

Measurement of the cross section for inclusive B_s production in e^+e^- collisions at energies around 11 GeV



**PhD thesis defence
(demo-version)**

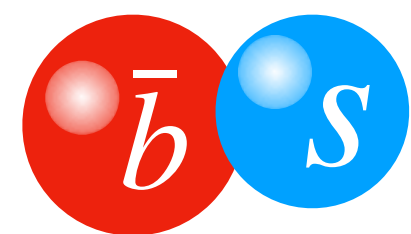
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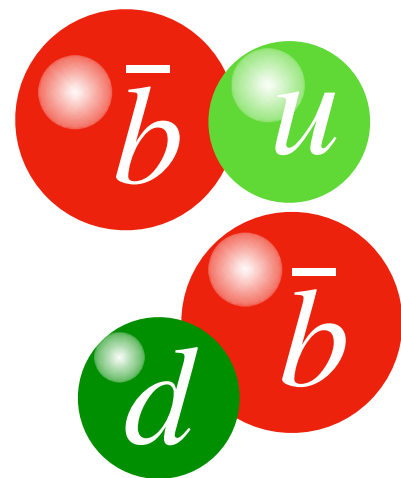
Ljubljana, Slovenia
9 October 2023

Goal

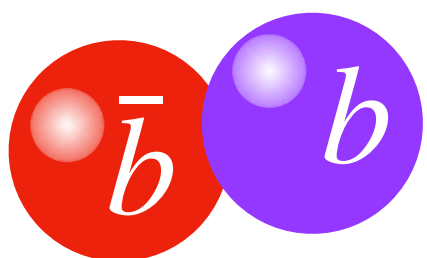
Goal of this dissertation — $\sigma(e^+e^- \rightarrow B_s\bar{B}_sX)$ and $\sigma(e^+e^- \rightarrow B\bar{B}X)$ at E_{cm} from 10.63 to 11.02 GeV



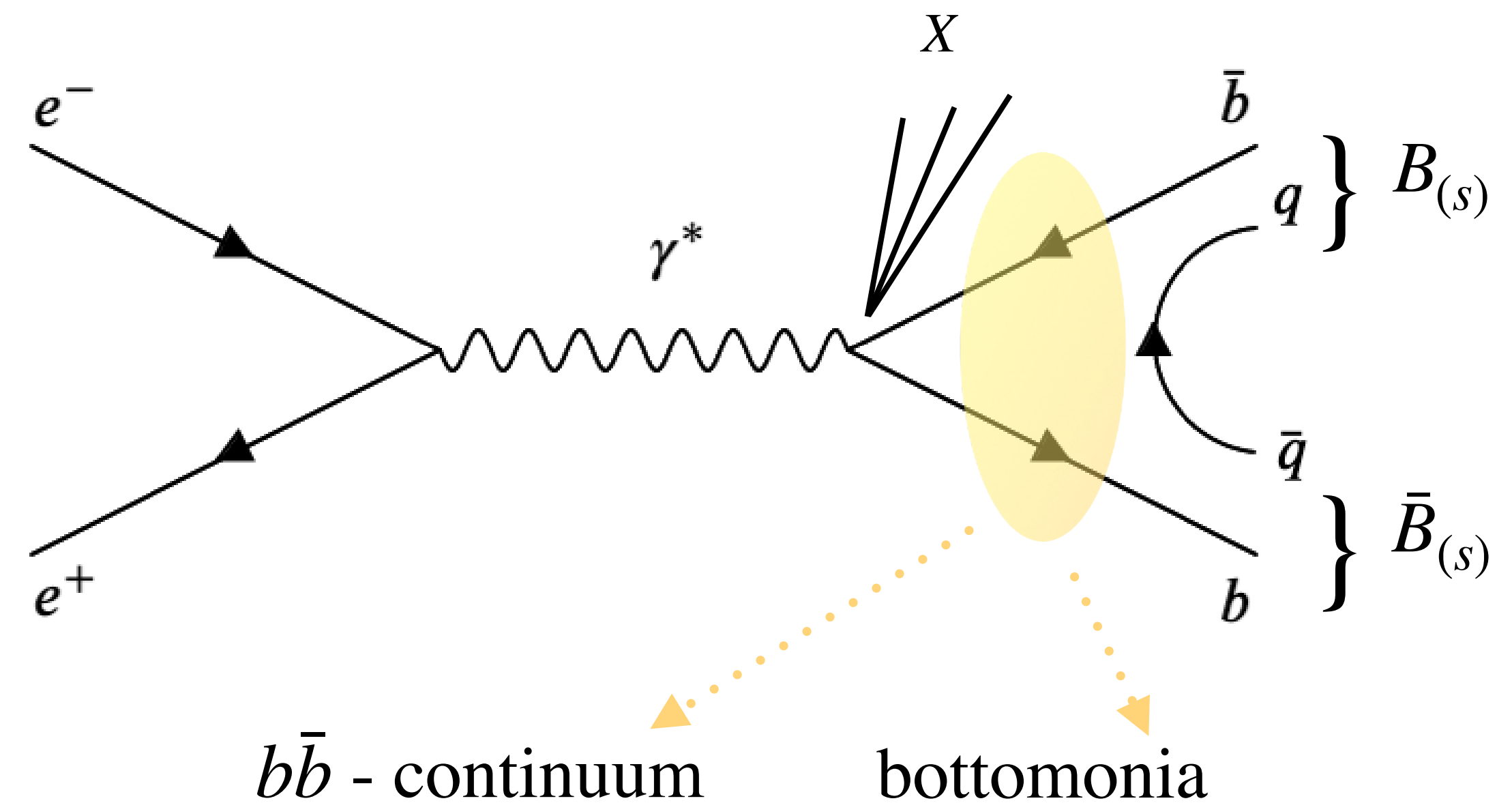
B_s mesons — open-flavor,
 $m = (5366.92 \pm 0.10)$ MeV



B^0 and B^+ mesons — open-flavor,
 $m = (5279.66 \pm 0.12)$ MeV



Bottomonia — hidden-flavor



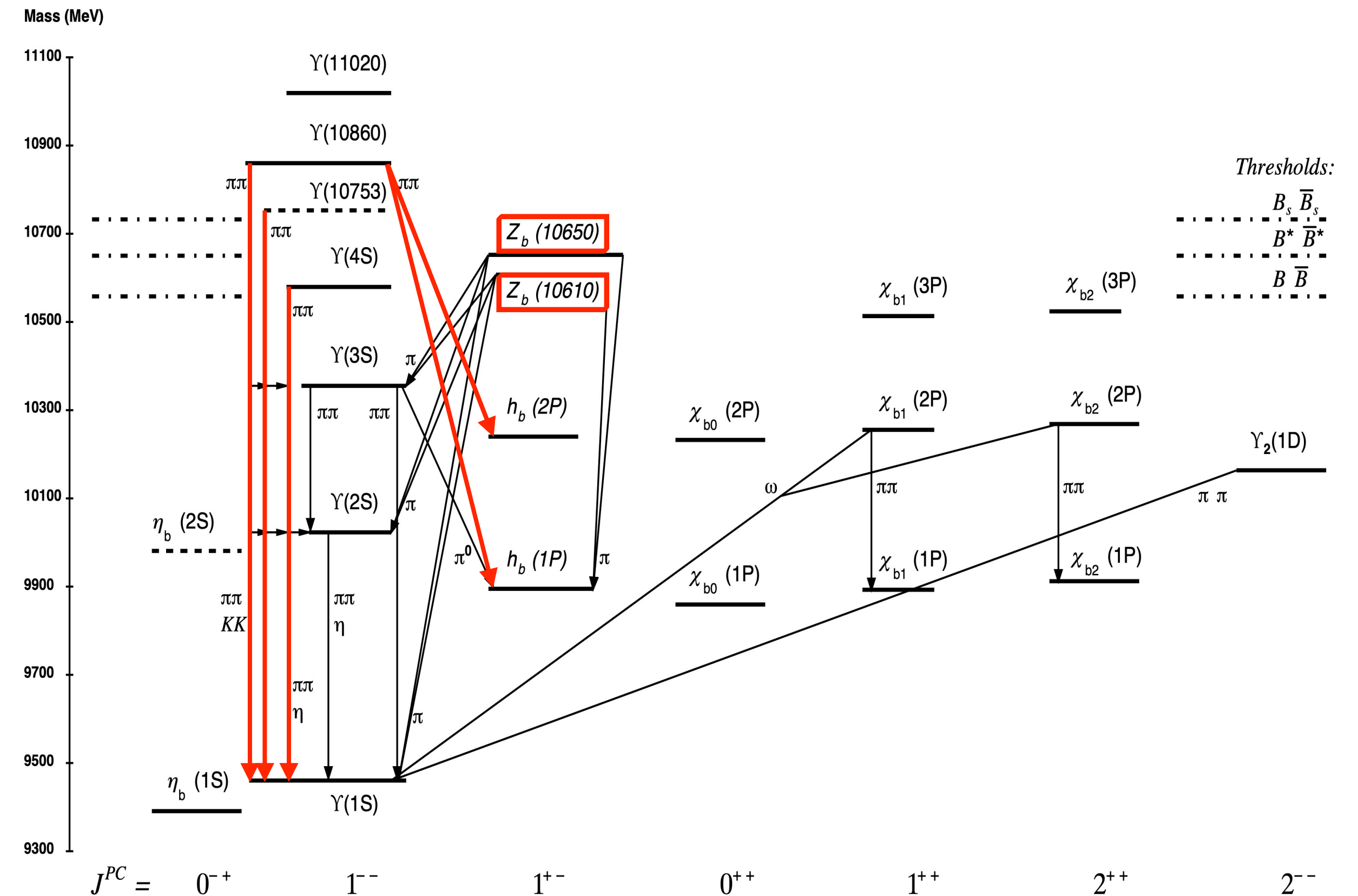
Bottomonium spectroscopy

Heavy quarkonium spectroscopy is an excellent laboratory to study non-perturbative QCD

Bottomonium states below $B\bar{B}$ threshold are well described by quark model

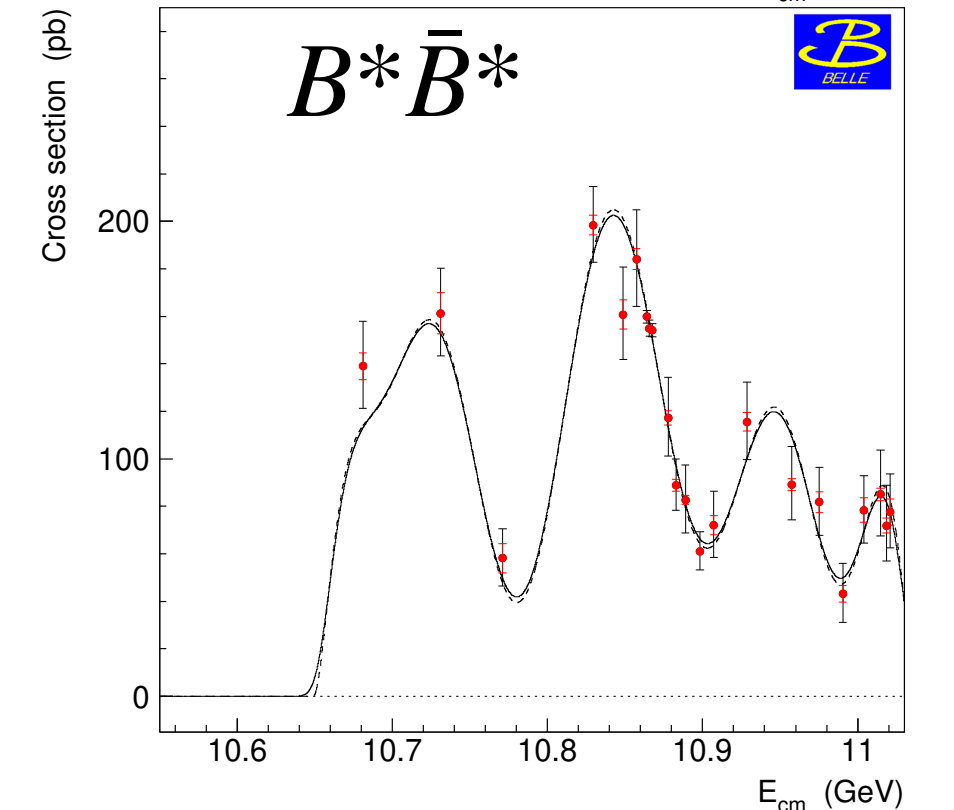
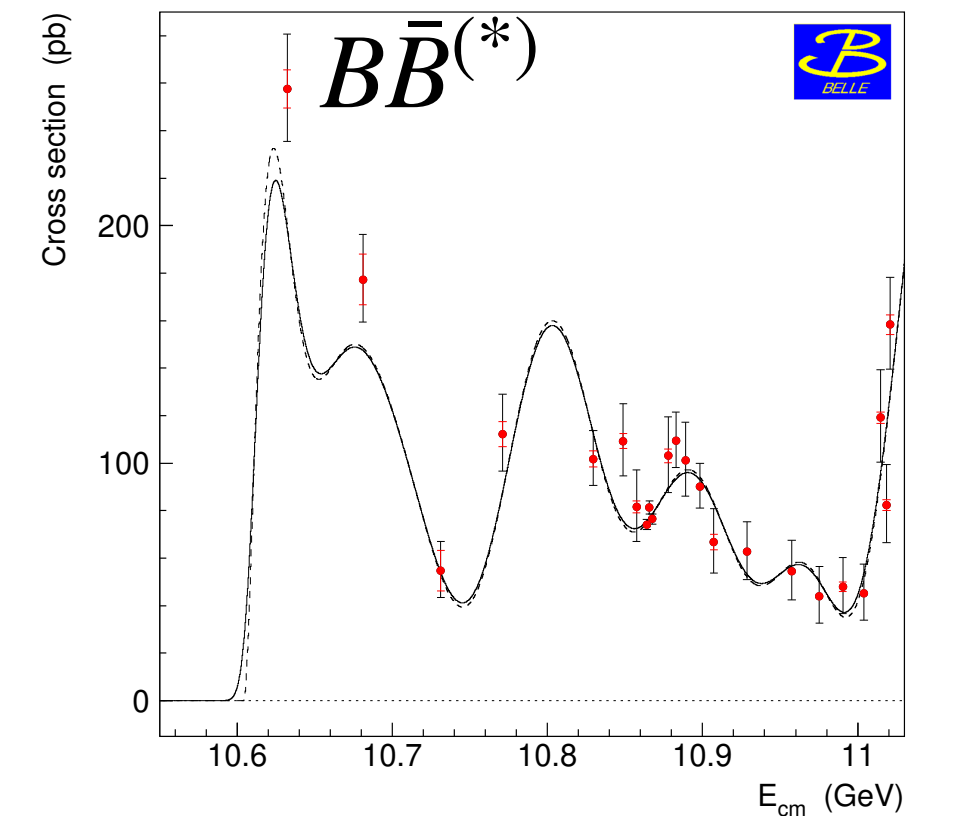
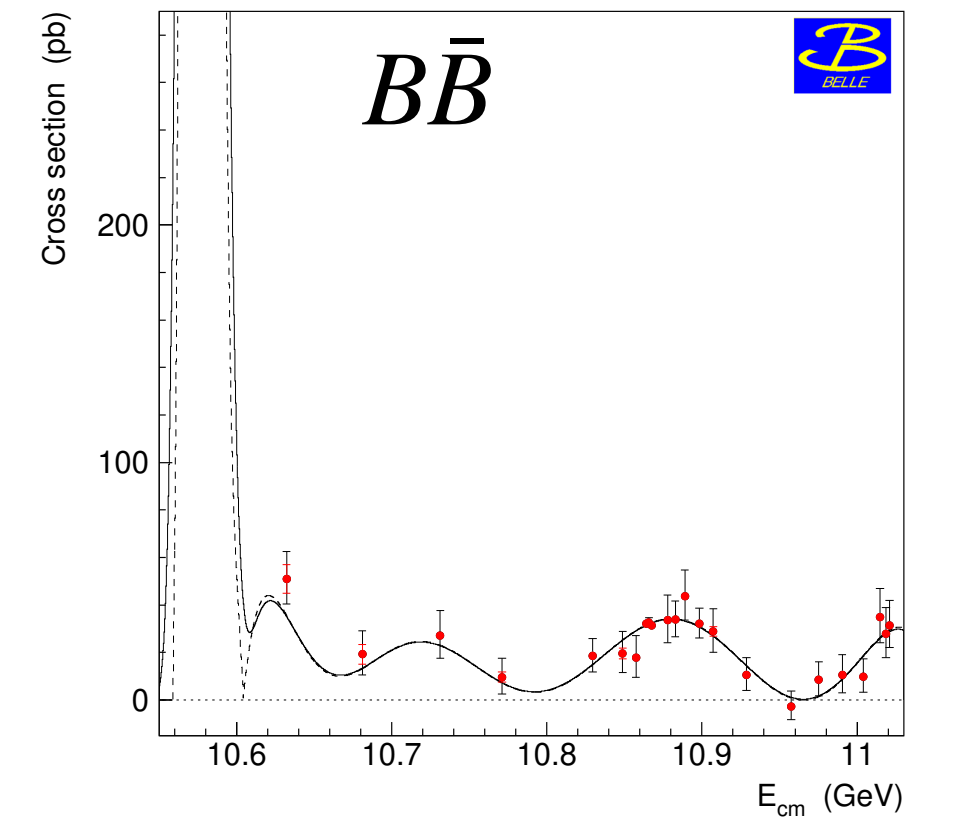
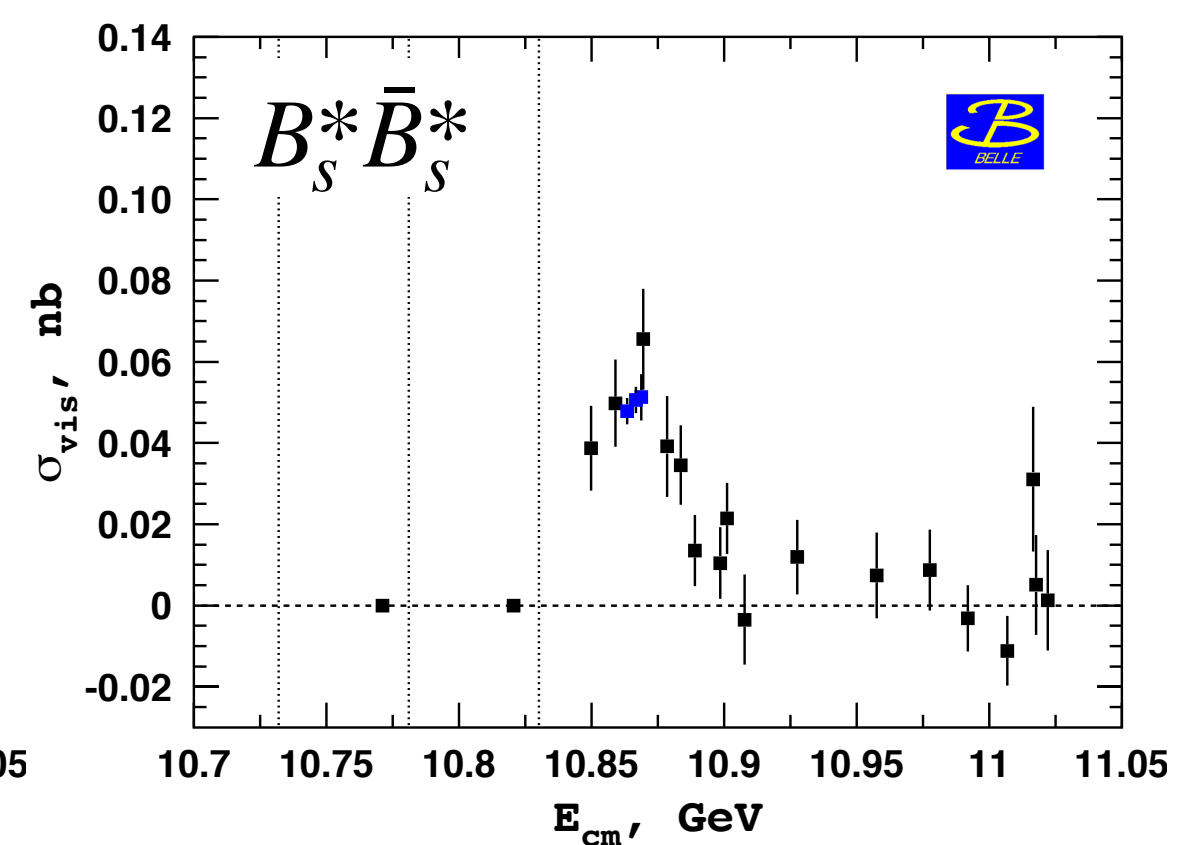
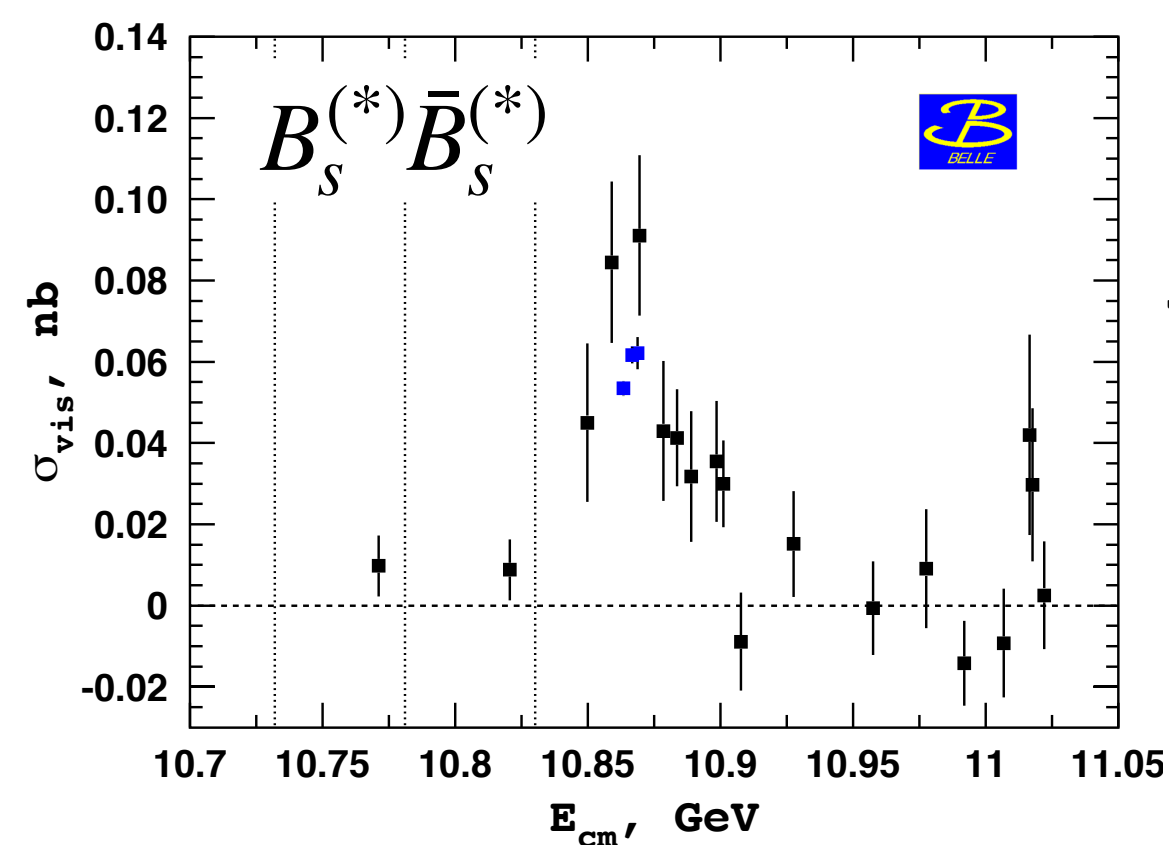
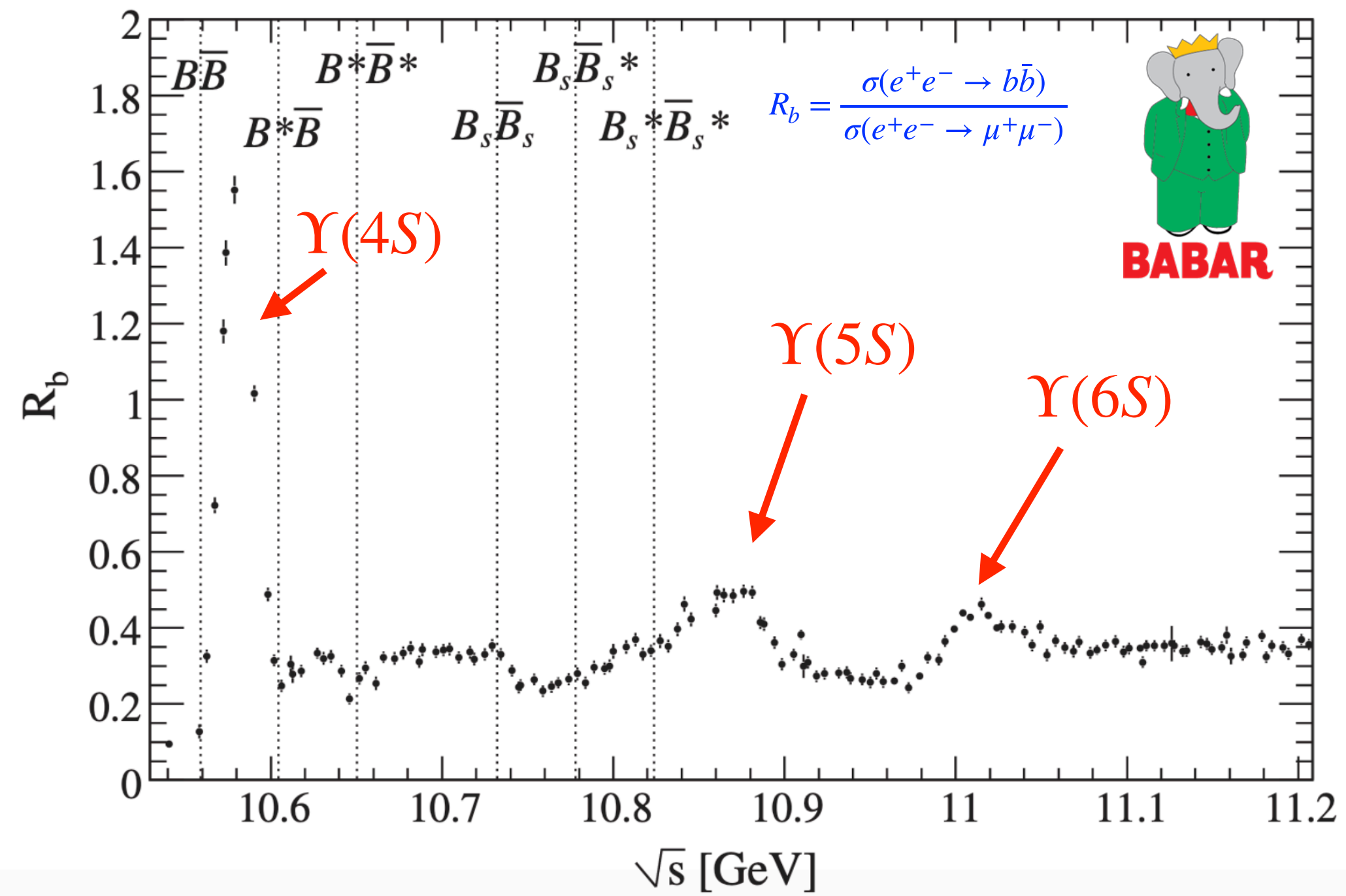
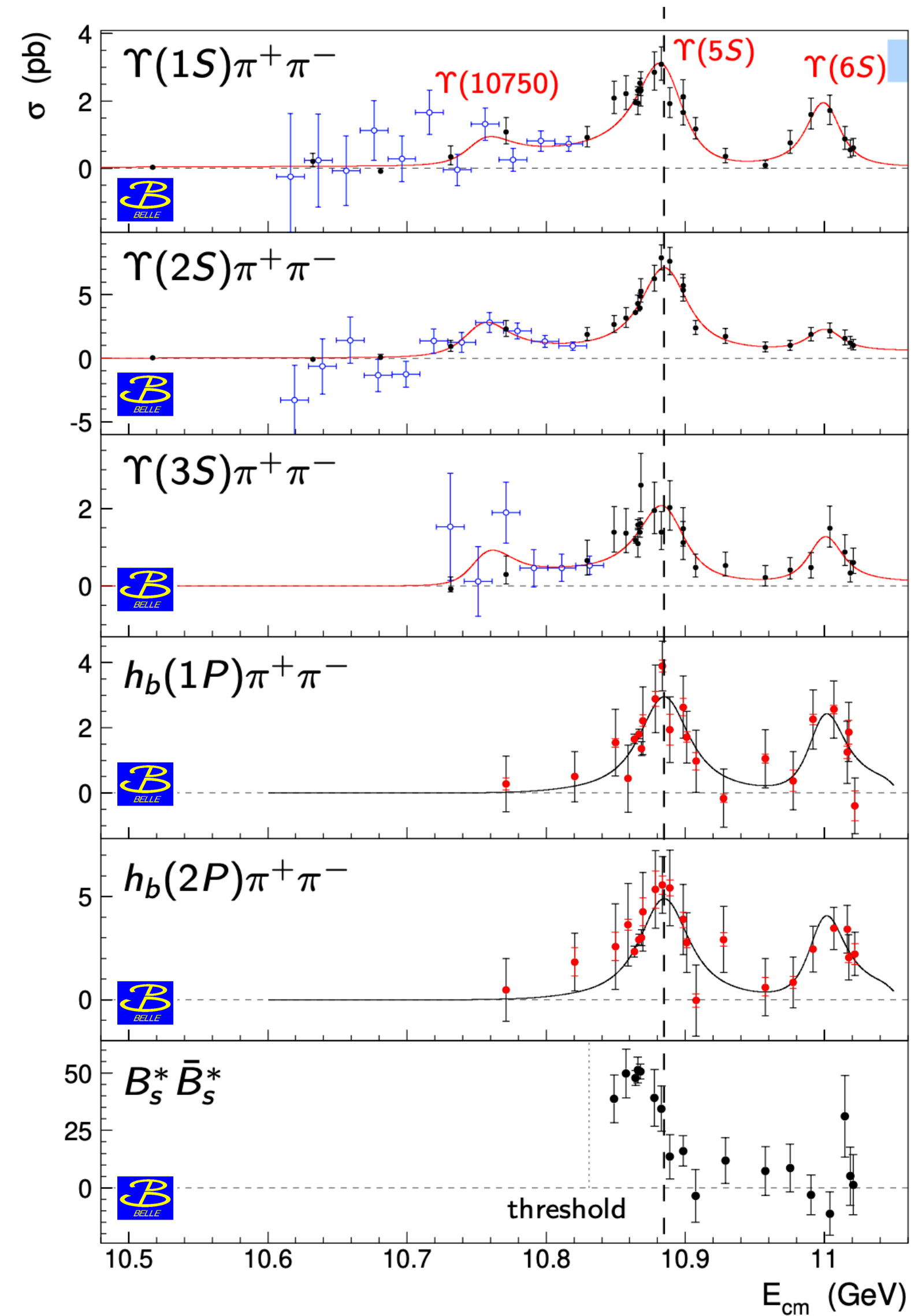
Bottomonium states above $B\bar{B}$ threshold demonstrate unexpected properties

- ➔ Z_b and Z'_b are charged (at least 4 quarks)
- ➔ Rates of hadronic transition to lower bottomonia are higher than expected for pure $b\bar{b}$ (violate OZI-rules)
- ➔ η transitions are not suppressed relative to dipion transitions (violate HQSS)



Nature of bottomonia above threshold is not well understood yet!

Analysis of the individual cross sections



Analysis of the individual cross sections

Problems with the analysis of the individual cross sections

Parameters of the resonances extracted from different channels may differ

— $\Upsilon(5S)$ peak position in $\Upsilon(nS)\pi^+\pi^-$ and $h_b(1,2P)\pi^+\pi^-$ are shifted from peak in $B_s^{(*)}\bar{B}_s^{(*)}$

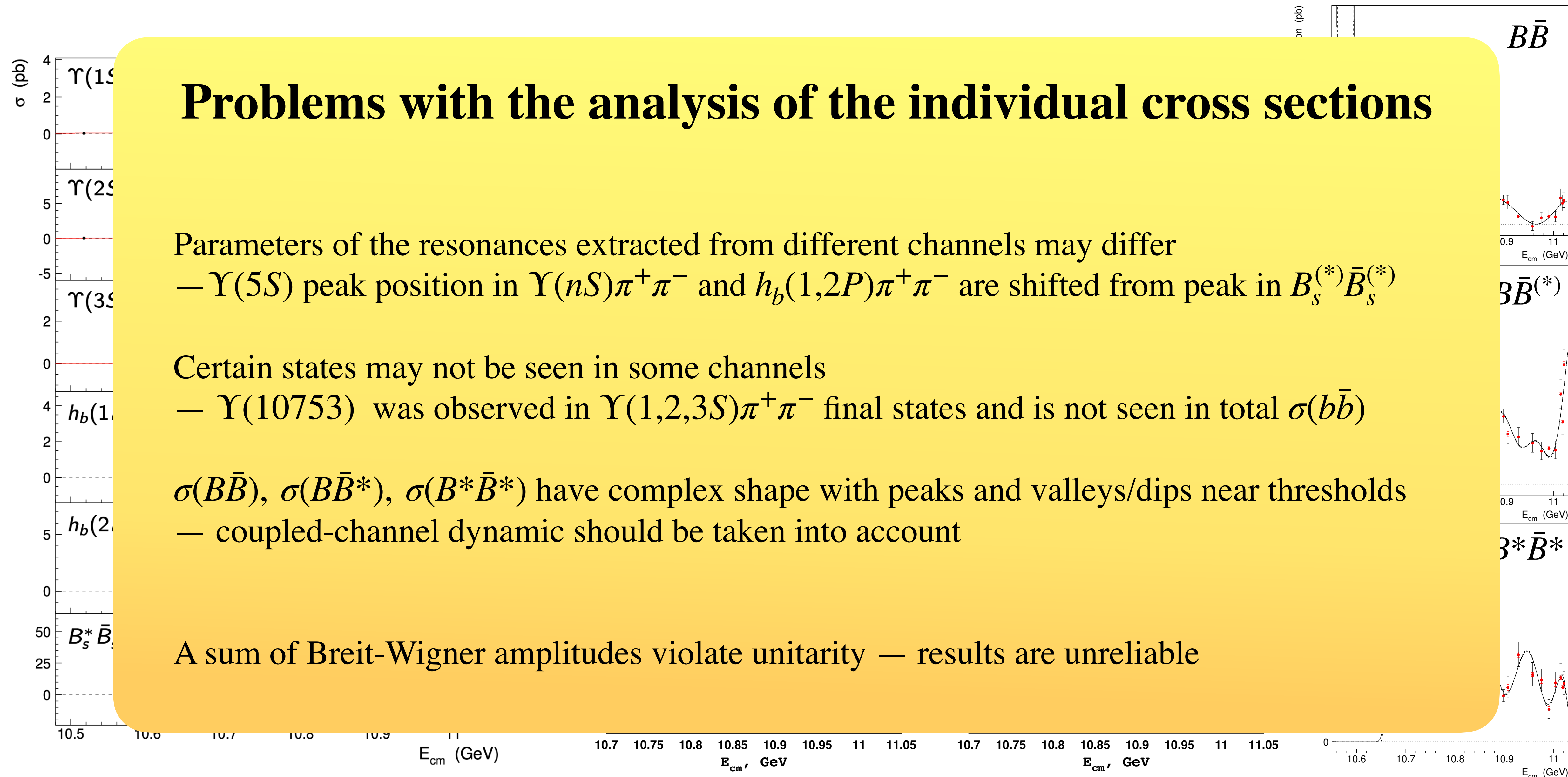
Certain states may not be seen in some channels

— $\Upsilon(10753)$ was observed in $\Upsilon(1,2,3S)\pi^+\pi^-$ final states and is not seen in total $\sigma(b\bar{b})$

$\sigma(B\bar{B})$, $\sigma(B\bar{B}^*)$, $\sigma(B^*\bar{B}^*)$ have complex shape with peaks and valleys/dips near thresholds

— coupled-channel dynamic should be taken into account

A sum of Breit-Wigner amplitudes violate unitarity — results are unreliable



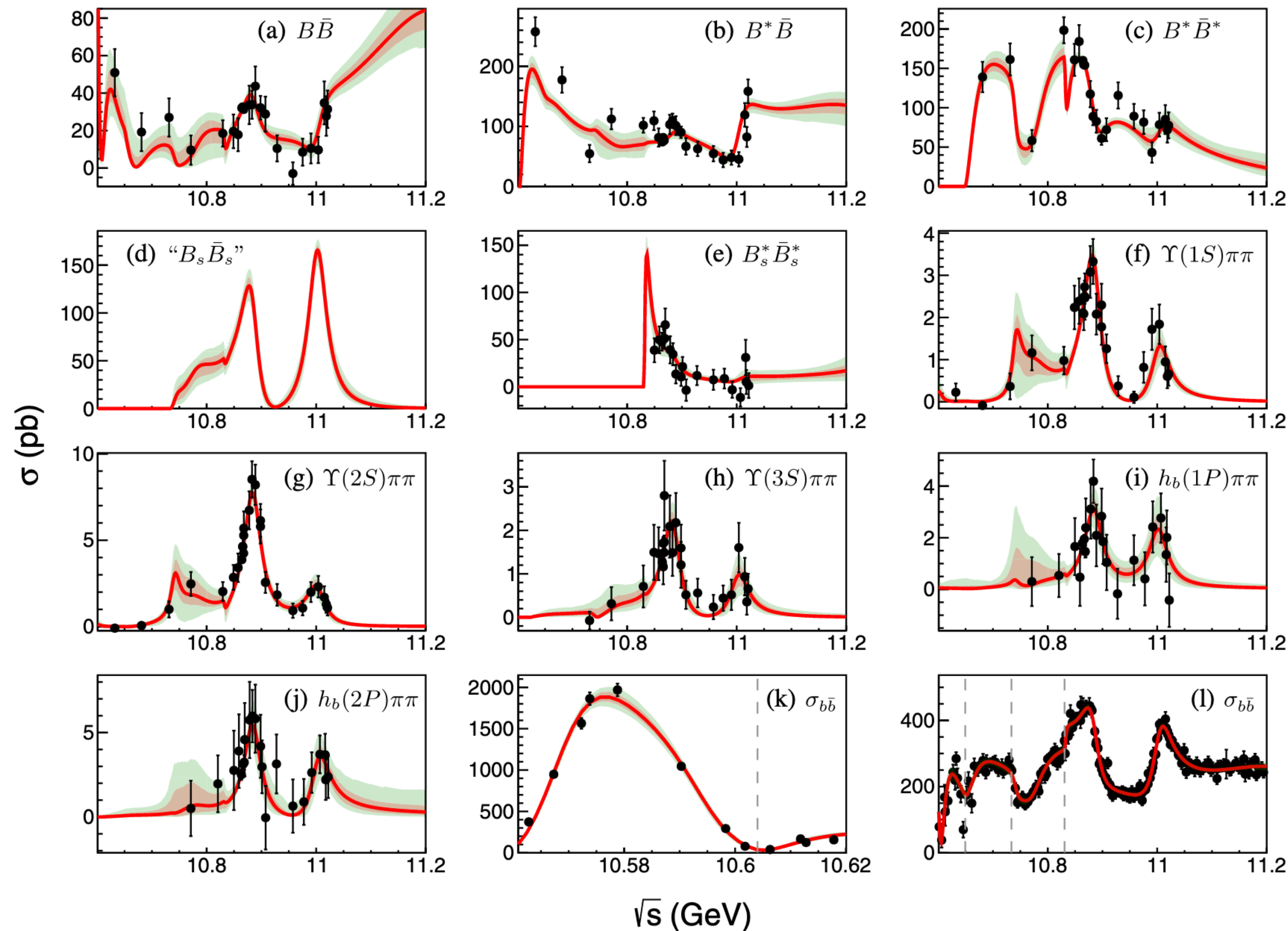
Global phenomenological analysis

N. HÜSKEN, R. E. MITCHELL, and E. S. SWANSON

[PRD 106 \(2022\) 9, 094013](#)

Used data:

$B\bar{B}$, $B^*\bar{B}$, $B^*\bar{B}^*$, $B_s^*\bar{B}_s^*$, $\Upsilon(1S)\pi^+\pi^-$,
 $\Upsilon(2S)\pi^+\pi^-$, $\Upsilon(3S)\pi^+\pi^-$, $h_b(1P)\pi^+\pi^-$,
 $h_b(2P)\pi^+\pi^-$, and $\sigma_{b\bar{b}}$



Poles for:

$\Upsilon(4S)$, $\Upsilon(10753)$, $\Upsilon(5S)$, $\Upsilon(6S)$

Various \mathcal{B} 's and electronic widths

The uncertainties are still large

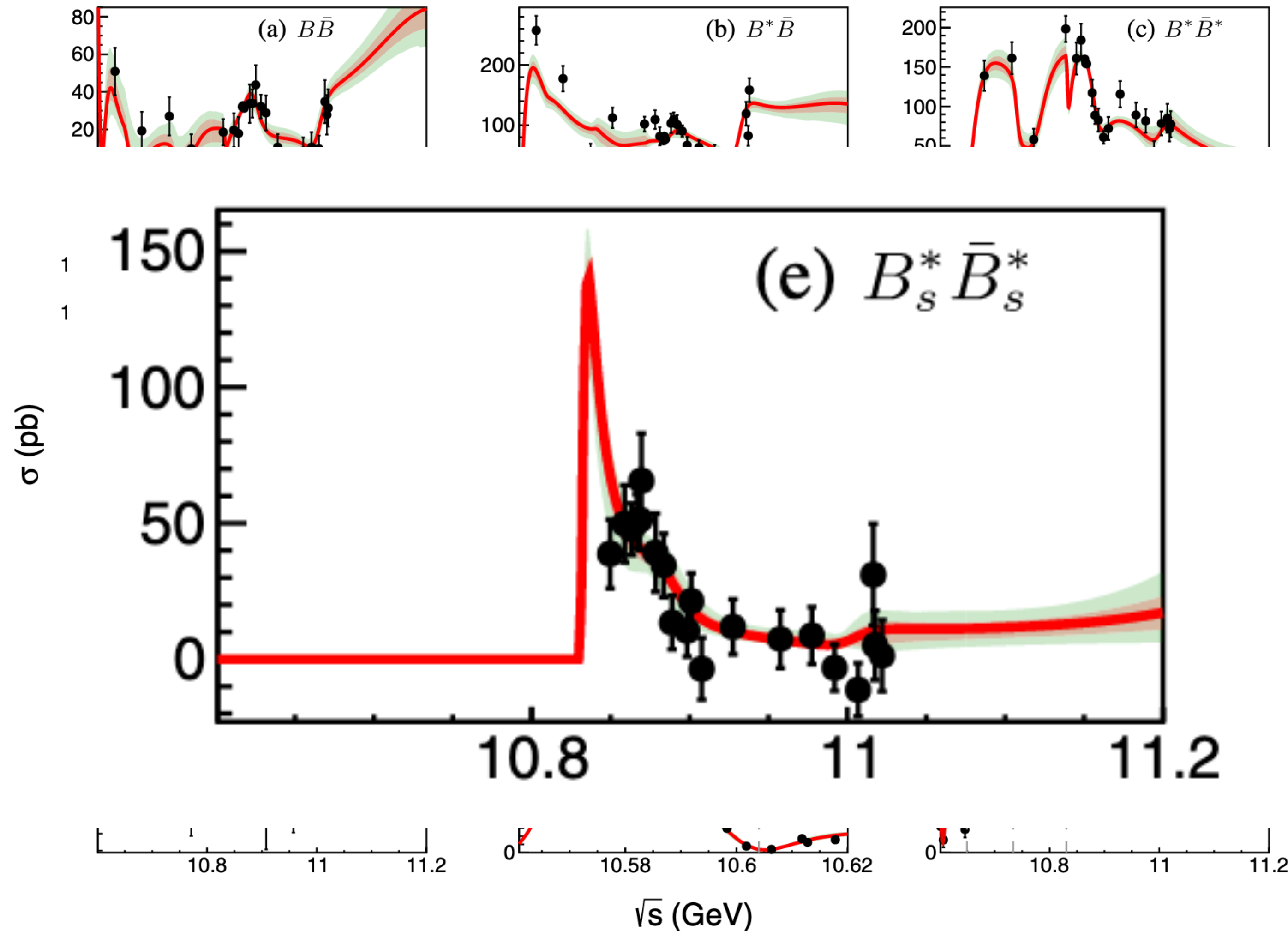


Need more data

Channel $e^+e^- \rightarrow B_s^{(*)}\bar{B}_s^{(*)}$

N. HÜSKEN, R. E. MITCHELL, and E. S. SWANSON

[PRD 106 \(2022\) 9, 094013](#)



$B_s^{(*)}\bar{B}_s^{(*)}$ channel — the current data doesn't constrain the fit function well

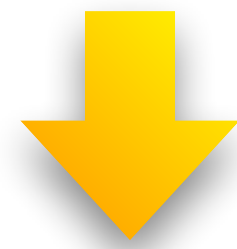


Need to improve the accuracy in $B_s^{(*)}\bar{B}_s^{(*)}$ channel

Summary of introduction

- Bottomonia **above** the open-bottom threshold are still **puzzling**
- Global **combined** analysis is promising approach to investigate the bottomonia nature
- **Every** additional channel is very **important** for the global analysis
- Improving **accuracy** in particular channels will allow better **constrained** fitting function

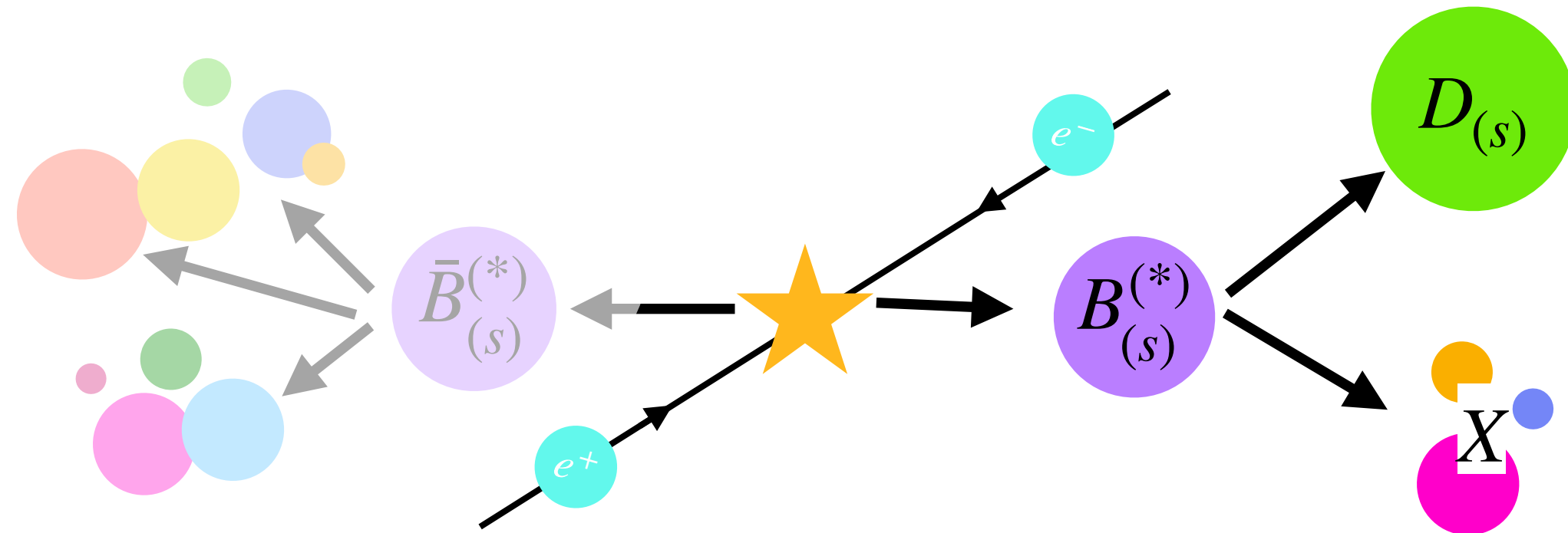
More experimental data and new measurements are welcome!



Goal:

Measuring $\sigma(e^+e^- \rightarrow B_s\bar{B}_sX)$ and $\sigma(e^+e^- \rightarrow B\bar{B}X)$ with high accuracy

Reconstruct inclusive D_s and D^0 at each energy scan point,



$x_p = \frac{p}{P_{max}}$ is used to separate continuum and $b\bar{b}$ - events;

$$\sigma(D_s X) \text{ and } \sigma(D^0 X)$$

Measured cross sections can be expressed as:

$$(60.2 \pm 6.2) \%$$

$$(8.7 \pm 1.2) \%$$

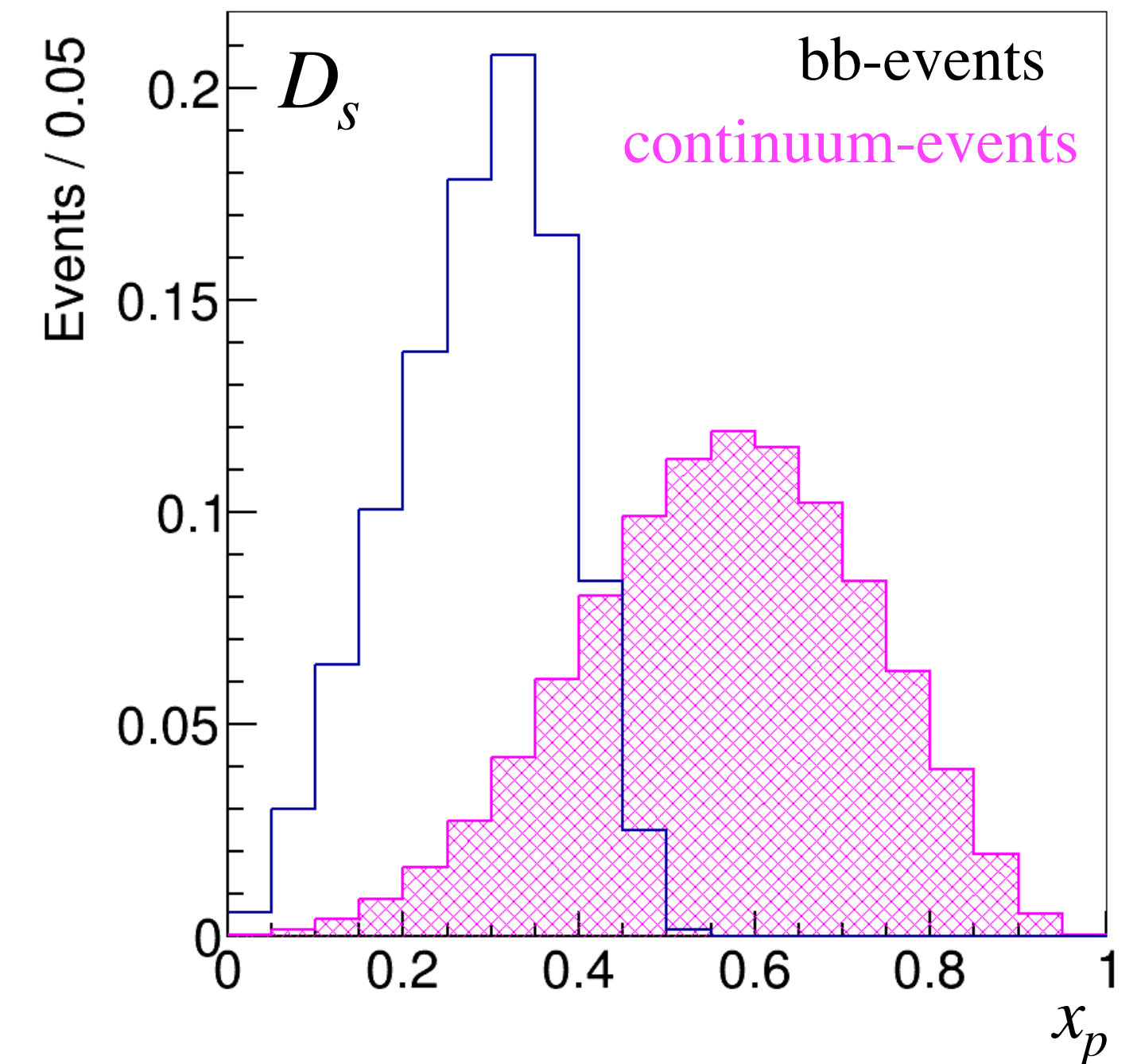
$$\sigma(D_s X)/2 = \mathcal{B}(B_s \rightarrow D_s X) \cdot \sigma(B_s \bar{B}_s X) + \mathcal{B}(B \rightarrow D_s X) \cdot \sigma(B \bar{B} X)$$

$$\sigma(D^0 X)/2 = \mathcal{B}(B_s \rightarrow D^0 X) \cdot \sigma(B_s \bar{B}_s X) + \mathcal{B}(B \rightarrow D^0 X) \cdot \sigma(B \bar{B} X)$$

$$\text{model: } (8 \pm 7) \%$$

$$(64.0 \pm 3.0) \%$$

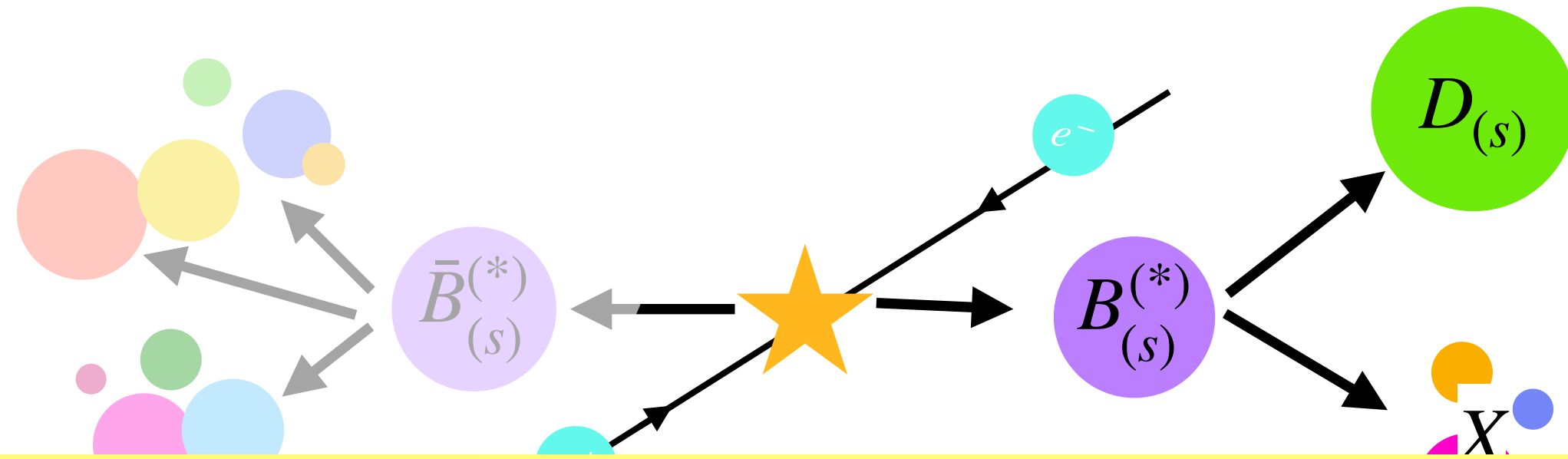
MC at $\Upsilon(5S)$ energy



Explicite formulas for:

$$\sigma(B_s \bar{B}_s X) \text{ and } \sigma(B \bar{B} X)$$

Reconstruct inclusive D_s and D^0 at each energy scan point,



but $\mathcal{B}(B_s \rightarrow D_s X)$ has large uncertainty
 $\mathcal{B}(B_s \rightarrow D^0 X)$ is not measured, only prediction

$(60.2 \pm 6.2) \%$

$(8.7 \pm 1.2) \%$

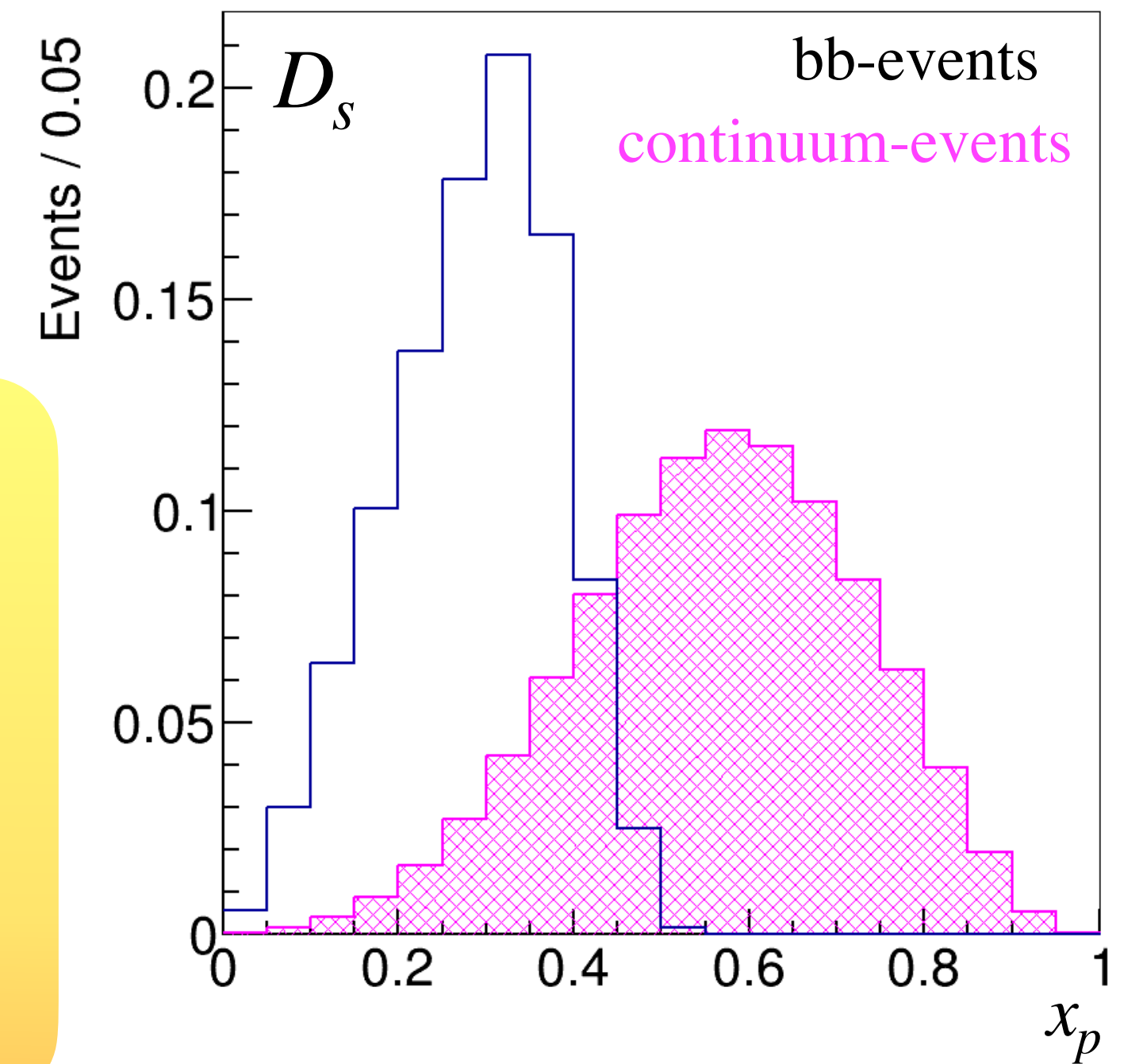
$$\sigma(D_s X)/2 = \mathcal{B}(B_s \rightarrow D_s X) \cdot \sigma(B_s \bar{B}_s X) + \mathcal{B}(B \rightarrow D_s X) \cdot \sigma(B \bar{B} X)$$

$$\sigma(D^0 X)/2 = \mathcal{B}(B_s \rightarrow D^0 X) \cdot \sigma(B_s \bar{B}_s X) + \mathcal{B}(B \rightarrow D^0 X) \cdot \sigma(B \bar{B} X)$$

model: $(8 \pm 7) \%$

$(64.0 \pm 3.0) \%$

MC at $\Upsilon(5S)$ energy



Explicite formulas for:

$\sigma(B_s \bar{B}_s X)$ and $\sigma(B \bar{B} X)$

No B_s at energy point near $\Upsilon(4S)$:

Measure with high accuracy $\mathcal{B}(B \rightarrow D_s X)$, $\mathcal{B}(B \rightarrow D^0 X)$

At energy point near $\Upsilon(5S)$:

$$\sigma(D_s X) |_{\Upsilon(5S)}/2 = \mathcal{B}(B_s \rightarrow D_s X) \cdot \sigma(B_s \bar{B}_s X) |_{\Upsilon(5S)} + \mathcal{B}(B \rightarrow D_s X) \cdot \sigma(B \bar{B} X) |_{\Upsilon(5S)}$$

$$\sigma(D^0 X) |_{\Upsilon(5S)}/2 = \mathcal{B}(B_s \rightarrow D^0 X) \cdot \sigma(B_s \bar{B}_s X) |_{\Upsilon(5S)} + \mathcal{B}(B \rightarrow D^0 X) \cdot \sigma(B \bar{B} X) |_{\Upsilon(5S)}$$

$$C = \frac{\mathcal{B}(B_s \rightarrow D^0 X)}{\mathcal{B}(B_s \rightarrow D_s X)} = \frac{\sigma(D^0 X) |_{\Upsilon(5S)} - \mathcal{B}(B \rightarrow D^0 X) \cdot \sigma(B \bar{B} X) |_{\Upsilon(5S)}}{\sigma(D_s^\pm X) |_{\Upsilon(5S)} - \mathcal{B}(B \rightarrow D_s X) \cdot \sigma(B \bar{B} X) |_{\Upsilon(5S)}}$$

We can measure using $\Upsilon(5S)$ data

We can measure using $\Upsilon(4S)$ data

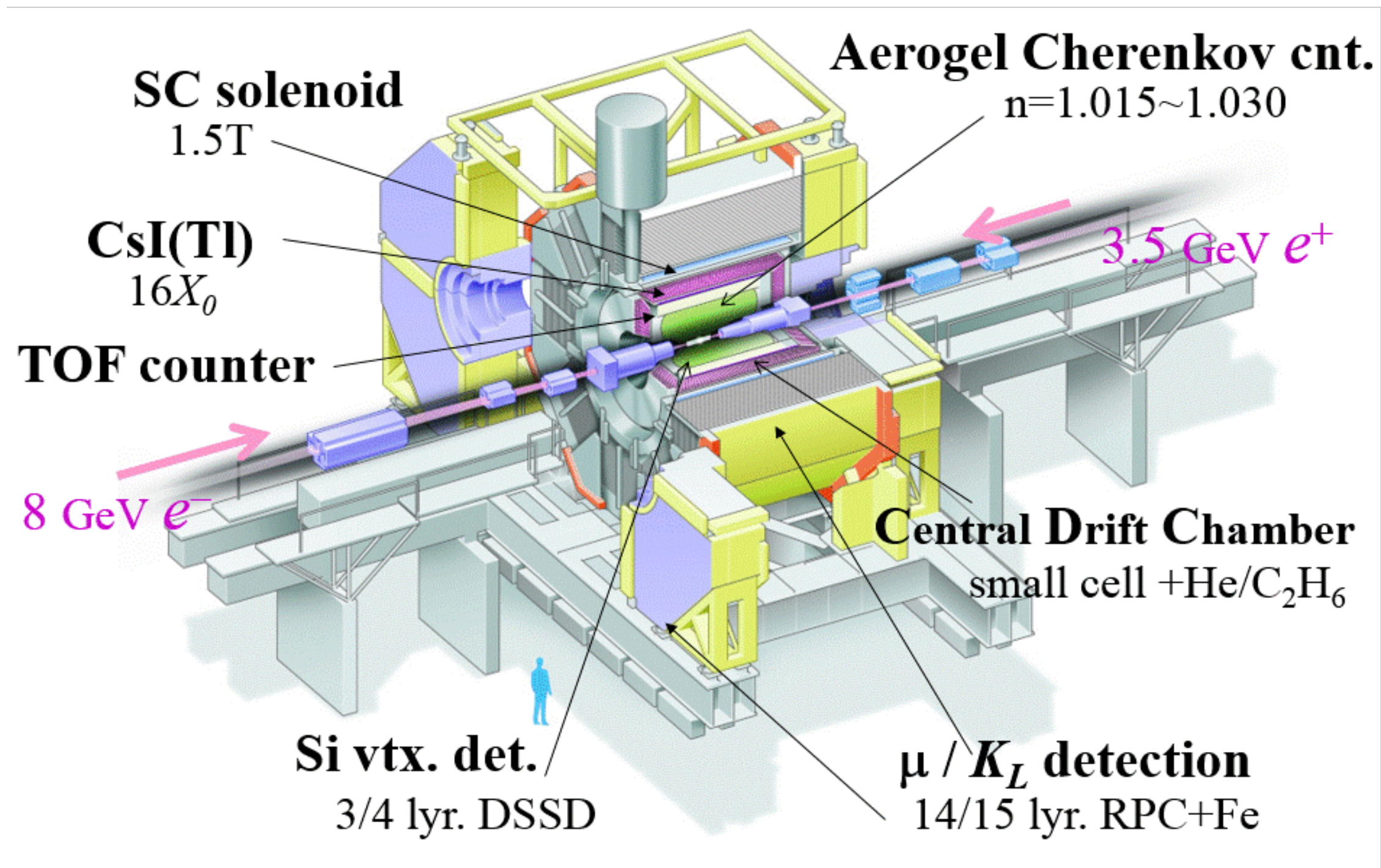
from [JHEP 06 \(2021\) 137](#)

At scan points:

$$\begin{cases} \sigma(D_s X)/2 = \mathcal{B}(B_s \rightarrow D_s X) \cdot \sigma(B_s \bar{B}_s X) + \mathcal{B}(B \rightarrow D_s X) \cdot \sigma(B \bar{B} X) \\ \sigma(D^0 X)/2 = C \cdot \mathcal{B}(B_s \rightarrow D_s X) \cdot \sigma(B_s \bar{B}_s X) + \mathcal{B}(B \rightarrow D^0 X) \cdot \sigma(B \bar{B} X) \end{cases}$$

Solving eq's system:  energy dependence of the $\sigma(B_s \bar{B}_s X) \cdot \mathcal{B}(B_s \rightarrow D_s X)$ and $\sigma(B \bar{B} X)$

Data samples and selection criteria



Charged tracks:

$$|dr| < 0.5 \text{ cm and } |dz| < 2.0 \text{ cm}$$

$$\mathcal{L}_{K/\pi} = \mathcal{L}_K / (\mathcal{L}_K + \mathcal{L}_\pi) > 0.6$$

$$\mathcal{L}_{\pi/K} = \mathcal{L}_\pi / (\mathcal{L}_K + \mathcal{L}_\pi) > 0.1$$

$$D_s^+ \rightarrow \phi\pi^+, \phi \rightarrow K^+K^-$$

$$|M_{inv}(K^-K^+) - m_\phi| < 19 \text{ MeV}/c^2$$

$$|\cos \theta_{hel}| > 0.25$$

$$1.9 < M(D_s) < 2.02 \text{ GeV}/c^2$$

θ_{hel} — the angle between K^+ and D_s^+ in ϕ rest frame

$$D^0 \rightarrow K^-\pi^+$$

$$1.8 < M(D^0) < 1.932 \text{ GeV}/c^2$$

Data used in this analysis:

data at $\Upsilon(4S)$ energy:

$$\mathcal{L}_{4S} = 571 \text{ fb}^{-1}$$

data at $\Upsilon(5S)$ energy:

$$\mathcal{L}_{5S} = 121 \text{ fb}^{-1}$$

data at $E_{cm} = 10.52 \text{ GeV}$:

$$\mathcal{L}_{cont} = 74 \text{ fb}^{-1}$$

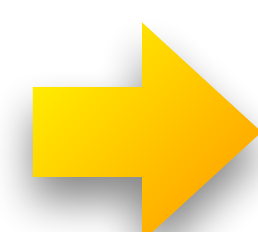
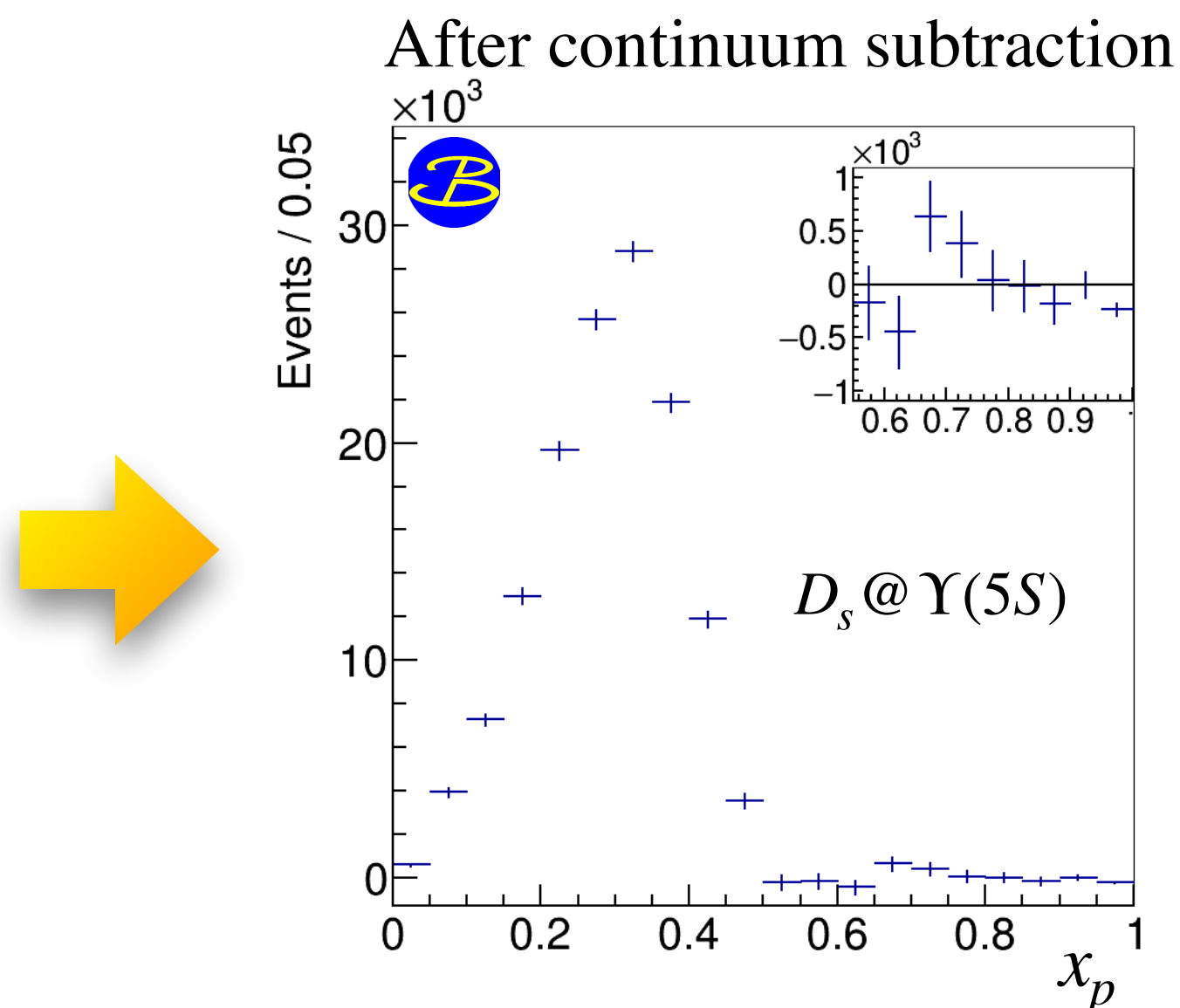
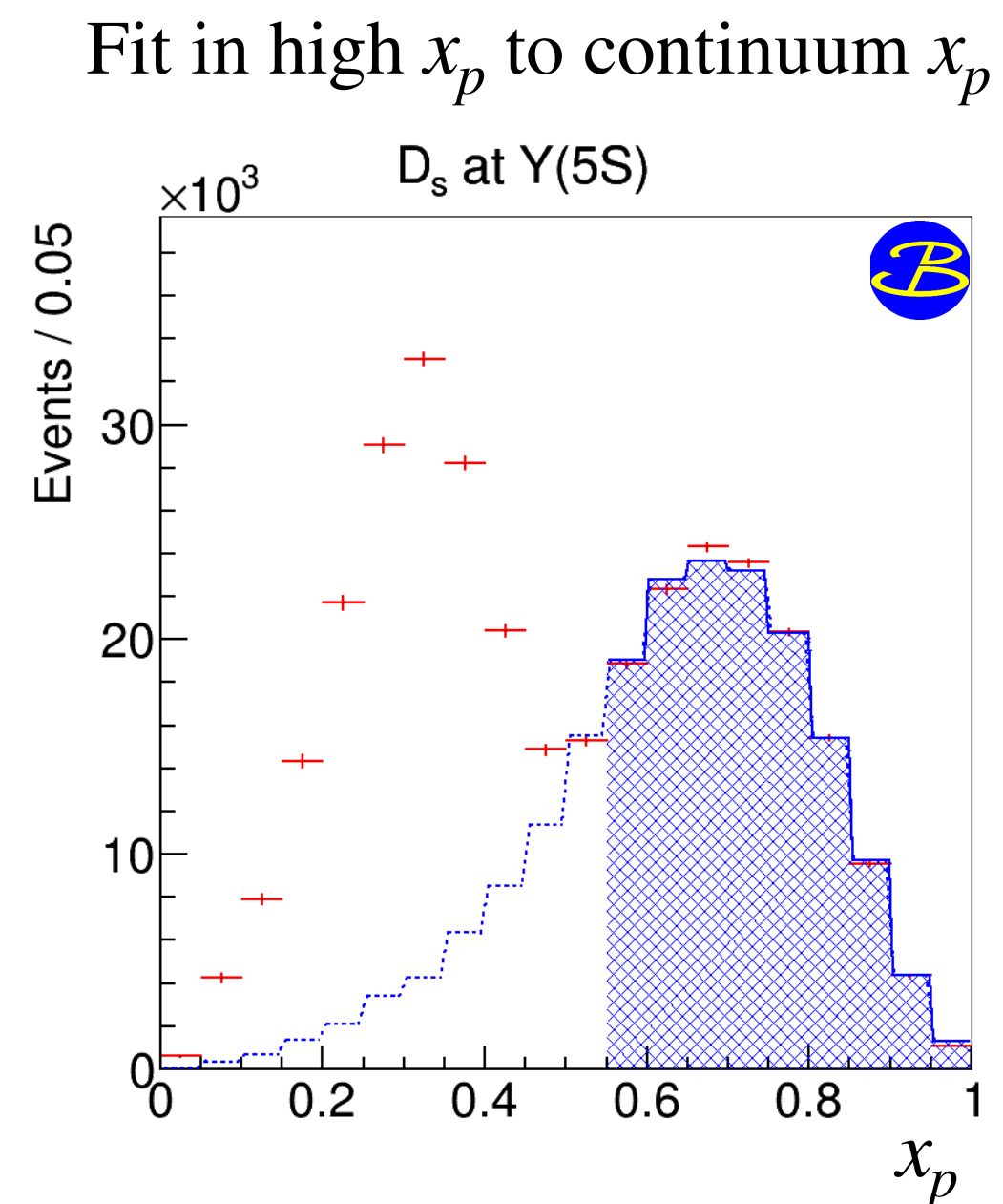
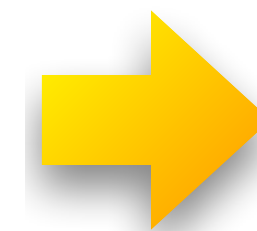
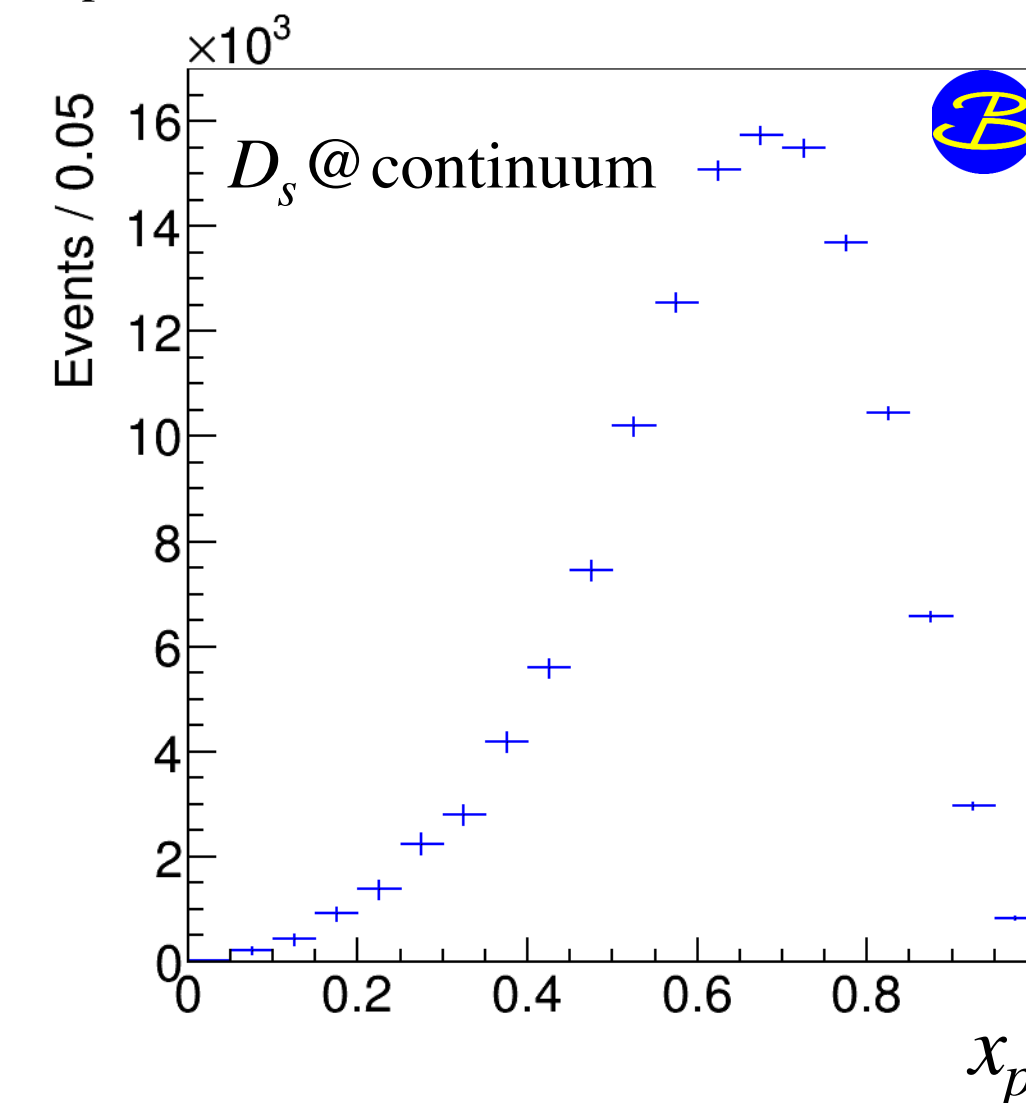
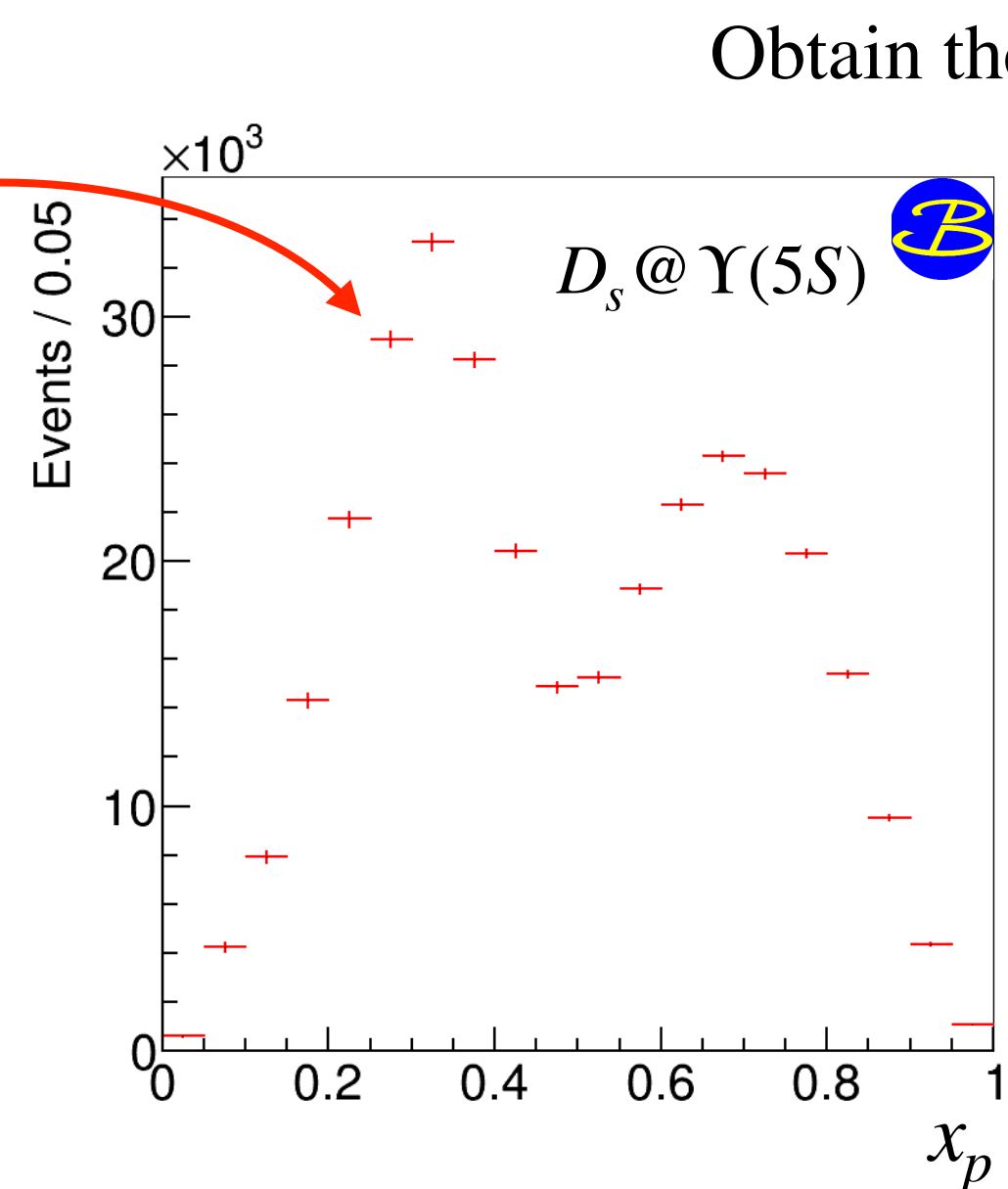
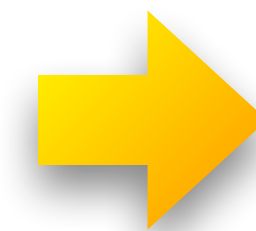
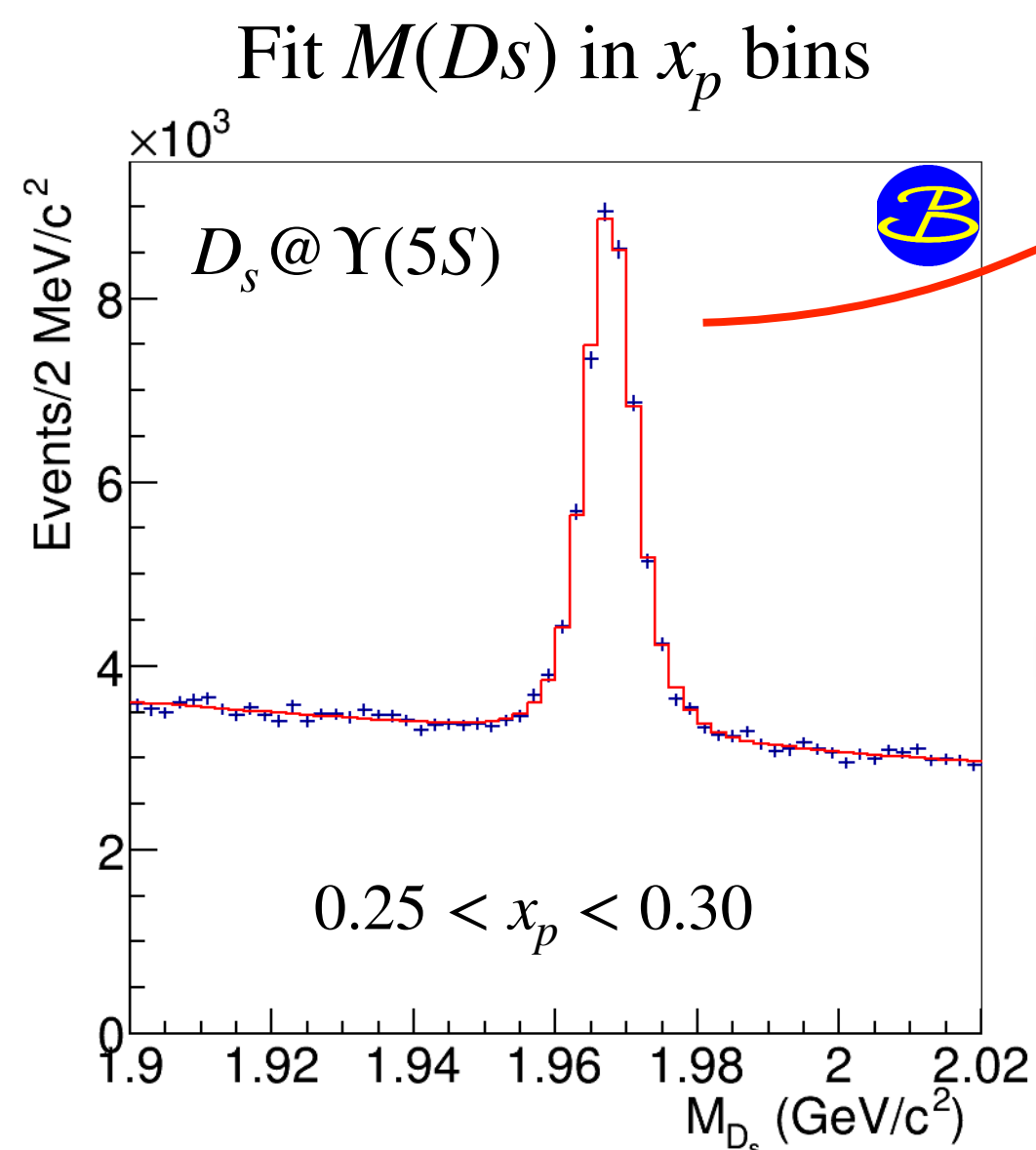
(continuum data sample)

22 energy scan points:

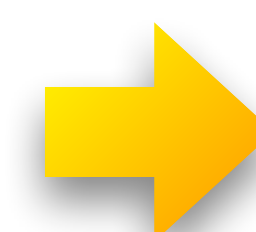
$$\mathcal{L}_i \approx 1 \text{ fb}^{-1}$$

E_{cm} from 10.63 GeV to 11.02 GeV

Method



D cross sections

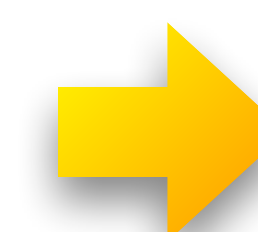


D cross sections at $\Upsilon(4S)$ and $\Upsilon(5S)$:

$$\mathcal{B}(B \rightarrow D_s X)$$

$$\mathcal{B}(B \rightarrow D^0 X)$$

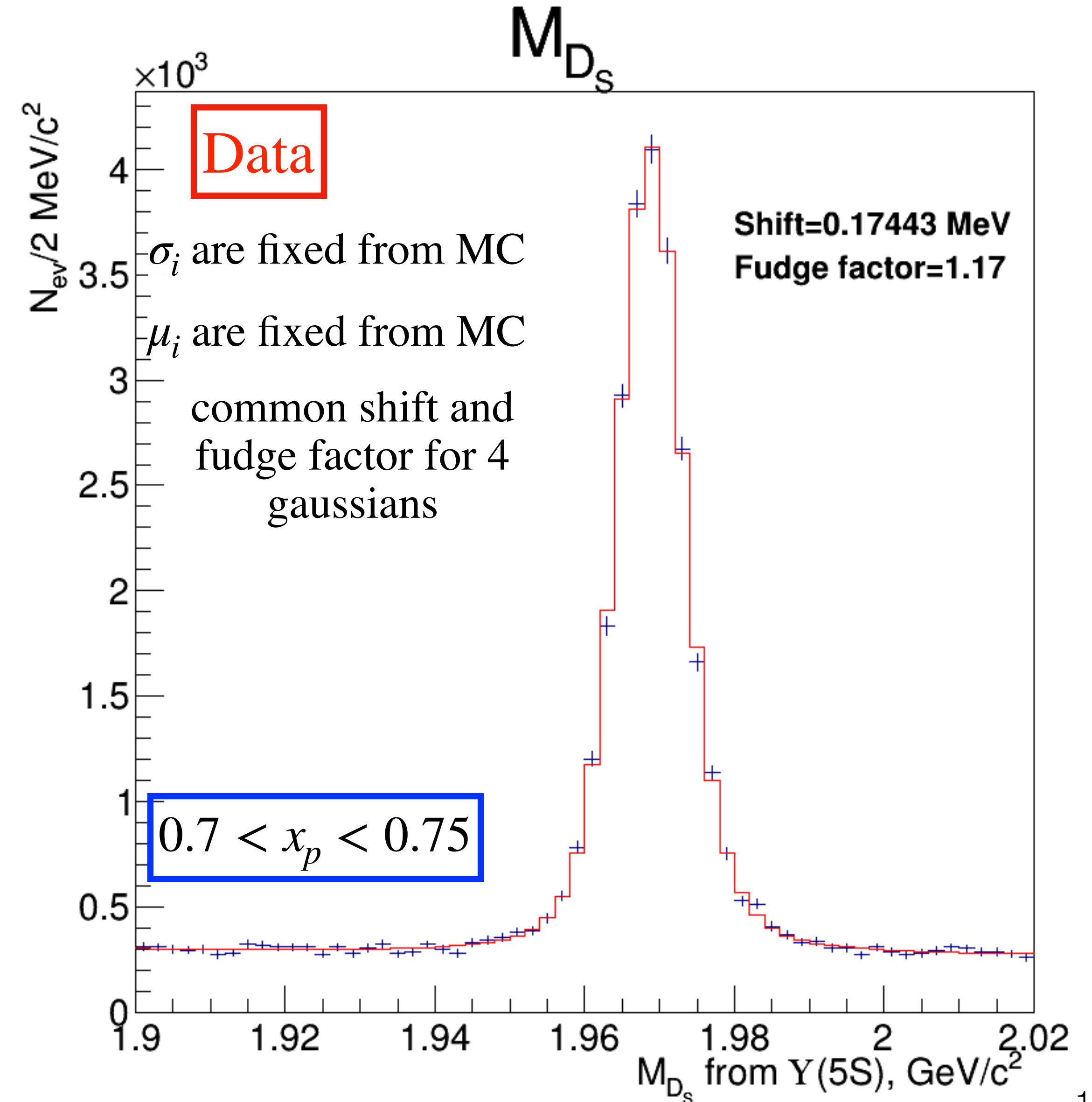
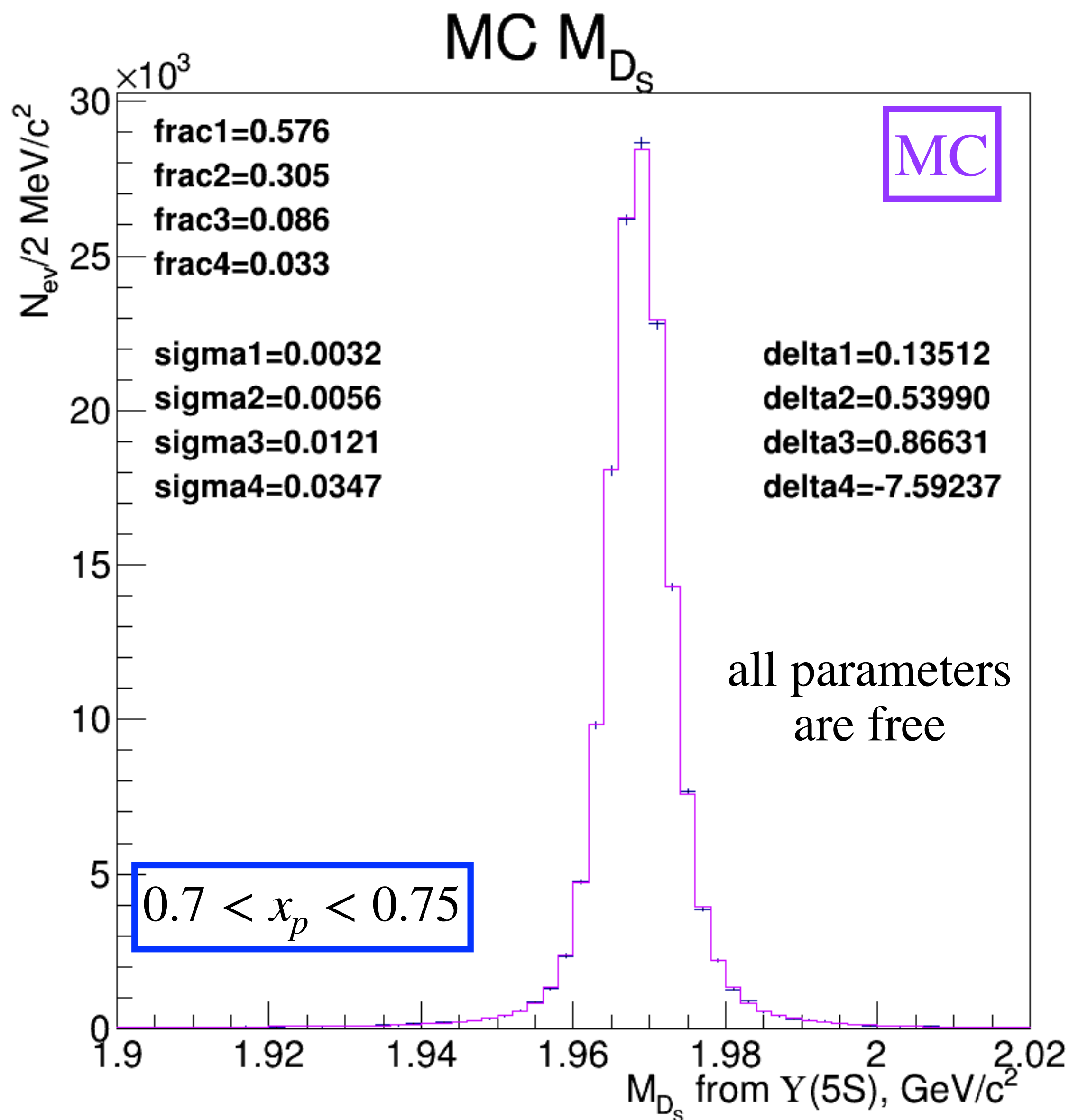
$$\frac{\mathcal{B}(B_s \rightarrow D^0 X)}{\mathcal{B}(B_s \rightarrow D_s X)}$$



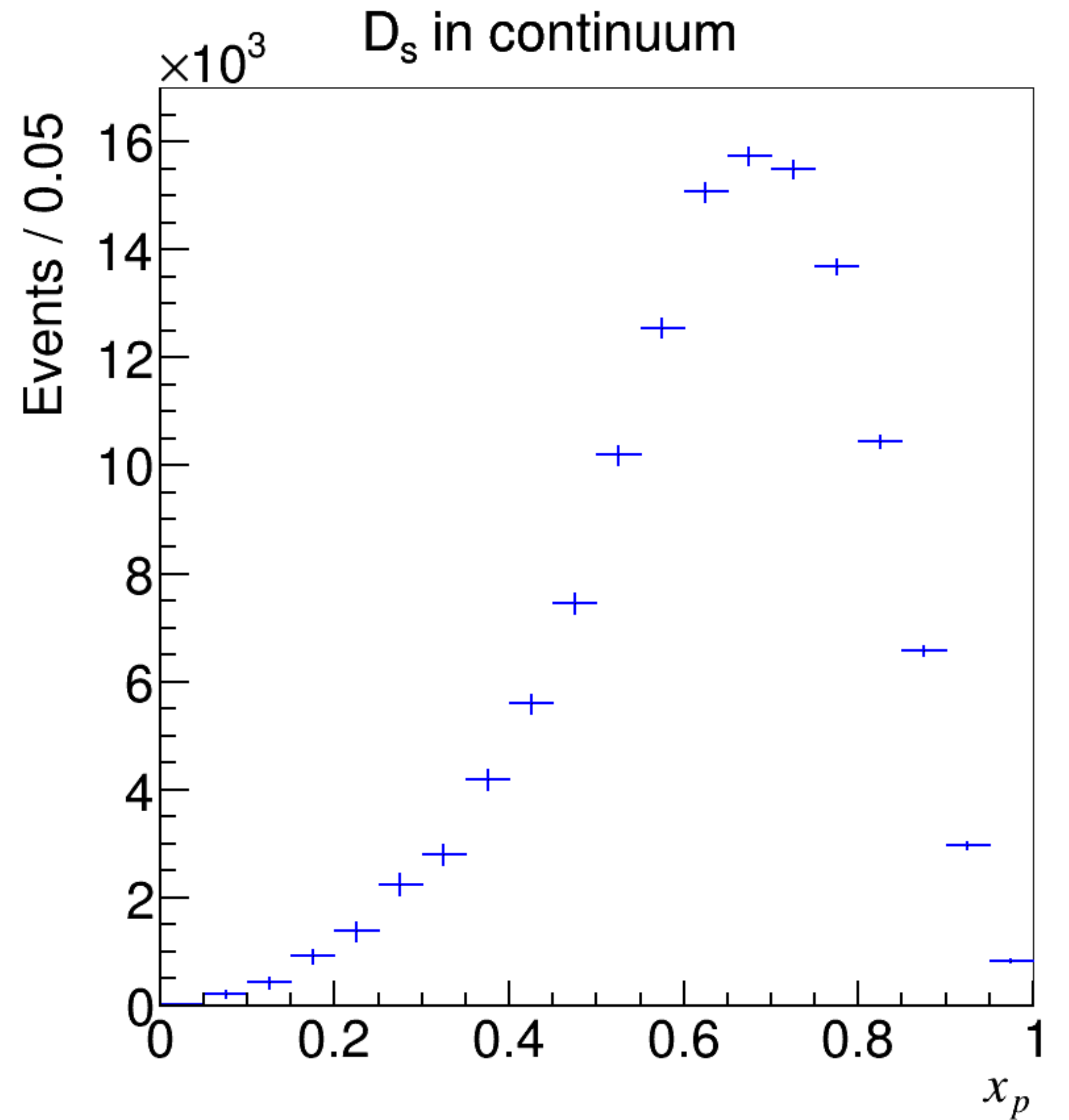
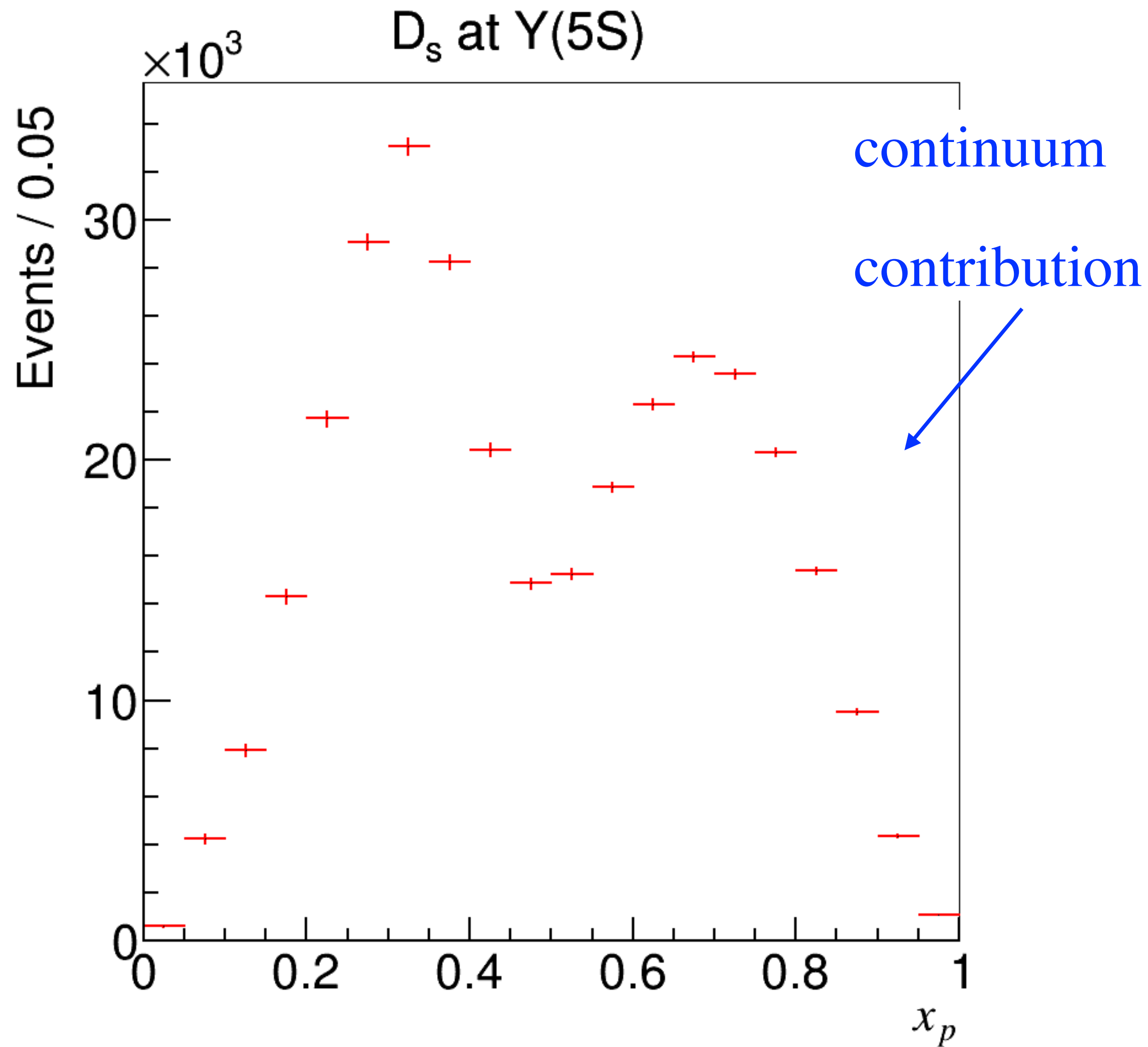
At each scan point:

$B_s \bar{B}_s X$ and $B \bar{B} X$
cross sections

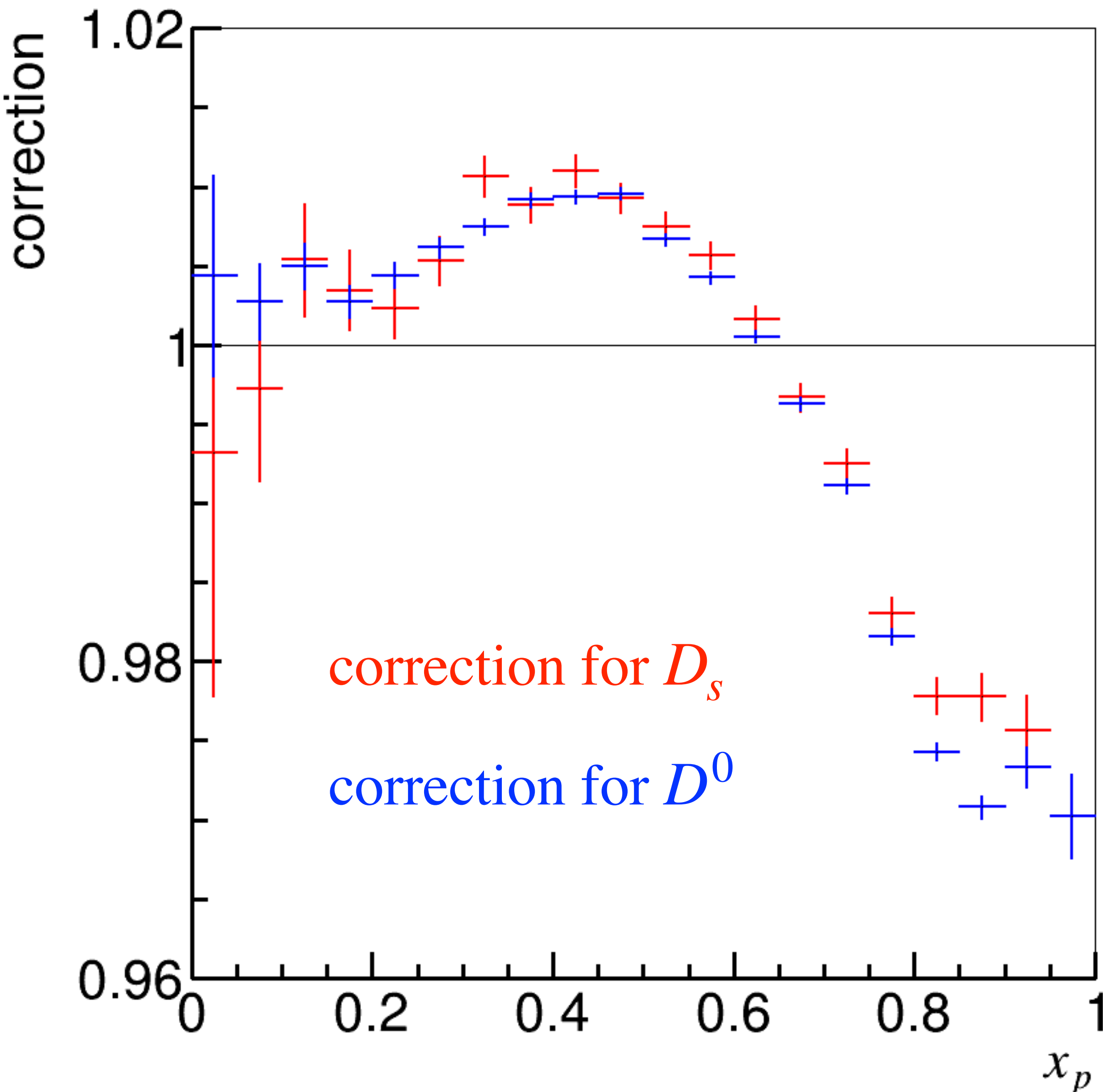
Fit the D_s mass distributions in the different x_p bins at $\Upsilon(5S)$



x_p spectra of D_s at $\Upsilon(5S)$ and below $\Upsilon(4S)$



Continuum spectrum correction



Due to the evolution of fragmentation with energy the shape of the continuum spectrum changes noticeably between $E_{\text{cm}} = 10.52$ GeV and the $\Upsilon(5S)$ energy



The continuum x_p spectra should be corrected

Belle II generators:
KKMC — initial state radiation,
Pythia 8.2 — c-quark fragmentation

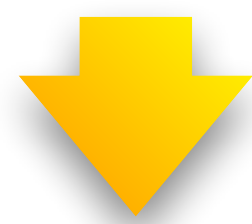
x_p spectra at $\Upsilon(5S)$ and $\Upsilon(4S)$ data

Red points — on-resonance data

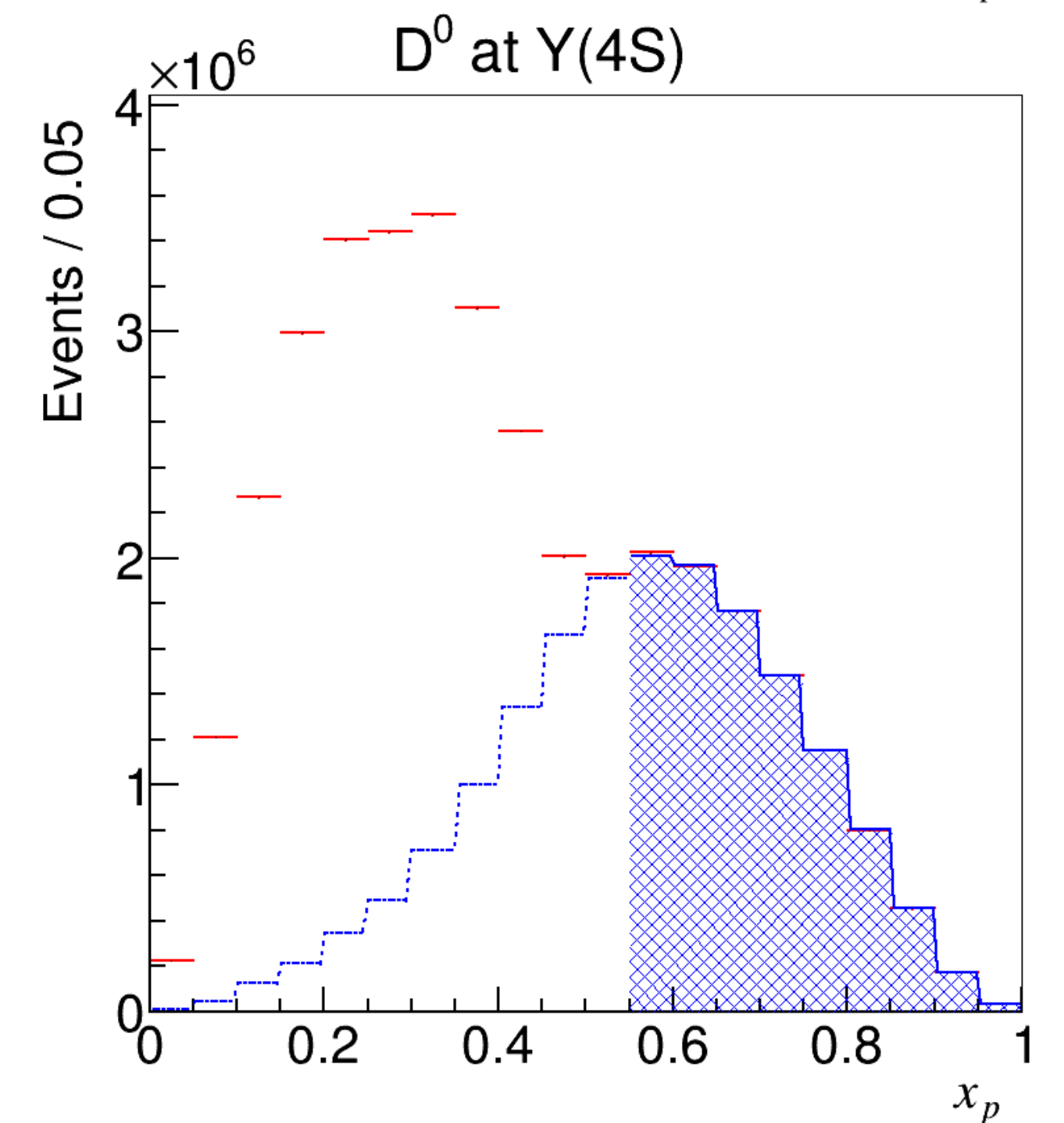
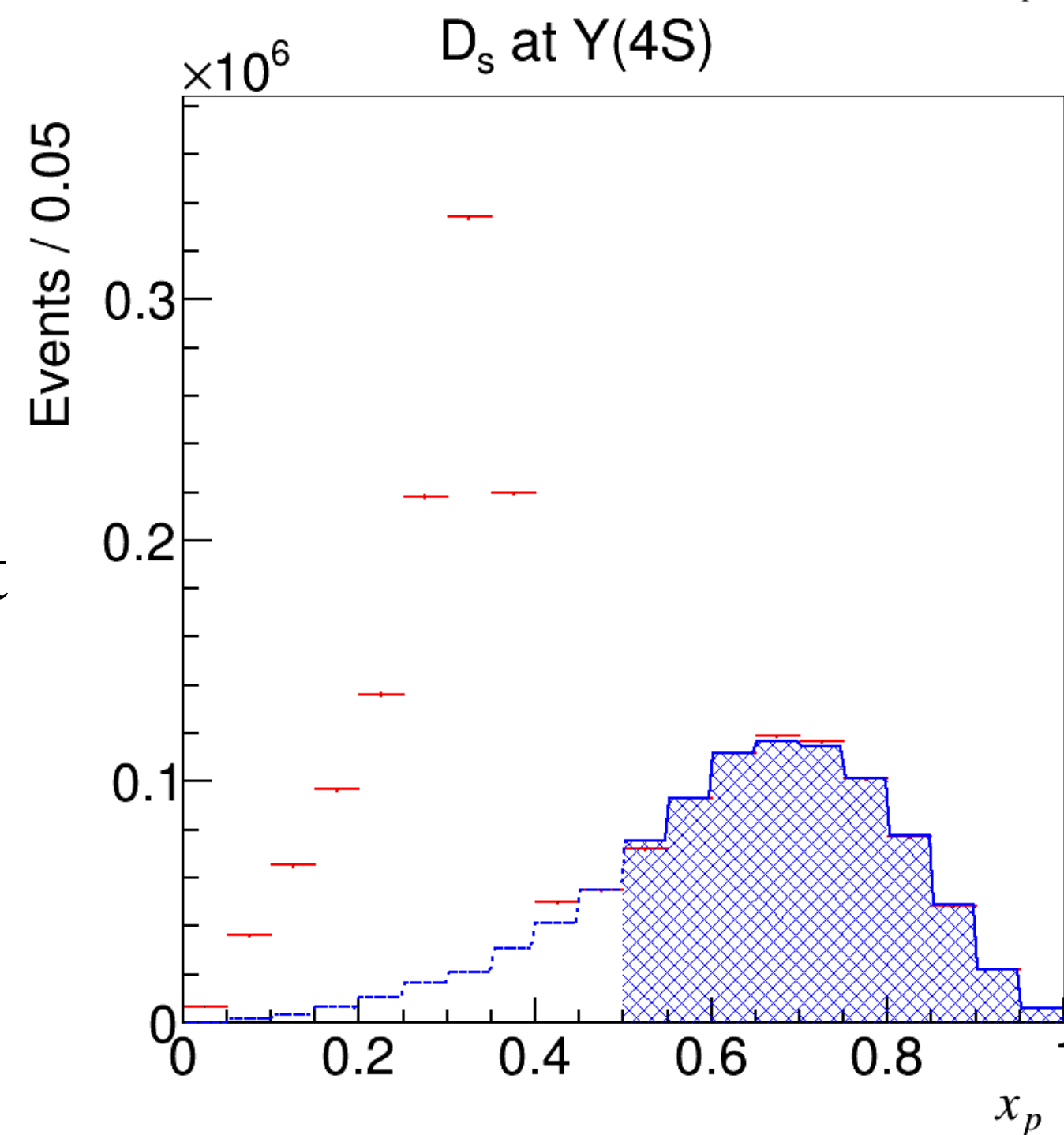
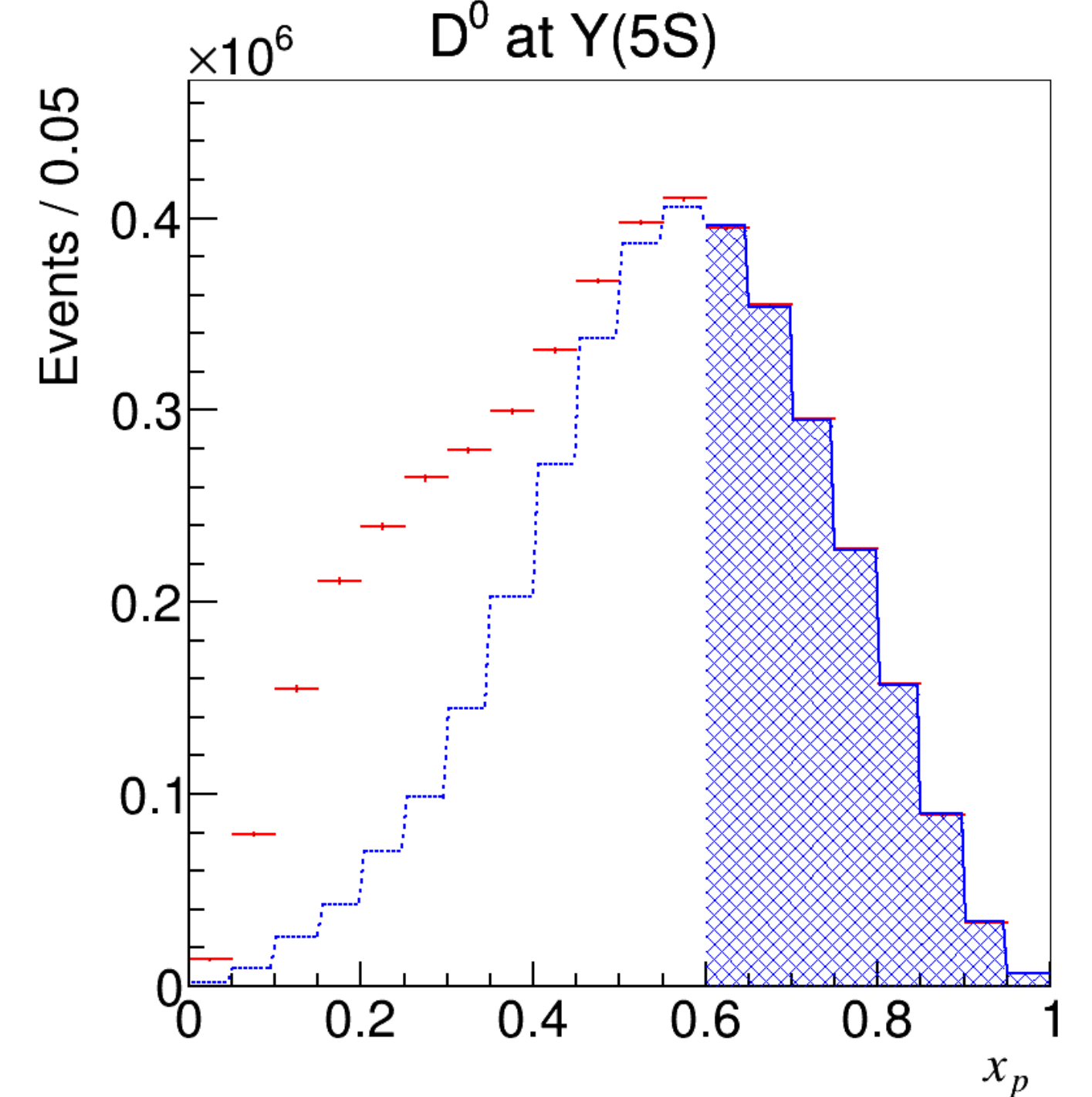
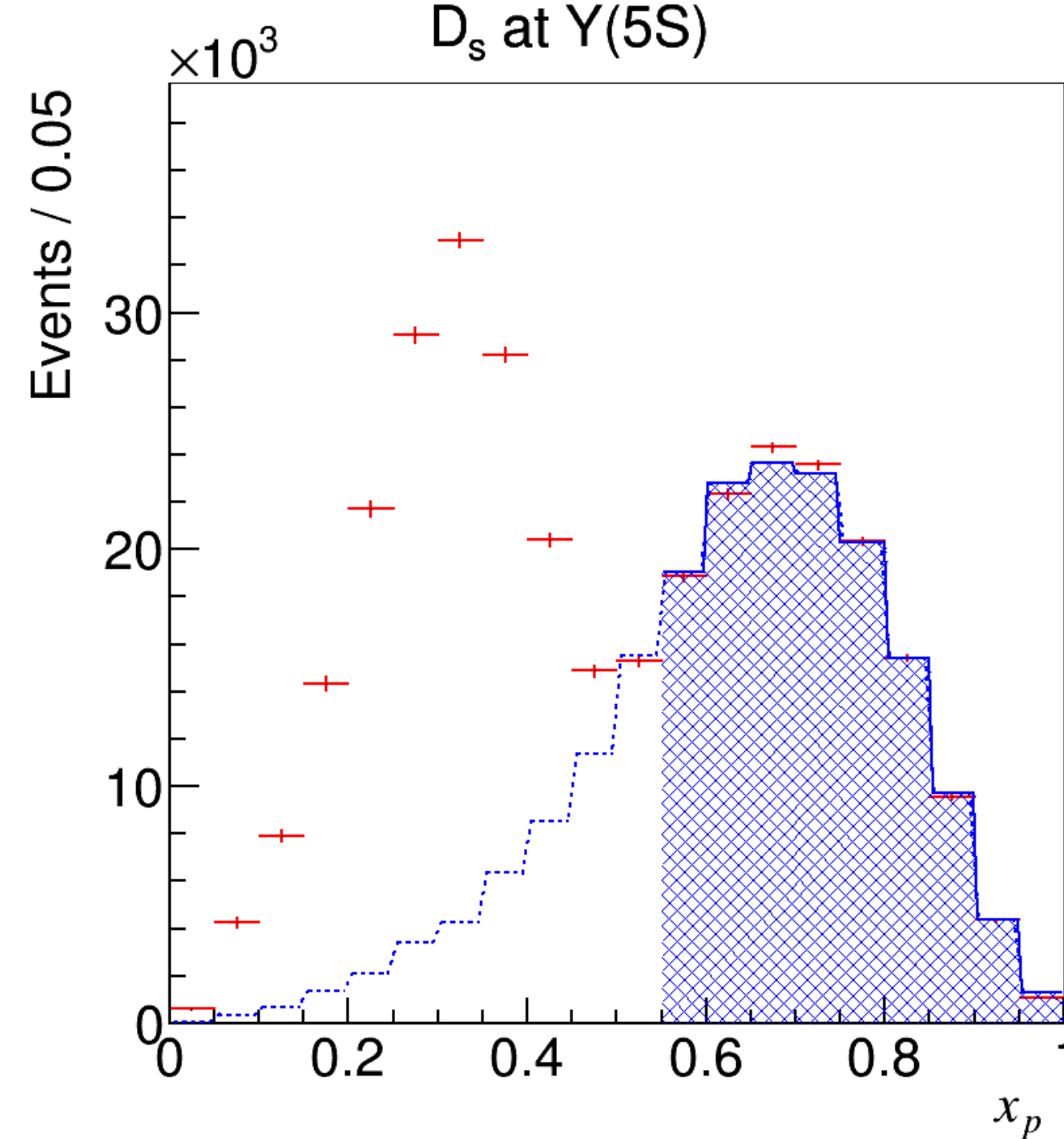
We fit the large x_p part of the on-resonance spectra to find the continuum contribution in the $b\bar{b}$ region

Fitting function — shape of the x_p spectra for the data below the $\Upsilon(4S)$

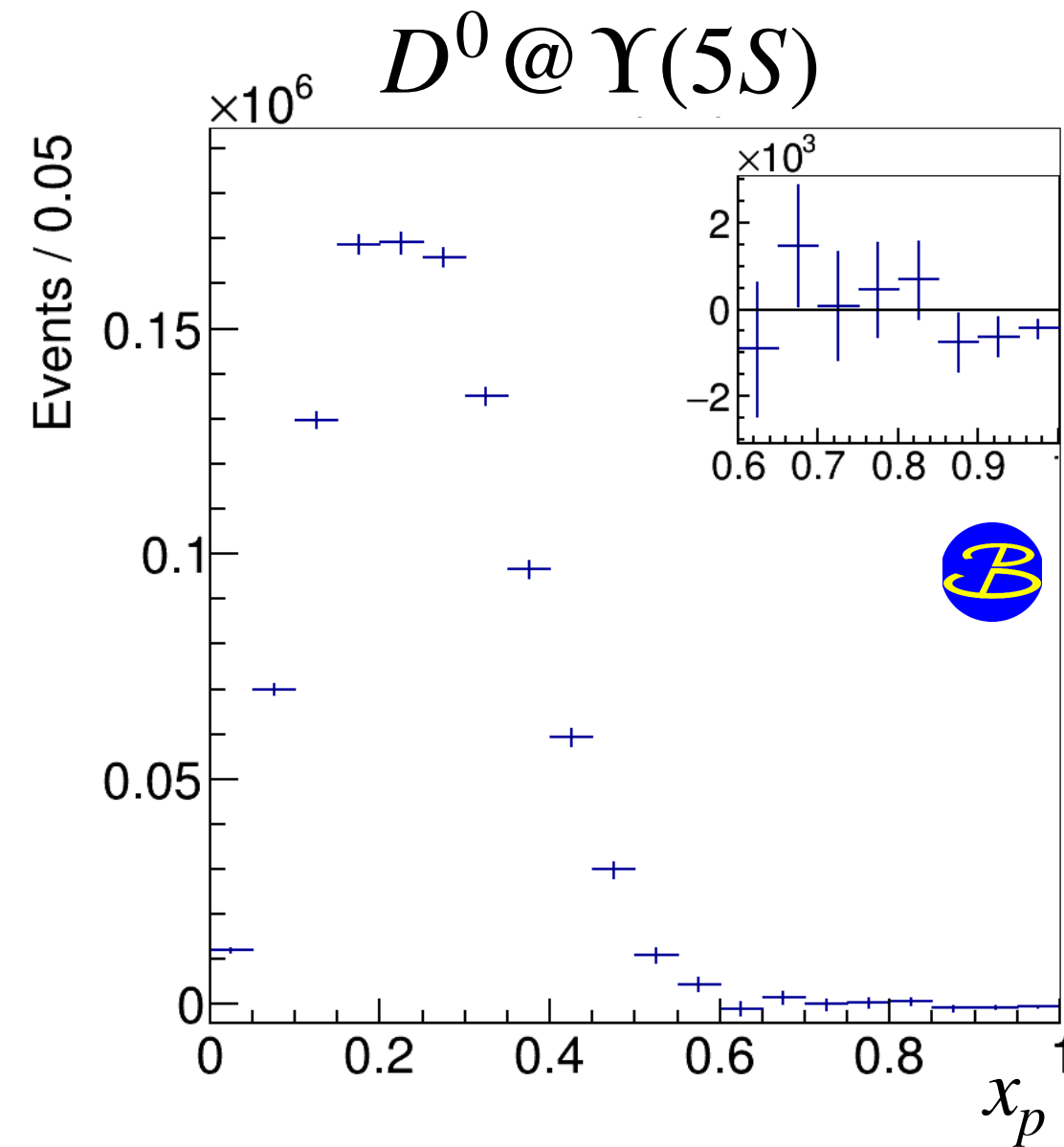
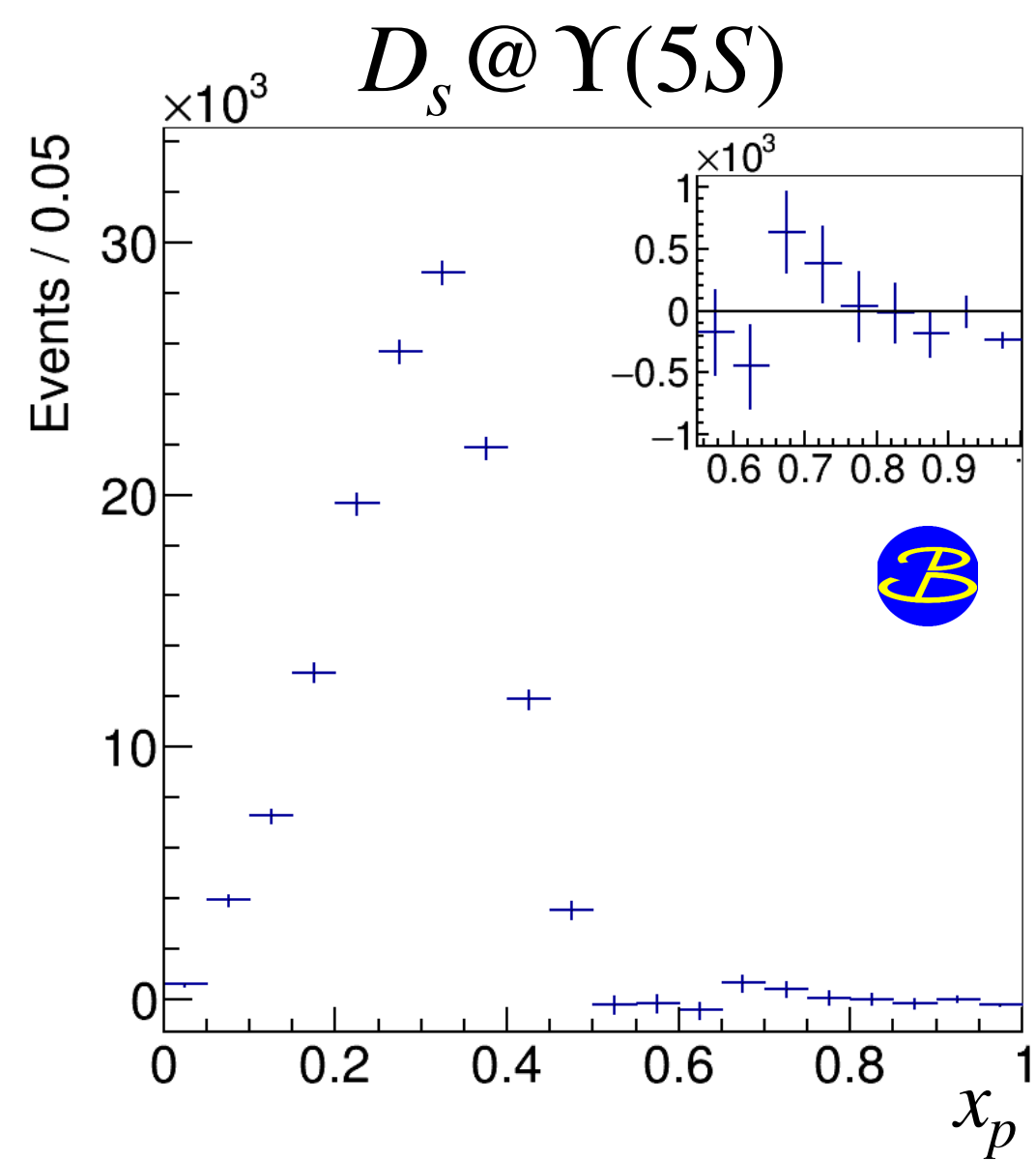
Blue hatched histograms — fit results
Open dashed histograms — extrapolation of the continuum component



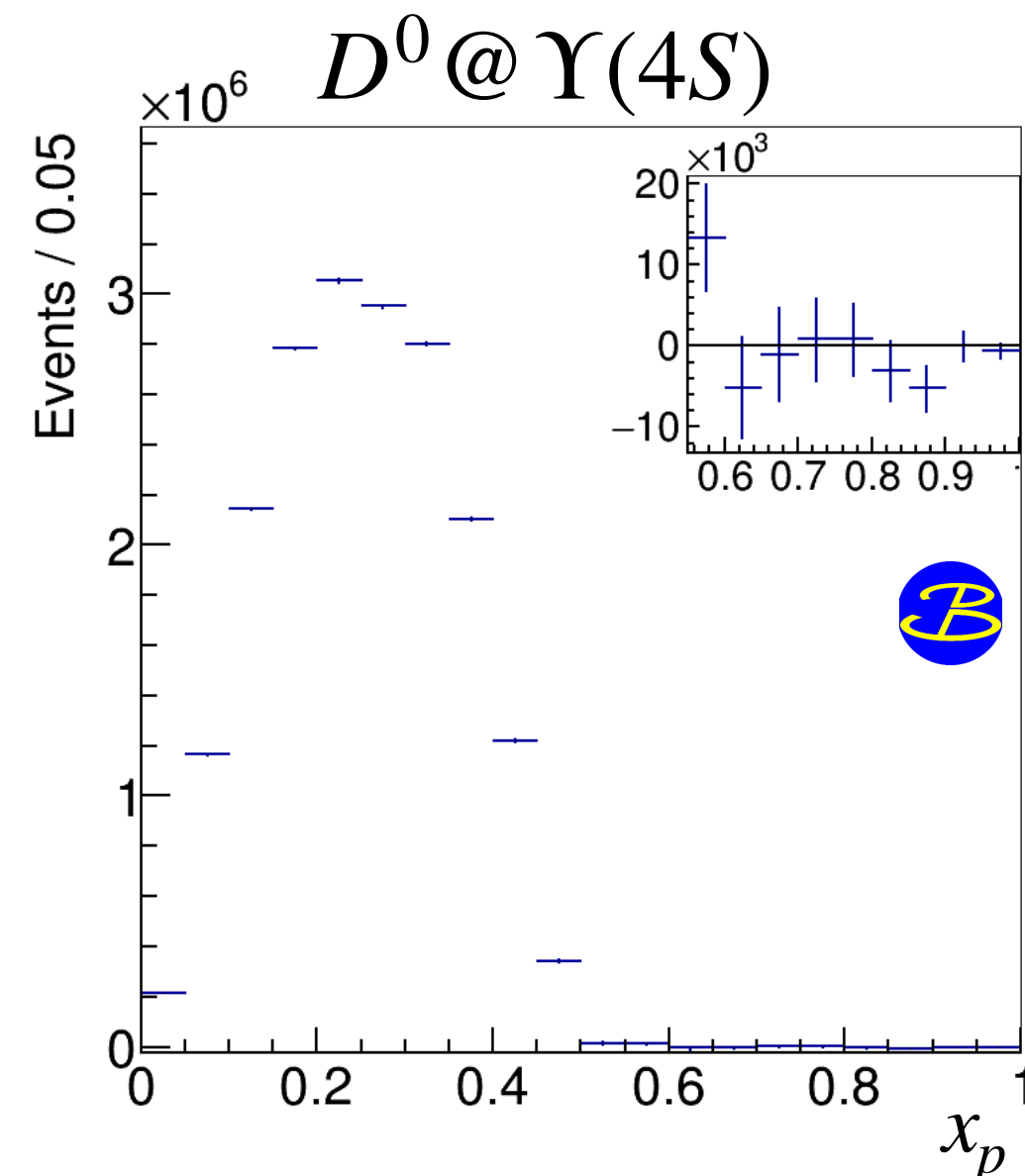
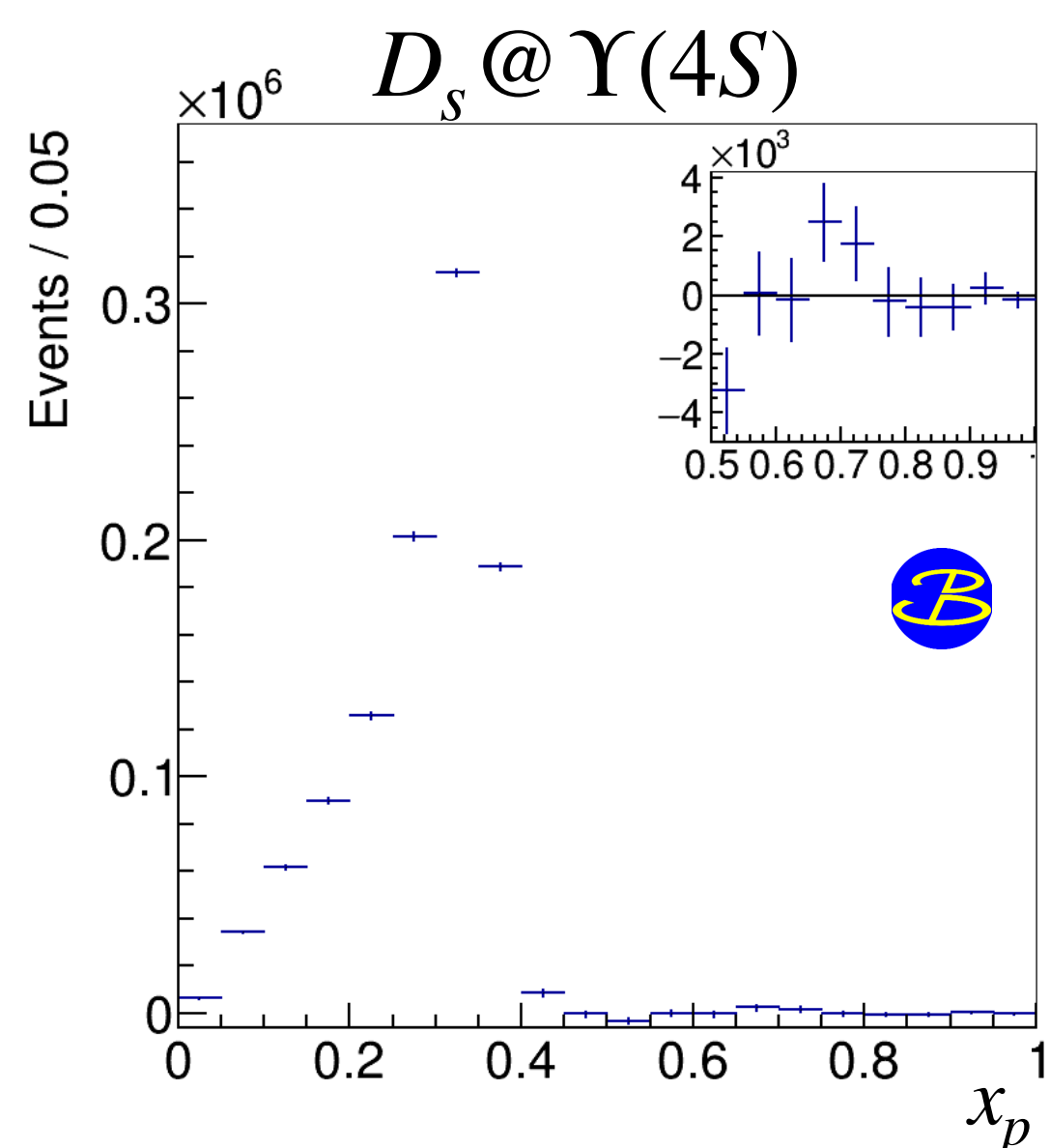
We subtract the continuum component to obtain pure $b\bar{b}$ spectra



Continuum subtraction



Points in the high x_p region are consistent with zero, it means that continuum spectra shapes are correct



Apply efficiency correction to calculate $e^+e^- \rightarrow b\bar{b} \rightarrow DX$ cross sections

$\sigma(e^+e^- \rightarrow DX)$ calculation

$$\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s X) = \sum_{i=1}^{i_{\max}} \frac{N_i(D_s) - k \cdot n_i(D_s)}{\mathcal{L} \cdot \mathcal{E}_i \cdot \mathcal{B}(D_s \rightarrow K^+K^-\pi) \cdot r_{\phi\text{-cut}}}$$

N_i — number of D events from fit in i -bin of the x_p spectrum for **on-resonance data**

$$\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D^0 X) = \sum_{i=1}^{i_{\max}} \frac{N_i(D^0) - k \cdot n_i(D^0)}{\mathcal{L} \cdot \mathcal{E}_i \cdot \mathcal{B}(D^0 \rightarrow K^-\pi^+)}$$

n_i — number of D events from fit in i -bin of the x_p spectrum for **continuum**

k — scale factor for continuum spectrum normalisation

$$r_{\phi\text{-cut}} = 0.981 \pm 0.006$$

$$\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s X) |_{\Upsilon(5S)} = \underline{(151.8 \pm 1.0 \pm 5.5) \text{ pb}} \quad \sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D^0 X) |_{\Upsilon(5S)} = \underline{(379.7 \pm 1.6 \pm 10.0) \text{ pb}}$$

$$\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s X) |_{\Upsilon(4S)} = \underline{(248.6 \pm 0.6 \pm 9.2) \text{ pb}} \quad \sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D^0 X) |_{\Upsilon(4S)} = \underline{(1468.5 \pm 0.9 \pm 36.6) \text{ pb}}$$

Results at $\Upsilon(4S)$ and $\Upsilon(5S)$

$\Upsilon(4S)$ data:

This measurement

PDG
full recon

PDG
same method

$$\mathcal{B}(B \rightarrow D_s X) = \frac{\sigma(D_s X) |_{\Upsilon(4S)}}{2 \cdot \sigma(e^+e^- \rightarrow b\bar{b}) |_{\Upsilon(4S)}} = \underline{(11.28 \pm 0.03 \pm 0.43) \%}$$

$(10.4^{+1.3}_{-1.8}) \%$
 $(8.3 \pm 0.8) \%$

$$\mathcal{B}(B \rightarrow D^0 X) = \frac{\sigma(D^0 X) |_{\Upsilon(4S)}}{2 \cdot \sigma(e^+e^- \rightarrow b\bar{b}) |_{\Upsilon(4S)}} = \underline{(66.63 \pm 0.04 \pm 1.77) \%}$$

$(71.6 \pm 4.6) \%$
 $(61.6 \pm 2.9) \%$

$\Upsilon(5S)$ data:

[JHEP 10 \(2019\), 220](#)
(255.5 ± 7.9) pb

$$C = \frac{\mathcal{B}(B_s \rightarrow D^0 X)}{\mathcal{B}(B_s \rightarrow D_s X)} = \frac{\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D^0 X) |_{\Upsilon(5S)} - \mathcal{B}(B^0 \rightarrow D^0 X) \cdot \sigma(e^+e^- \rightarrow B\bar{B}X) |_{\Upsilon(5S)}}{\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s X) |_{\Upsilon(5S)} - \mathcal{B}(B^0 \rightarrow D_s X) \cdot \sigma(e^+e^- \rightarrow B\bar{B}X) |_{\Upsilon(5S)}}$$

$C = 0.416 \pm 0.018 \pm 0.092$

Results at $\Upsilon(4S)$ and $\Upsilon(5S)$

Fractions of $B_s\bar{B}_sX$ events produced at $\Upsilon(5S)$:

$$f_s = \frac{\sigma(e^+e^- \rightarrow B_s\bar{B}_sX)|_{\Upsilon(5S)}}{\sigma(e^+e^- \rightarrow b\bar{b})|_{\Upsilon(5S)}} = \underbrace{(23.0 \pm 0.2 \pm 2.8) \%}_{\text{This measurement}} \quad \text{Belle 2013 } \underbrace{(17.2 \pm 3.0) \%}_{\text{PRD 87 (2013) 3, 031101}} \quad \text{Belle 2022 } \underbrace{(28.5 \pm 3.2 \pm 3.7) \%}_{\text{PRD 105 (2022) 012004}}$$

To improve accuracy we fit

$$f_s = (23.0 \pm 0.2 \pm 2.8) \%$$

$$f_{B\bar{B}X} = (75.1 \pm 4.0) \%$$

[JHEP 06 \(2021\) 137](#)

$$f_B^{\text{known}} = (4.9 \pm 0.6) \%$$

[JHEP 06 \(2021\) 137](#)

with one constraint

$$f_s + f_{B\bar{B}X} + f_B = 1$$

Result from the fit:

$$f_s = (22.0^{+2.0}_{-2.1}) \%$$

Source	Systematic uncertainty (%)
$\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s^\pm X) _{\Upsilon(5S)}$	1.4
$\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s^\pm X) _{\Upsilon(4S)}$	0.7
$\sigma(e^+e^- \rightarrow B\bar{B} X) _{\Upsilon(5S)}$	1.4
$\mathcal{B}(B_s^0 \rightarrow D_s^\pm X)$	10.5
$\sigma(e^+e^- \rightarrow b\bar{b}) _{\Upsilon(5S)}$	4.5
Correlated contributions	
– tracking	1.1
– K/π identification	2.3
– r_ϕ	0.6
– $\mathcal{B}(D_s^+ \rightarrow K^+K^-\pi^+)$	1.9
Total	12.0

Belle

[PRD 105 \(2022\) 1, 012004](#)

$$\mathcal{B}(B_s \rightarrow D_s X) = (60.2 \pm 5.8 \pm 2.3) \%$$

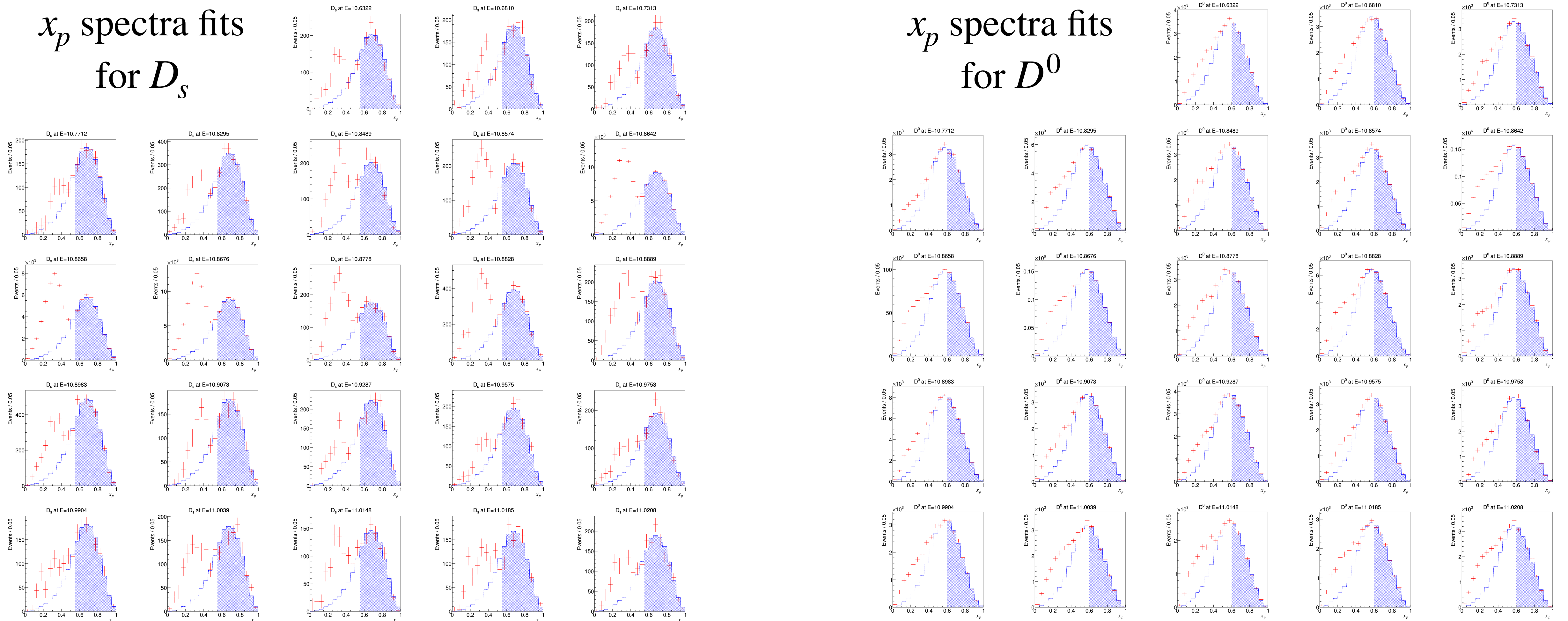
Energy scan points

23 energy points from 10.63 to 11.02 GeV — repeat the procedure at each of them

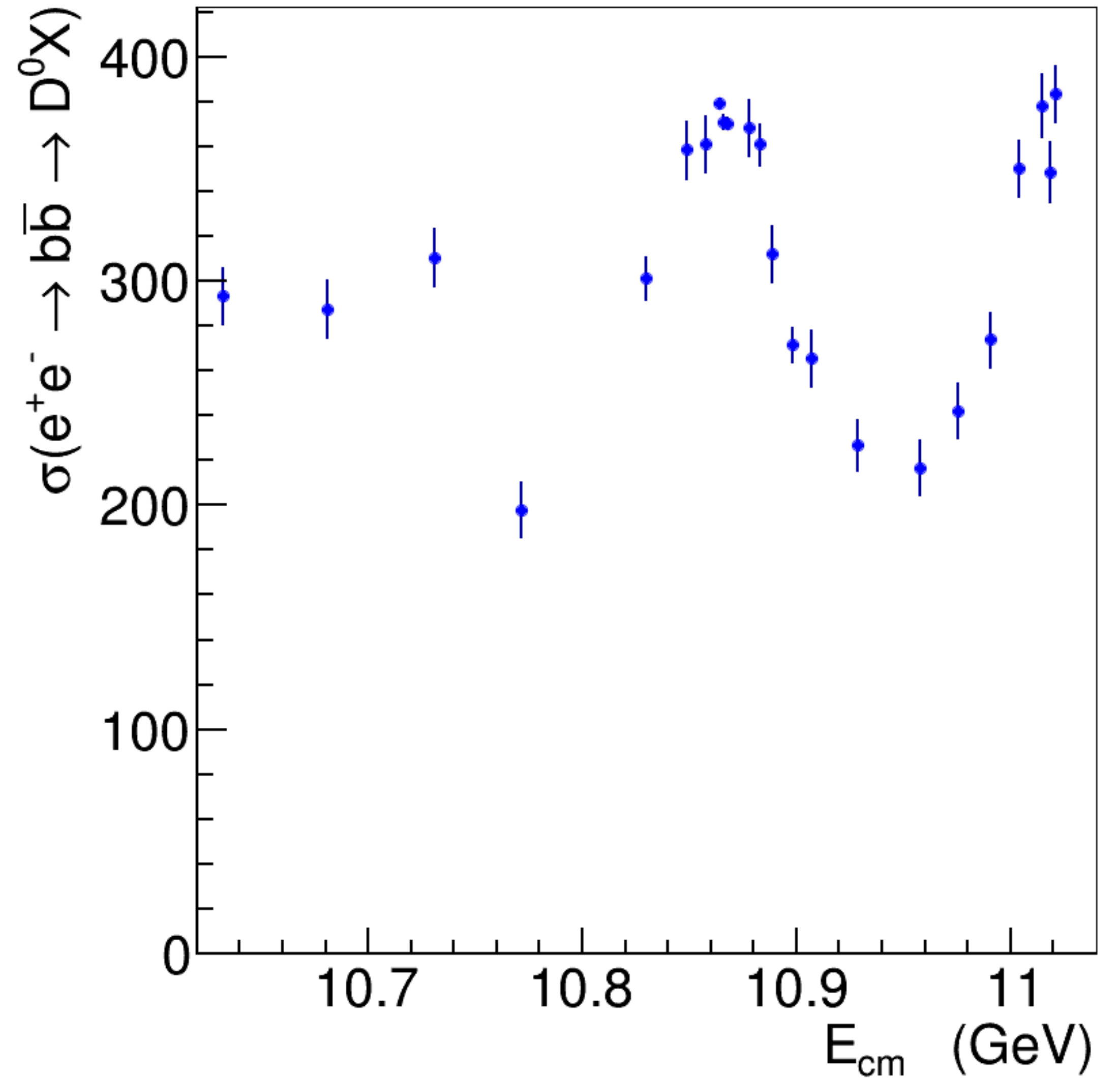
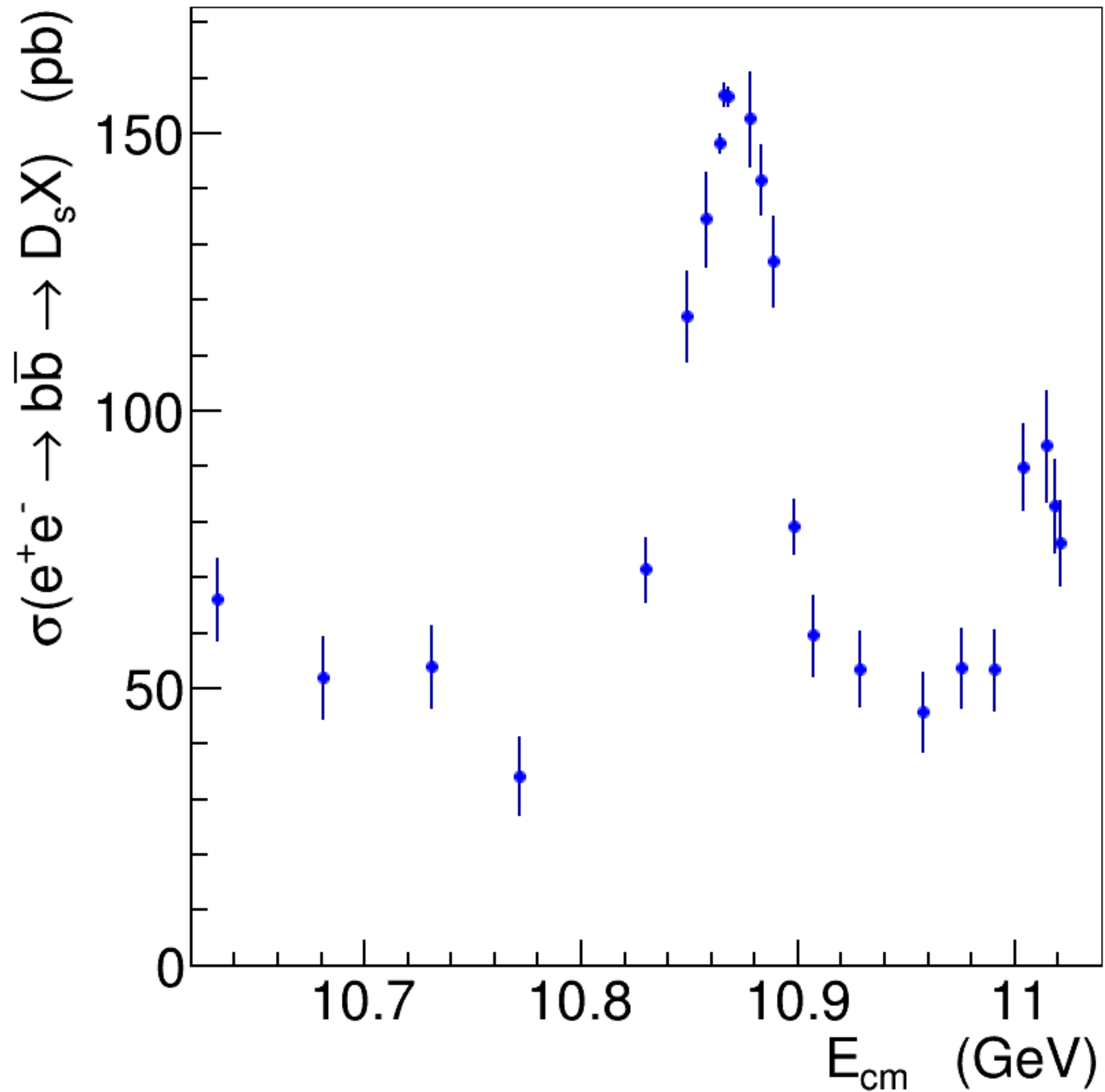
— $b\bar{b}$
— fit results

x_p spectra fits
for D_s

x_p spectra fits
for D^0



$\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s^\pm X)$ and $\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D^0/\bar{D}^0 X)$



From D to B

$$\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s^+ X)/2 = \mathcal{B}(B_s^0 \rightarrow D_s^+ X) \cdot \sigma(e^+e^- \rightarrow B_s \bar{B}_s X) + \mathcal{B}(B \rightarrow D_s X) \cdot \sigma(e^+e^- \rightarrow B \bar{B} X)$$

$$\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D^0 X)/2 = C \cdot \mathcal{B}(B_s^0 \rightarrow D_s^+ X) \cdot \sigma(e^+e^- \rightarrow B_s^0 \bar{B}_s^0 X) + \mathcal{B}(B \rightarrow D^0 X) \cdot \sigma(e^+e^- \rightarrow B \bar{B} X)$$

This work:

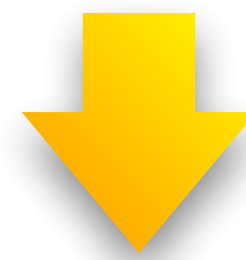
$$\mathcal{B}(B \rightarrow D^\pm X) = (11.28 \pm 0.03 \pm 0.43) \%$$

$$\mathcal{B}(B \rightarrow D^0/\bar{D}^0 X) = (66.63 \pm 0.04 \pm 1.77) \%$$

$$C = \frac{\mathcal{B}(B_s \rightarrow D^0 X)}{\mathcal{B}(B_s \rightarrow D_s X)} = 0.416 \pm 0.018 \pm 0.092$$

$$\sigma(e^+e^- \rightarrow B_s \bar{B}_s X) = \sigma(e^+e^- \rightarrow B_s^{(*)} \bar{B}_s^{(*)})$$

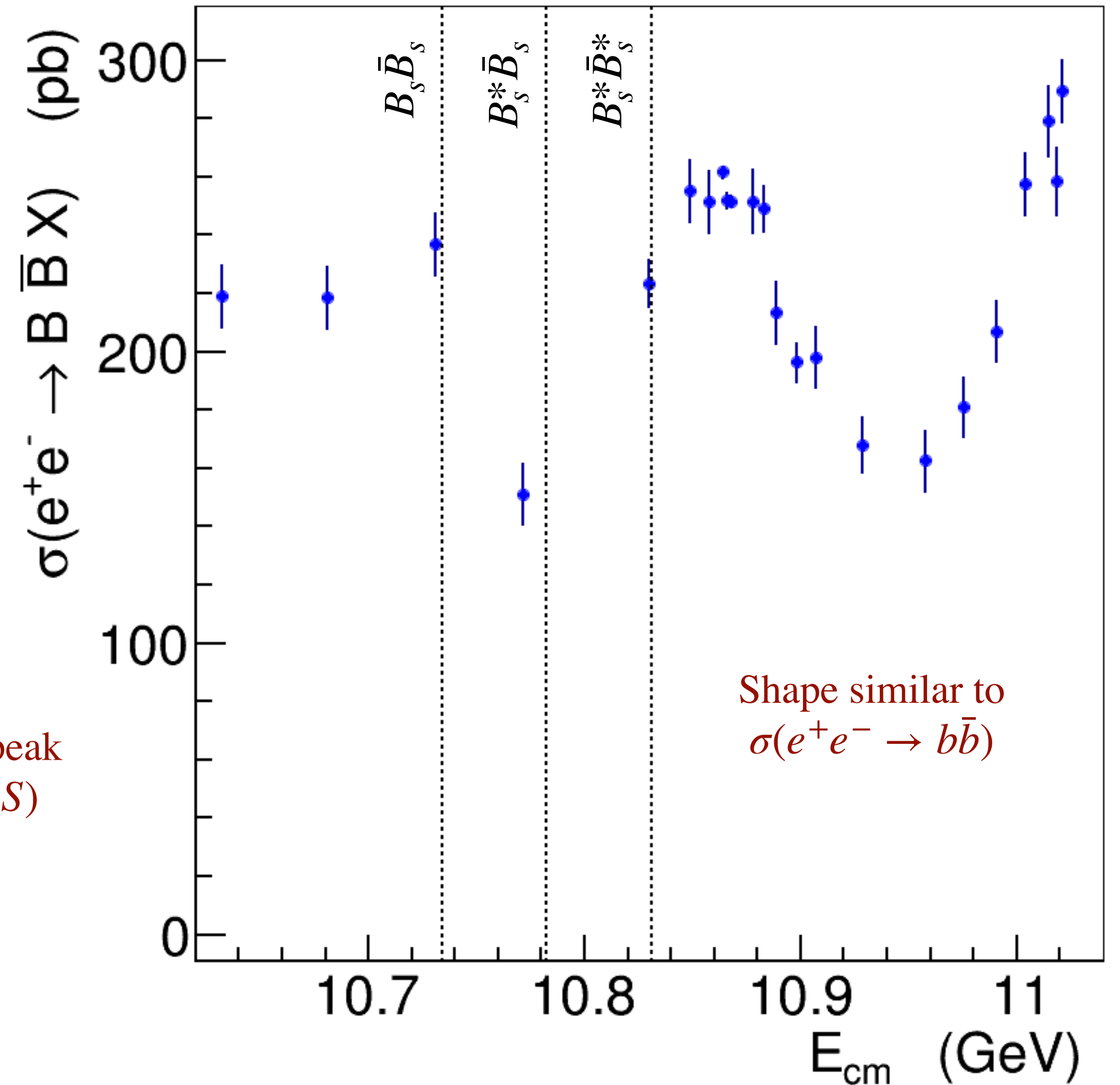
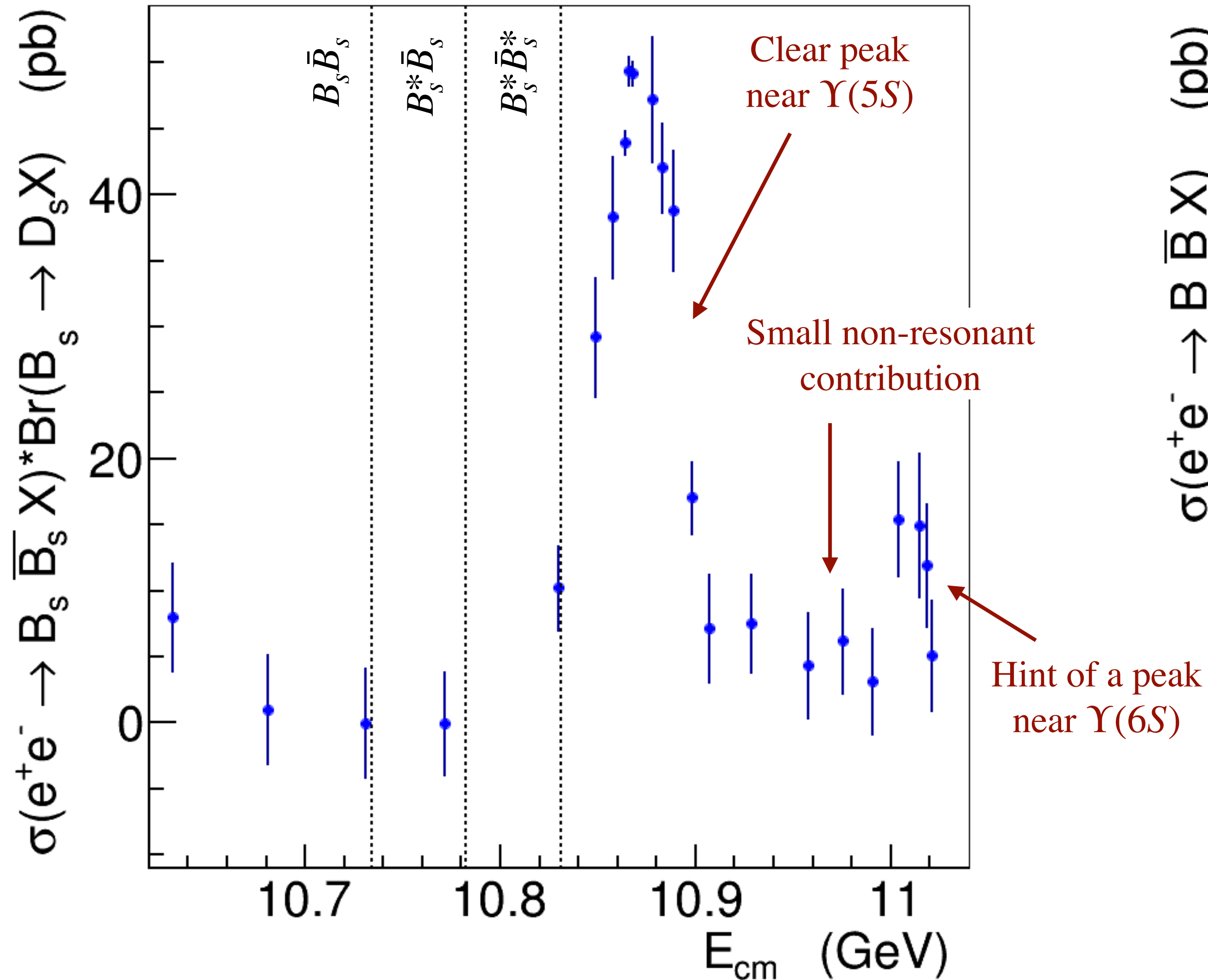
up to $B_s \bar{B}_s \pi^0 \pi^0$ threshold (11.004 GeV)



$$\sigma(e^+e^- \rightarrow B_s^0 \bar{B}_s^0 X) \cdot \mathcal{B} = 0.54 \cdot \sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s^+ X) - 0.09 \cdot \sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D^0 X),$$

$$\sigma(e^+e^- \rightarrow B \bar{B} X) = -0.34 \cdot \sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s^+ X) + 0.81 \cdot \sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D^0 X)$$

$\sigma(e^+e^- \rightarrow B_s \bar{B}_s X)$ and $\sigma(e^+e^- \rightarrow B \bar{B} X)$



Summary

- ✓ Cross sections $\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D_s^\pm X)$ and $\sigma(e^+e^- \rightarrow b\bar{b} \rightarrow D^0\bar{D}^0 X)$ as well as $\sigma(e^+e^- \rightarrow B_s\bar{B}_s X)$ and $\sigma(e^+e^- \rightarrow B\bar{B} X)$ are measured from 10.63 to 11.02 GeV
- ✓ Inclusive $\mathcal{B}(B \rightarrow D^0 X)$ and $\mathcal{B}(B \rightarrow D_s X)$ are obtained
- ✓ Ratio $\mathcal{B}(B_s \rightarrow D^0 X)/\mathcal{B}(B_s \rightarrow D_s X) = 0.416 \pm 0.018 \pm 0.092$ is determined
- ✓ The fraction of B_s mesons at $\Upsilon(5S)$ is measured to be $f_s = (22.0_{-2.1}^{+2.0})\%$

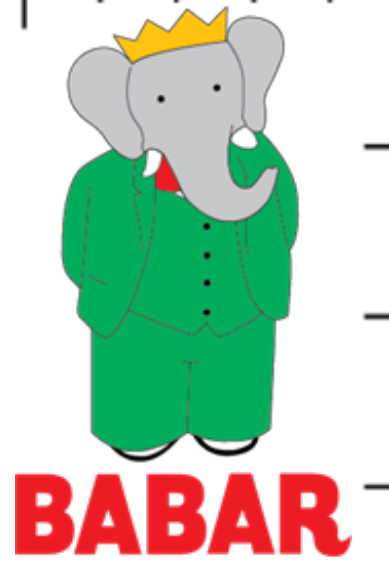


Thank you very much for your attention!

Backup

Cross sections for open flavour channels

$$R_b = \frac{\sigma(e^+e^- \rightarrow b\bar{b})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

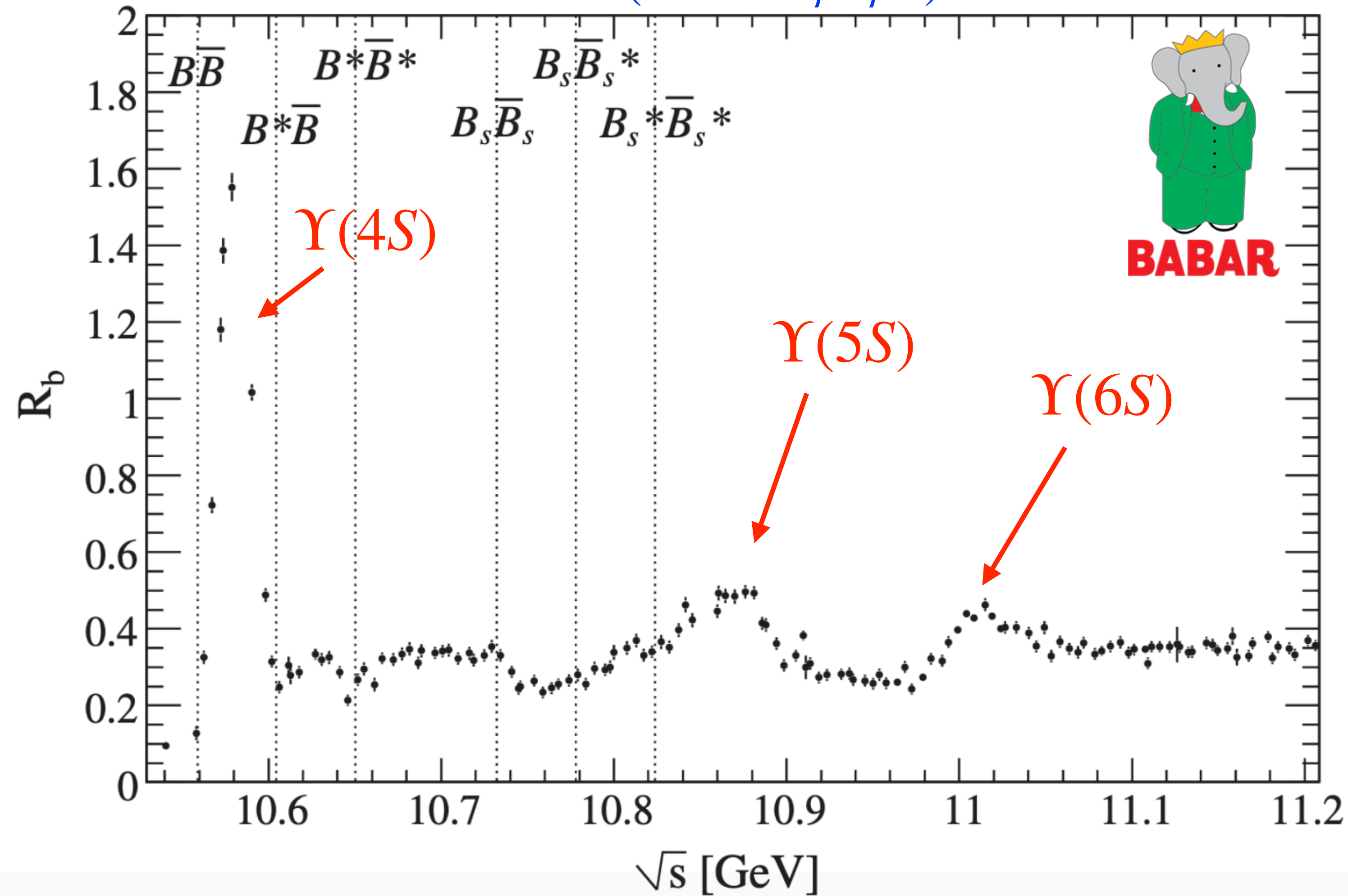


Total **hadronic cross section** has **peaks** at the $\Upsilon(4S)$, $\Upsilon(5S)$ and $\Upsilon(6S)$, and **dips** near the open bottom thresholds

$\Upsilon(5S)$ and $\Upsilon(6S)$ could provide an **oscillatory** behaviour of the corresponding **exclusive** cross sections

The **individual** cross sections contain considerably **more information** than their sum

$e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^-$, $e^+e^- \rightarrow h_b\pi^+\pi^-$ and $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}(\pi)$ has been **already** measured



Measurements of the **exclusive cross sections** should shed light on the nature of bottomonium states

Puzzling bottomonium states

Mass splitting is too large

$$M(\Upsilon(5S)) - M(\Upsilon(4S)) = 305.8 \text{ MeV}/c^2$$

$$M(\Upsilon(4S)) - M(\Upsilon(3S)) = 224.2 \text{ MeV}/c^2 \quad \longrightarrow \quad \Delta = 81.6 \text{ MeV}/c^2$$

$$\Delta_{b\bar{b}}^{\text{expected}} \approx 40 \text{ MeV}/c^2$$

Anomalous production of $\Upsilon(nS)\pi^+\pi^-$

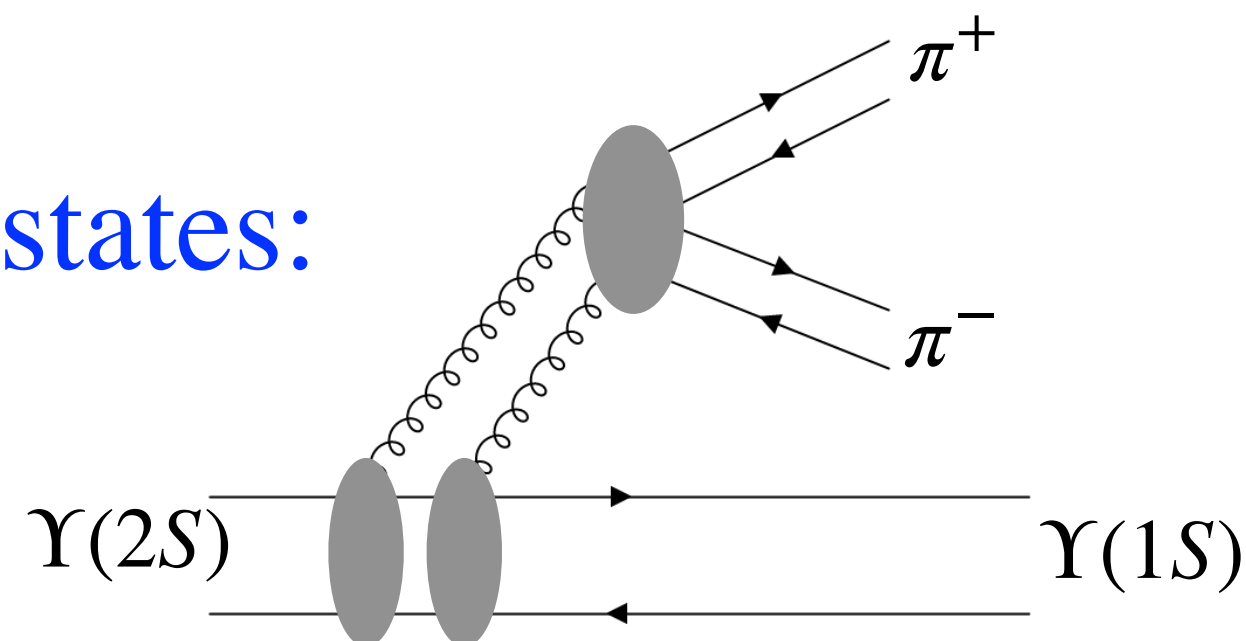
PRL100,112001(2008)	Γ, MeV
$\Upsilon(5S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	$0.59 \pm 0.04 \pm 0.09$
$\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-$	$0.85 \pm 0.07 \pm 0.16$
$\Upsilon(5S) \rightarrow \Upsilon(3S)\pi^+\pi^-$	$0.52 \pm 0.20 \pm 0.17 \pm 0.013$
$\Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0060
$\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0009
$\Upsilon(4S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0019

10^2

η transitions are not suppressed

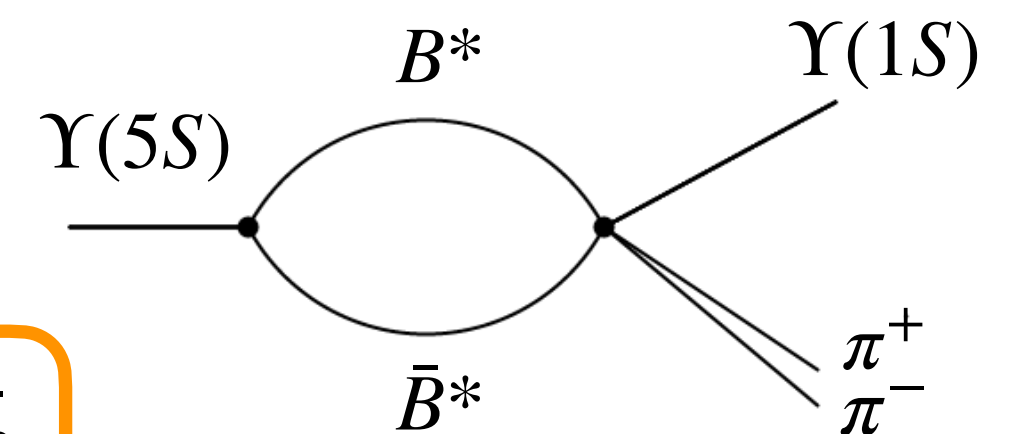
Transition	Partial width (keV)
$\Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	5.7 ± 0.5
$\Upsilon(2S) \rightarrow \Upsilon(1S)\eta$	$(9.3 \pm 1.5) \times 10^{-3}$
$\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.89 ± 0.08
$\Upsilon(3S) \rightarrow \Upsilon(1S)\eta$	$< 2 \times 10^{-3}$
$\Upsilon(3S) \rightarrow \Upsilon(2S)\pi^+\pi^-$	0.57 ± 0.06
$\Upsilon(4S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	1.7 ± 0.2
$\Upsilon(4S) \rightarrow \Upsilon(1S)\eta$	4.0 ± 0.8
$\Upsilon(4S) \rightarrow \Upsilon(2S)\pi^+\pi^-$	1.8 ± 0.3
$\Upsilon(4S) \rightarrow h_b(1P)\eta$	45 ± 7
$\Upsilon(5S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	238 ± 41
$\Upsilon(5S) \rightarrow \Upsilon(1S)\eta$	39 ± 11
$\Upsilon(5S) \rightarrow \Upsilon(1S)K^+K^-$	33 ± 11
$\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-$	428 ± 83
$\Upsilon(5S) \rightarrow \Upsilon(2S)\eta$	204 ± 44

Pure $b\bar{b}$ -states:

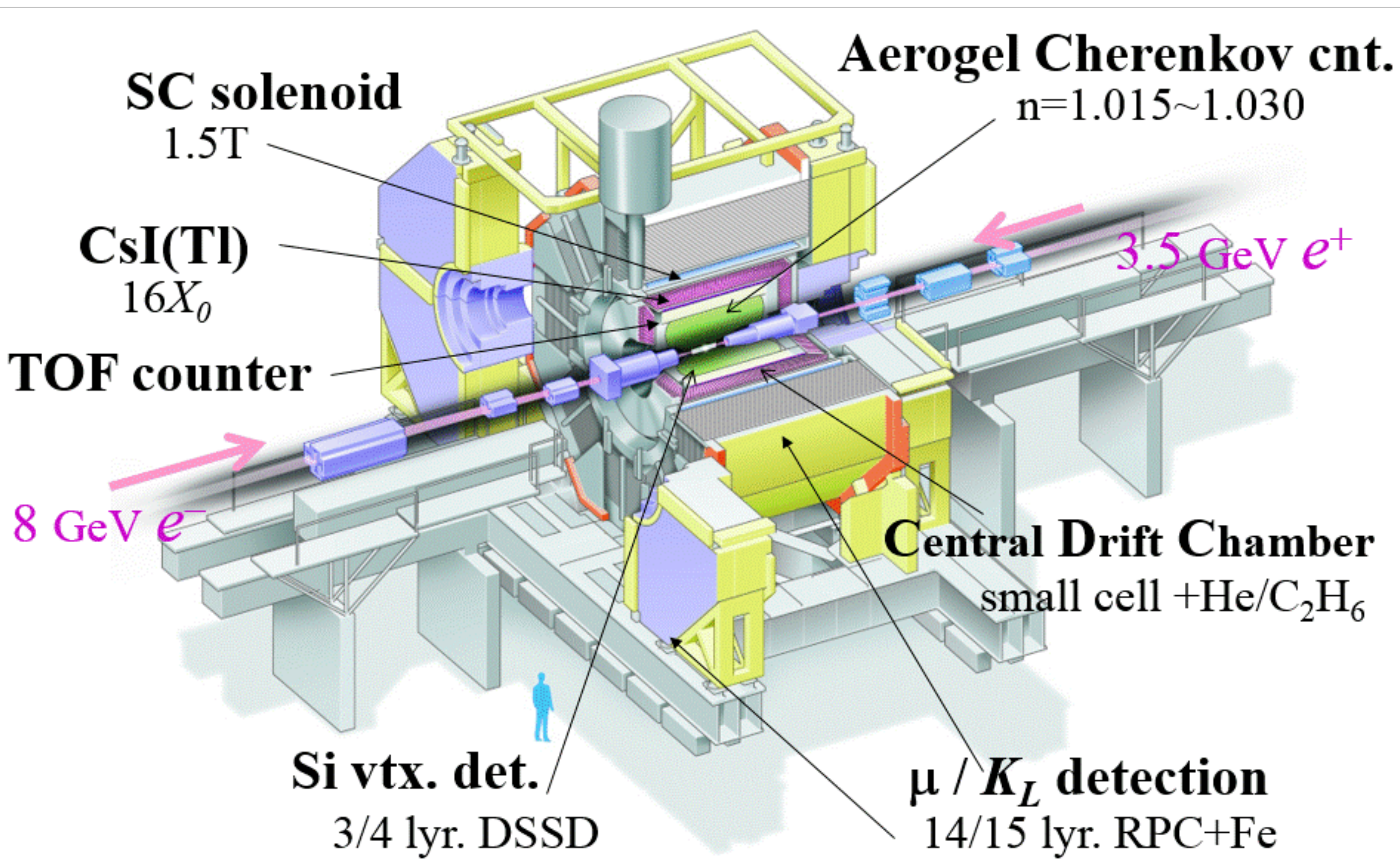


Rescattering $\Upsilon(5S) \rightarrow B^{(*)}B^{(*)} \rightarrow \Upsilon(nS)\pi\pi$?

Conclusion: states above threshold are not pure $b\bar{b}$



Data samples for the analysis



Data used in this analysis:

data at $\Upsilon(4S)$ energy:

$$\mathcal{L}_{4S} = 571 \text{ fb}^{-1}$$

data at $\Upsilon(5S)$ energy:

$$\mathcal{L}_{5S} = 121 \text{ fb}^{-1}$$

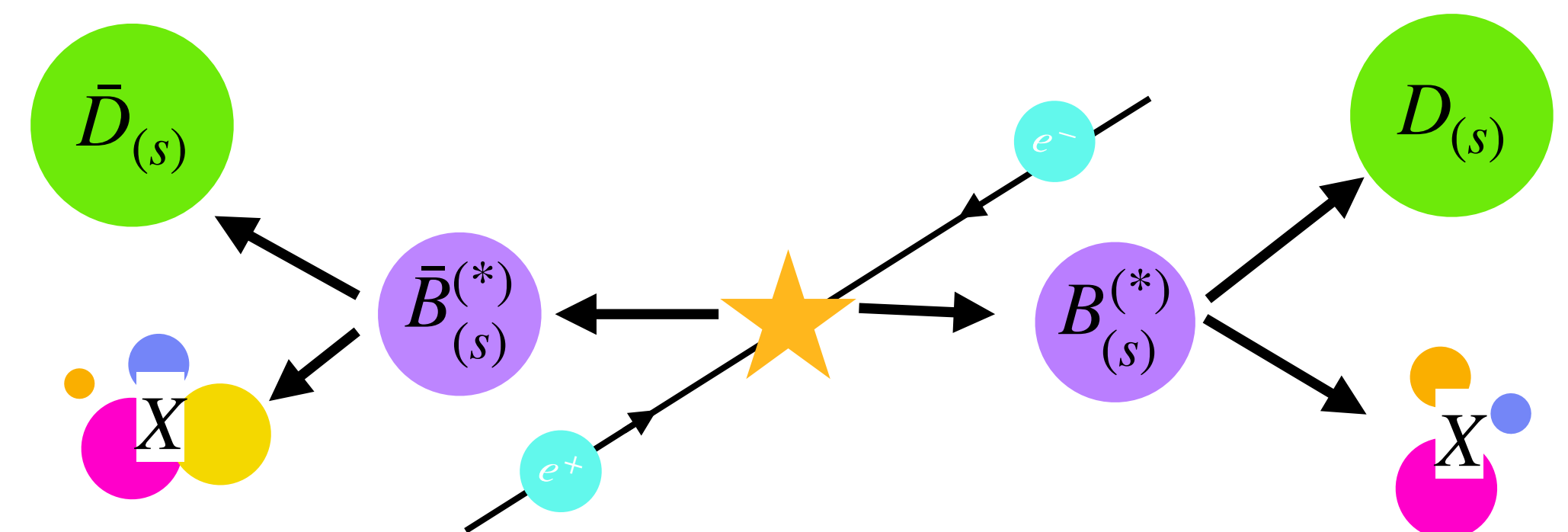
data at $E_{cm} = 10.52$ GeV
 (continuum data sample):

$$\mathcal{L}_{cont} = 74 \text{ fb}^{-1}$$

22 energy scan points

(E_{cm} from 10.63 GeV to 11.02 GeV):

$$\mathcal{L}_i \approx 1 \text{ fb}^{-1}$$



Belle detector

Charged particles: $e^\pm, \mu^\pm, \pi^\pm, K^\pm, p^\pm$

Neutral particles: γ, K_L

Decay vertices - SVD

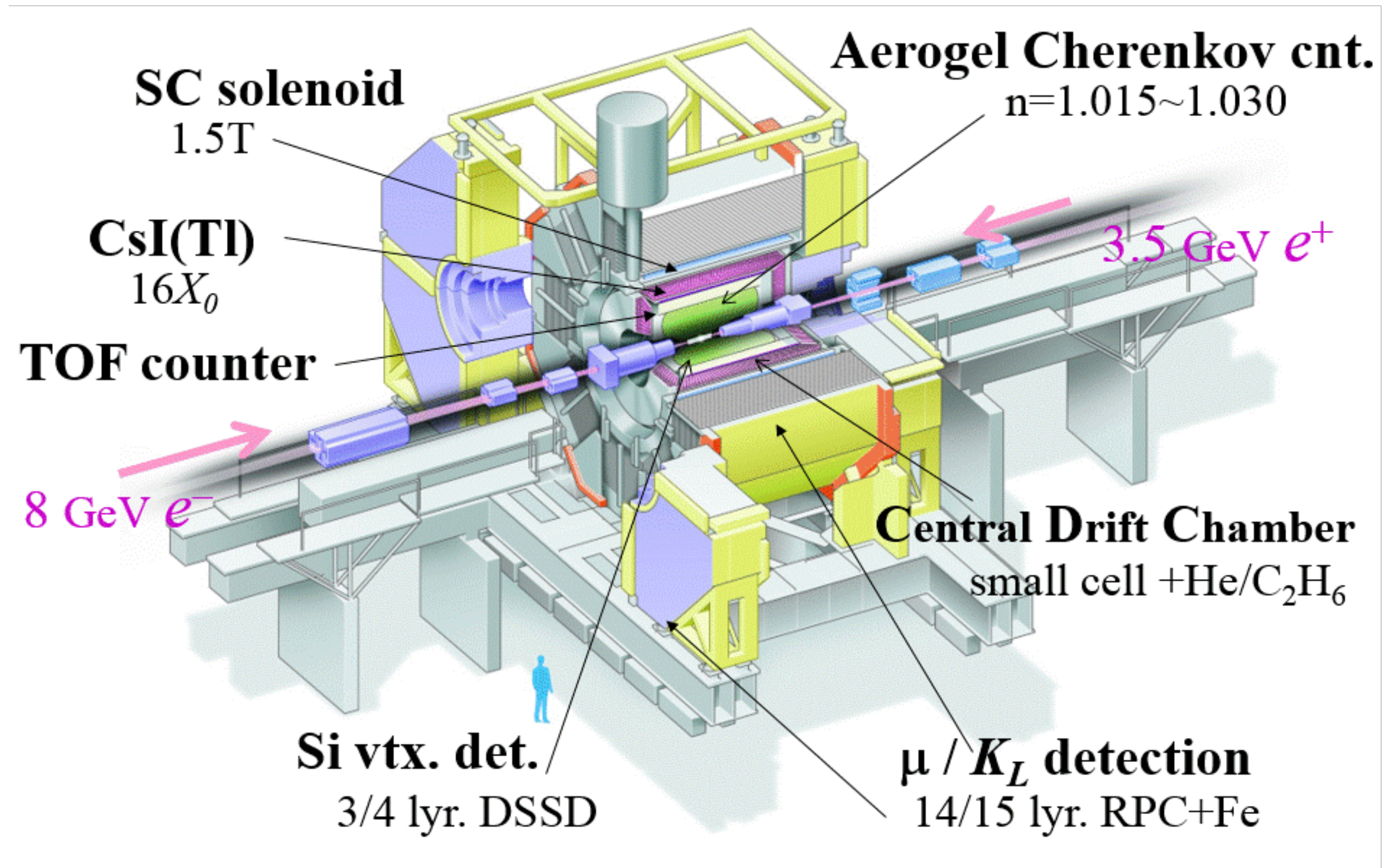
Charged particle tracking — CDC

Particle ID — $\frac{dE}{dx}$ in CDC ($p < 1$ GeV),

ACC ($1.2 < p < 3.5$ GeV), and
TOF ($p < 1.2$ GeV)

Electromagnetic showers — ECL

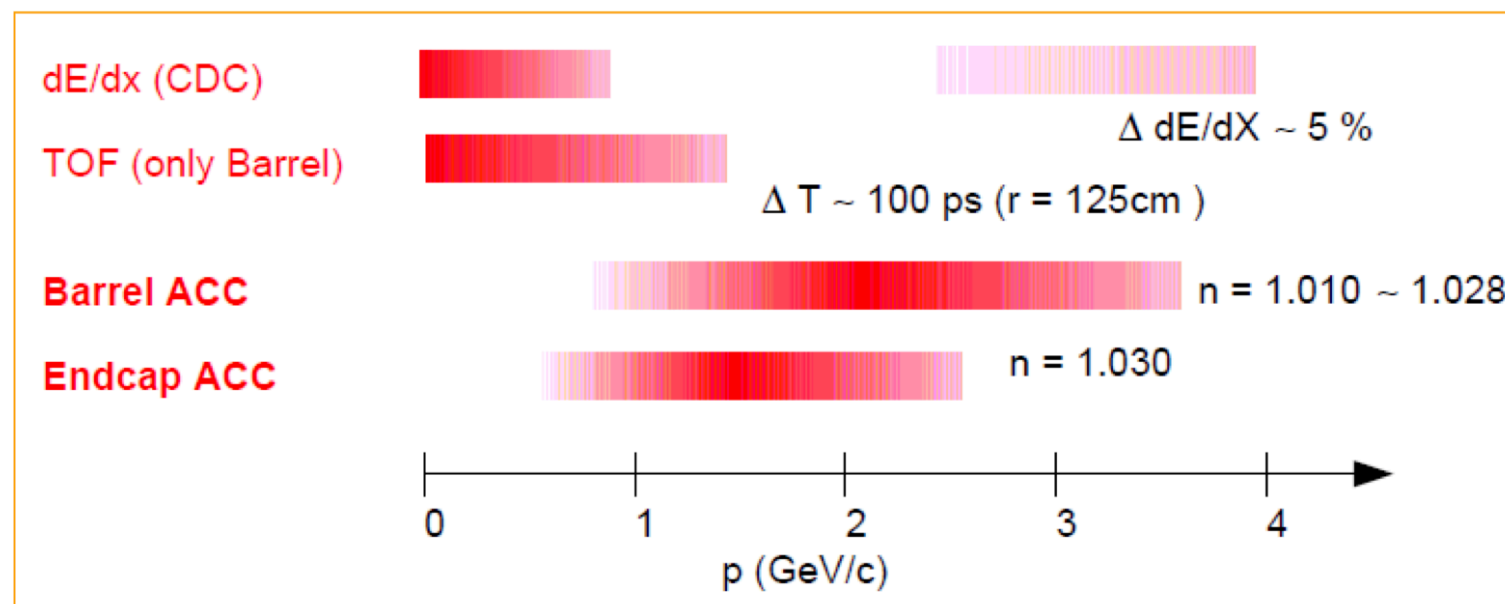
μ and K_L — KLM system



Belle detector

Performance parameters expected (or achieved) for the Belle detector

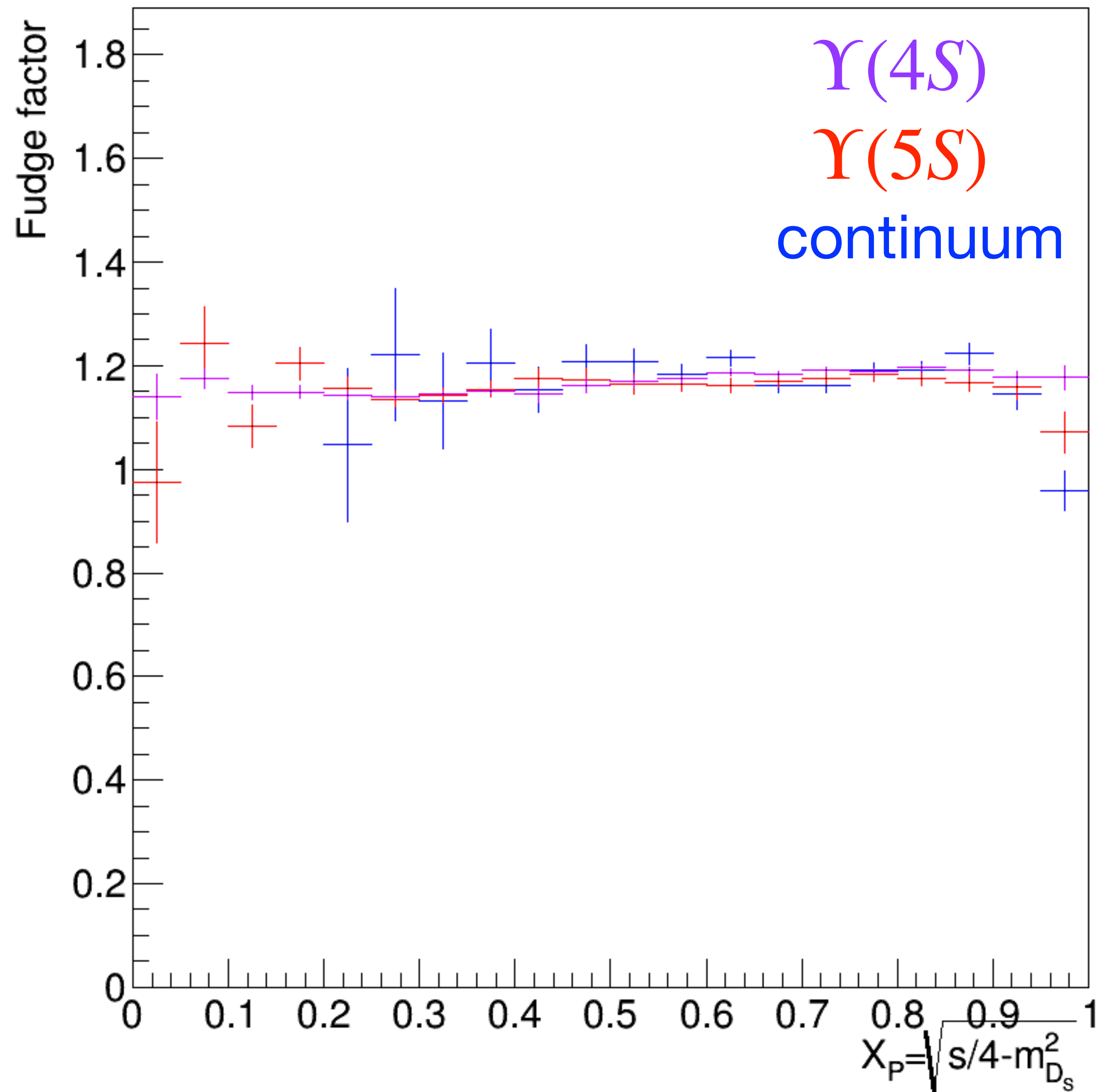
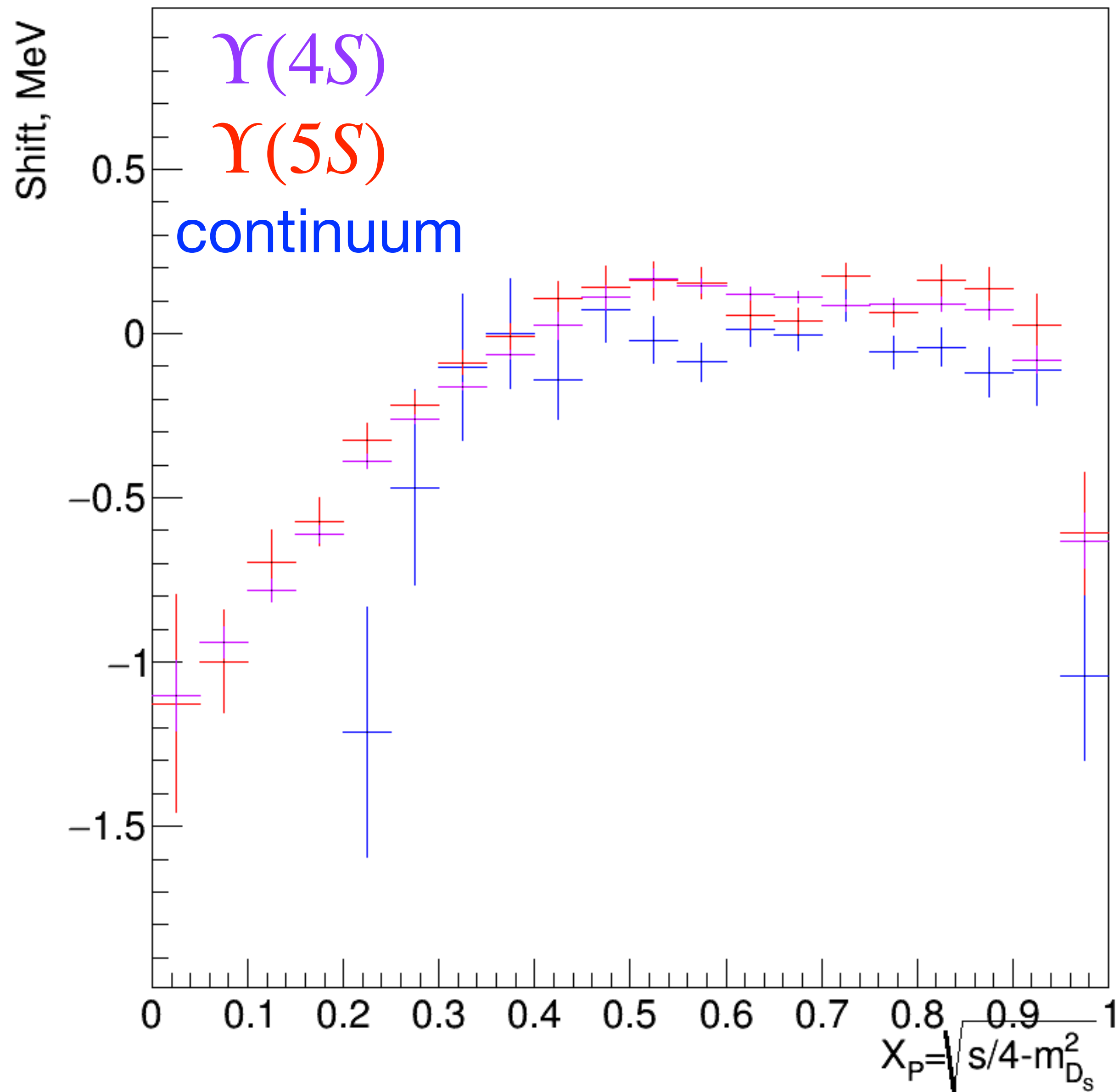
Detector	Type	Configuration	Readout	Performance
Beam pipe	Beryllium double wall	Cylindrical, $r = 20$ mm 0.5/2.5/0.5 (mm) = Be/He/Be		He gas cooled
EFC	$\text{Bi}_4\text{Ge}_3\text{O}_{12}$	Photodiode readout segmentation: 32 in ϕ ; 5 in θ	160×2	RMS energy resolution: 7.3 % at 8 GeV 5.8% at 3.5 GeV
SVD	Double-sided Si strip	Chip size: 57.5×33.5 mm ² Strip pitch: 25 (p)/50 (n) μm 3 layers: 8/10/14 ladders	ϕ : 40.96k z : 40.96k	$\sigma_{\Delta z} \sim 80$ μm
CDC	Small cell drift chamber	Anode: 50 layers Cathode: 3 layers $r = 8.3\text{--}86.3$ cm $-77 \leq z \leq 160$ cm	A : 8.4k C : 1.8k	$\sigma_{r\phi} = 130$ μm $\sigma_z = 200\text{--}1400$ μm $\sigma_{p_t}/p_t = 0.3\% \sqrt{p_t^2 + 1}$ $\sigma_{dE/dx} = 6\%$
ACC	Silica aerogel	960 barrel/228 end-cap FM-PMT readout		$N_{\text{p.e.}} \geq 6$ K/π separation: $1.2 < p < 3.5$ GeV/ c
TOF	Scintillator	128 ϕ segmentation $r = 120$ cm, 3-m long	128×2	$\sigma_t = 100$ ps K/π separation: up to 1.2 GeV/ c
TSC		64 ϕ segmentation	64	
ECL	CsI (towered structure)	Barrel: $r = 125\text{--}162$ cm End-cap: $z = -102$ cm and $+196$ cm	6624 1152 (F) 960 (B)	$\sigma_E/E = 1.3\% / \sqrt{E}$ $\sigma_{\text{pos}} = 0.5$ cm/ \sqrt{E} (E in GeV)
KLM	Resistive plate counters	14 layers (5 cm Fe + 4 cm gap) 2 RPCs in each gap	θ : 16k ϕ : 16k	$\Delta\phi = \Delta\theta = 30$ mr for K_L $\sim 1\%$ hadron fake
Magnet	Supercon.	Inner radius = 170 cm		$B = 1.5$ T



Fit the D_S mass distributions in the different x_p bins at $\Upsilon(4S)$

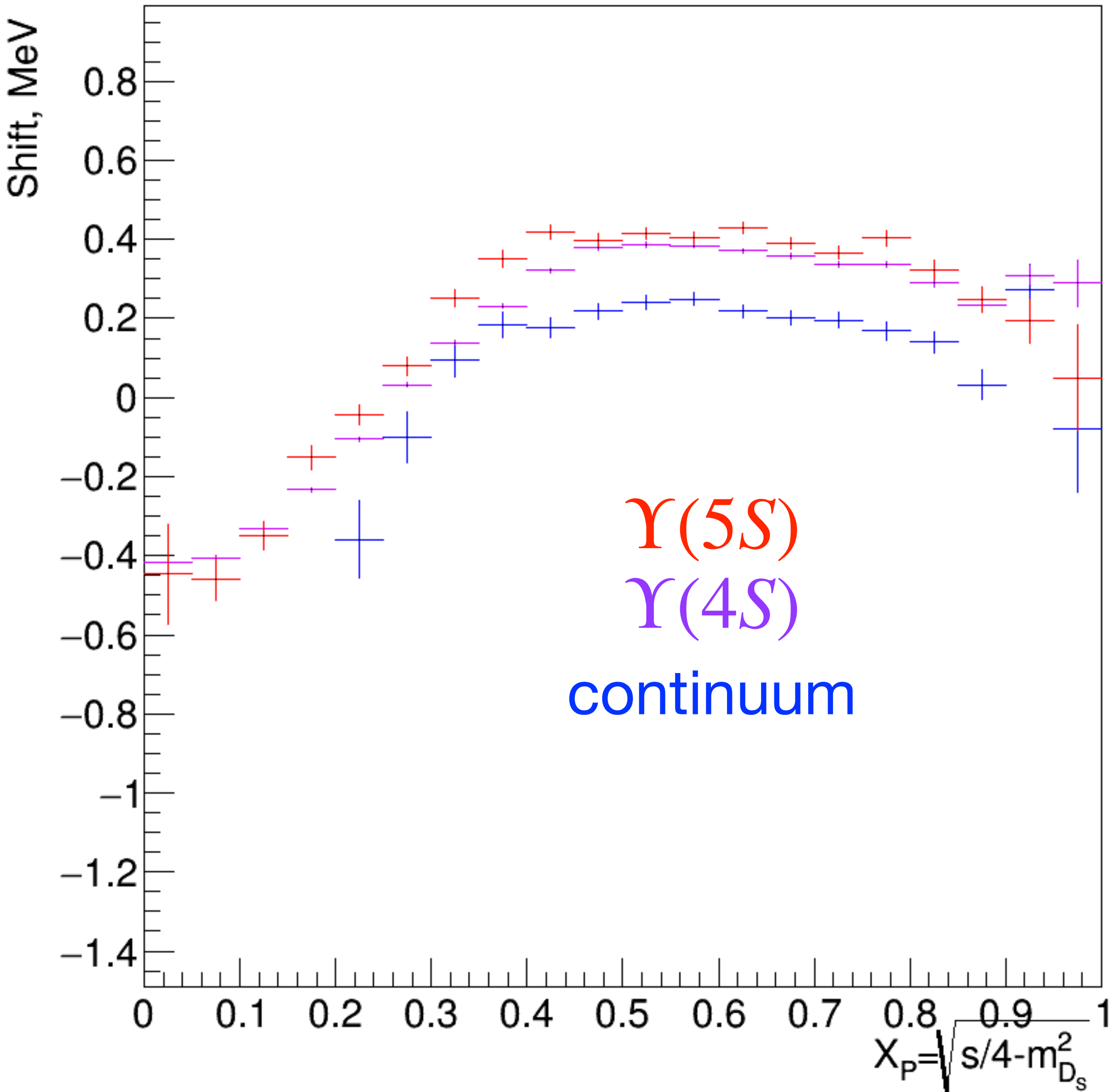
Shift for 4S

Fudge factor for 4S

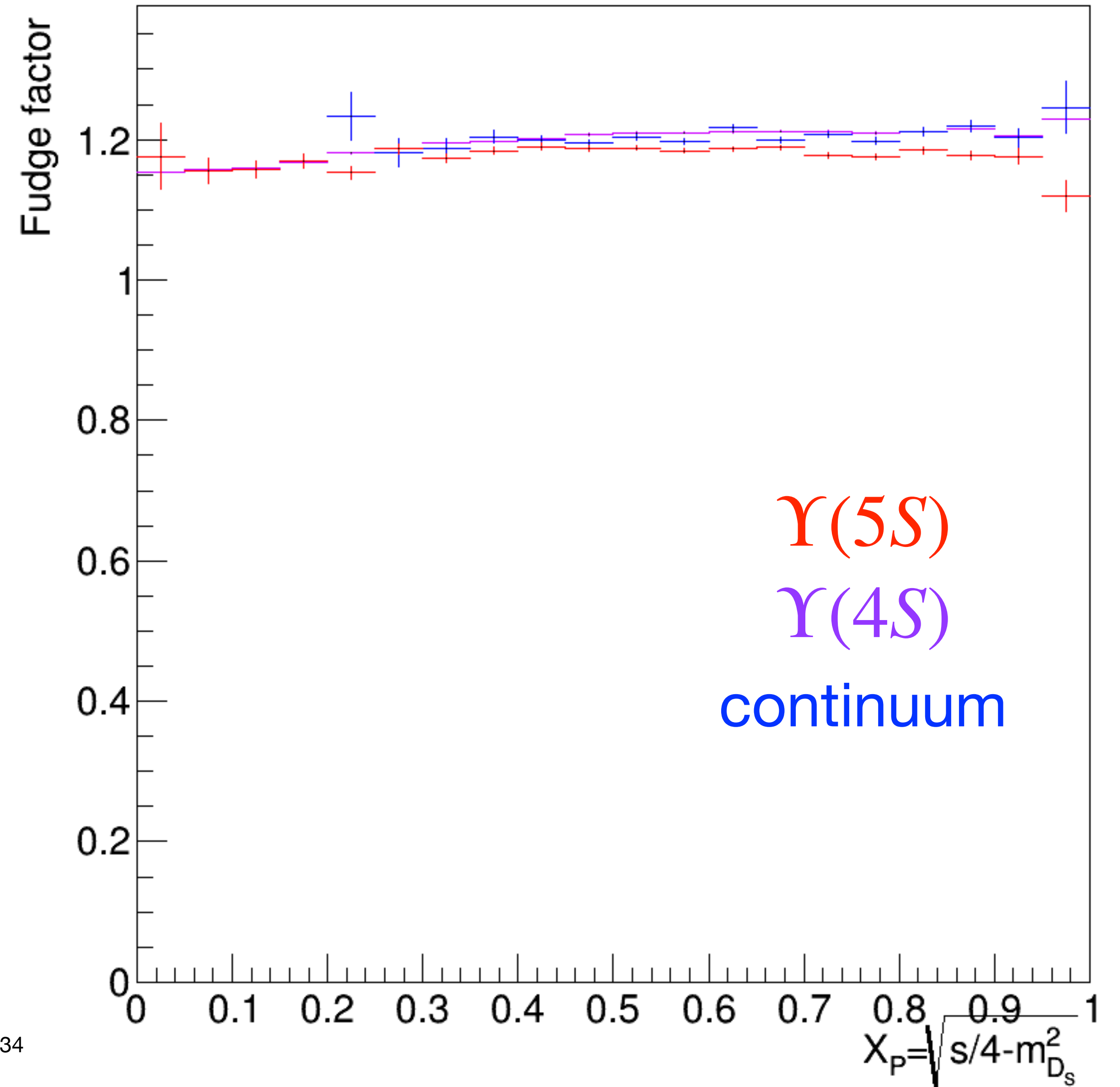


Fit the D^0 mass distributions in the different x_p bins at $\Upsilon(4S)$

Shift for 5S

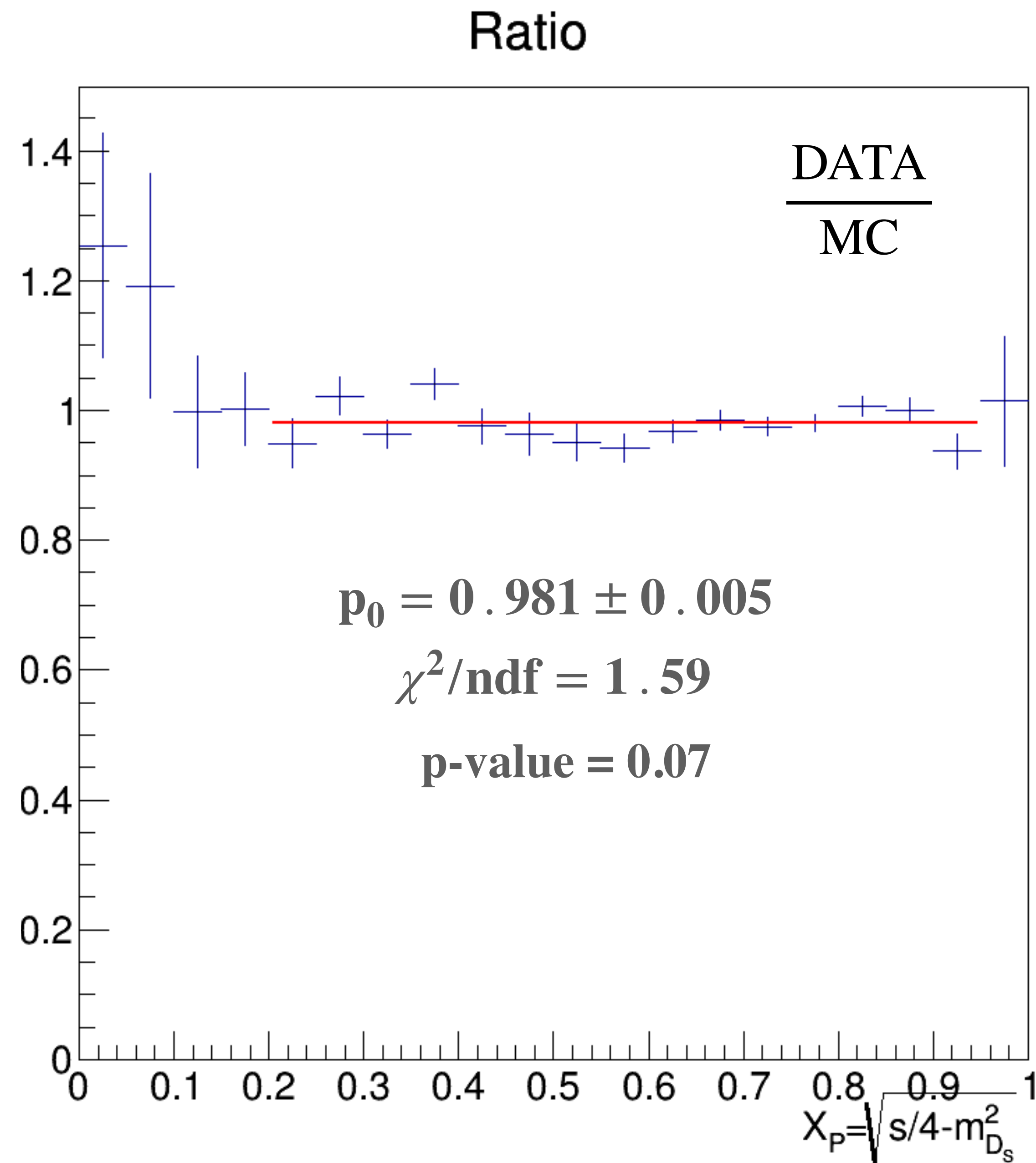
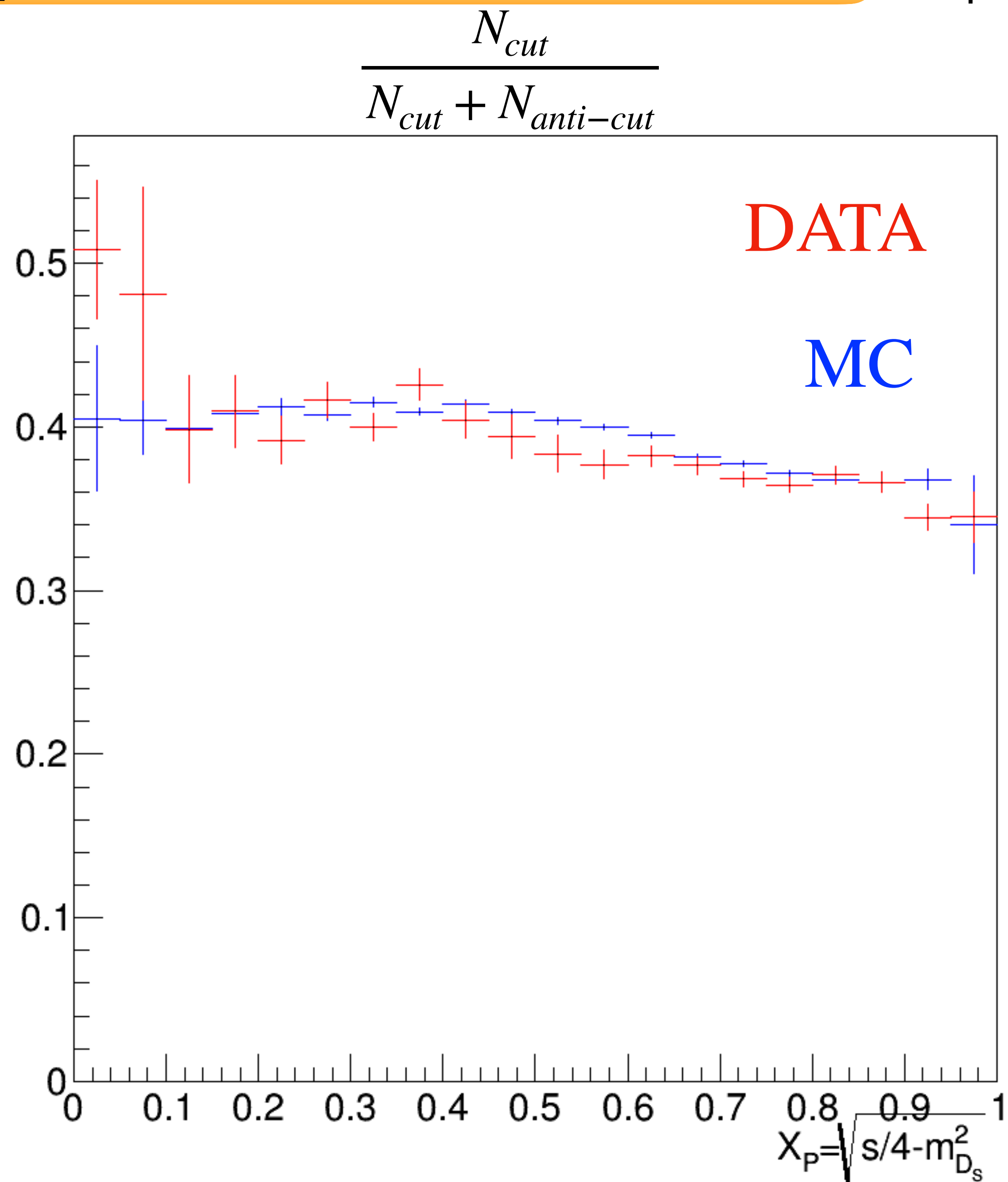


Fudge factor for 5S



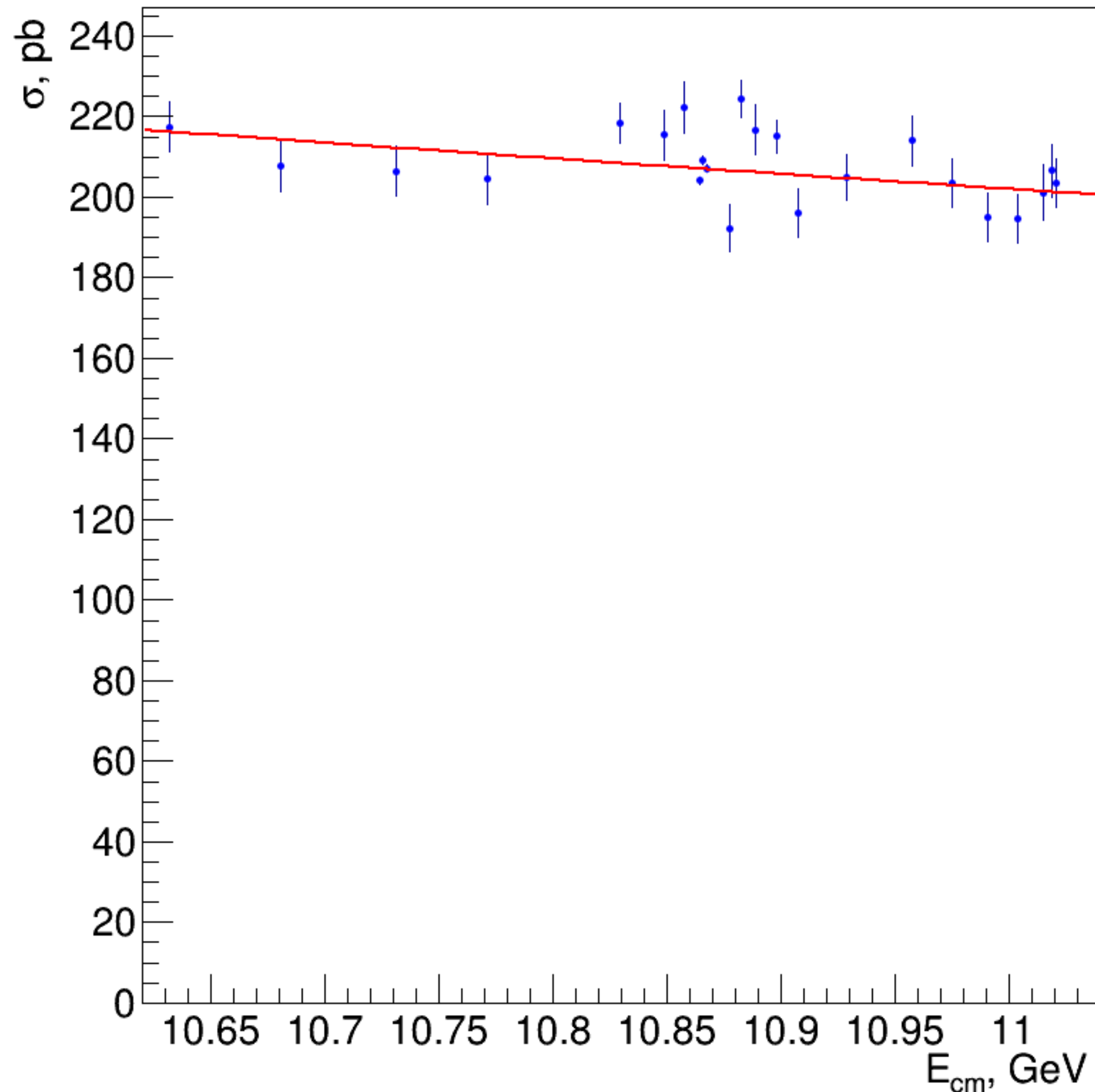
ϕ -cut efficiency correction

$$|M_{inv}(K^-K^+) - m_\phi| < 19 \text{ MeV}/c^2, |\cos \theta_{hel}| > 0.25$$

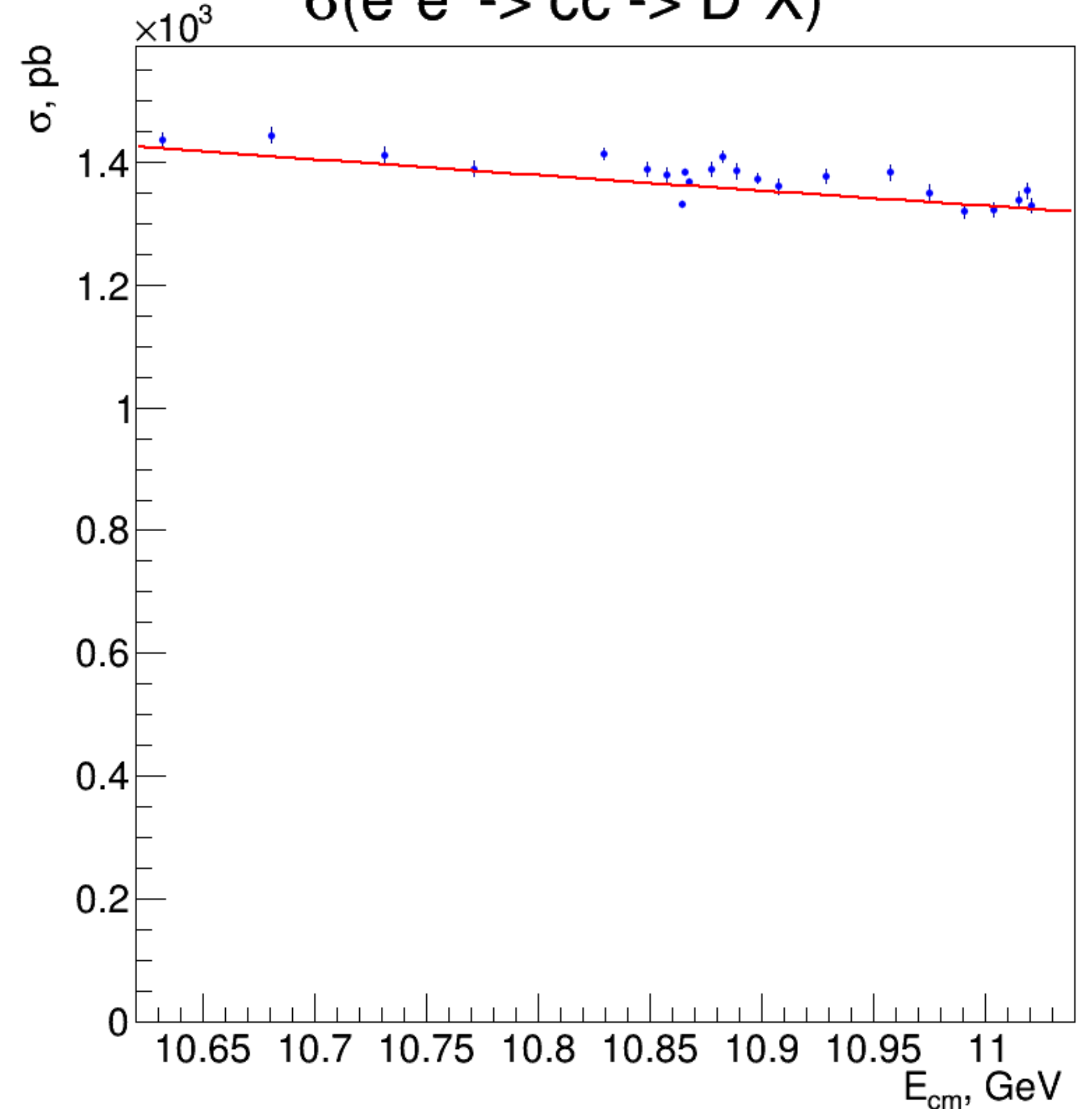


$\sigma(e^+e^- \rightarrow c\bar{c} \rightarrow D_s X)$ and $\sigma(e^+e^- \rightarrow c\bar{c} \rightarrow D^0 X)$

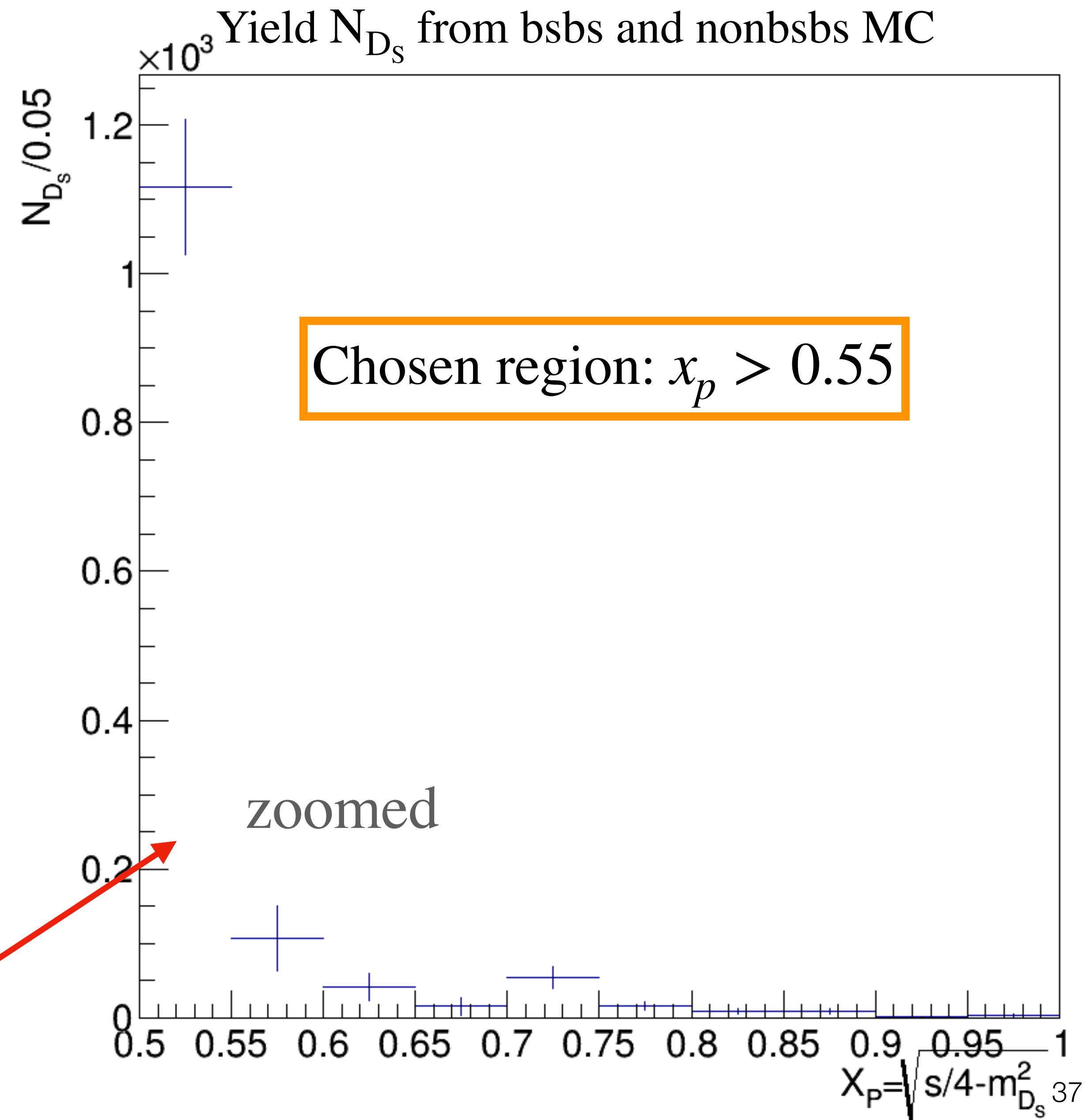
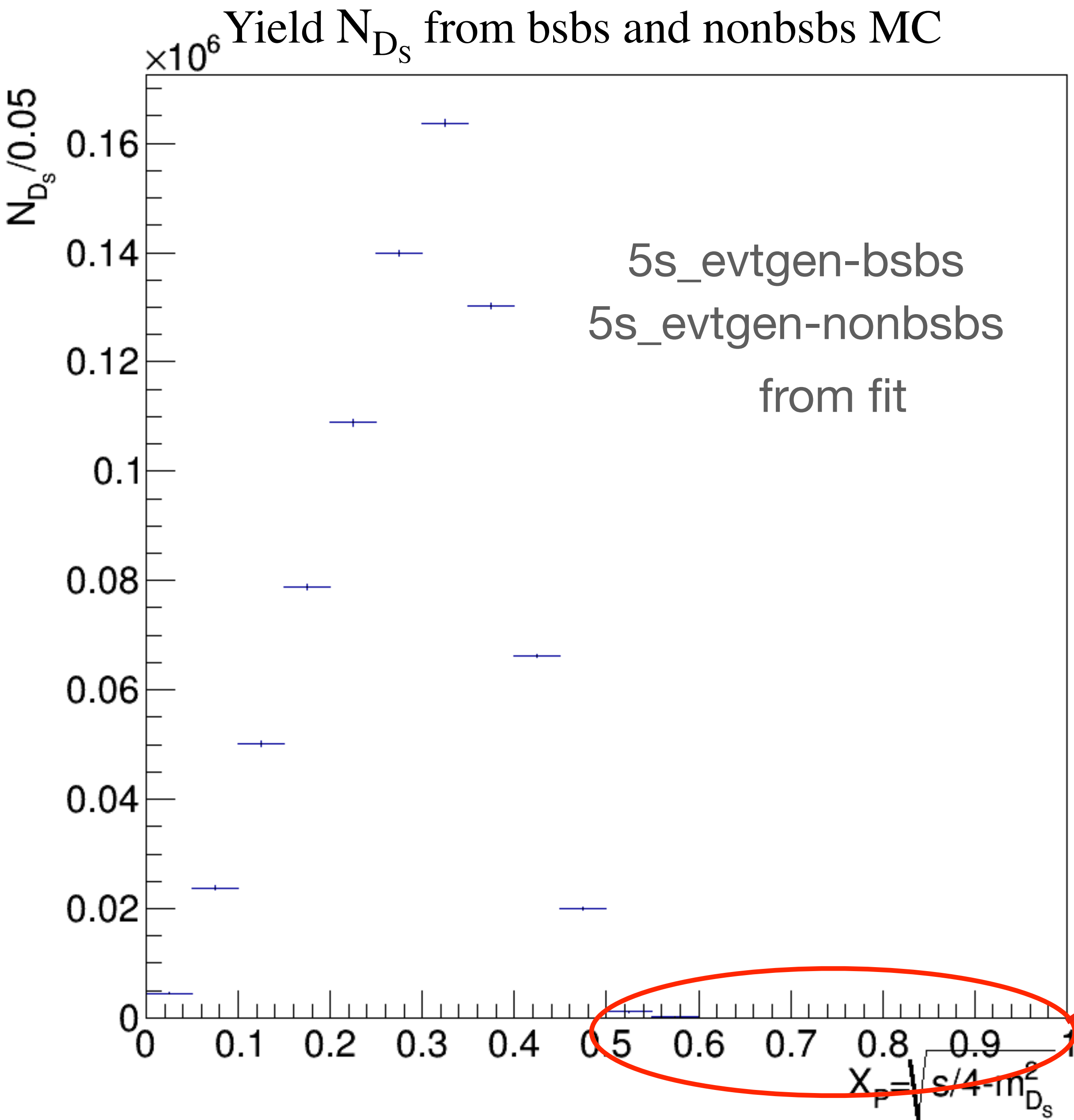
$\sigma(e^+e^- \rightarrow c\bar{c} \rightarrow D_s X)$



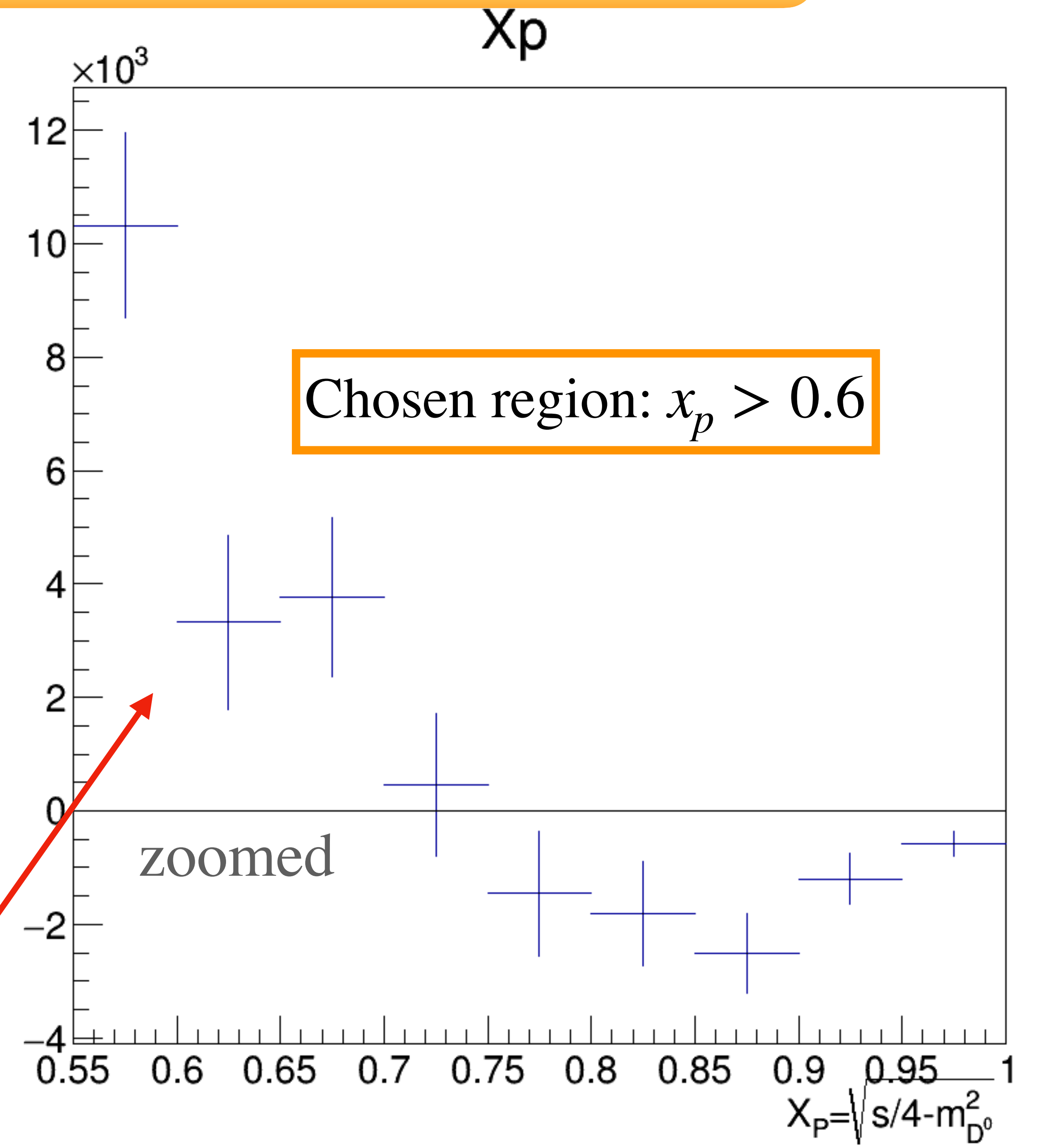
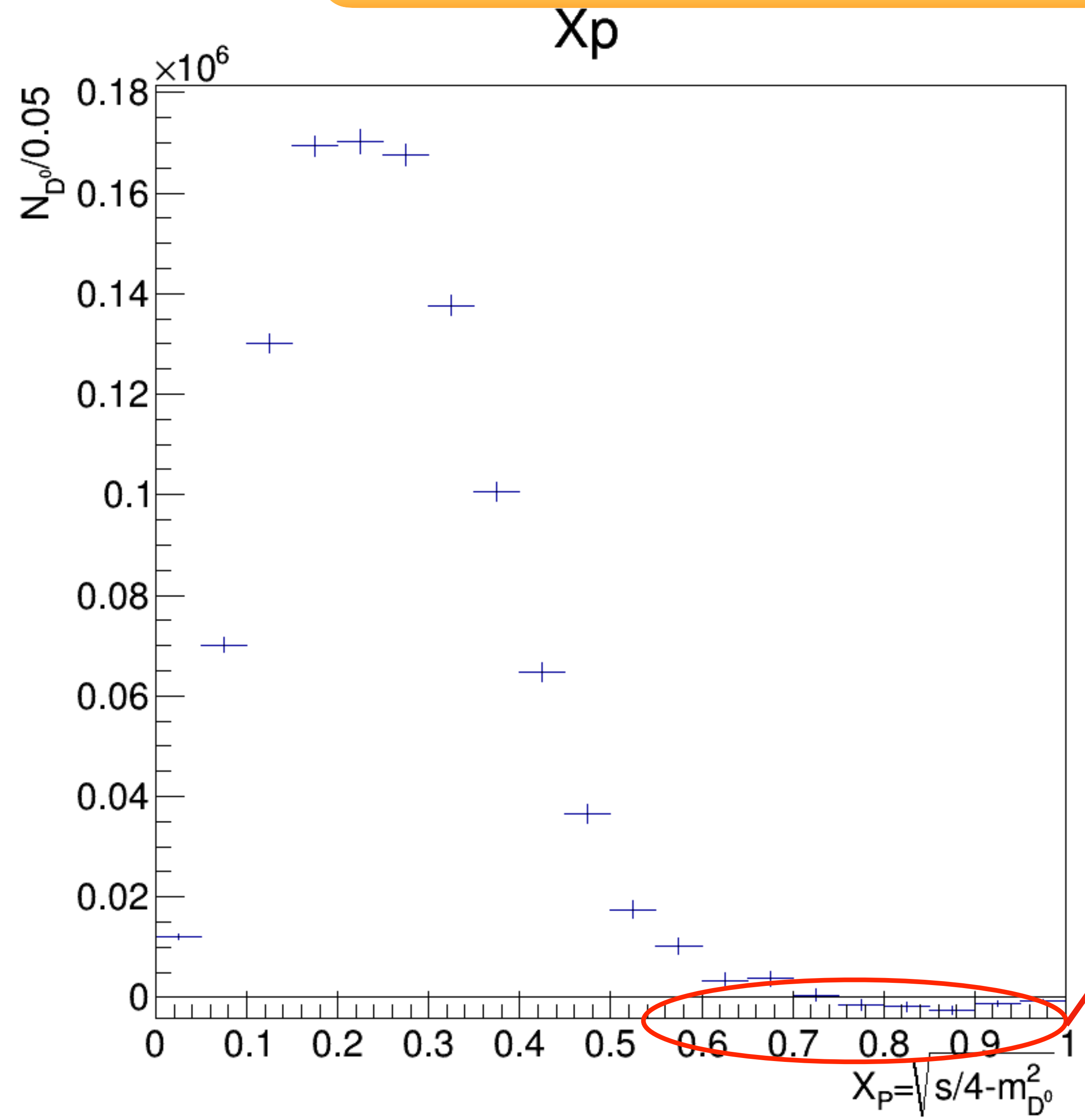
$\sigma(e^+e^- \rightarrow c\bar{c} \rightarrow D^0 X)$



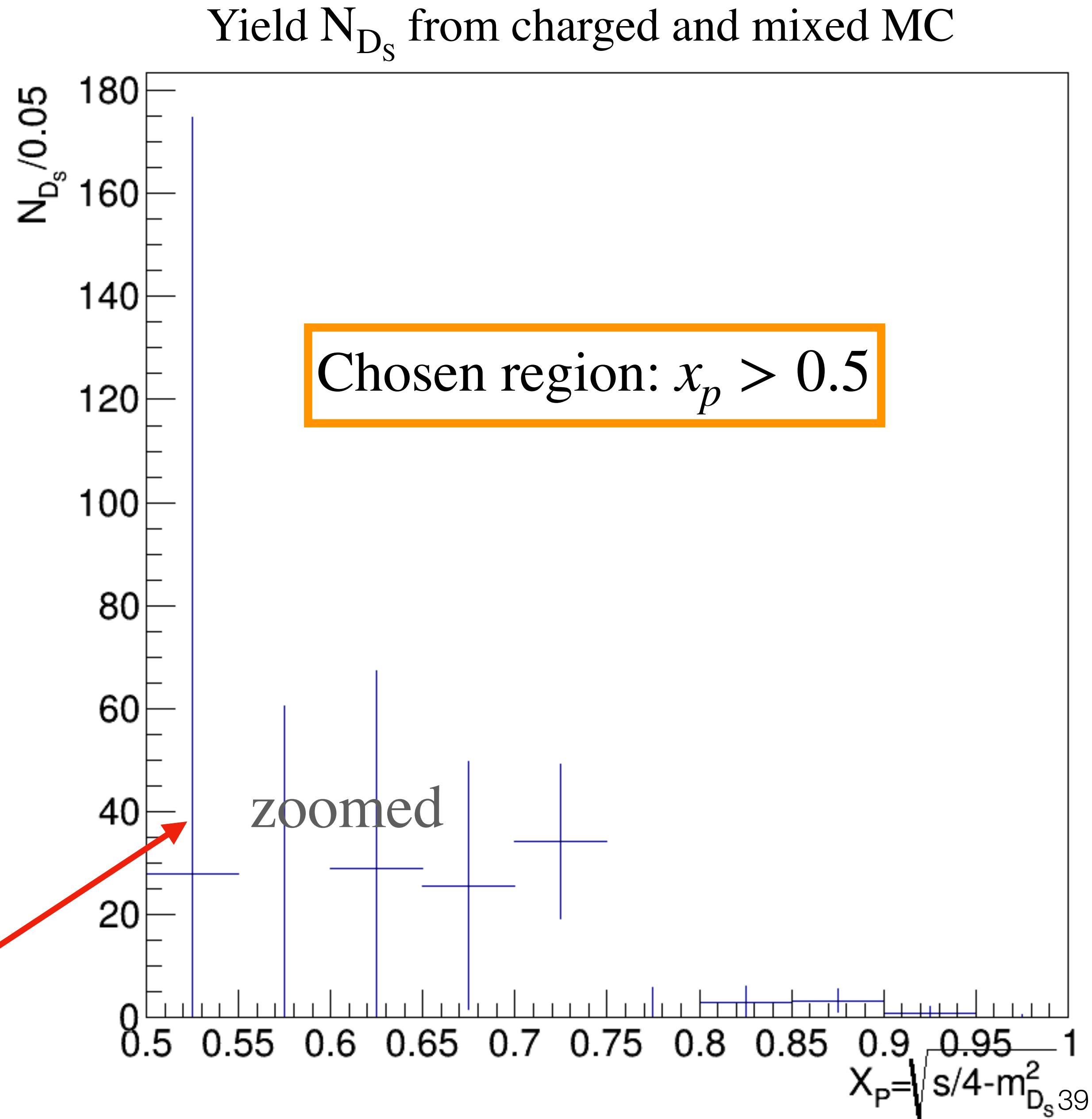
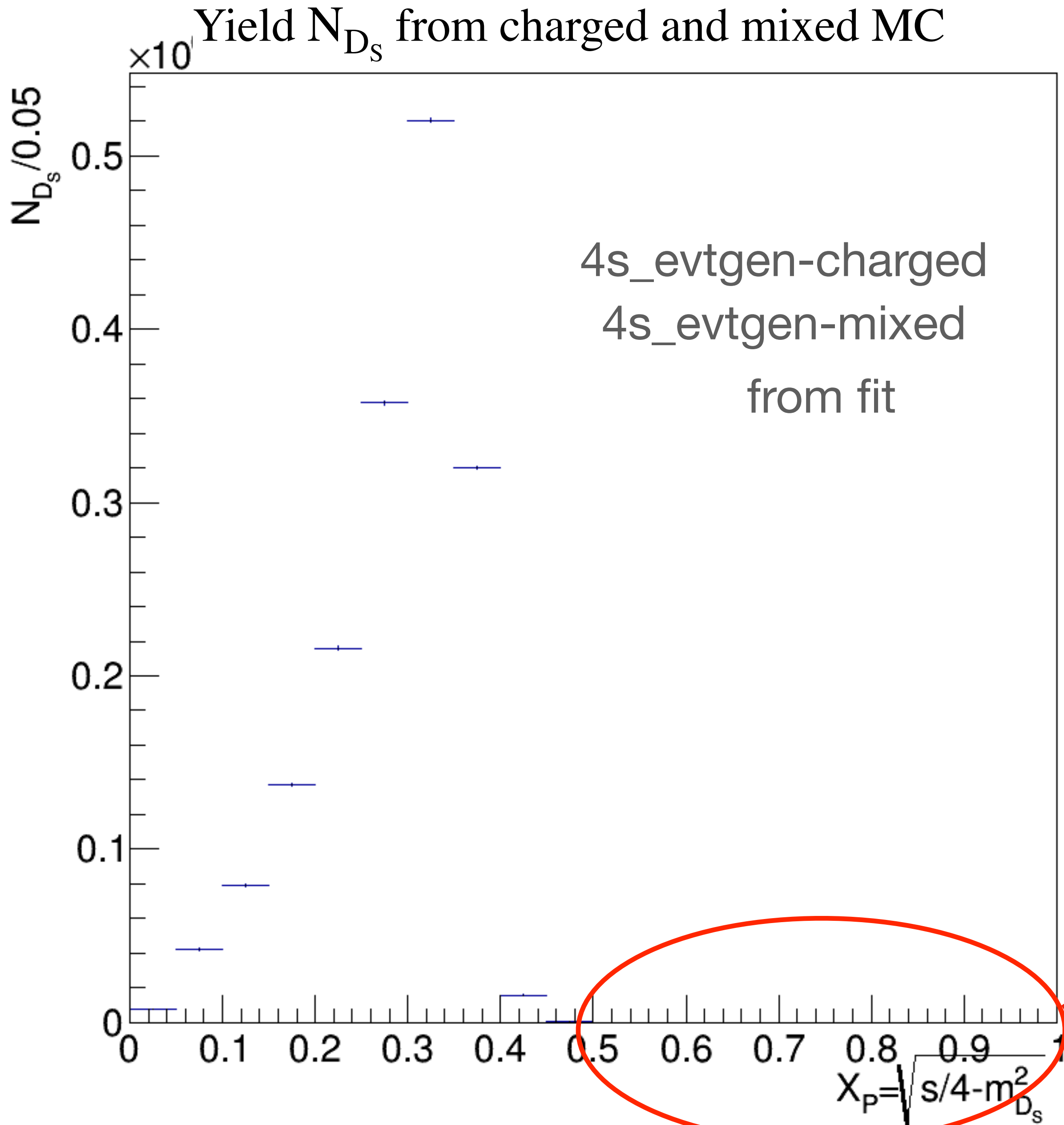
x_p spectra of D_S in bb MC at $\Upsilon(5S)$



Continuum spectrum subtraction for D^0 at $\Upsilon(5S)$

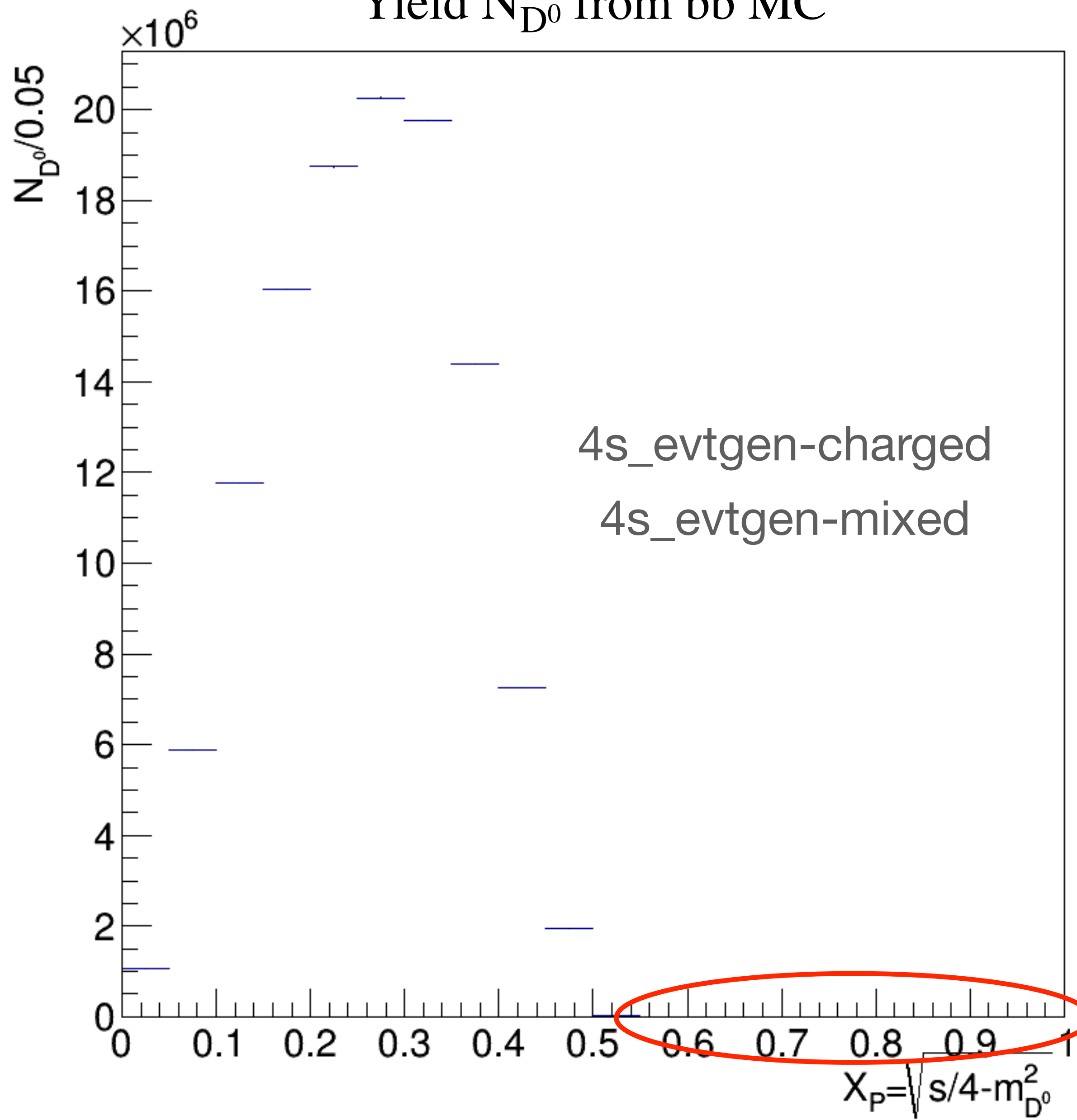


x_p spectra of D_S in bb MC at $\Upsilon(4S)$

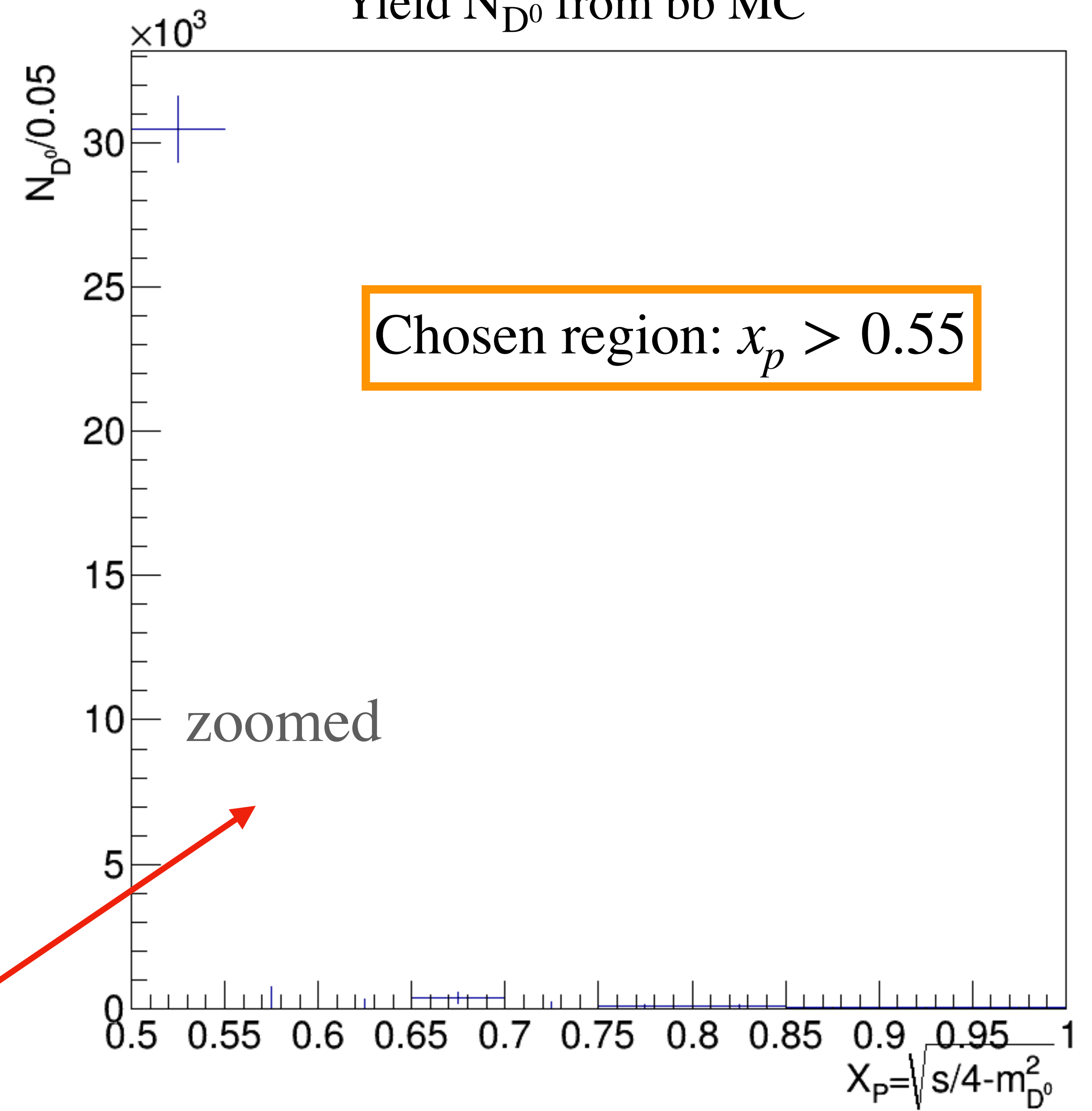


x_p spectra of D^0 in bb MC at $\Upsilon(4S)$

Yield N_{D^0} from bb MC

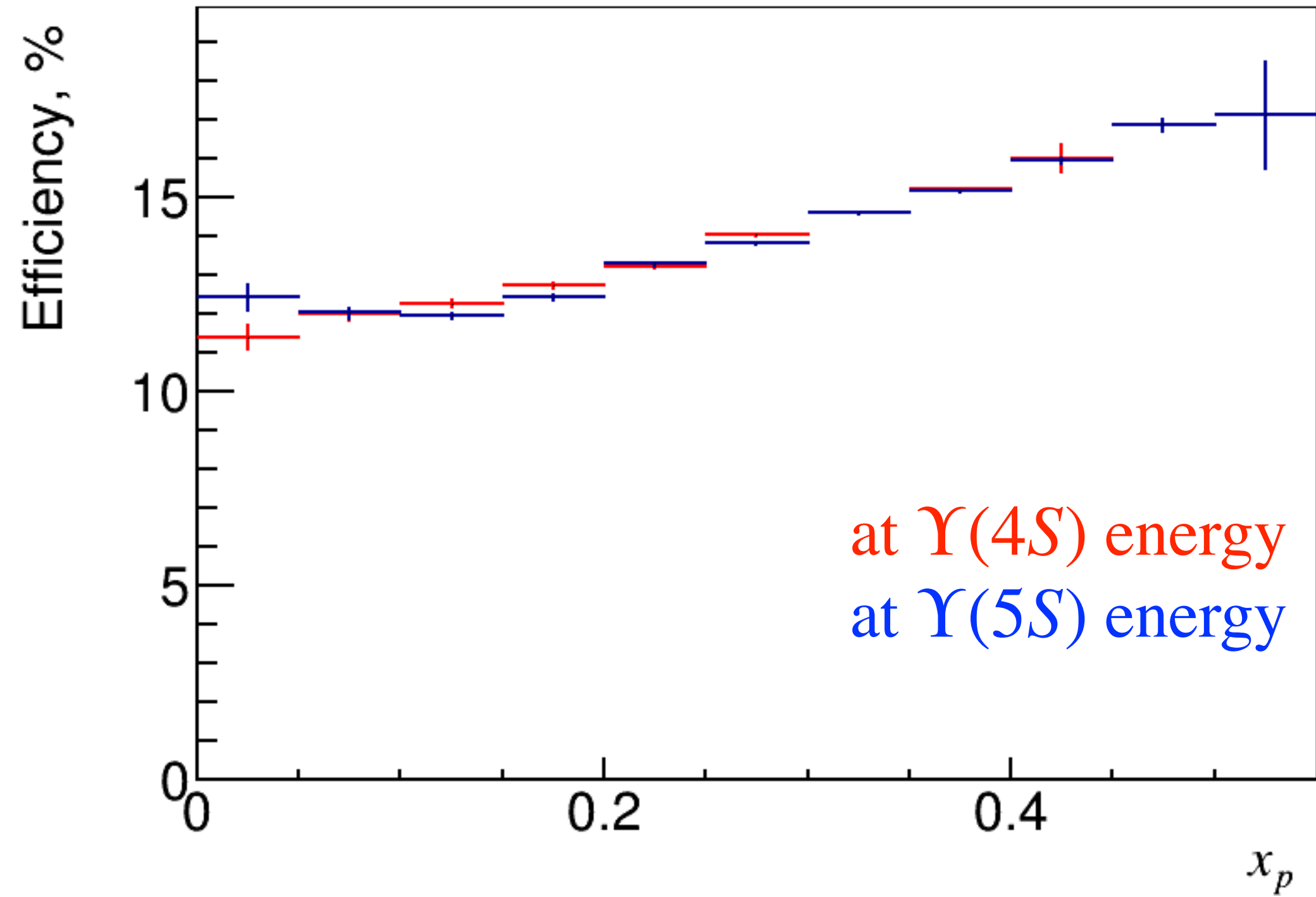


Yield N_{D^0} from bb MC

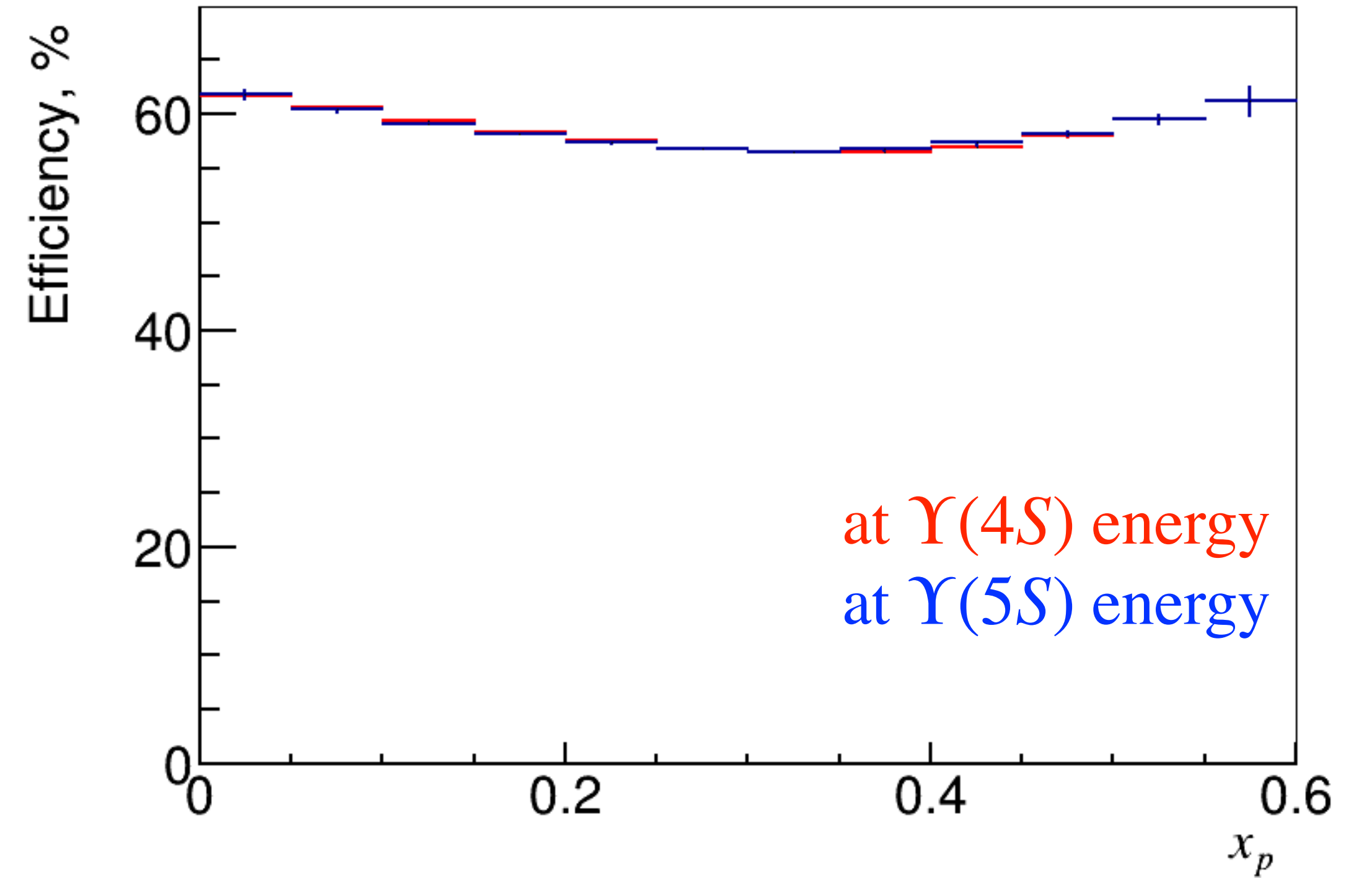


Reconstruction efficiency

D_s efficiency as function x_p



D^0 efficiency as function x_p



Systematic uncertainties in $\sigma(e^+e^- \rightarrow DX)$

Source	D _s at Y(5S)	D ⁰ at Y(5S)	D _s at Y(4S)	D ⁰ at Y(4S)
Fit model	0.6	0.3	1.0	1.1
Continuum xp spectrum statistical error	0.6	0.4	0.4	0.1
Continuum xp spectrum correction	0.3	1.3	-	-
MC statistical error	0.2	0.1	0.1	0.0
r ϕ	0.6	-	0.6	-
Tracking	1.1	0.7	1.1	0.7
K/ π identification	2.3	1.4	2.3	1.4
Luminosity	1.4	1.4	1.4	1.4
Branching fraction	1.9	0.8	1.9	0.8
Total	3.6	2.6	3.7	2.5

Continuum xp spectrum statistical error:

$$\frac{1}{\sigma} \sqrt{\sum_{i=1}^{i_{\max}} \left(\sigma_i \frac{\Delta n_i k}{N_i - k n_i} \right)^2}$$

MC statistical error:

$$\frac{1}{\sigma} \sqrt{\sum_{i=1}^{i_{\max}} \left(\sigma_i \frac{\Delta \mathcal{E}_i}{\mathcal{E}_i} \right)^2}$$