 3.5s spill
- Beryllium target
- Secondary positive beam with momentum  $\sim 75$  GeV/c
- Secondary beam content:  
 $K^+$  (6%),  $\pi^+$  (70%), p (24%)
- 2017 Intensity: 450 MHz @ GTK3
- Kaon decay rate  $\sim 3$  MHz

## Detectors:

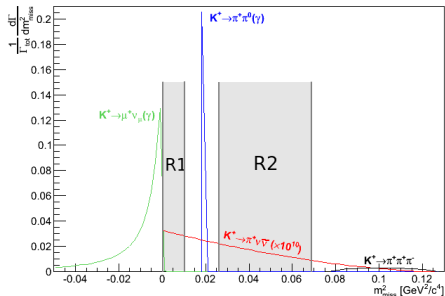
- KTAG - Cherenkov det. for  $K^+$  tagging
- GTK - beam spectrometer
- Decay region - 60 m long, in vacuum
- STRAW - downstream spectrometer
- CHOD - charged particle hodoscope
- LAV, IRC, SAC - photon veto
- RICH, LKr - Cherenkov detector and calorimeter for PID
- MUV3 - muon veto

[INST 12(2017) P05025]

# $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ Measurement Strategy

## Measurement strategy:

- $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  signature: one  $K^+$  in the initial state, one  $\pi^+$  and missing energy (neutrinos) in the final state
- Two kinematic signal regions
- Blind analysis
- Trigger streams (HW+SW): PNN and Control (minimum bias)



True  $m_{\text{miss}}^2$  computed under the hypothesis that the charged particle is  $\pi^+$ .

## Main background processes:

Process	BR
$K^+ \rightarrow \mu^+ \nu(\gamma)$	0.6356
$K^+ \rightarrow \pi^+ \pi^0(\gamma)$	0.2067
$K^+ \rightarrow \pi^+ \pi^+ \pi^-$	0.0558

## Keystones:

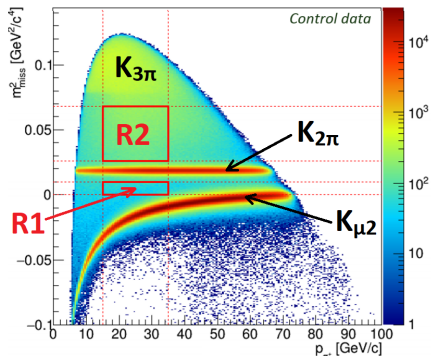
- $\mathcal{O}(100 \text{ ps})$  timing between subdetectors
- $\sim \mathcal{O}(10^3)$  kinematic background suppression
- PID background suppression ( $\mu^+$  and  $\pi^0$ )  $> 10^7$

## Main kinematic variable:

$$m_{\text{miss}}^2 = (P_{K^+} - P_{\pi^+})^2$$

## Signal selection:

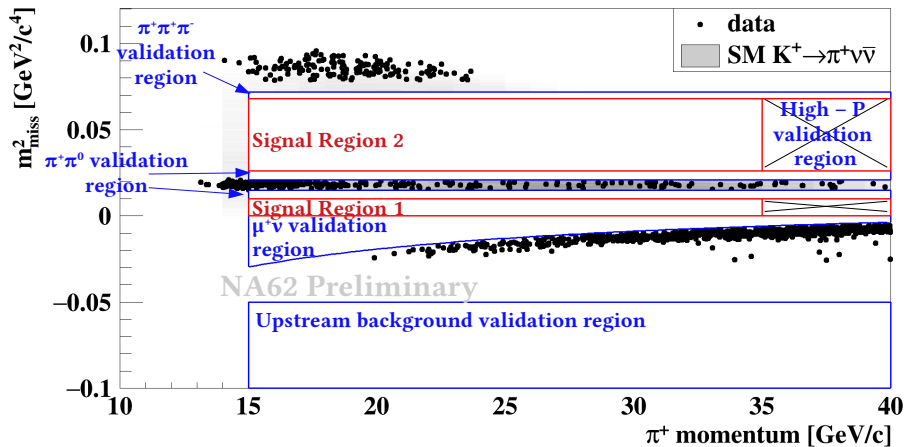
- Single track topology
- $K^+$  and  $\pi^+$  momentum reconstruction (GTK, STRAW)
- $K^+ - \pi^+$  matching
- $K^+$  decays in the fiducial region
- $\pi^+$  identification ( $\epsilon_{\pi^+} \sim 64\%$ )
- $\gamma$  rejection
- Multi-track event rejection
- Upstream background suppression
- $15 \text{ GeV} < P_{\pi^+} < 35 \text{ GeV}$
- Signal regions defined by  $m_{\text{miss}}^2(\pi^+)$



Reconstructed  $m_{\text{miss}}^2$  (assuming  $\pi^+$  mass) as a function of the track momentum for control data before PID and  $\gamma$  and multi-track rejection. [Phys.Lett.B 791, 156-166(2019)]



# Data After Signal Selection (2017 Dataset)



- Validation regions dedicated to background validation
- Signal and validation regions blinded

# Single Event Sensitivity (SES) (2017 Dataset)

$$N_{\pi\nu\nu}^{\text{exp}} \approx N_{\pi\pi} \epsilon_{\text{trig}} \epsilon_{RV} \frac{A_{\pi\nu\nu}}{A_{\pi\pi}} \frac{\mathcal{B}(\pi\nu\nu)}{\mathcal{B}(\pi\pi)} \quad \Rightarrow \quad \text{SES} = \frac{\mathcal{B}(\pi\nu\nu)}{N_{\pi\nu\nu}^{\text{exp}}}$$

- $N_{\pi\nu\nu}^{\text{exp}}$  = expected number of  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  events
- $N_{\pi\pi}$  = Number of  $\pi^+ \pi^0$  events from Control sample with  $\pi\nu\nu$ -like selection without  $\gamma$ /multiplicity rejection
- $\epsilon_{\text{trig}}$  = efficiency of PNN trigger
- $\epsilon_{RV}$  =  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  loss due to  $\gamma$ /multi-track rejection bc of random activity
- $A_{\pi\nu\nu, \pi\pi}$  = MC acceptances for  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  ( $\sim 3\%$ ) and  $K^+ \rightarrow \pi^+ \pi^0$  ( $\sim 8.5\%$ )
- $\mathcal{B}(\pi\pi)$  = PDG branching ratio for  $K^+ \rightarrow \pi^+ \pi^0$
- $\mathcal{B}(\pi\nu\nu)$  = SM branching ratio for  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$
  
- Ratio of acceptances allows for cancellation of systematic effects
- Computation in bins of  $\pi^+$  momentum and instantaneous beam intensity

Measured single event sensitivity:

$$\text{SES} = (3.89 \pm 0.21) \times 10^{-11} \quad (\text{Preliminary})$$

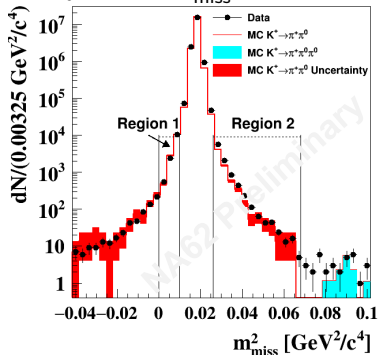
Expected number of  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  events in both signal regions combined:

$$N_{\pi\nu\nu}^{\text{exp}} = 2.16 \pm 0.12 \pm 0.26_{\text{ext}} \quad (\text{Preliminary})$$

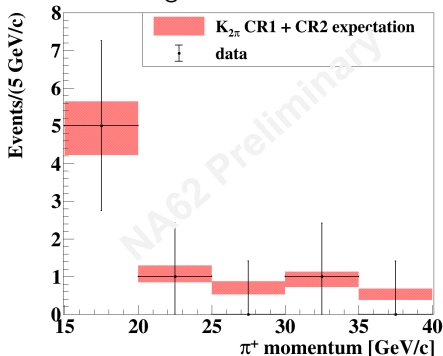
External error coming from  $\mathcal{B}(\pi\nu\nu)$ .

# $K^+ \rightarrow \pi^+ \pi^0$ Background

$K^+ \rightarrow \pi^+ \pi^0$  Control data used to study tails of  $m_{\text{miss}}^2$  distribution



Expected and observed  $K^+ \rightarrow \pi^+ \pi^0$  bckg in validation regions after PNN selection



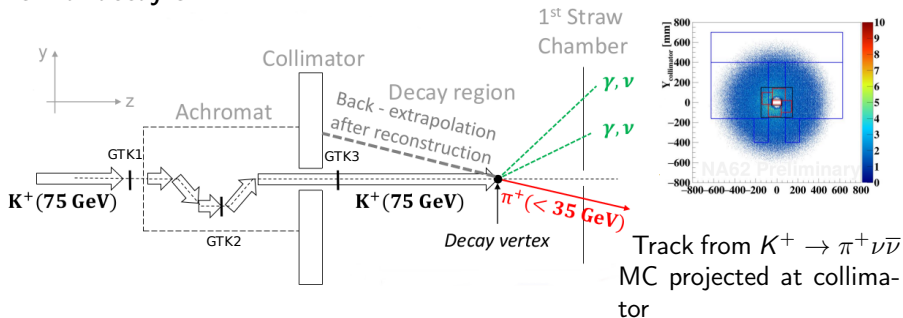
$$N_{\pi\pi}^{\text{exp}}(\text{region}) = N(\pi^+ \pi^0) \cdot f^{\text{kin}}(\text{region})$$

- $N_{\pi\pi}^{\text{exp}}(\text{region}) =$  Expected  $K^+ \rightarrow \pi^+ \pi^0$  events in signal region after PNN selection
- $N(\pi^+ \pi^0) =$  Data in  $\pi^+ \pi^0$  peak after PNN selection
- $f^{\text{kin}}(\text{region}) =$  Fraction of  $K^+ \rightarrow \pi^+ \pi^0$  in signal region measured on Control data

By-product:  $\mathcal{B}(\pi^0 \rightarrow \text{invisible}) < 4.4 \times 10^{-9}$  90% CL

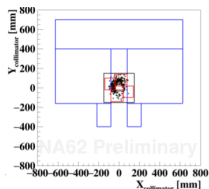
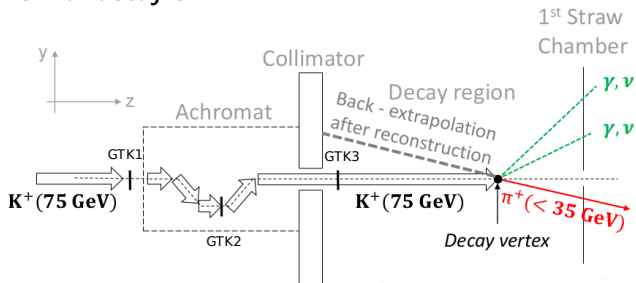
# Upstream Background

## Normal decay of $K^+$ :



# Upstream Background

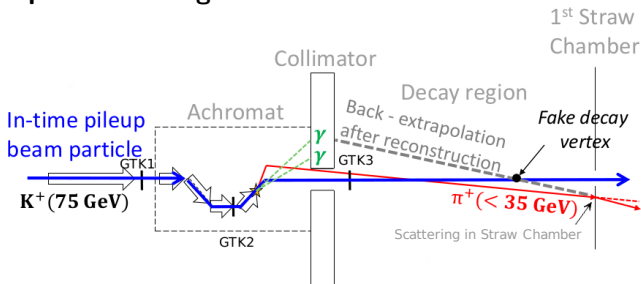
## Normal decay of $K^+$ :



## Upstream bckg:

- $K^+$  decays/interacts in the achromat
- Secondary  $\pi^+$  downstream
- Beam elements block additional particles
- $\pi^+$  scattering in Straw Chamber 1
- Pileup beam particle tagged as  $K^+$

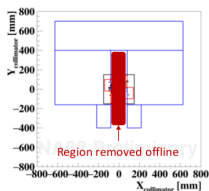
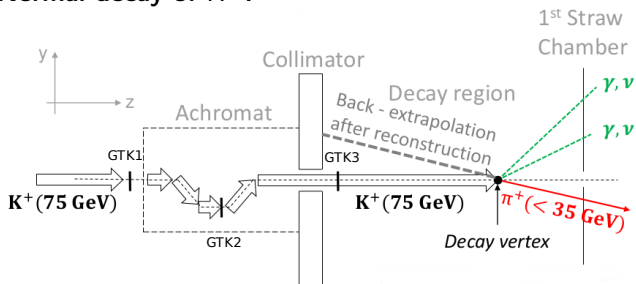
## Upstream Background:



Sketches from G. Ruggiero

# Upstream Background

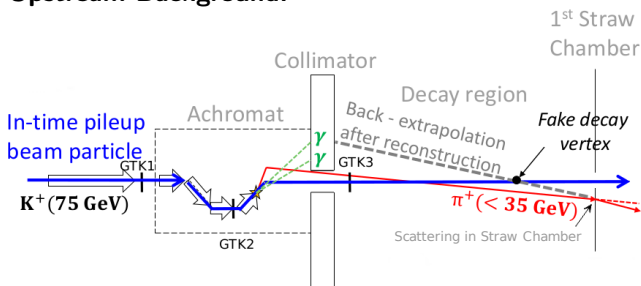
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## Upstream Background:



Sketches from G. Ruggiero

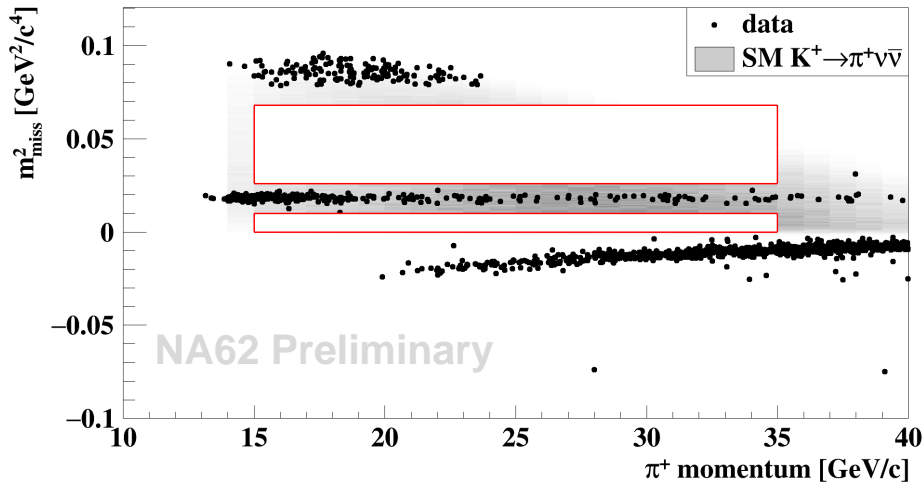
# Background Summary (2017 Dataset)

Expected number of events in both signal regions combined (Preliminary):

Process	Expected events
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$ (SM)	$2.16 \pm 0.12_{stat} \pm 0.26_{ext}$
$K^+ \rightarrow \pi^+ \pi^0(\gamma)$ IB	$0.29 \pm 0.03_{stat} \pm 0.03_{syst}$
$K^+ \rightarrow \mu^+ \nu_\mu(\gamma)$ IB	$0.11 \pm 0.02_{stat} \pm 0.03_{syst}$
$K^+ \rightarrow \mu^+ \nu_\mu(\mu^+ \rightarrow e^+ \text{decay})$	$0.04 \pm 0.02_{syst}$
$K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$	$0.12 \pm 0.05_{stat} \pm 0.03_{syst}$
$K^+ \rightarrow \pi^+ \pi^- \pi^+$	$0.02 \pm 0.02_{syst}$
$K^+ \rightarrow \pi^+ \gamma \gamma$	$0.005 \pm 0.005_{syst}$
$K^+ \rightarrow l^+ \pi^0 \nu_l$	negligible
Upstream background	$0.9 \pm 0.2_{stat} \pm 0.2_{syst}$
Total background	$1.5 \pm 0.2_{stat} \pm 0.2_{syst}$

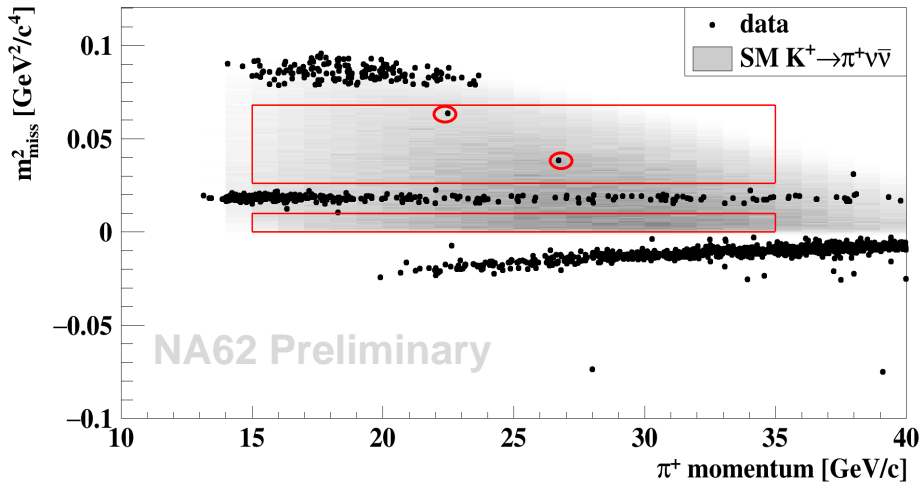
$K^+ \rightarrow \pi^+ \pi^0(\gamma)$ ,  $K^+ \rightarrow \mu^+ \nu(\gamma)$ ,  $K^+ \rightarrow \pi^+ \pi^- \pi^+$  and upstream backgrounds estimated from Control data and validated using the validation regions. Other backgrounds estimated from the MC simulations validated on data.

# Opening the Boxes (2017 Dataset)





# Opening the Boxes (2017 Dataset)



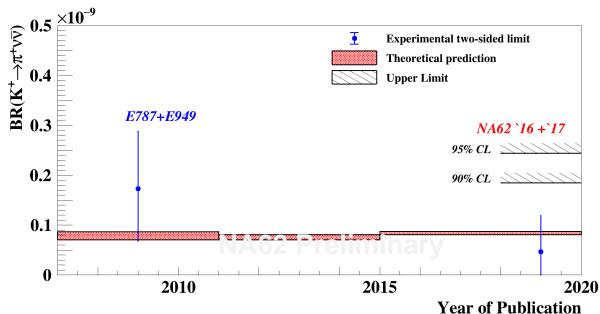
# Preliminary Results from the 2016+2017 Datasets

Single event sensitivity	$(0.346 \pm 0.017) \times 10^{-10}$
Expected number of background events	$1.65 \pm 0.31$
<b>Observed number of events</b>	<b>3</b>

## Observed upper limits:

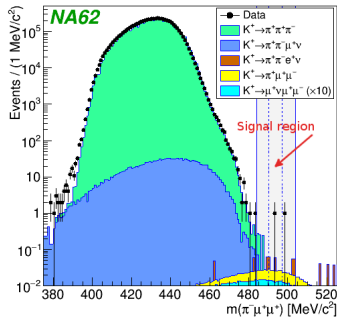
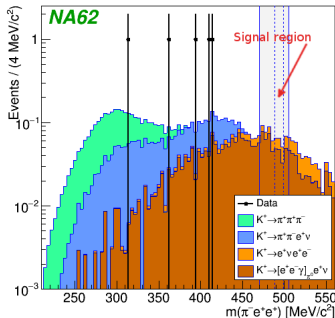
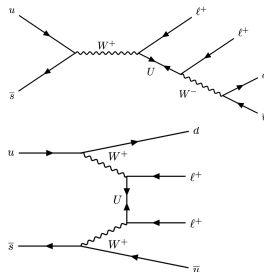
- $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) < 1.85 \times 10^{-10}$  @ 90% CL (Preliminary)
- $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) < 2.44 \times 10^{-10}$  @ 95% CL (Preliminary)

**Grossman-Nir limit:**  $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 8.14 \times 10^{-10}$  @ 90% CL (Preliminary)



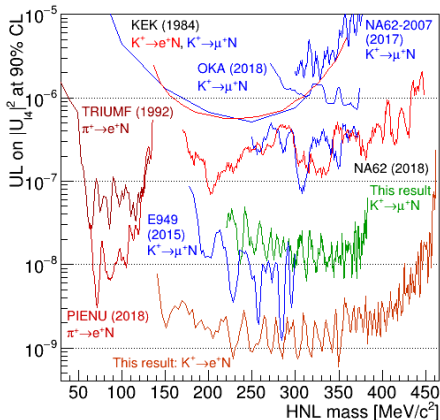
# Forbidden Decays (LNV) at NA62

- Study of  $K^+ \rightarrow \pi^- \mu^+ \mu^+$  and  $K^+ \rightarrow \pi^- e^+ e^+$  ( $\Delta L_I = 2$ )
- Processes in BSM with massive Majorana neutrinos  $U$  [JHEP 0905 (2009) 030], [Phys. Lett. B491(2000) 285]
- Signal selection using  $|M(\pi^- l^+ l^+) - M(K^+)|$  and PID
- 2017 results [Phys. Lett. B797 (2019) 134794]
  - **improvement by factor 2-3 wrt previous result:**
    - $B(K^+ \rightarrow \pi^- e^+ e^+) < 2.2 \times 10^{-10}$  @ 90% CL
    - $B(K^+ \rightarrow \pi^- \mu^+ \mu^+) < 4.2 \times 10^{-11}$  @ 90% CL
- Full data-sample (2016-2018):  $3 \times$  more statistics



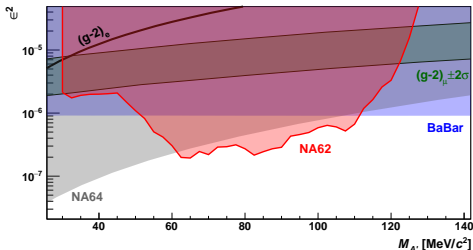
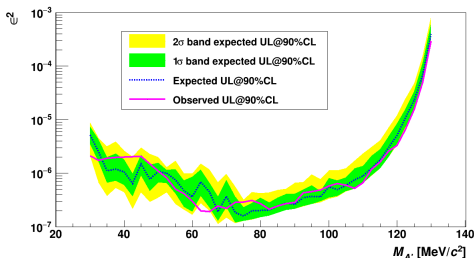
# Hidden Sector Searches: Heavy Neutral Leptons (HNL)

- Study of  $K^+ \rightarrow l^+ N$  ( $l = e, \mu$ ) – production search
- $\nu$ MSM – mixing of three massive sterile neutrinos (HNL) with the three ordinary active neutrinos – fermion portal to a hidden sector
- Kinematic variable: squared missing mass  $m_{\text{miss}}^2 = (P_K - P_l)^2$
- Signal: a spike above continuous missing mass spectrum
- Mass scan in the range of 141–462 (220–383) MeV/ $c^2$  in the  $e^+$  ( $\mu^+$ ) case
- Last published results: 2015 dataset [Phys. Lett. B778 (2018)]
- Preliminary 2016+2017 results  $\rightarrow$  **new upper limit on mixing parameter  $|U_{l4}|^2$**  [Goudzovski, KAON 2019]
- Improvement by less than a factor of 2 with full dataset (2016-2018)
- Intention to collect data in beam-dump mode in 2021-2023 for HNL decay (and other) searches



# Hidden Sector Searches: Dark Photon $A'$

- Search for dark photon using  $K^+ \rightarrow \pi^+ \pi^0$ ,  $\pi^0 \rightarrow A' \gamma$ , decay chain with  $A'$  decaying to invisibles – vector portal to a hidden sector
- SM extension – new vector field  $A'$  mixing with the SM  $\gamma$
- Signal signature:  $\pi^0$  decay, one  $\gamma$  and missing energy, no additional activity
- Kinematic variable: squared missing mass  $m_{\text{miss}}^2 = (P_K - P_{\pi^+} - P_\gamma)^2$
- Signal: a spike above continuous missing mass spectrum
- Mass scan in range 30–130 MeV/ $c^2$  of  $M_{A'}$
- 2016 results  $\rightarrow$  no statistically significant excess identified  $\rightarrow$  **new upper limit on  $\epsilon^2$  coupling of  $A'$  to  $\gamma$**  [JHEP 05 (2019) 182]
- Expected  $\sim 100\times$  more statistics from full 2016–2018 dataset



## All physics analyses ongoing (2017 and/or 2018 datasets):

- 2018  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  dataset
  - Analysis ongoing
  - $2\times$  more data than in 2017
  - Optimization studies to increase signal efficiency
  - New collimator installed – increased signal acceptance

## NA62 After 2021 (LHC Run 3):

- Plans to modify the beamline setup in order to strongly suppress upstream background
- Add 4<sup>th</sup> GTK station to reduce  $K^+ - \pi^+$  mistagging probability
- Plans for new vetoes in the beamline to detect extra particles
- Plans for data-taking:
  - $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  at nominal beam intensity
  - Rare decays + Exotics
  - NA62++:
    - Beam dump experiment (closed TAX) with  $10^{18}$  POT
    - Decays of exotic particles
    - New ANTI0 detector under construction to veto muons produced in the TAX
    - Studies to increase proton beam intensity by 20-50% above nominal

**NA62 has initiated feasibility study for running at considerably higher intensity...**

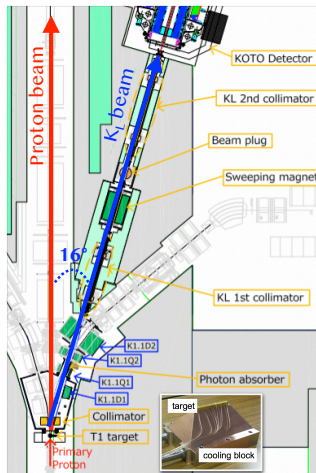
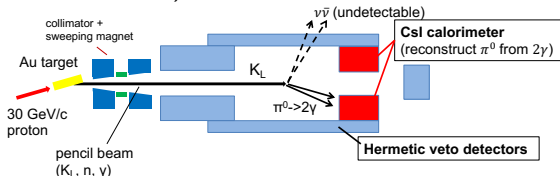
- Physics goals:
  - NA62 $\times$ 4 – improve precision on  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$
  - KLEVER – measure  $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$ , complementary to NA62 and KOTO
- 4 $\times$  higher intensity in  $K^+$  mode, 6 $\times$  higher intensity in  $K_L$  mode
  - Challenging for tracking and beam detectors ( $K^+$  mode)
  - Challenging for calorimetry and photon detection ( $K_L$  mode)
- Large commonality in terms of upgrades required (hardware, readout)

- **Search for new physics with CP-violating (and highly suppressed FCNC) process  $K_L \rightarrow \pi^0 \nu \bar{\nu}$**
- SM prediction for branching ratio is  $\mathcal{B}_{\text{SM}} = (3.0 \pm 0.3) \times 10^{-11}$   
[Buras.et.al., JHEP11(2015) 033]
- $\sim 50$  people from 16 institutes
- First physics run in 2013
- **2015 dataset:**
  - Results published in Physical Review Letters [PRL.122.021802 (2019)]
  - Measured SES:  $(1.30 \pm 0.01_{\text{stat}} \pm 0.14_{\text{syst}}) \times 10^{-9}$
  - Expected number of background events in the signal region:  $0.42 \pm 0.18$
  - **No signal candidate events were observed**
  - **New upper limit for  $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 3.0 \times 10^{-9}$  at 90% C.L.**  
→ **10x improvement wrt prev. limit from KEK E391a** [Phys.Rev.D 81, 072004, 2010]
- Current status of 2016-2018 data analysis presented at KAON 2019
- Future – major upgrades planned for KOTO Step-2 [Nomura, KAON 2019]



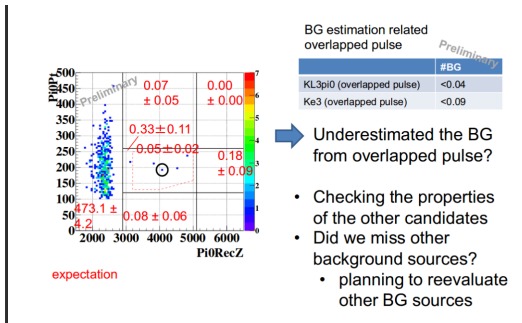
# $K_L \rightarrow \pi^0 \nu \bar{\nu}$ at KOTO, J-PARC Center, Japan

- 30 GeV/c proton beam hitting a gold target
- Secondary neutral beam (neutrons, photons,  $K_L$ ) produced at an angle and transported to the decay region via neutral beamline
- Peak  $K_L$  momentum 1.4 GeV/c
- Calorimeter and hermetic veto counters for neutral and charged particles around decay region in vacuum
- **Signature: two photons + missing energy**
- Main sources of background: charged ( $K_L \rightarrow \pi^\pm e^\pm \nu$ ,  $K_L \rightarrow \pi^\pm \mu^\pm \nu$ ,  $K_L \rightarrow \pi^+ \pi^- \pi^0$ ,  $K_L \rightarrow \pi^+ \pi^-$ ), neutral ( $K_L \rightarrow \pi^0 \pi^0 \pi^0$ ,  $K_L \rightarrow \gamma \gamma$ ,  $K_L \rightarrow \pi^0 \pi^0$ )



## 2016–2018 dataset:

- 1.4× more statistics
- New veto counters
- **Current status presented at KAON 2019** →  
[Shinohara, KAON 2019]:
  - Measured SES =  $6.9 \times 10^{-10}$
  - Expected number of background events in the signal region:  $0.05 \pm 0.02$
  - **4 events found in signal region**

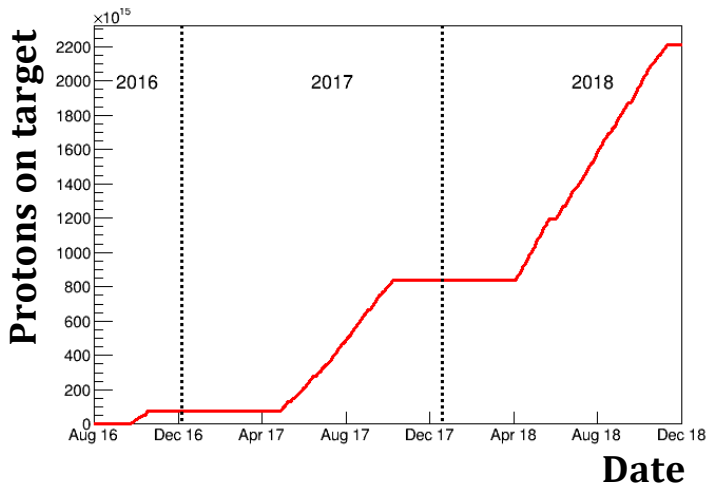


**Stay tuned...**

**More results from Kaon experiments coming soon...**

For more Kaon related searches see presentations at KAON 2019 [KAON 2019, Perugia]

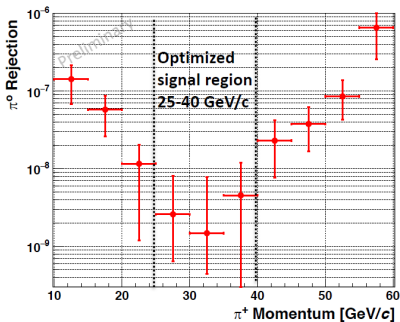
- Intensity:
  - 2016: 40% of nominal
  - 2017: 55% of nominal
  - 2018: 65% of nominal
  
- Kaon decays:
  - 2017:  $2 \times 10^{12}$   $K^+$  decays
  - 2016+2017+2018:  $6 \times 10^{12}$   $K^+$  decays
  
- 2017 signal acceptance: 1.34% (including random veto, trigger and total detector efficiency)
  
- Rolke-Lopez 68% confidence interval:  $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (0.47 \pm_{-0.47}^{+0.72}) \times 10^{-10}$   
(for comparison with BNL)



# $\pi^0$ rejection and search for $\pi^0 \rightarrow$ invisible

A-priori evaluation of  $\pi^0$  rejection in  $K^+ \rightarrow \pi^+\pi^0$  ( $0.015 < m_{miss}^2 < 0.021 \text{ GeV}^2/c^4$ )

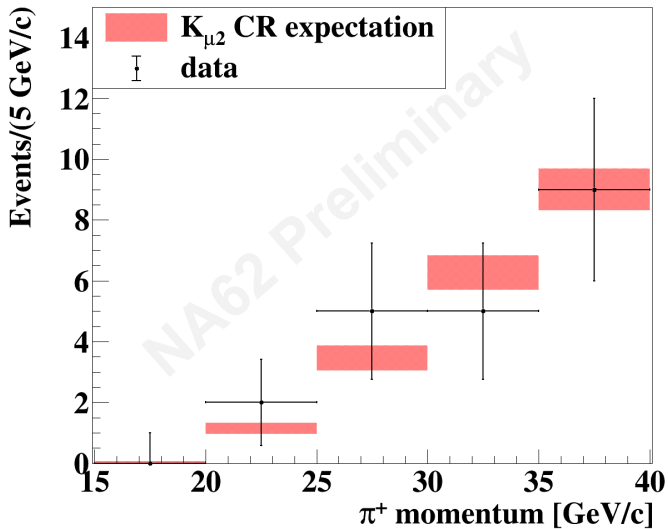
- Same selection, and trigger stream as  $K^+ \rightarrow \pi^+\nu\bar{\nu}$ , about 1/3 of the data used for  $\pi\nu\nu$
- Single- $\gamma$  detection efficiency from data minimum-bias  $K^+ \rightarrow \pi^+\pi^0$  (Tag & Probe)
- $\pi^0$  rejection evaluated from convolution with MC  $K^+ \rightarrow \pi^+\pi^0(\gamma)$
- Validation: side-bands with expected rejection  $\mathcal{O}(10^{-7})$  where  $\pi^0 \rightarrow$  invisible excluded [E949, PRD72 (2005)]
- $\pi^0$  rejection expected:  $(2.8^{+5.0}_{-2.1}) \times 10^{-9}$  ( $\pi^+$  momentum 25-40 GeV/c)



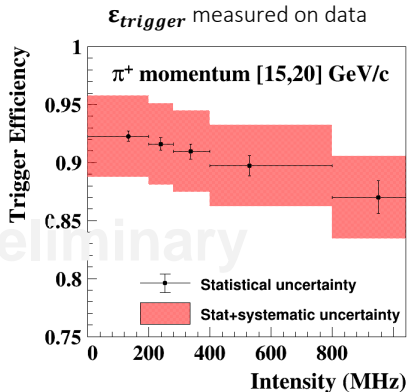
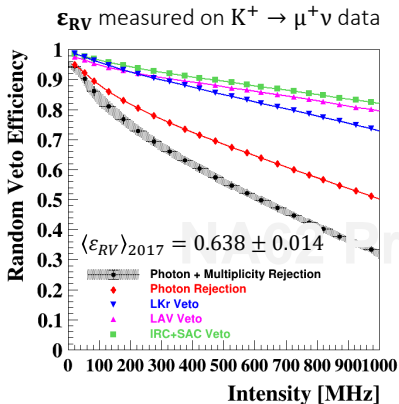
## Result

- $\text{BR}(\pi^0 \rightarrow \text{invisible})$  normalized to  $\pi^0 \rightarrow \gamma\gamma$
- Background expected:  $10^{+22}_{-8}$  ( $K^+ \rightarrow \pi^+\pi^0$ )
- Events observed: 12

$\text{BR}(\pi^0 \rightarrow \text{invisible}) < 4.4 \times 10^{-9}$  @ 90% CL  
UL 60 times stronger than past measurement



# $\pi\nu\nu$ Single Event Sensitivity



- Intensity measured event-by-event using Gigatracker time sidebands



## $\pi\nu\nu$ S.E.S: Results

- Integrated over beam intensity and  $\pi^+$  momentum

$$S.E.S. = (0.389 \pm 0.021) \times 10^{-10}$$

$$N_{\pi\nu\nu}^{exp} = 2.16 \pm 0.12 \pm 0.26_{ext}$$

- Error budget (S.E.S.)

Source	Uncertainty $\times 10^{-10}$
L0 trigger	$\pm 0.015$
Acceptance	$\pm 0.012$
Random veto	$\pm 0.008$
L1 trigger	$\pm 0.003$
Normalization background	negligible

- External error on  $N_{\pi\nu\nu}^{exp}$  from  $Br(\pi\nu\nu) = (0.84 \pm 0.10) \times 10^{-10}$