

The Neutrino Magnetic Moment Portal: Cosmology, Astrophysics, and Direct Detection

Admir Greljo

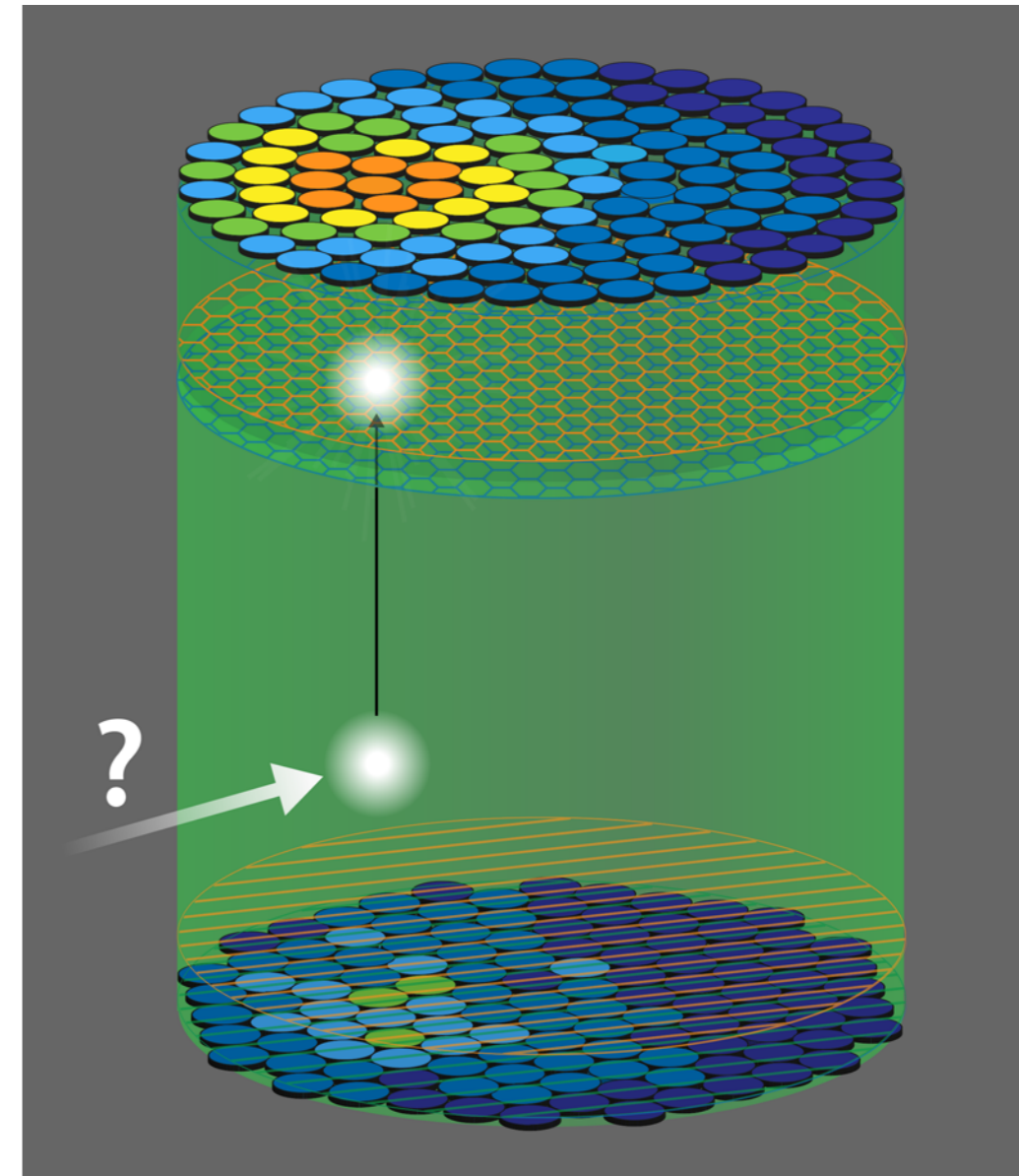
*Thanks to Toby Opferkuch for many slides.

IJS, 15.10.2020

Motivation

Dark matter direct detection experiments

- Underground laboratories waiting for the dark matter hits
- Electronic & nuclear recoils
prompt scintillation (S1) and delayed electroluminescence (S2)
- Challenge: Low background rate, large target mass, and low energy threshold
- Quietest and darkest laboratory environments



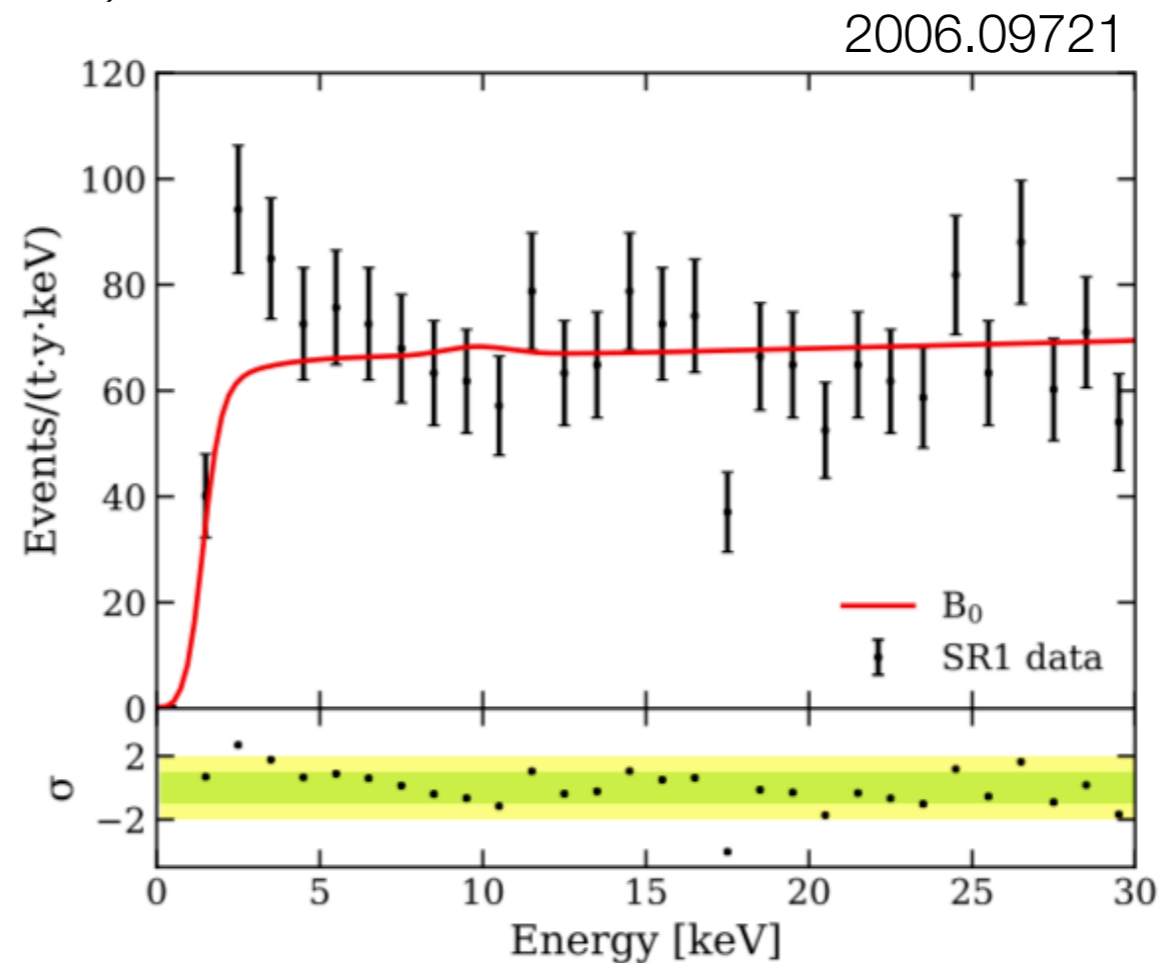
XENON1T; adapted by APS/Alan Stonebraker

Enormous tank of purified liquid xenon surrounded by photomultiplier tubes.

Motivation

Dark matter direct detection experiments

- XENONIT **3.3 sigma** anomaly:
 - Large e/γ ratio (S2/S1) = Electronic recoils

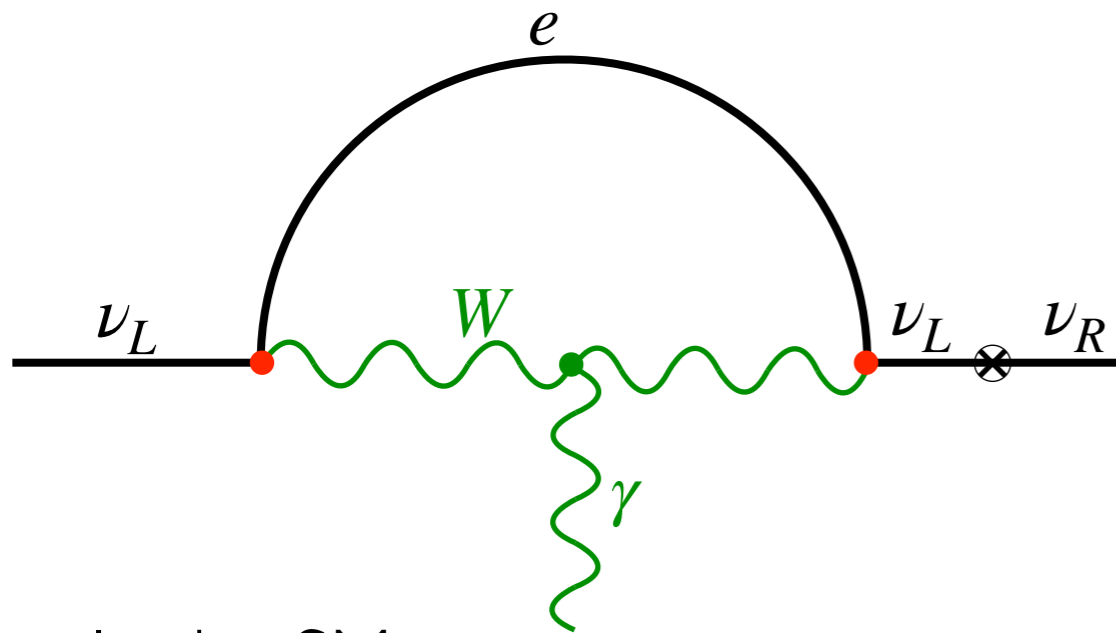


- Fluctuation, tritium, **new physics**?!

Neutrino magnetic moment

XENON1T, 2006.09721

$$\mathcal{L}_\mu = \frac{\mu_\nu^{\alpha\beta}}{2} F_{\mu\nu} \bar{\nu}_L^\alpha \sigma^{\mu\nu} \nu_R^\beta + \text{h.c.}$$



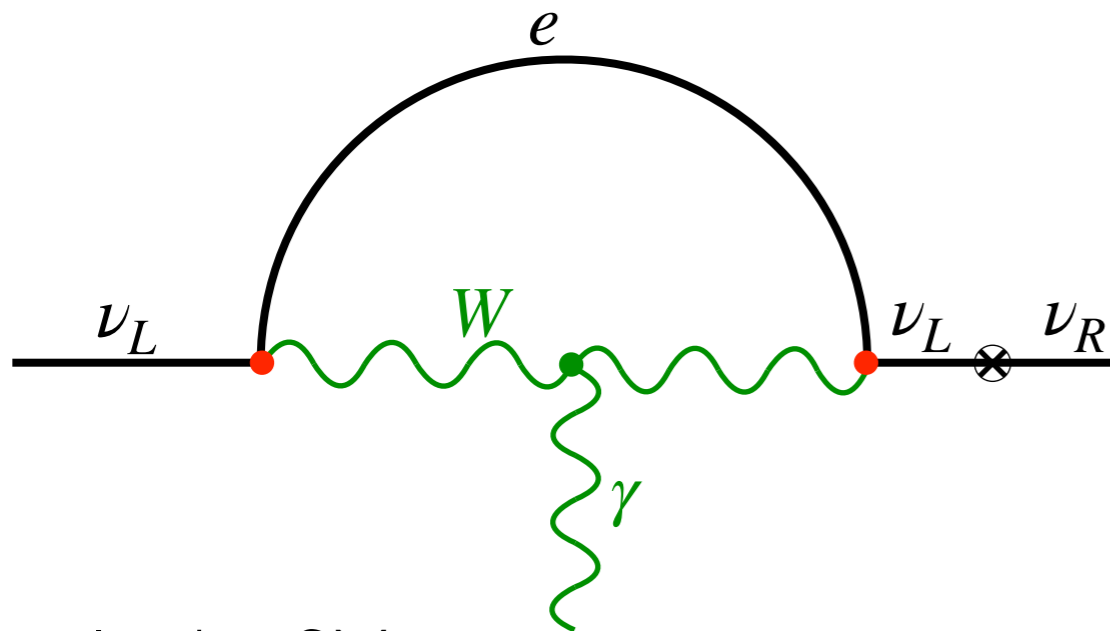
In the SM

$$\mu_\nu^{SM} \sim 10^{-20} \mu_B$$

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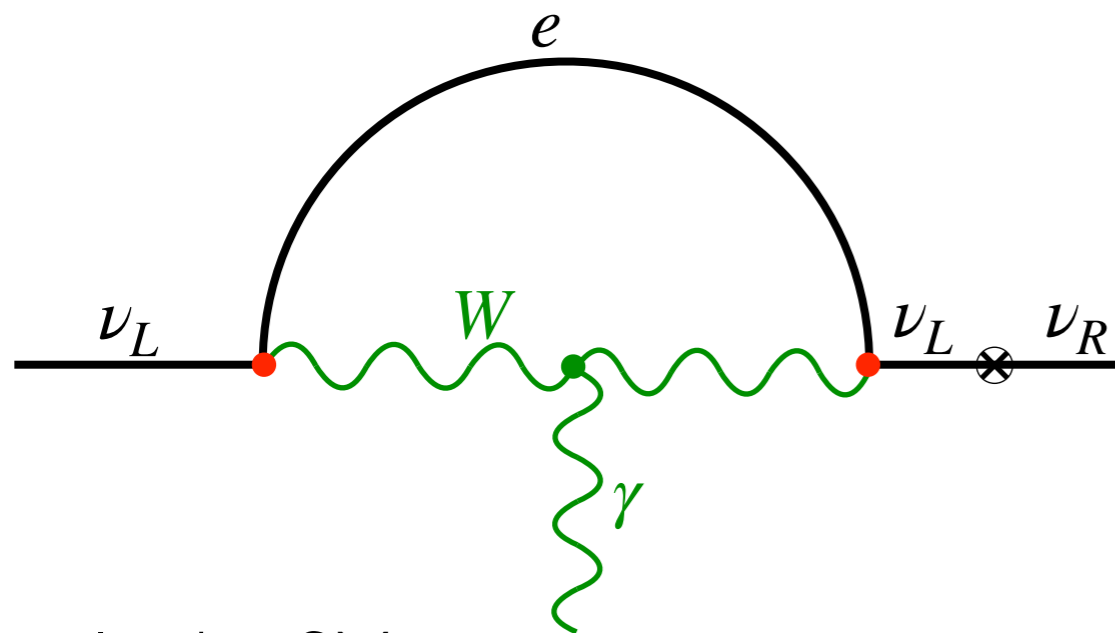
Neutrino solution

- The source of incoming particles is known.
- However, the expected signal is tiny in the SM (the neutrino floor).
- How to lift up the neutrino floor?
 - * Modifying neutrino properties

Neutrino magnetic moment

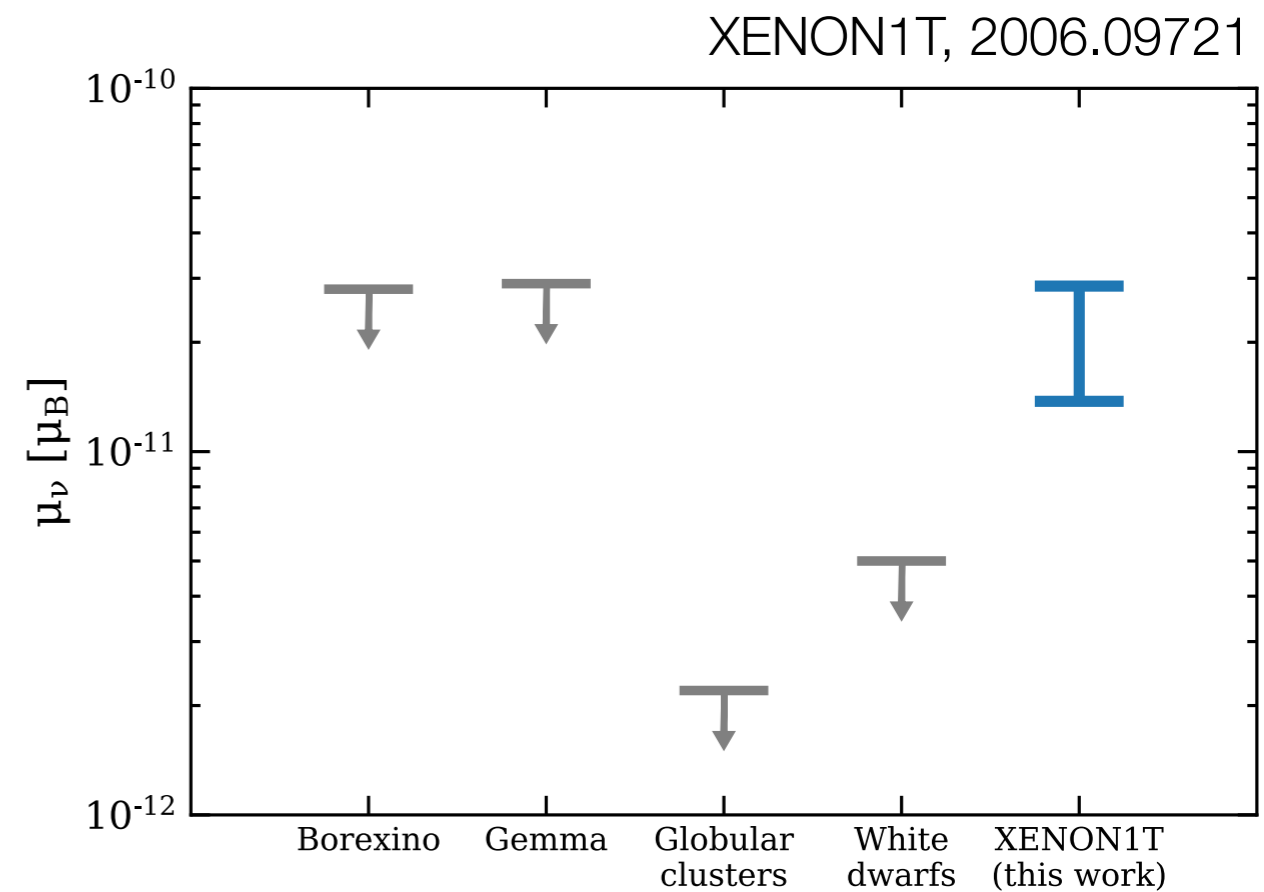
XENON1T, 2006.09721

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In the SM

$$\mu_\nu^{SM} \sim 10^{-20} \mu_B$$



- *Magnetic moments of active flavours ruled out by stellar cooling constraints*

Vedran Brdar (MPIK Heidelberg), Admir Greljo, Joachim Kopp, Toby Opferkuch (CERN)

We wanted to fix the problem; ended up answering some interesting questions in

■ ***Neutrino physics***

Questions

- What dark matter direct detection experiments tell us about the electromagnetic properties of neutrinos?

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- Is it possible to observe the signal in present/future experiments, given complementary constraints from astrophysics and cosmology?

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- Is it possible to observe the signal in present/future experiments, given complementary constraints from astrophysics and cosmology?
- Is there a viable model which predicts the observable signal, while still consistent with known neutrino masses and other phenomenology?

Transition magnetic moment

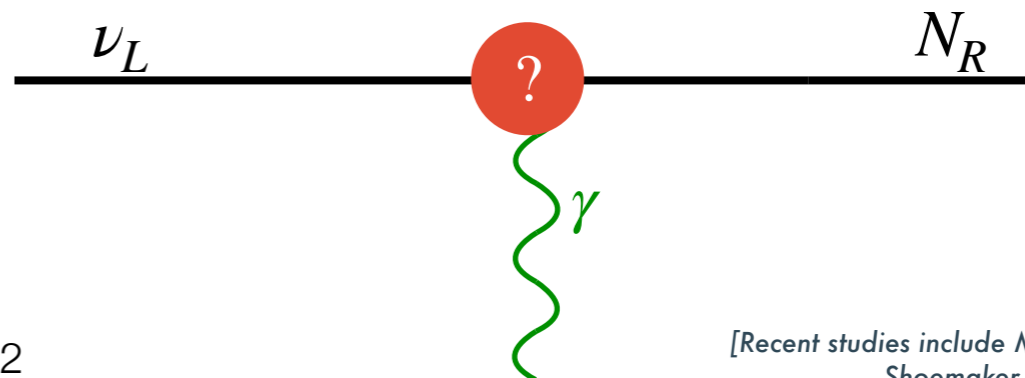
- Problem
Magnetic moments of active flavours ruled out by stellar cooling constraints

Transition magnetic moment

- Problem
Magnetic moments of active flavours ruled out by stellar cooling constraints
- Idea

- Heavy sterile neutrino N_R with mass M_N

$$\mathcal{L}_\mu = \frac{\mu_\nu^\alpha}{2} F_{\mu\nu} \bar{\nu}_L^\alpha \sigma^{\mu\nu} N_R + \text{h.c.},$$



Transition magnetic moment

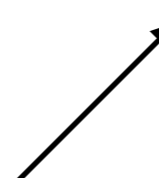
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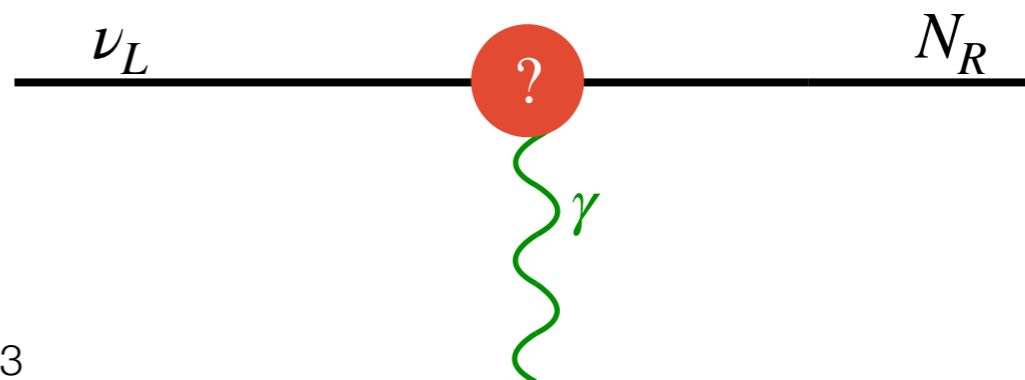
New sterile neutrino

1) Heavy enough to avoid cooling

$$\gamma^* \longrightarrow \nu_L + N \quad m_{\gamma^*} \propto T_{\text{star}}$$


- Heavy sterile neutrino N_R with mass M_N

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Transition magnetic moment

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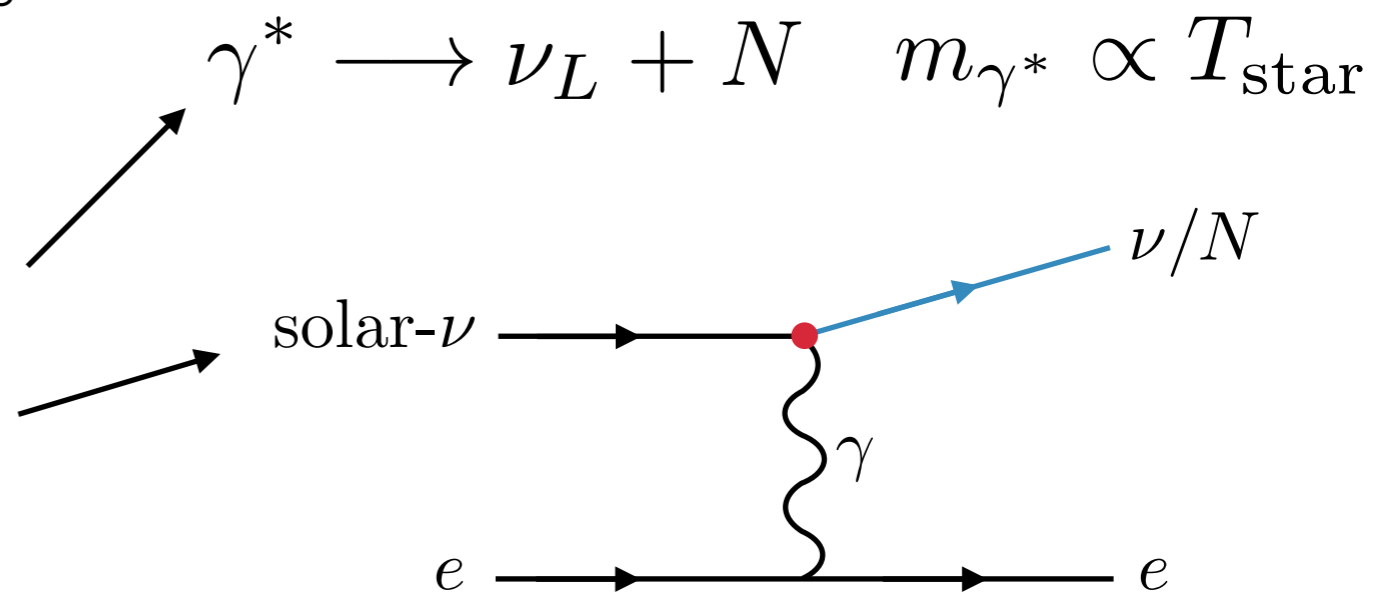
Magnetic moments of active flavours ruled out by stellar cooling constraints

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New sterile neutrino

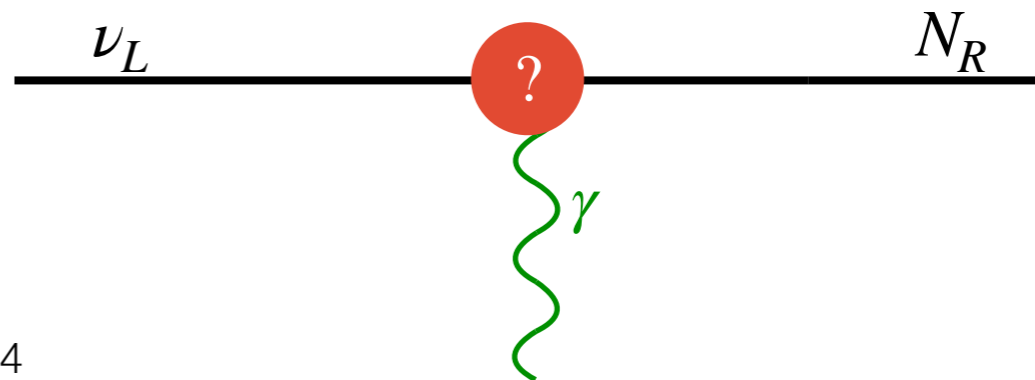
1) Heavy enough to avoid cooling

2) Light enough to be produced in the up-scattering



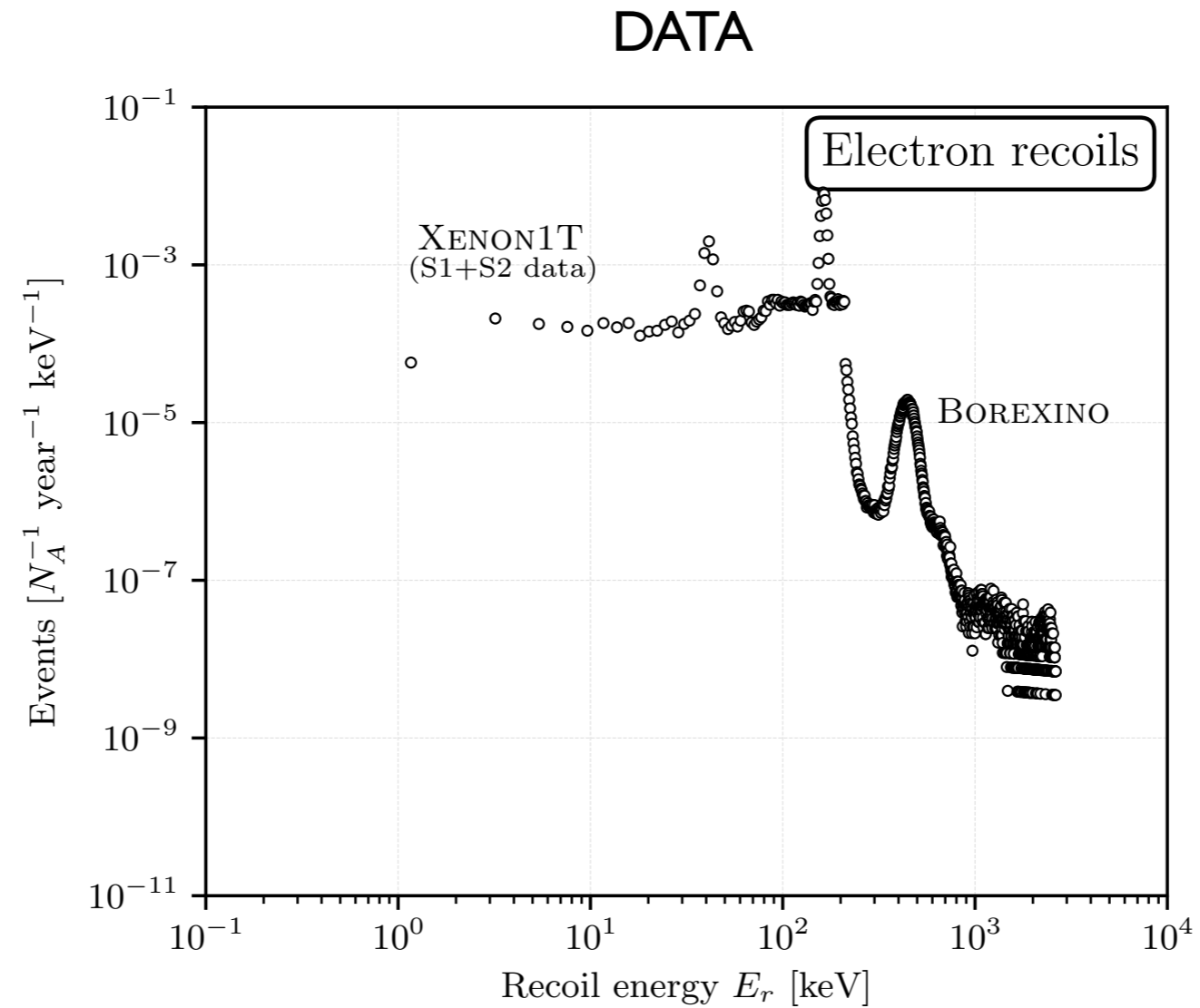
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$$\mathcal{L}_\mu = \frac{\mu_\nu^\alpha}{2} F_{\mu\nu} \bar{\nu}_L^\alpha \sigma^{\mu\nu} N_R + \text{h.c.},$$



***Neutrino (up -)scattering in
the detector***

Electronic recoil signal

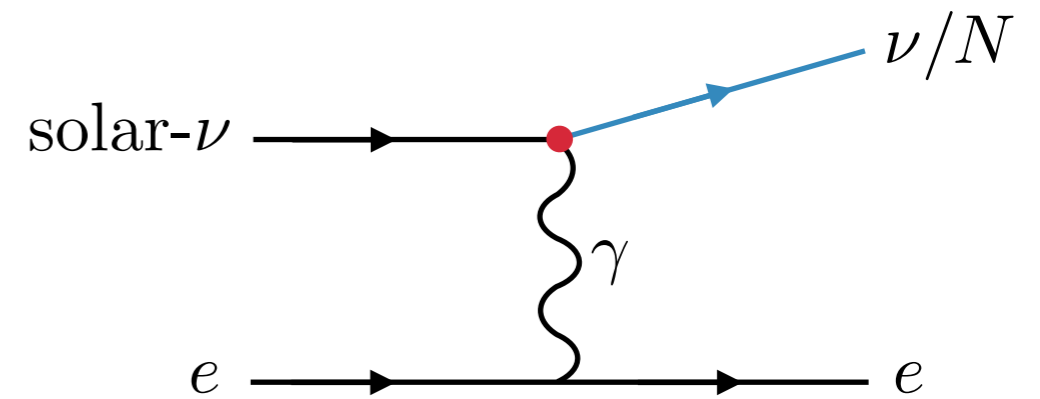


We consider the entire measured range

Electronic recoil signal

Differential event rate:

$$\frac{\Delta R}{\Delta E_r} = N_T \epsilon(E_r) \int_{E_\nu^a}^{E_\nu^b} dE_\nu \frac{d\Phi}{dE_\nu} \frac{d\sigma}{dE_r}$$



[Pospelov 1103.3261, Harnik et. al 1202.6073]

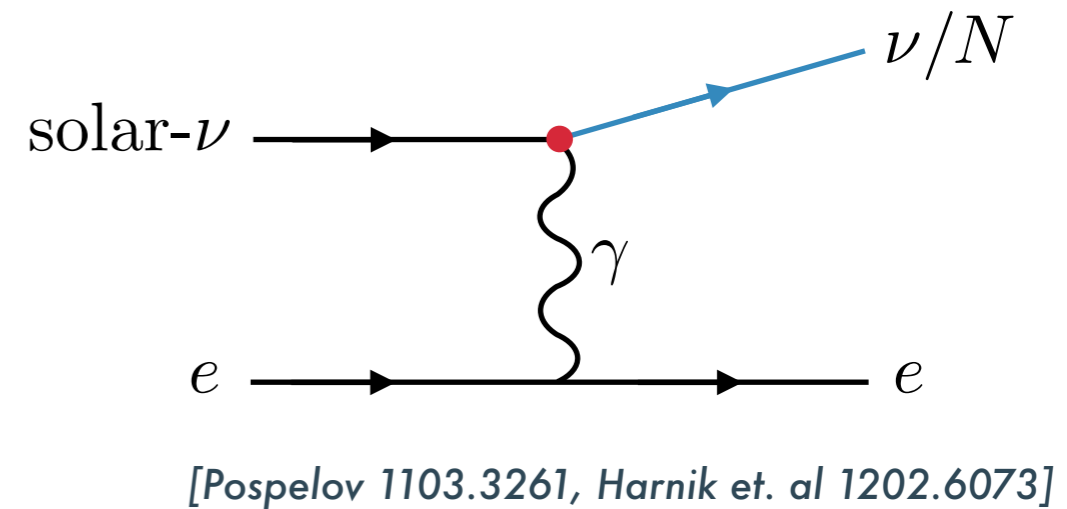
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- Scattering targets

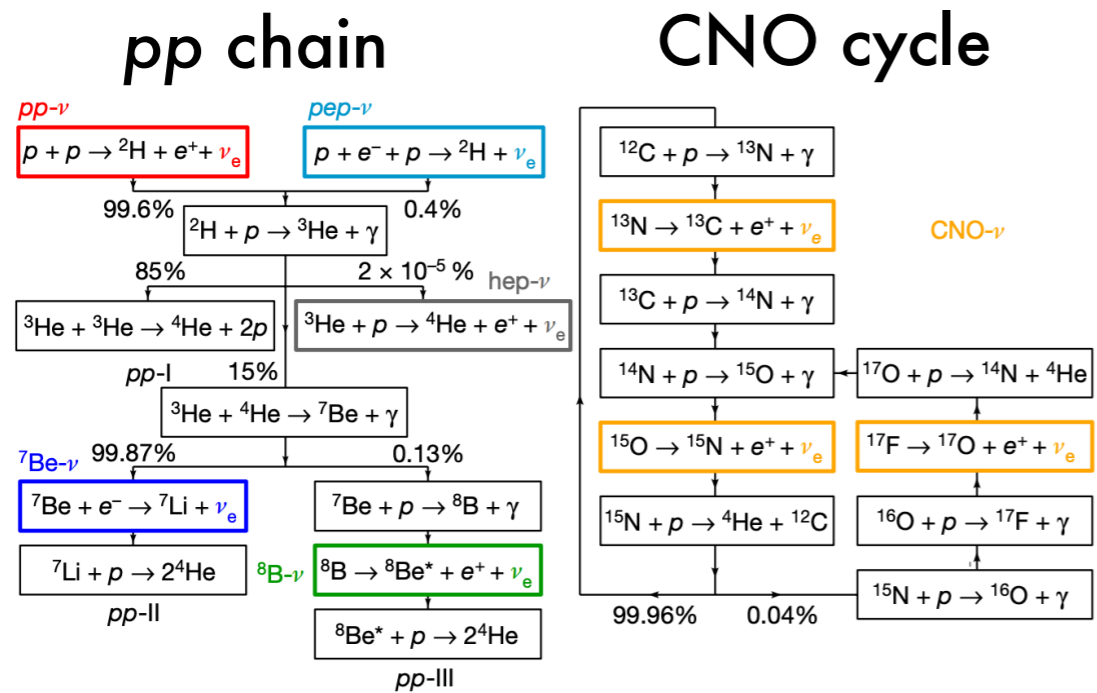
- Solar neutrino flux



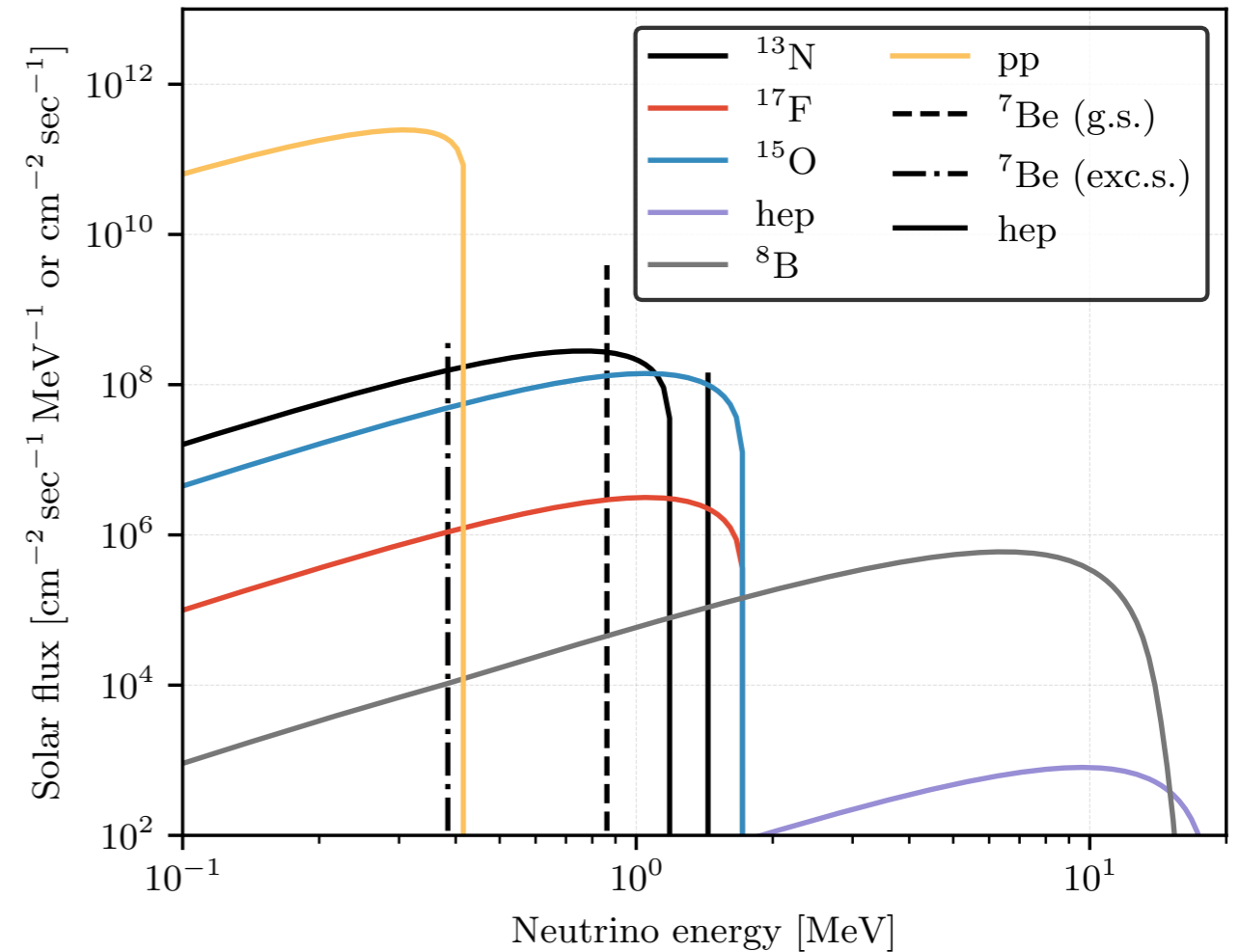
- Neutrino cross-sections and kinematics

Solar neutrino flux

Two branches:



[Comprehensive measurement of pp-chain solar neutrinos
Borexino Collaboration 2018]



Both continuous and monochromatic spectra. Input: theoretical model BS05(OP)

[Bahcall, Serenelli and Basu 2005]

Differential cross sections

$$\frac{d\sigma_\mu(\nu_L e \rightarrow \nu_R e)}{dE_r} = \alpha\mu_\nu^2 \left[\frac{1}{E_r} - \frac{1}{E_\nu} \right]$$

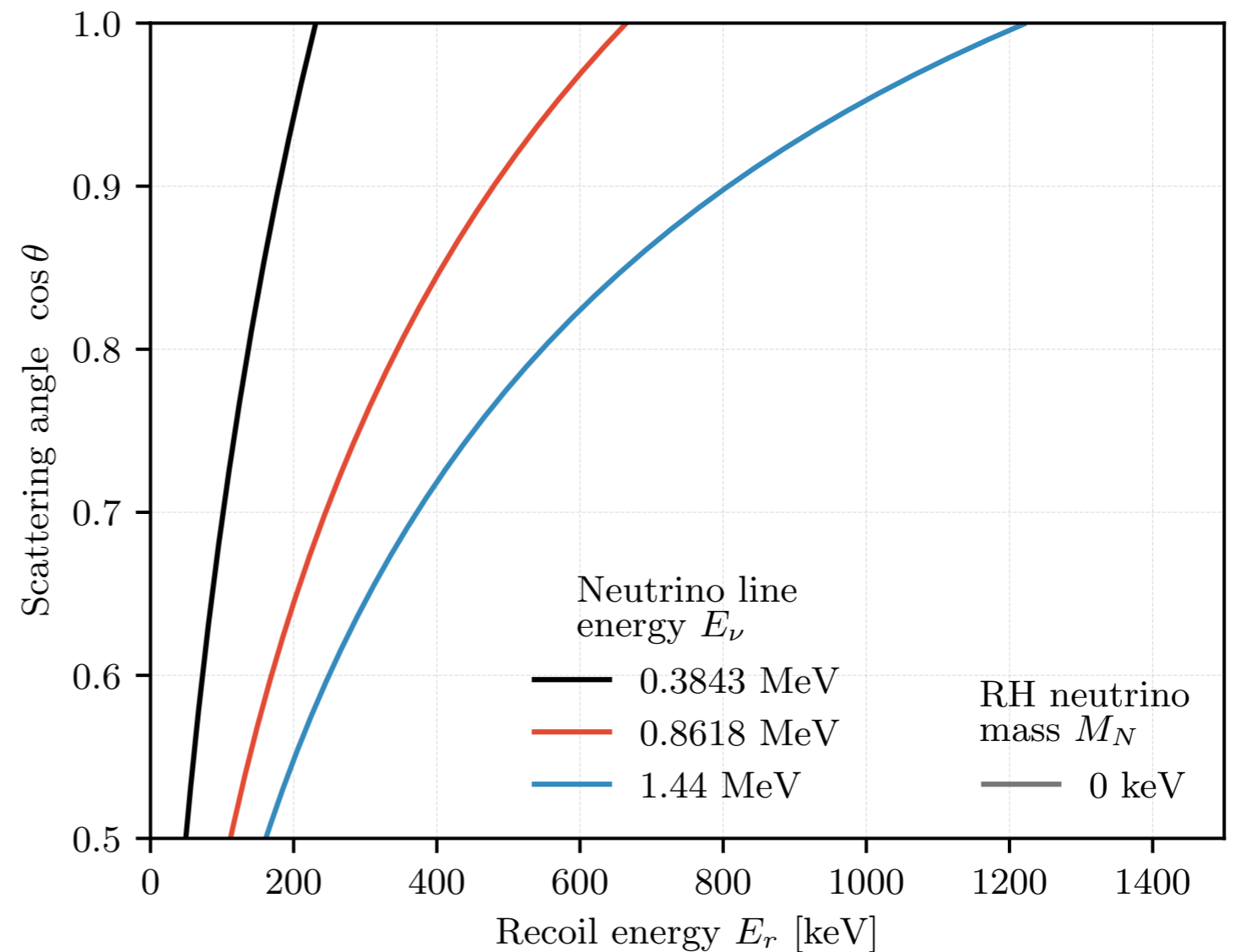
Kinematics:

$$\cos \theta = \frac{E_r(E_\nu + m_e)}{E_\nu \sqrt{E_r(2m_e + E_r)}}$$

↗
angle between outgoing
electron and incoming neutrino



$$(E_r^{\min}, E_r^{\max}) = \left(0, \frac{2E_\nu^2}{m_e + 2E_\nu} \right)$$



Differential cross sections

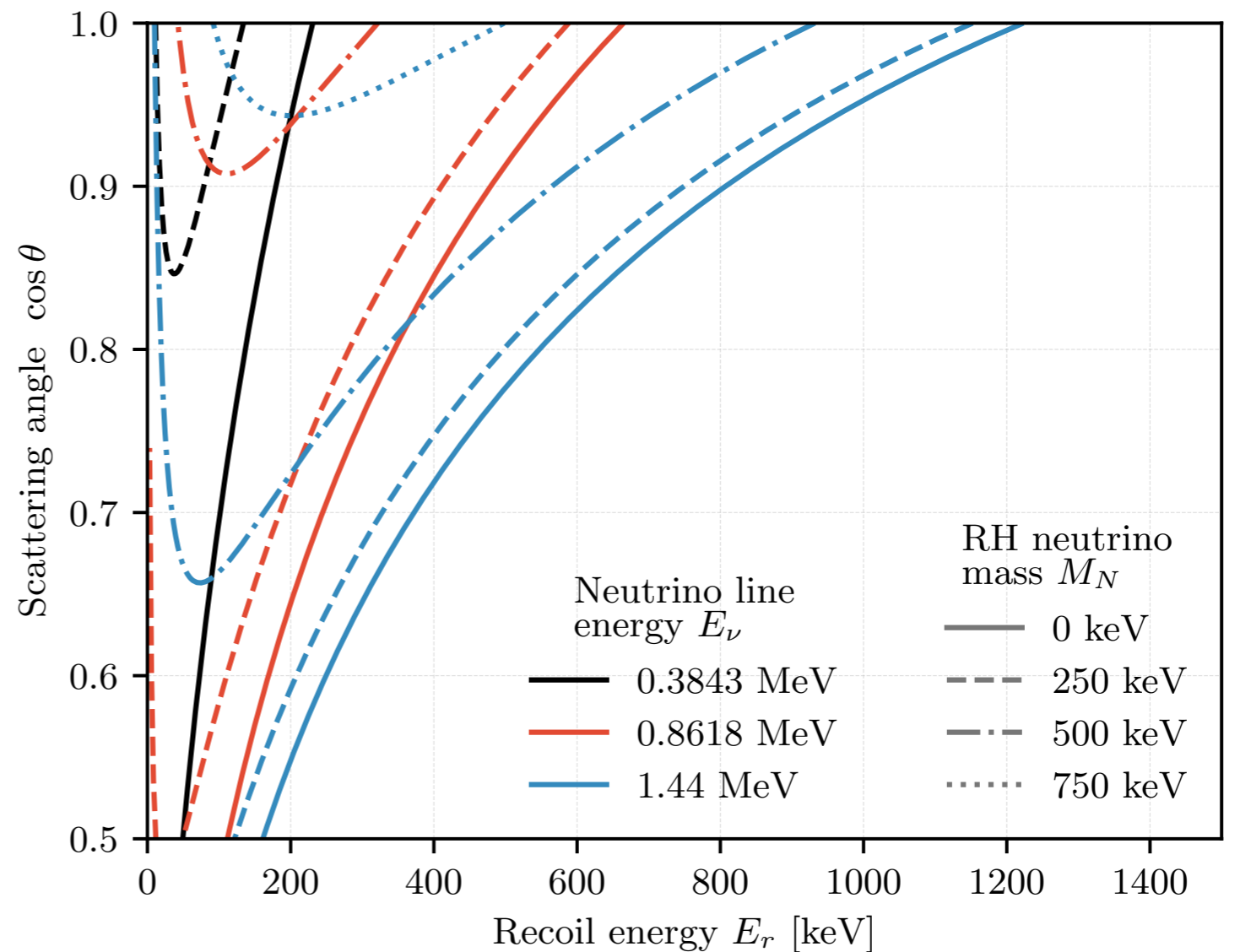
$$\frac{d\sigma_\mu(\nu_L e \rightarrow N_R e)}{dE_r} = \alpha\mu_\nu^2 \left[\frac{1}{E_r} - \frac{1}{E_\nu} + M_N^2 \frac{E_r - 2E_\nu - m_e}{4E_\nu^2 E_r m_e} + M_N^4 \frac{E_r - m_e}{8E_\nu^2 E_r^2 m_e^2} \right]$$

Kinematics:

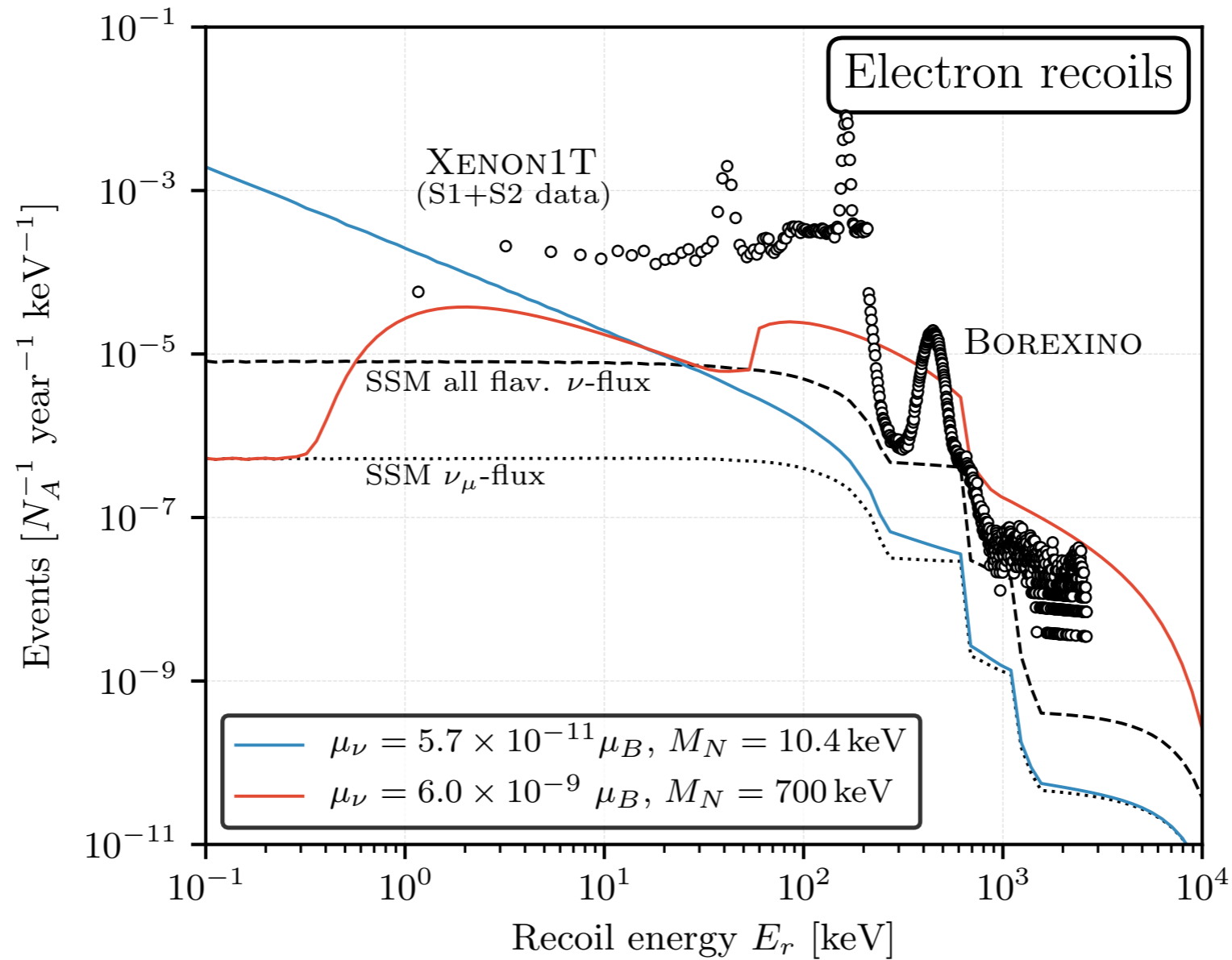
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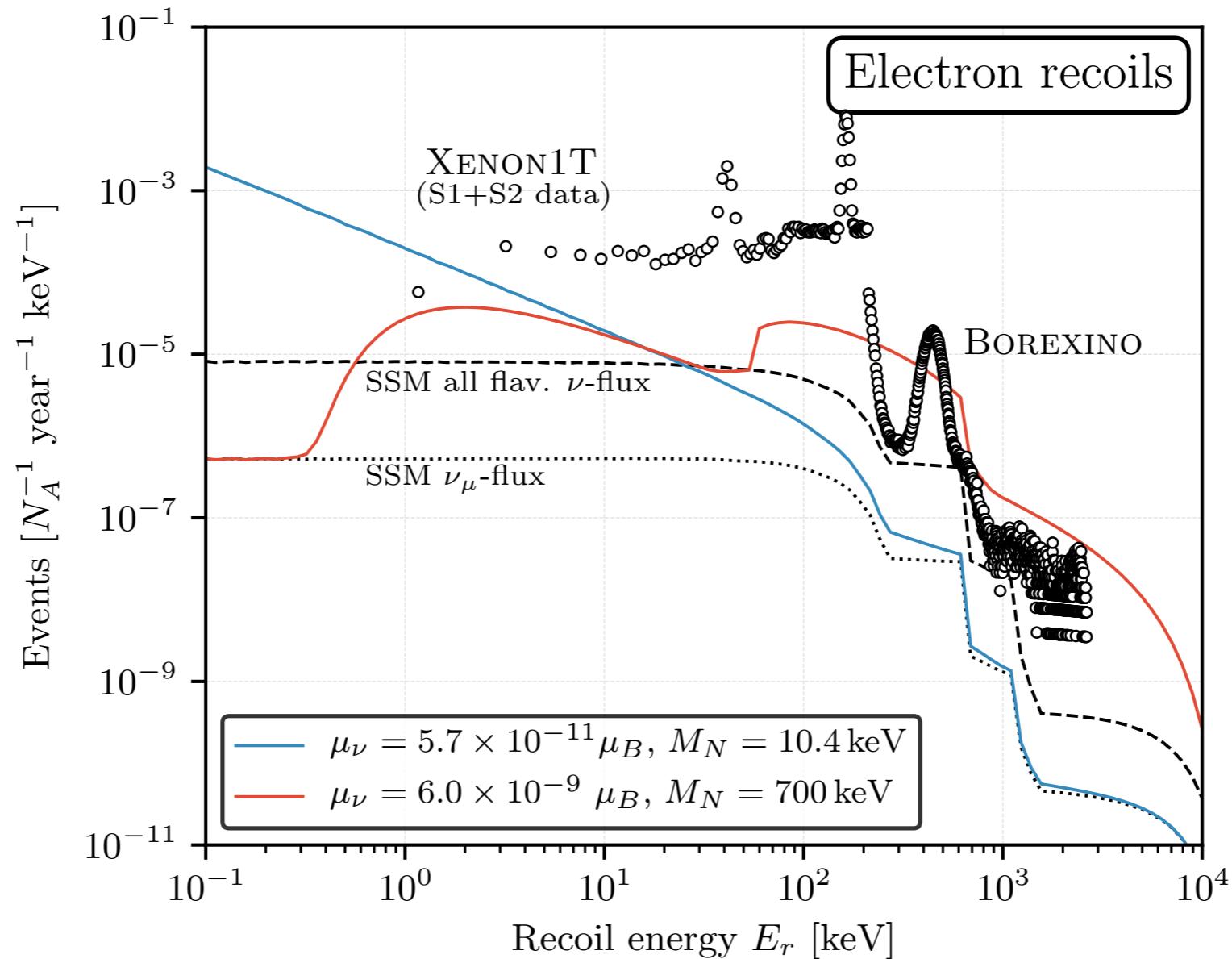
$$E_r^{\min} \simeq \frac{M_N^2}{2(m_e + M_N)} > 0$$



The predicted spectra



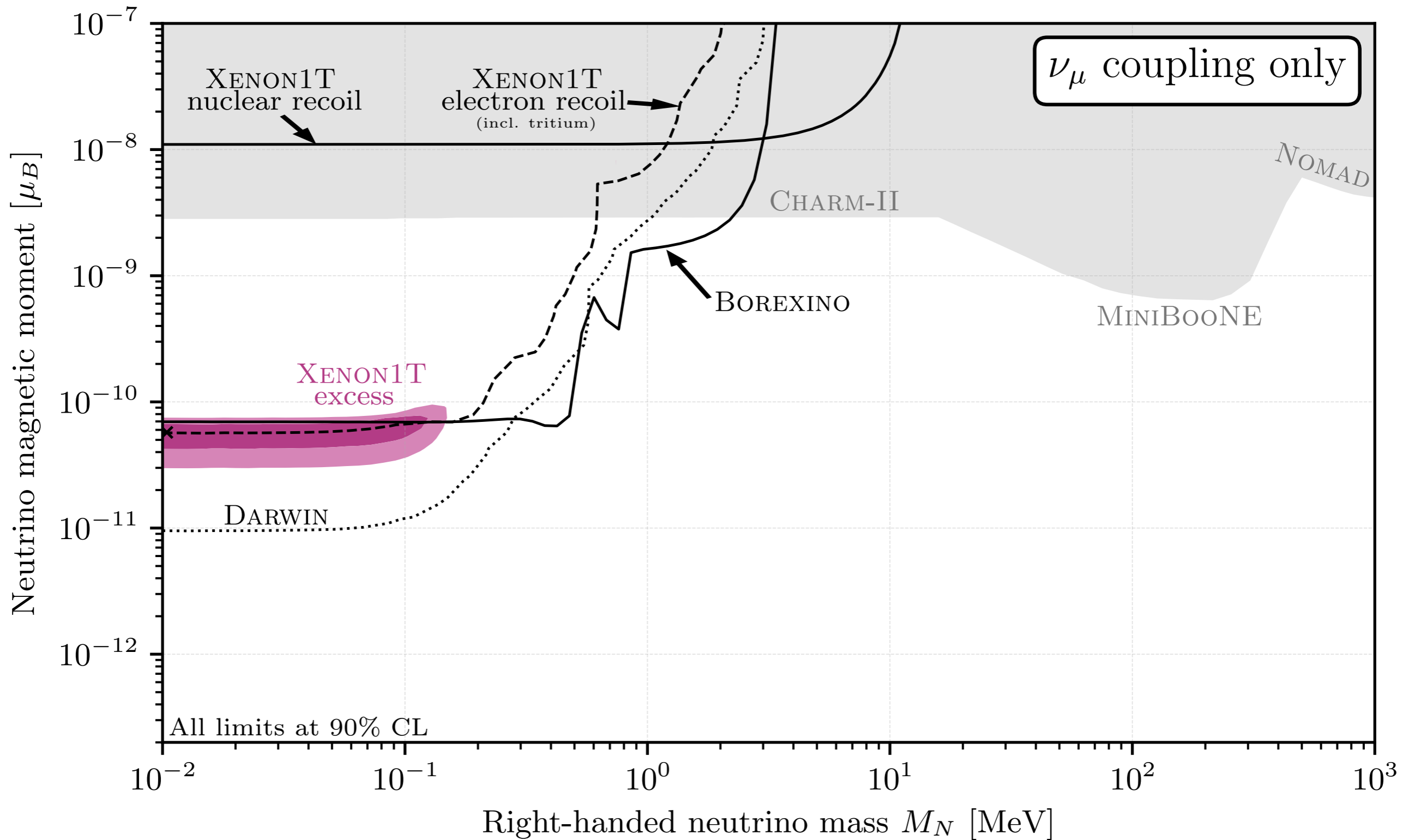
The predicted spectra



We did a binned likelihood fit to all data:

- Full recoil energy range
- Systematics for the solar flux
- Reproduced Xenon IT and Borexino limits on the magnetic moment of active neutrinos

Results



Astrophysics

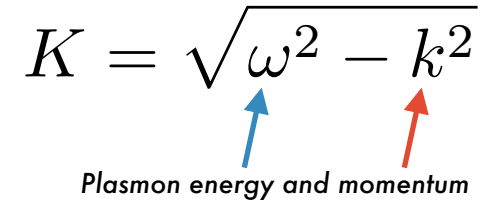
Stellar cooling

- Plasmon decays in dense charged medium kinematically allowed

$$\gamma^* \longrightarrow \nu_L + N \quad \text{where} \quad m_{\gamma^*} \propto T_{\text{star}}$$

- This additional energy loss mechanism affects stellar evolution — increased fuel burning rate!
- Energy loss per unit volume

$$Q = \int_0^\infty \frac{k^2 dk}{\pi^2} \int_{M_N^2}^\infty \frac{d\omega^2}{\pi} \frac{\omega \Gamma_T}{(K^2 - \omega_p^2)^2 + (\omega \Gamma_T)^2} \frac{\omega \Gamma_{\gamma^*}}{e^{\omega/T_\gamma} - 1} \quad K = \sqrt{\omega^2 - k^2}$$



Plasmon width

$$\Gamma_{\gamma^*} = \frac{|\mu_\nu|^2 K^4}{24\pi \omega} \left(1 - \frac{M_N^2}{K^2}\right)^2 \left(1 + 2 \frac{M_N^2}{K^2}\right) \theta(K - M_N)$$

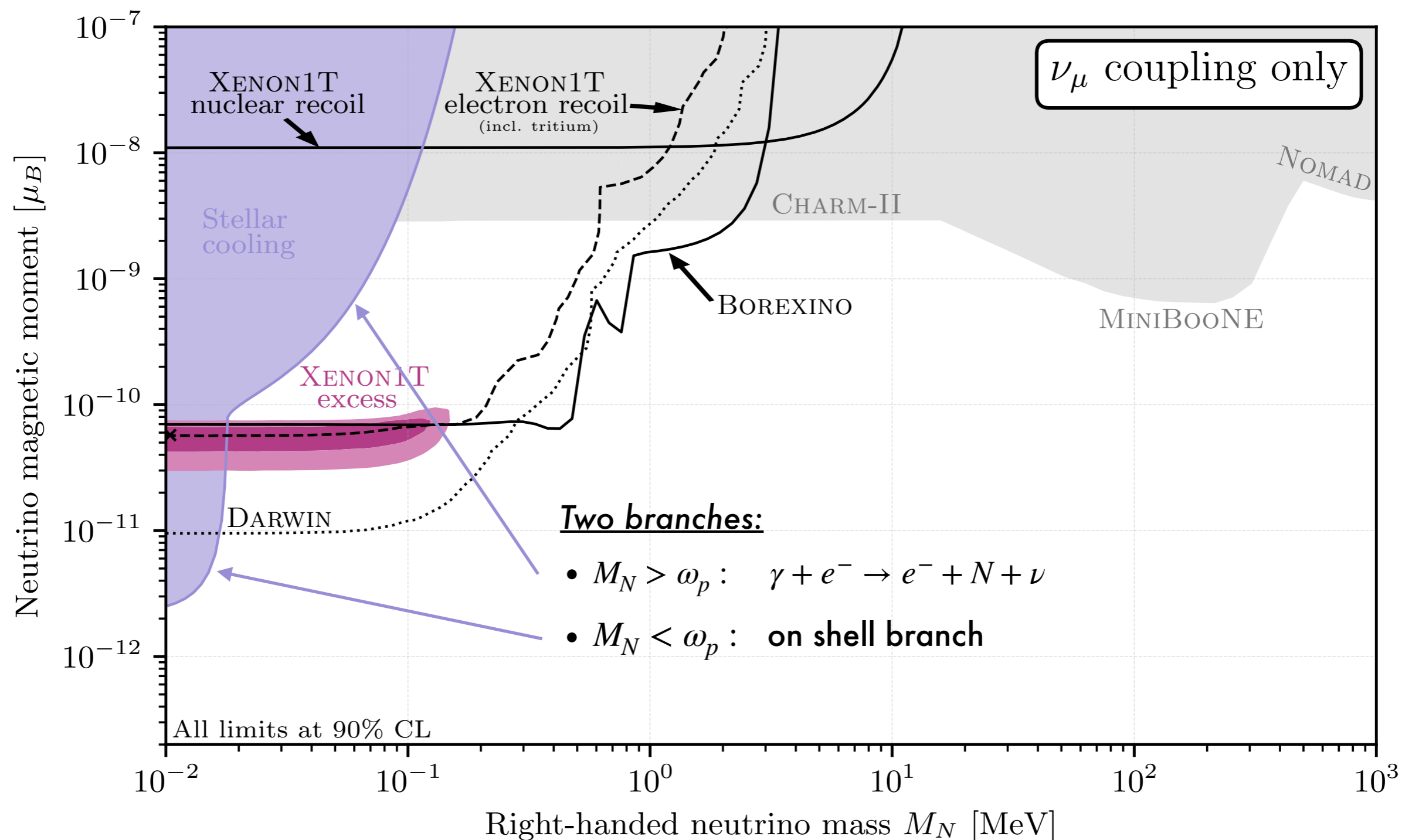
Thomson scattering rate

$$\Gamma_T = \frac{8\pi\alpha^2 n_e}{3m_e^2}$$

Limit set via energy-loss comparison with the $M_N = 0$ case where $\mu_\nu < 2.2 \times 10^{-12} \mu_B$

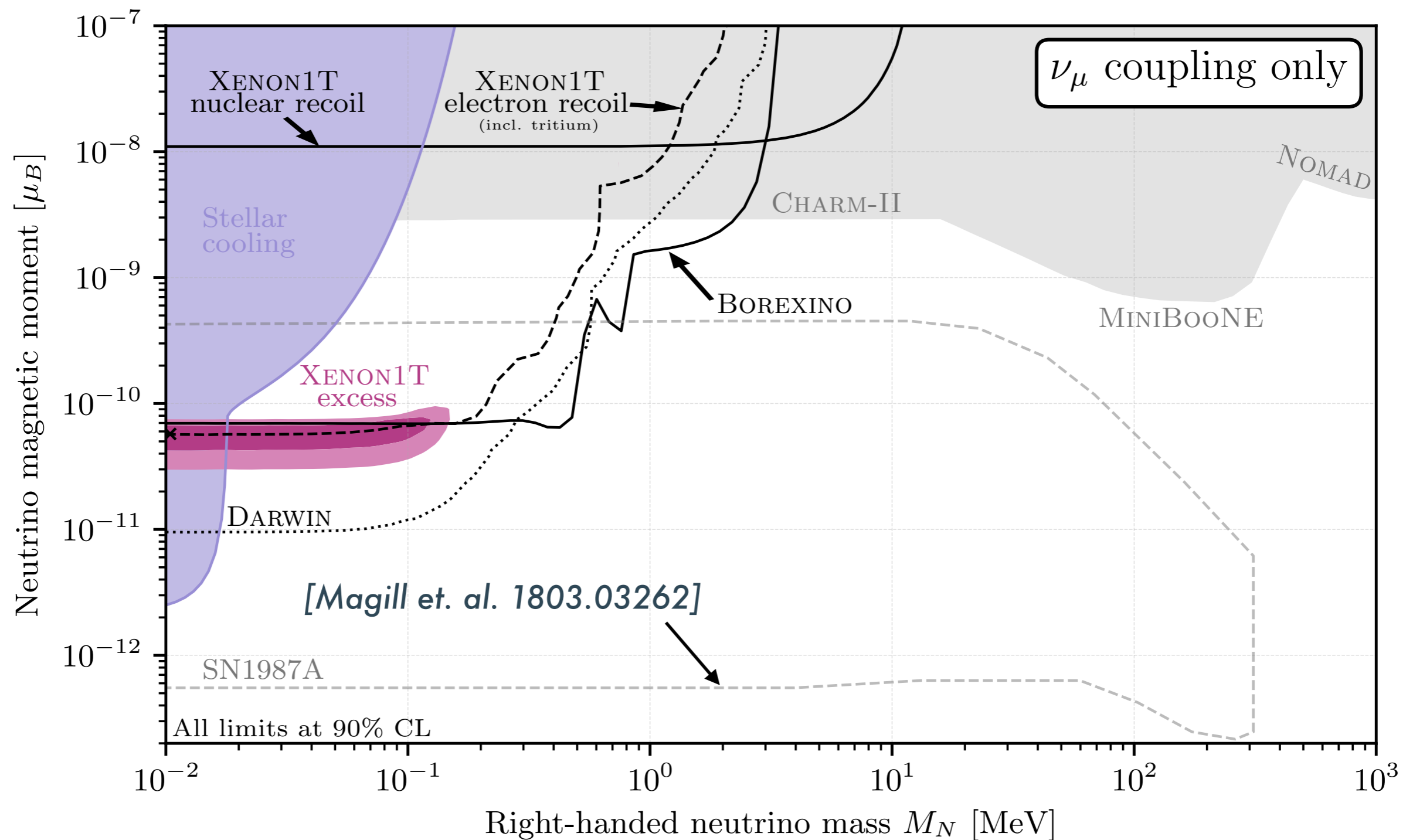
[Arceo-Díaz et. al. 1910.10568]

Stellar cooling

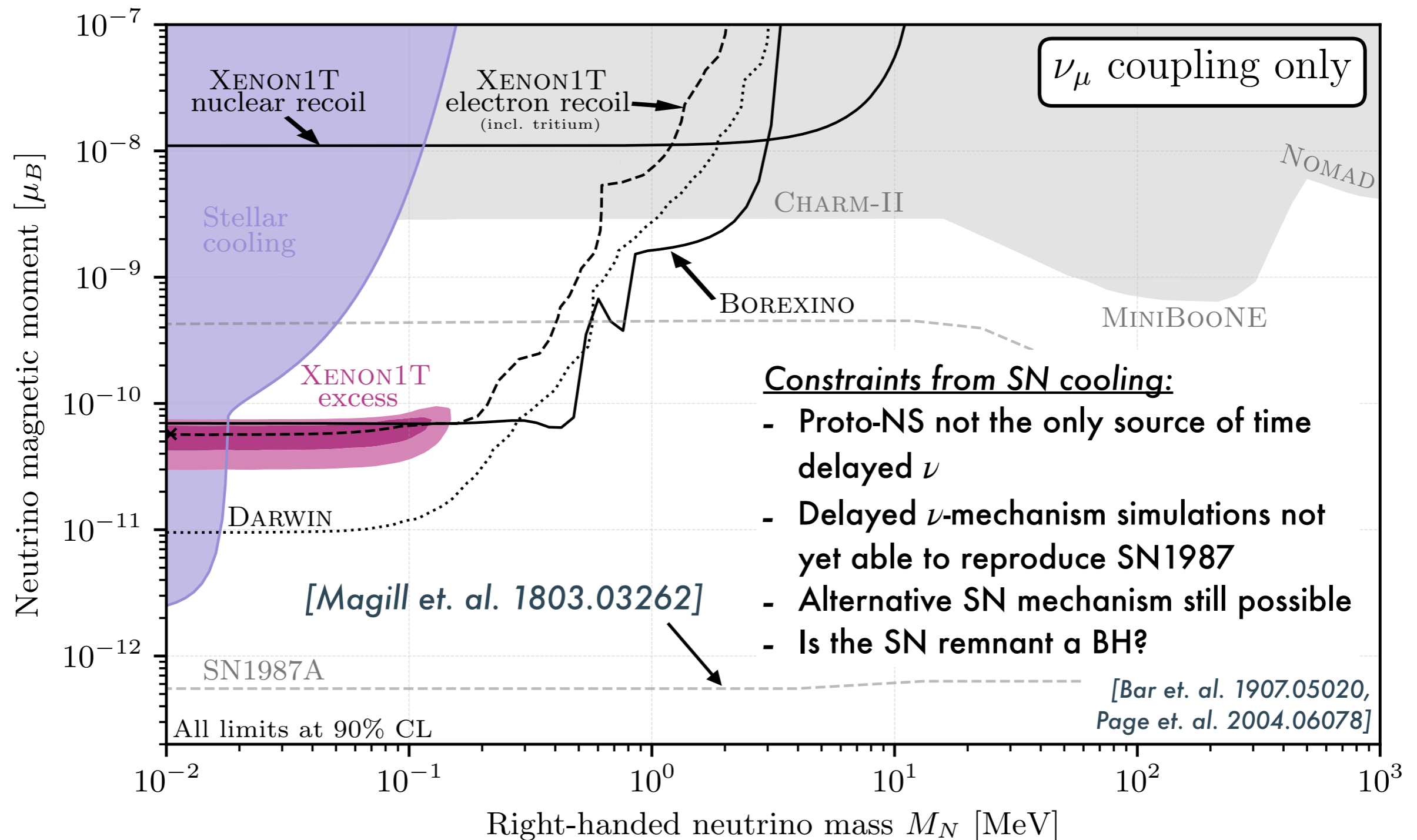


Use following RG parameters $\omega_p = \frac{18}{27}$ keV, $T_\gamma = 8.6$ keV and $n_e = 3 \times 10^{29}$ cm $^{-3}$

Supernova constraints



Supernova constraints



Cosmology

Cosmological constraints

Solve integrated Boltzmann equations:

$$\begin{aligned}\dot{\rho}_\gamma &= -4H\rho_\gamma + \langle\sigma v\rangle_{ee}(n_e\rho_e - n_e^{\text{eq}}\rho_e^{\text{eq}}) + \frac{\Gamma_N}{2}(\rho_N - \rho_N^{\text{eq}}) \\ \dot{\rho}_e &= -s_e H\rho_e - \langle\sigma v\rangle_{ee}(n_e\rho_e - n_e^{\text{eq}}\rho_e^{\text{eq}}) \\ \dot{\rho}_\nu &= -4H\rho_\nu + \frac{\Gamma_N}{2}(\rho_N - \rho_N^{\text{eq}}) + \Gamma_{eN}(\rho_N - \rho_N^{\text{eq}}) \\ \dot{\rho}_N &= -s_N H\rho_N - \Gamma_N(\rho_N - \rho_N^{\text{eq}}) - \Gamma_{eN}(\rho_N - \rho_N^{\text{eq}}).\end{aligned}$$

Dilution factors

Note: equilibrium densities for N_R function of both T_γ and T_ν i.e.

$$\rho_e^{\text{eq}} = (2T_\gamma^4/\pi^2)J_f(m_e/T_\gamma)$$

$$\rho_N^{\text{eq}} = (2T_R^4/\pi^2)J_f(M_N/T_R)$$

with $T_R \equiv \frac{1}{2}(T_\gamma + T_\nu)$

Rates:

Γ_N (Inverse) decays of N_R

Γ_{eN} Electron up-scattering $e + N_R \rightarrow e + \nu_L$

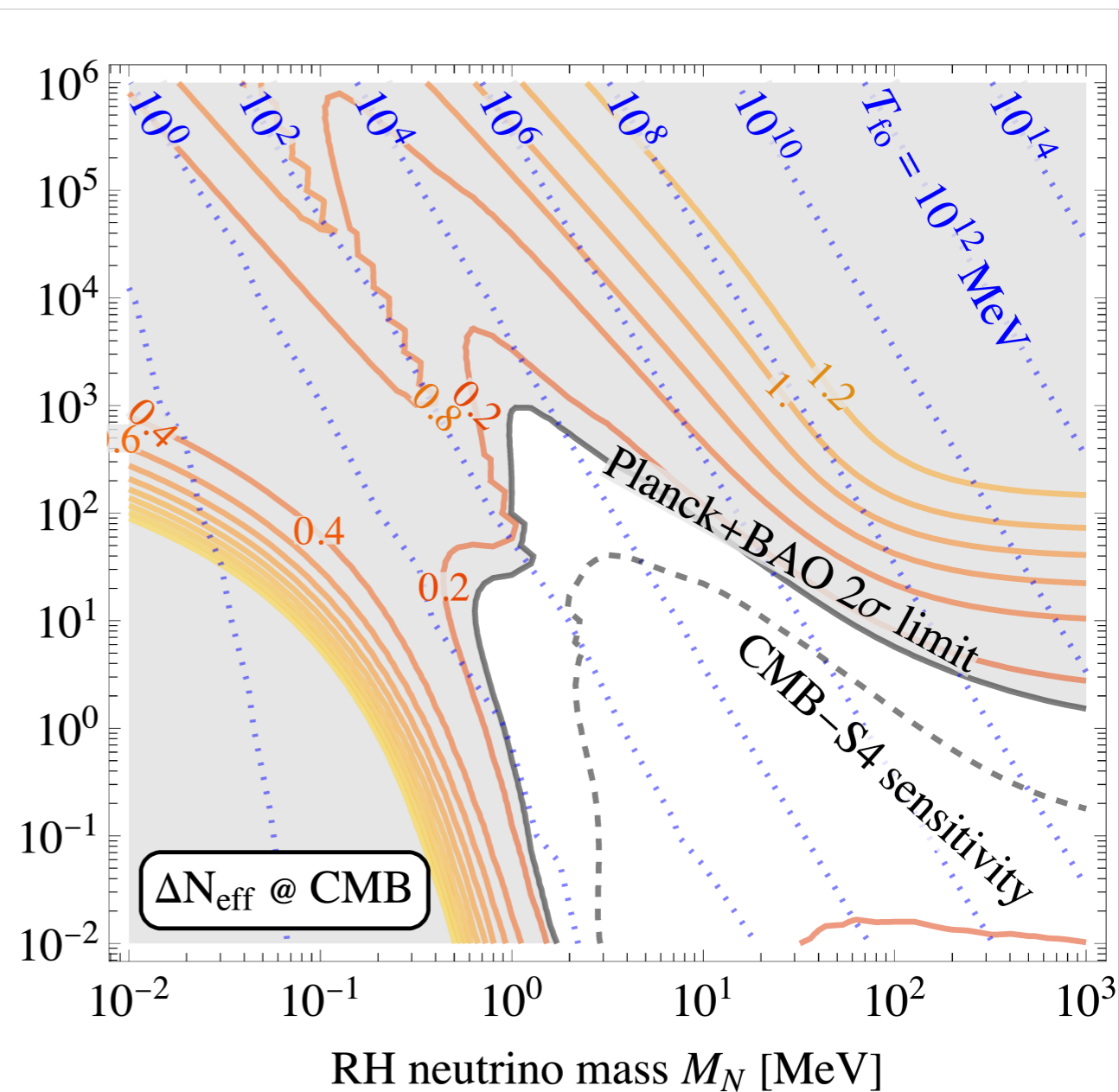
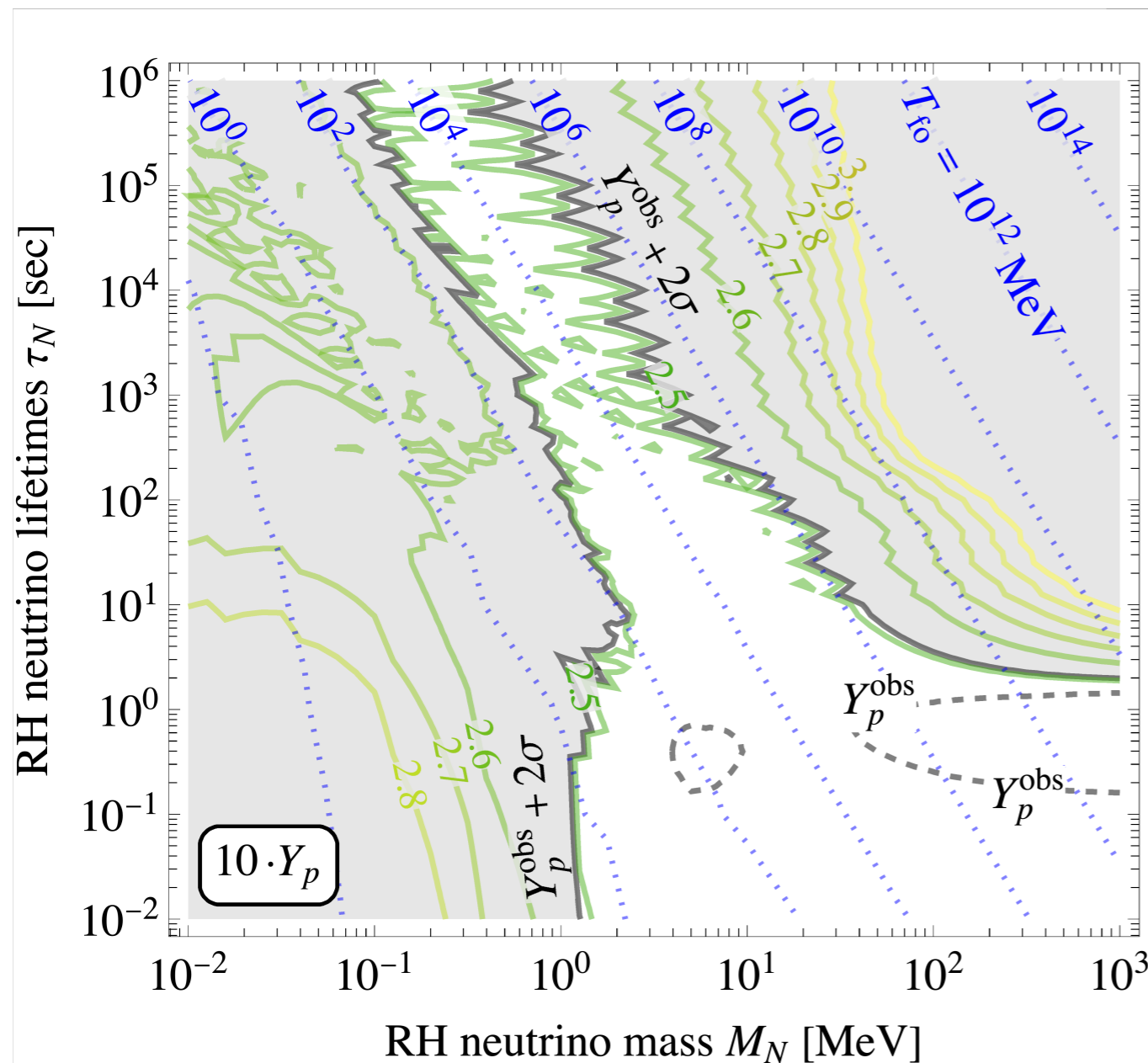
$\langle\sigma v\rangle_{ee}$ Standard model QED

Sanity check:
simplified treatment
reproduces ALP results

[Depta et. al. 2002.08370]

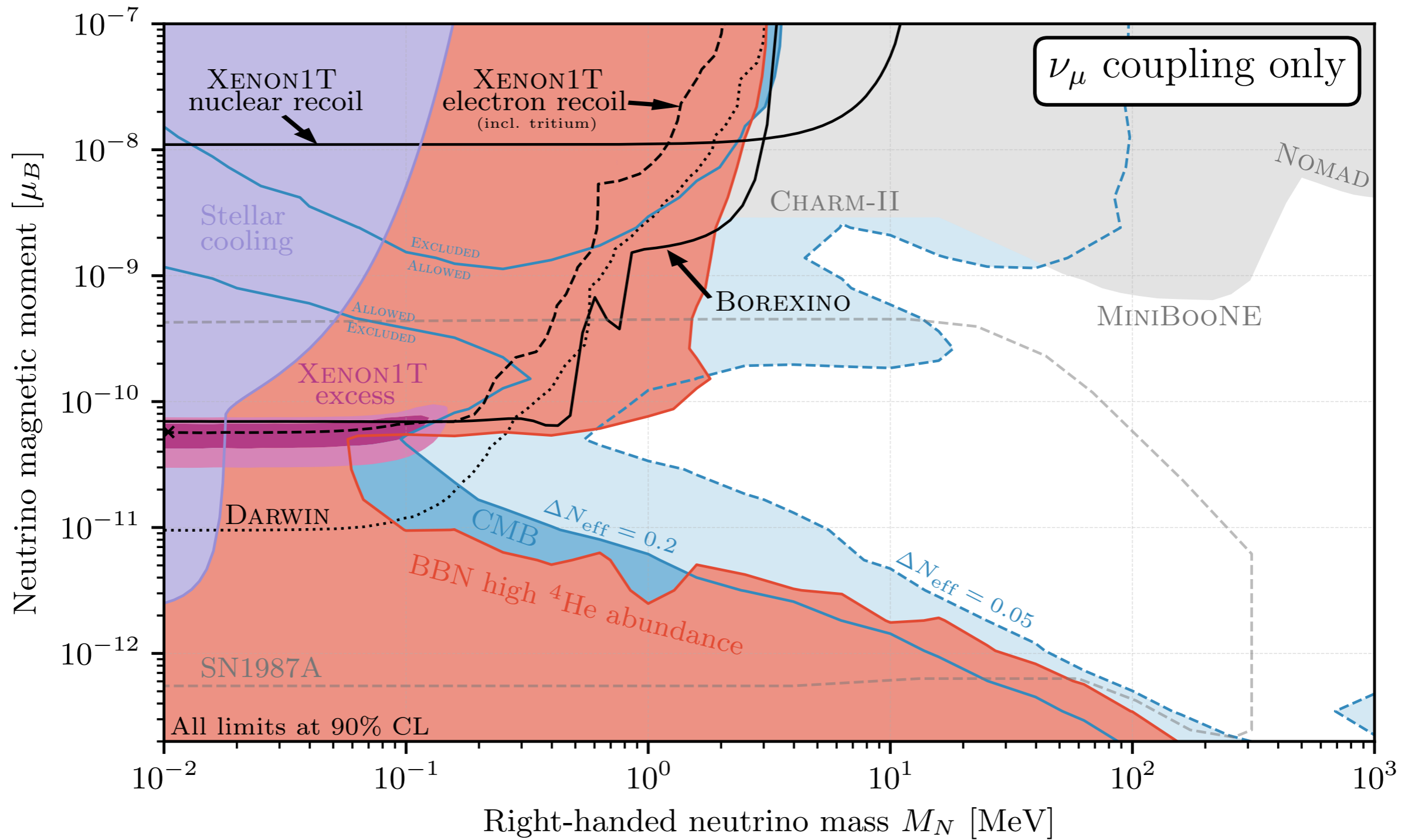
Code *AlterBBN* used.

Cosmological constraints



$$Y_p \equiv \rho(^4\text{He})/\rho_b$$

The final plot



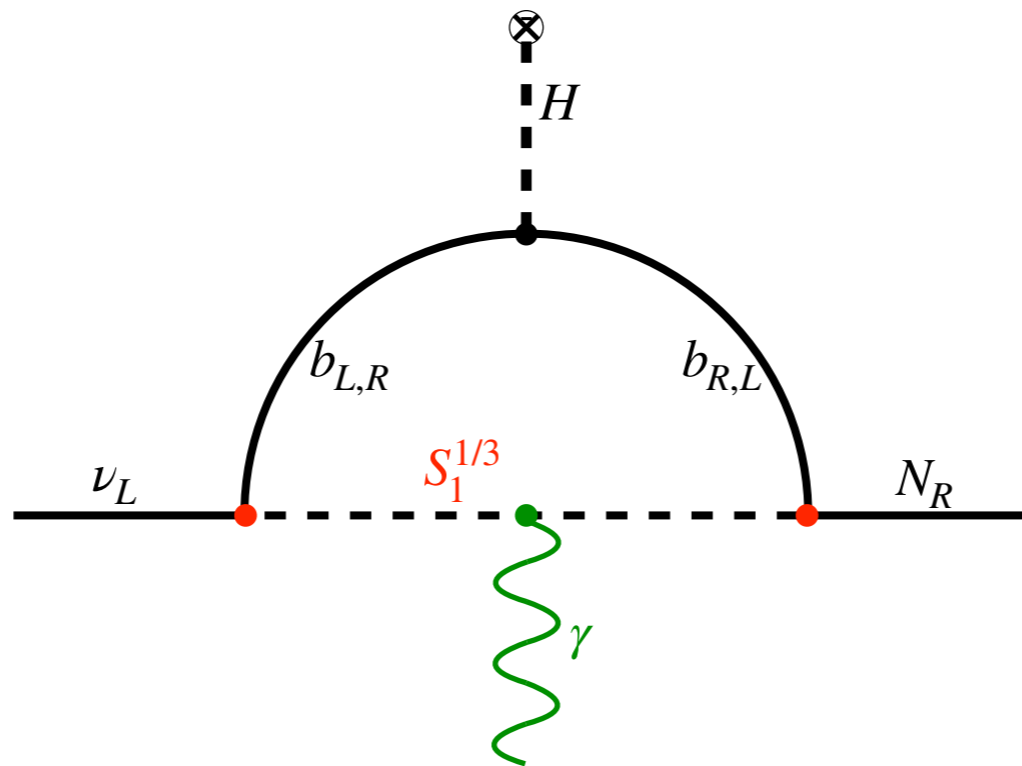
Model building

Neutrino masses

Natural relationship between μ_ν and Dirac mass $m_{\nu N}$ term

$$\frac{\mu_\nu}{\mu_B} \approx \frac{m_e m_{\nu N}}{\Lambda^2} \implies m_{\nu N} \sim \mathcal{O}(\text{MeV}) \left(\frac{10^{-11} \mu_B}{\mu_\nu} \right) \left(\frac{1 \text{ TeV}}{\Lambda} \right)^2$$

Example:



Neutrino masses

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Assuming type-I seesaw: $M_N \sim \frac{m_{\nu N}^2}{m_\nu} \gg \text{TeV}$ *Far far beyond reach of direct detection*

$M_N \sim \text{MeV}$ requires tuning tree level mass against this loop induced mass....

Neutrino masses

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Two ways out:

Inverse seesaw:

- Destroys mixing-mass relationship
- Large mixing between active-sterile states

Voloshin mechanism:

- Requires an additional $SU(2)$ horizontal symmetry

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Two ways out:

Inverse seesaw:

- Destroys mixing-mass relationship
- Large mixing between active-sterile states

$$\mathcal{L} \supset -m_{\nu N} \bar{\nu}_L N_R - m_N \bar{N}_L N_R + \text{h.c.}$$

(1 massless and 1 massive)

$$\tan \theta_{\nu N} = m_{\nu N} / m_N$$

Neutrino masses

Natural relationship between μ and Dirac mass m_ν term

- Interestingly large mixings are not excluded in terrestrial experiments for the MeV-mass sterile neutrino
- Still, we want the magnetic moment to dominate the phenomenology, not the mixing

Naive estimate of the relevant rates for cosmology*

$$\Gamma_{\mu\nu} \sim \mu_\nu^2 T^3$$

vs

\implies

$$\mu_\nu > G_F T \sin \theta \sim 10^{-11} \mu_B \left(\frac{\text{GeV}}{T} \right) \left(\frac{10^{-3}}{\sin \theta} \right)$$

$$\Gamma_\theta \sim G_F^2 T^5 \sin^2 \theta$$

- Large mixing between active-sterile states

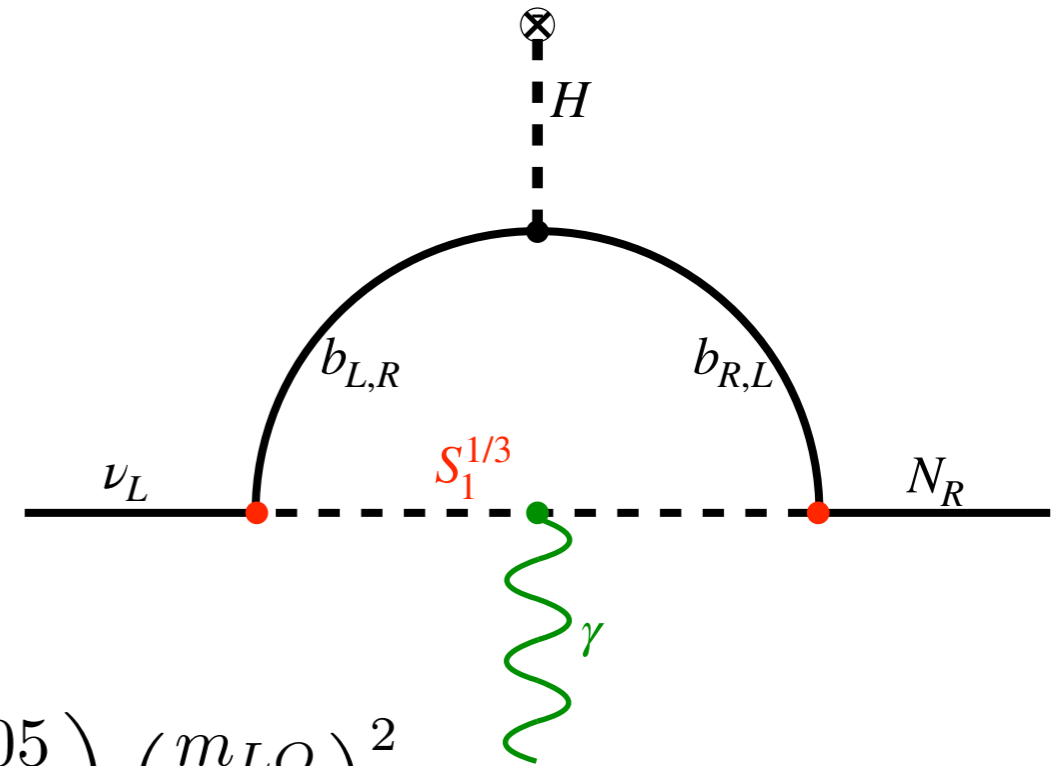
Leptoquark model

Introduce a single scalar leptoquark
 $S_1 \in (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$

$$\mathcal{L}_{S_1} \supset y_1 \bar{b}_R^c N_R S_1 + y_2 \overline{Q}_L^3 L_L^{i c} S_1^\dagger + \text{h.c.}$$

Naturally large magnetic moment

$$\mu_\nu \approx \frac{e y_1 y_2}{8\pi^2 m_{LQ}^2} m_b \log \frac{m_b^2}{m_{LQ}^2} \sim 3 \times 10^{-11} \mu_B \left(\frac{0.05}{y_1 y_2} \right) \left(\frac{m_{LQ}}{\text{TeV}} \right)^2$$



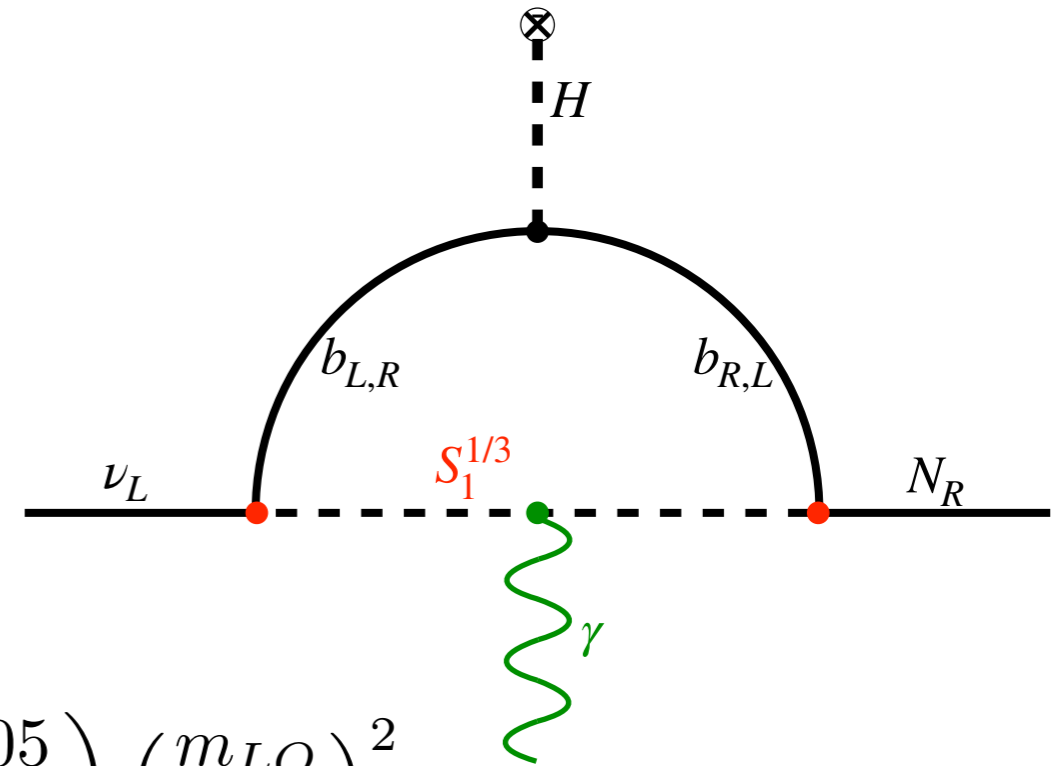
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Rich phenomenology:


- Unique collider signatures
- Contribution to $g - 2$ of the muon
- Contributions to both neutral ($b \rightarrow s \ell \ell$) and charged current transitions ($b \rightarrow c \tau \nu$)
- Can also be embedded in RPV supersymmetry

Leptoquark model

Additional approximate $SU(2)$ symmetry

[Voloshin 1988 – typically mechanism is implemented using additional neutral scalars]

$$(\nu_L^c, N_R) \in \mathbf{2} \implies \begin{cases} \bar{N}_R \sigma^{\mu\nu} \nu_L - \overline{\nu_L^c} \sigma^{\mu\nu} N_R^c & SU(2) \text{ singlet} \\ \bar{N}_R \nu_L + \overline{\nu_L^c} N_R^c & SU(2) \text{ triplet} \end{cases}$$

Dirac mass exactly zero 

Conclusions

- Active to sterile neutrino upscattering mediated by a transition magnetic moment in a neutrino or dark matter direct detection experiment.
- Complementary constraints from astrophysics and cosmology scrutinize most of the relevant parameter space.
- Model-building challenges arise in scenarios that feature large magnetic moments while keeping observed neutrino masses.