

# The effective theory of RHv

*d=5 operators @ future colliders*

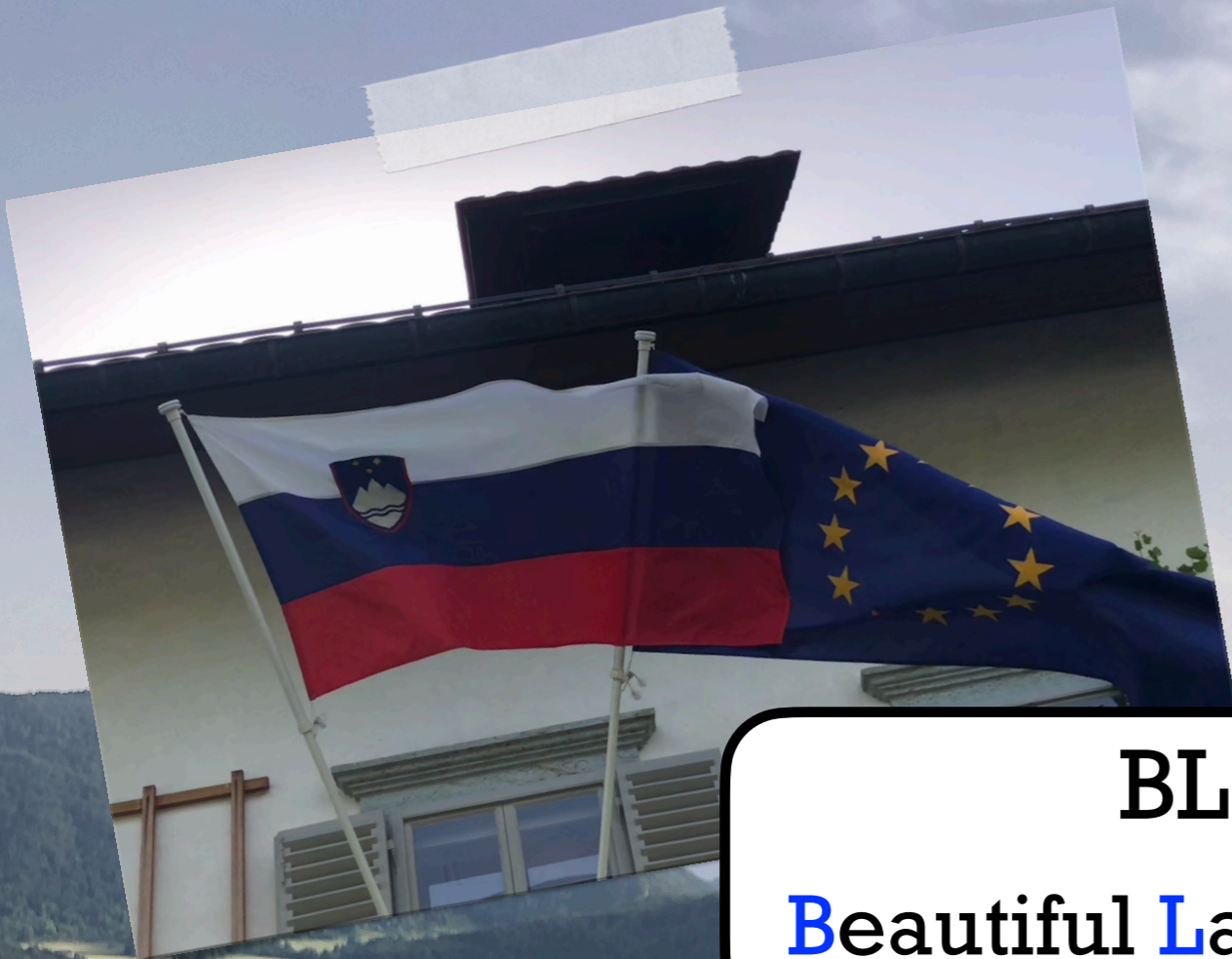
Daniele Barducci



Bled 2024 - International workshop on LNV

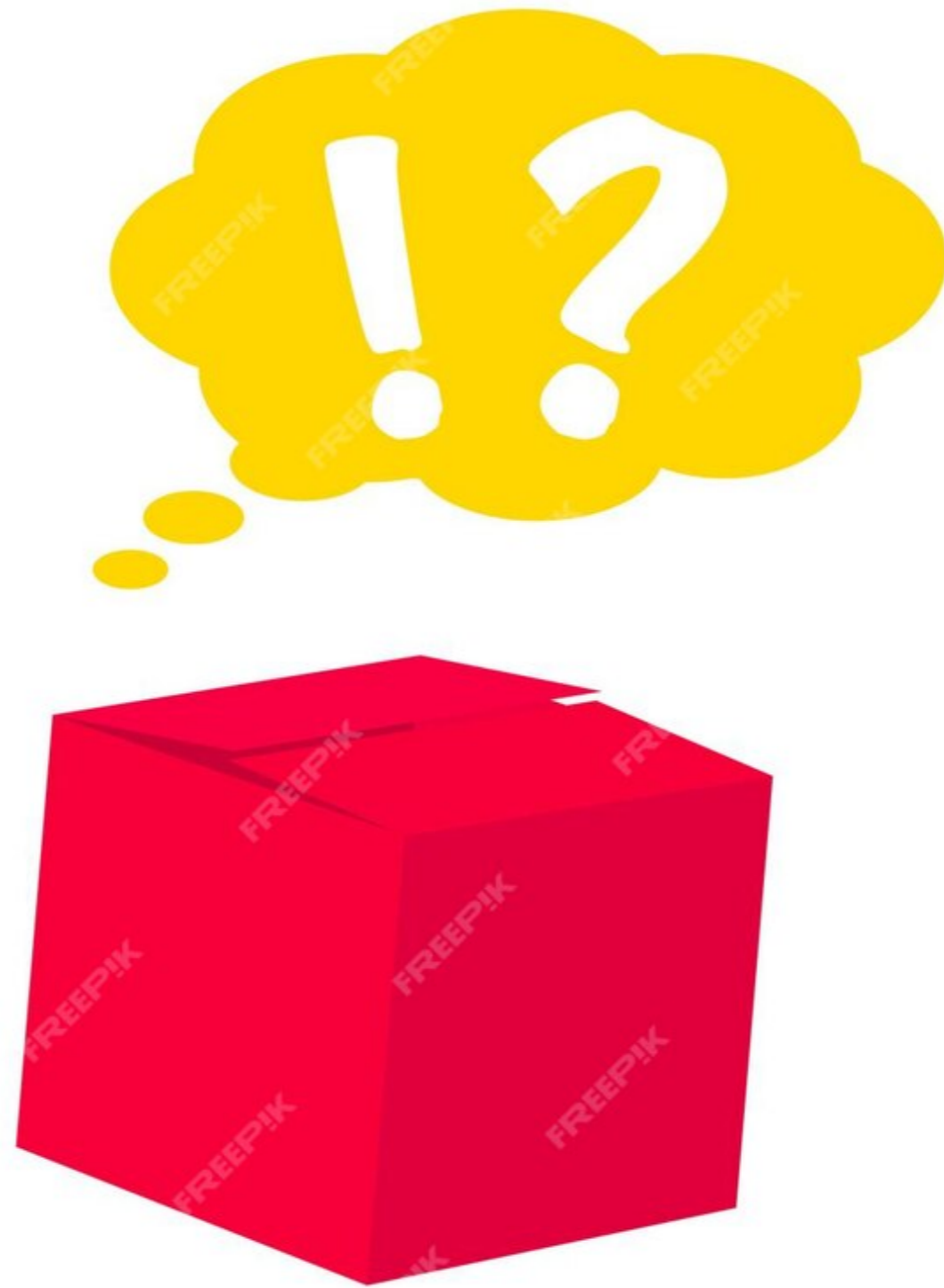






**BLED**  
Beautiful Lake Et D=5





Neutrinos have masses!!!



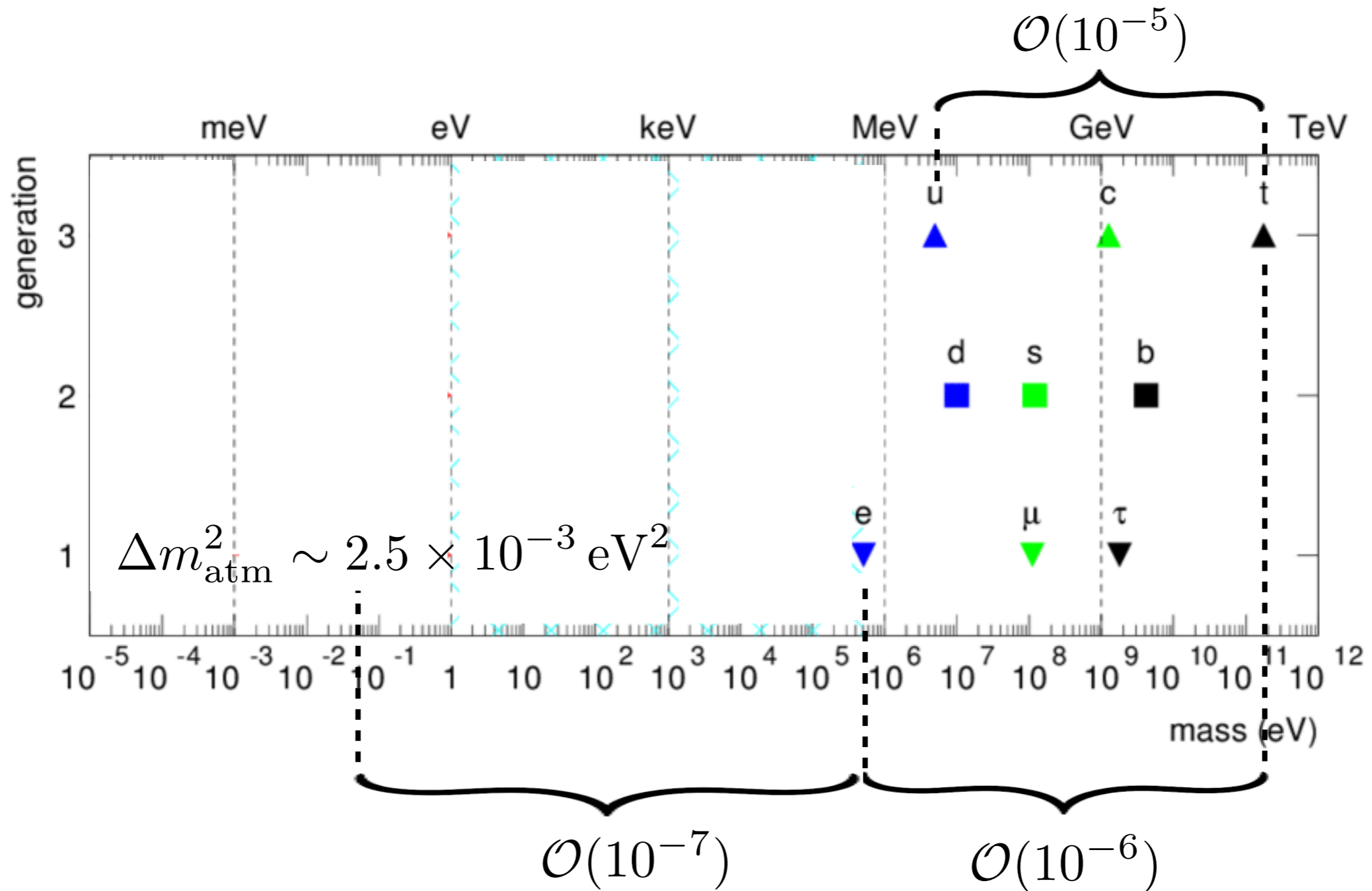
Neutrinos have masses!!!

Neutrinos oscillate!!!



# Neutrino masses

- Perhaps not too much a surprise, all the known fermions have mass...
- Also their lightness might not be an issue...



# Neutrino oscillation

- Neutrino flavor mix, but again this is not new...
- Quark flavor mixes too, even though quark oscillations are not visible

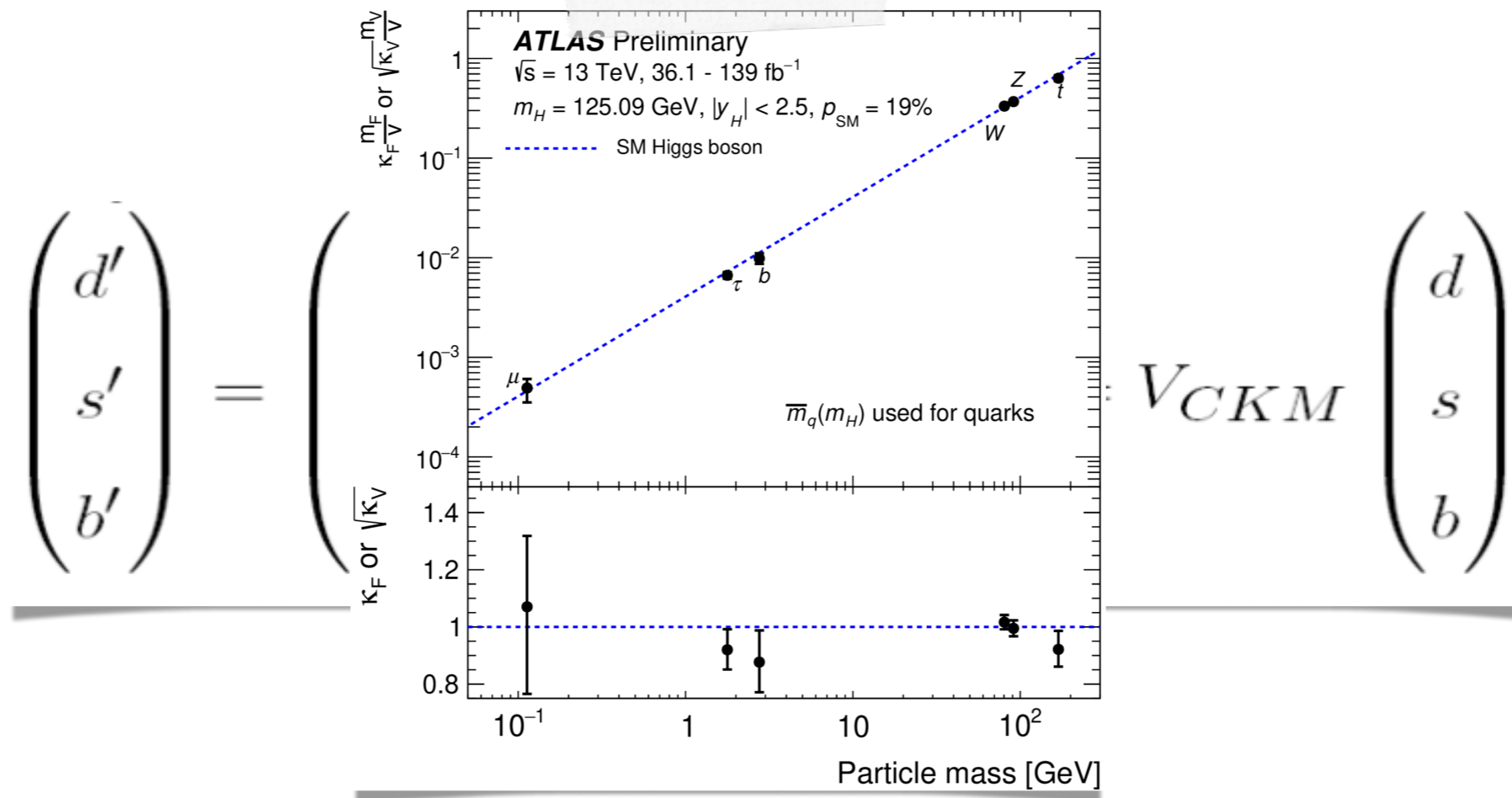
$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix} = V_{CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

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# Neutrino oscillation

- Neutrino flavor mix, but again this is not new...
- Quark flavor mixes too, even though quark oscillations are not visible



- CKM comes from the Yukawa sector, from which we believe fermions get mass
- We do not know if neutrinos get mass from the Higgs VEV, but we do not have direct evidence for  $e, u, d, s, c$  either...

**So... what's the big deal?**

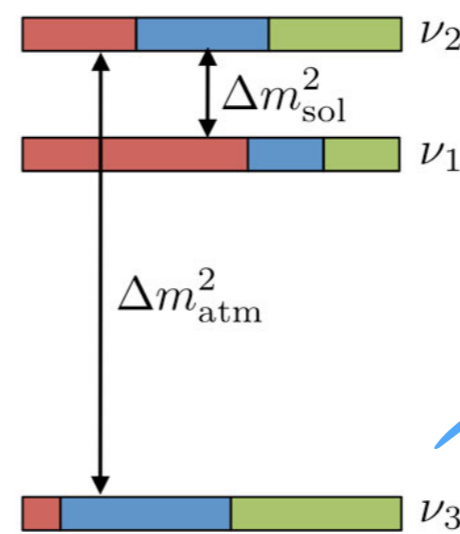
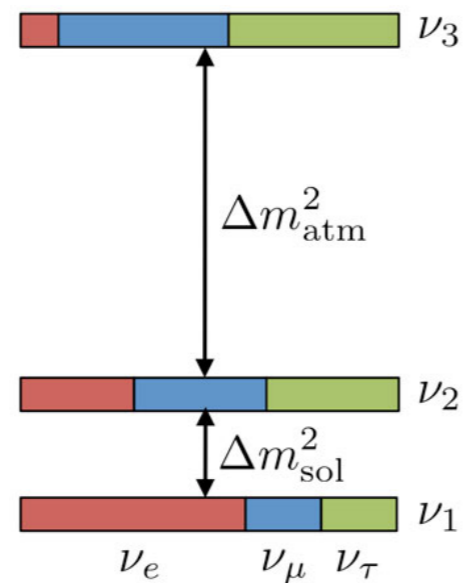
- Neutrino oscillations only require two out of three neutrino to have a mass

$$\Delta m_{\text{atm}}^2 \sim 2.5 \times 10^{-3} \text{ eV}^2$$

$$\Delta m_{\text{sol}}^2 \sim 7.5 \times 10^{-5} \text{ eV}^2$$

normal hierarchy (NH)

inverted hierarchy (IH)



can still be massless!

Still do not know what nature has chosen

- Neutrino masses can arise in a completely different way...

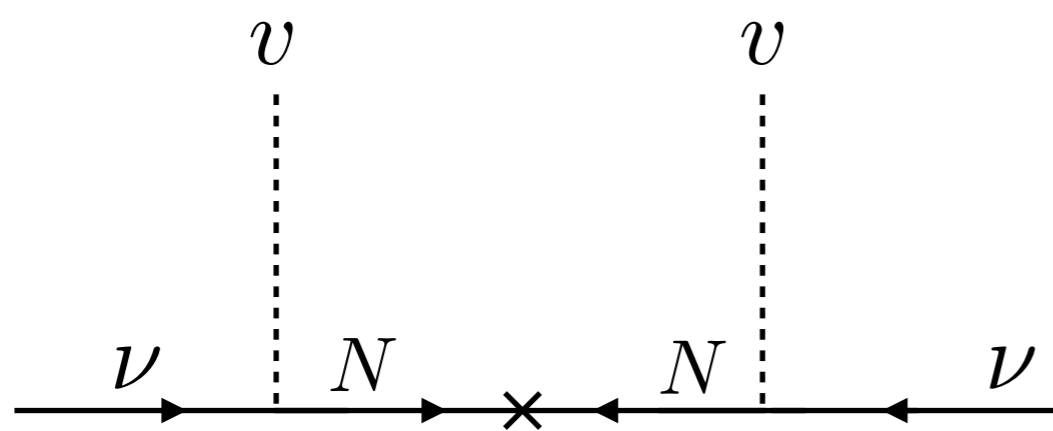
- Neutrino can get Dirac masses in the usual way via Yukawa interactions

$$-\mathcal{L} = Y_\nu L H N + h.c. \quad \begin{array}{c} \nu \\ \longrightarrow \bullet \longrightarrow \\ N \end{array} \quad m_\nu \sim Y_\nu v$$

- A fermion singlet under the SM group can also have a Majorana mass

$$-\mathcal{L} = Y_\nu L H N + \frac{M_N}{2} N^2 + h.c.$$

- Neutrinos acquire Majorana masses too



$$\left\{ \begin{array}{l} m_N \sim M_N \\ m_\nu \sim \frac{Y_\nu^2 v^2}{M_N} \end{array} \right.$$

- Neutrino can get Dirac masses in the usual way via Yukawa interactions

$$-\mathcal{L} = Y_\nu LHN + h.c. \quad \begin{array}{c} \nu \\ \longrightarrow \bullet \longrightarrow \\ N \end{array} \quad m_\nu \sim Y_\nu v$$

- Works also for  $SU(2)_L$  triplets, since they are real irreps

$$-\mathcal{L} = Y_\nu LH\Sigma + \frac{M_\Sigma}{2}\Sigma^2 + h.c.$$

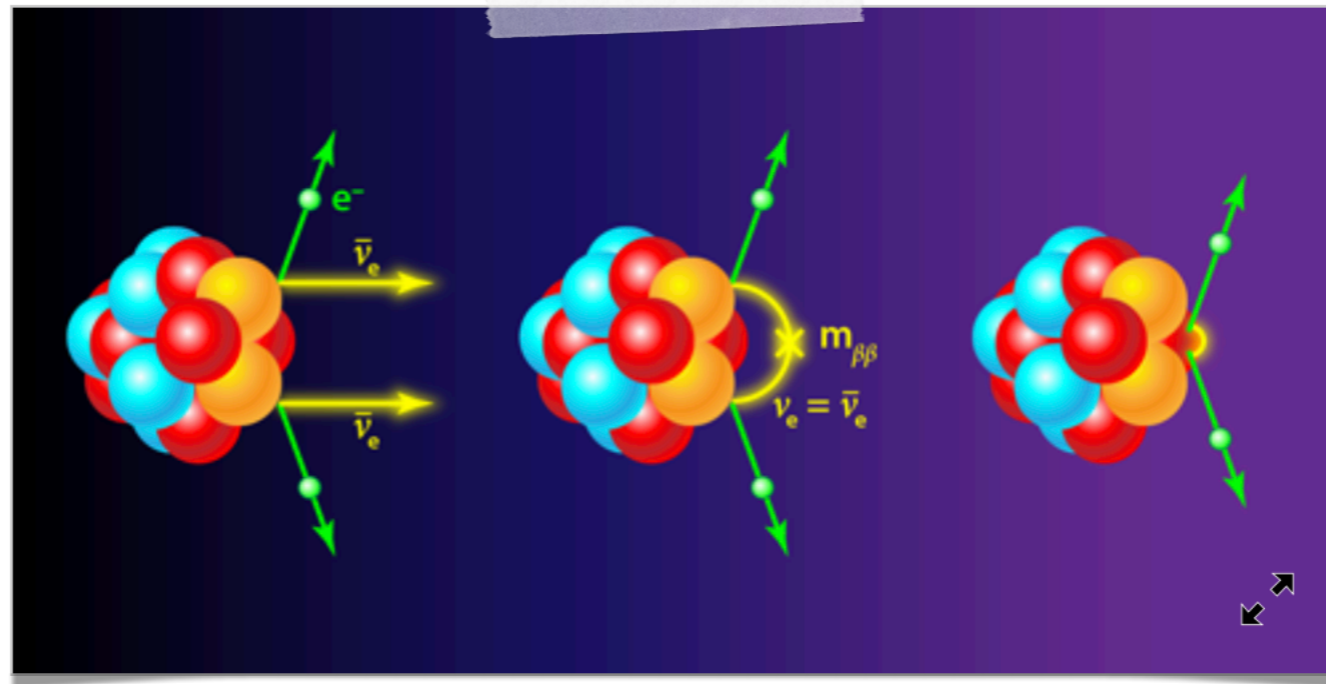
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$$\left\{ \begin{array}{l} m_N \sim M_\Sigma \\ m_\nu \sim \frac{Y_\nu^2 v^2}{M_\Sigma} \end{array} \right.$$

- In both cases lepton number is violated by two units

$$\Delta L = 2$$

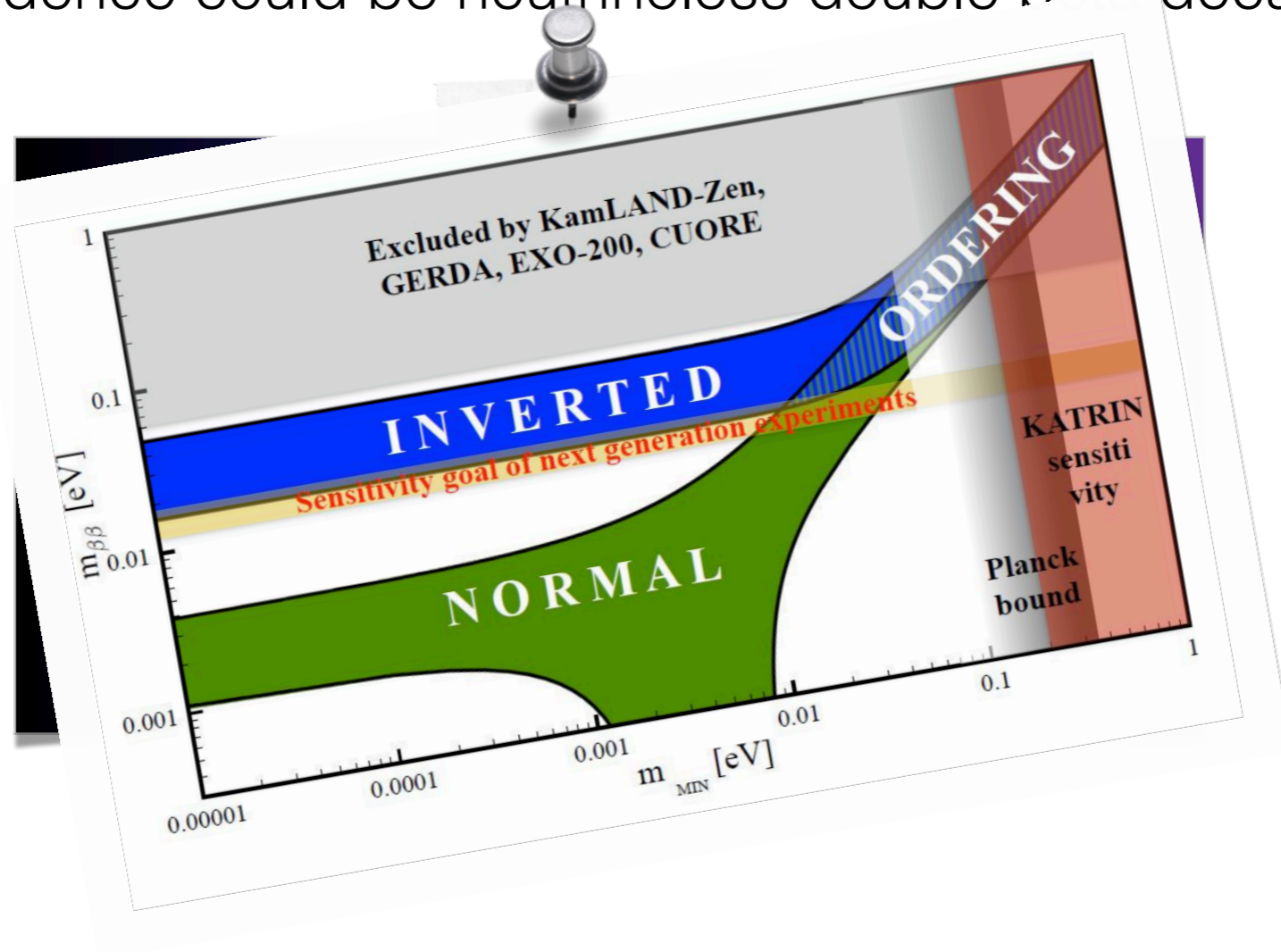
- Accidental symmetry of the SM, no need to be a symmetry of a final theory
- Most striking evidence could be neutrinoless double beta decay



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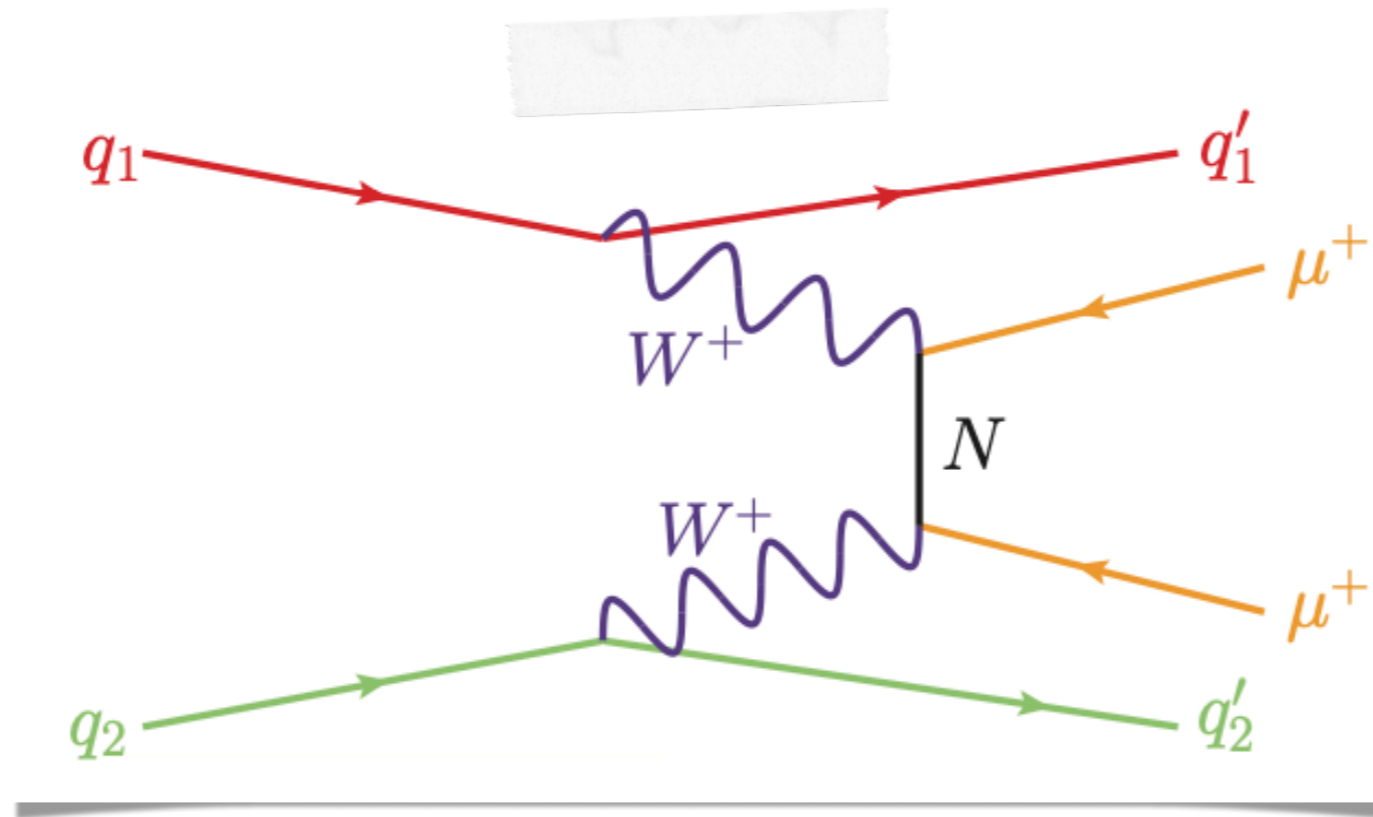
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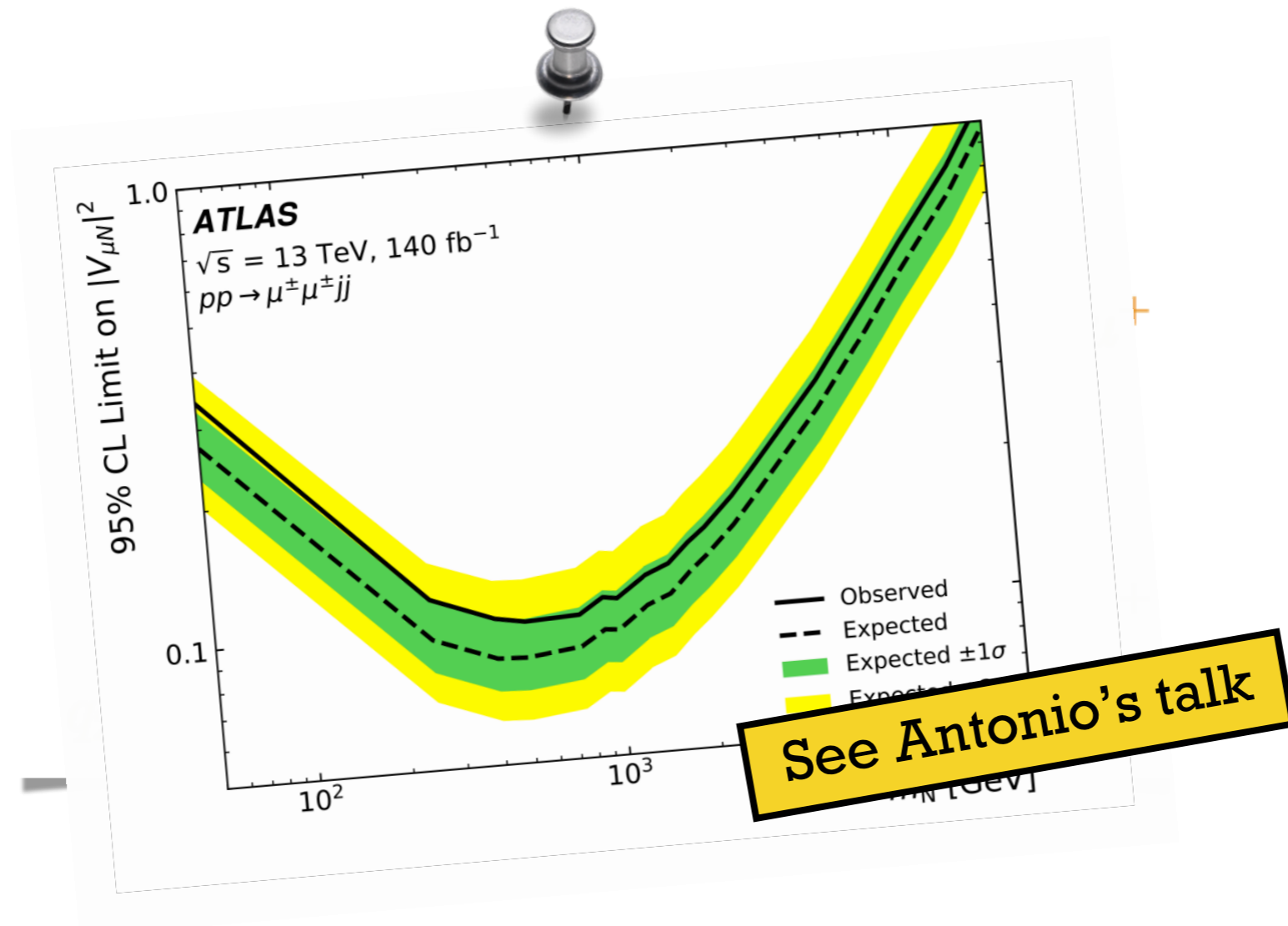
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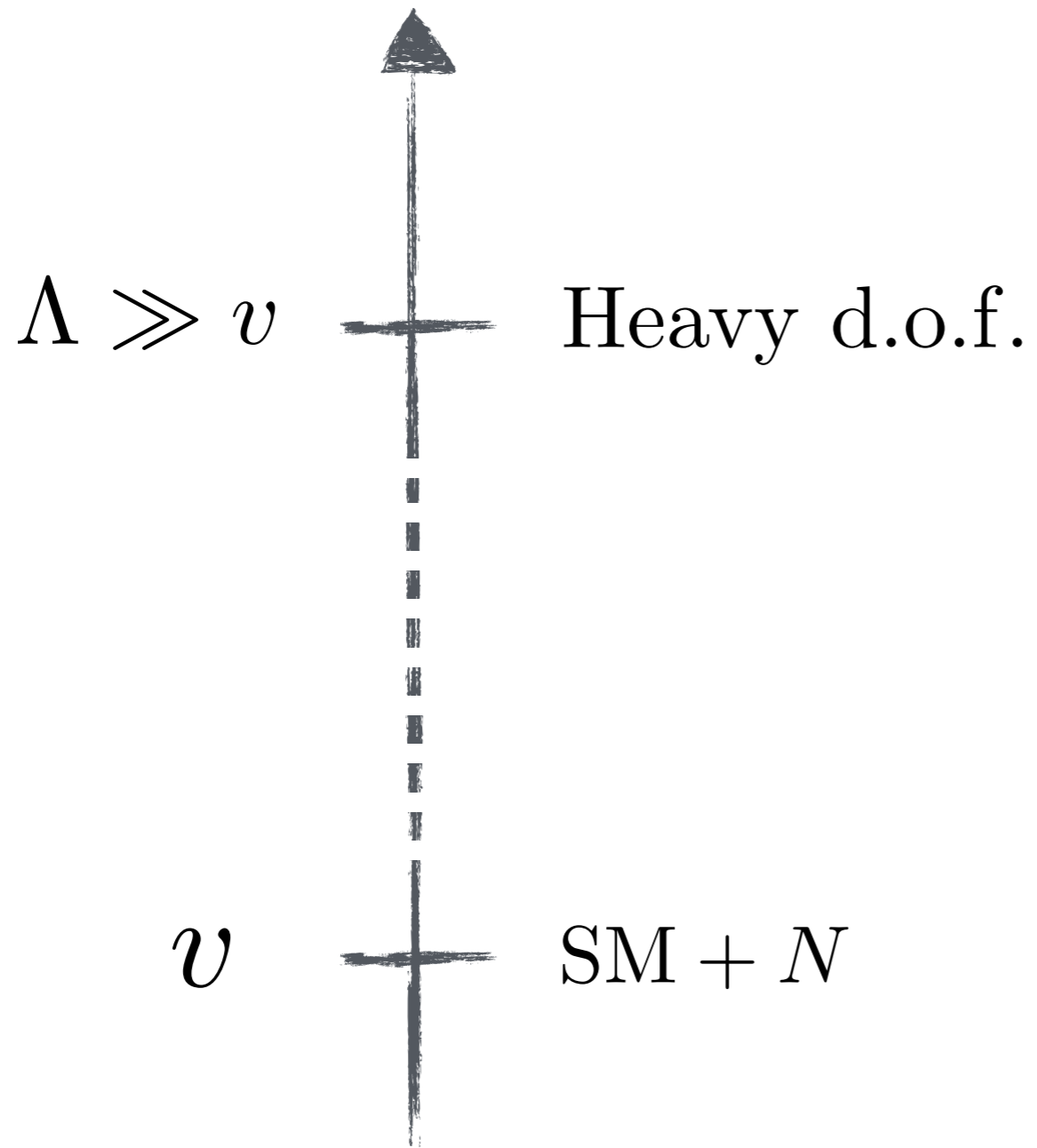
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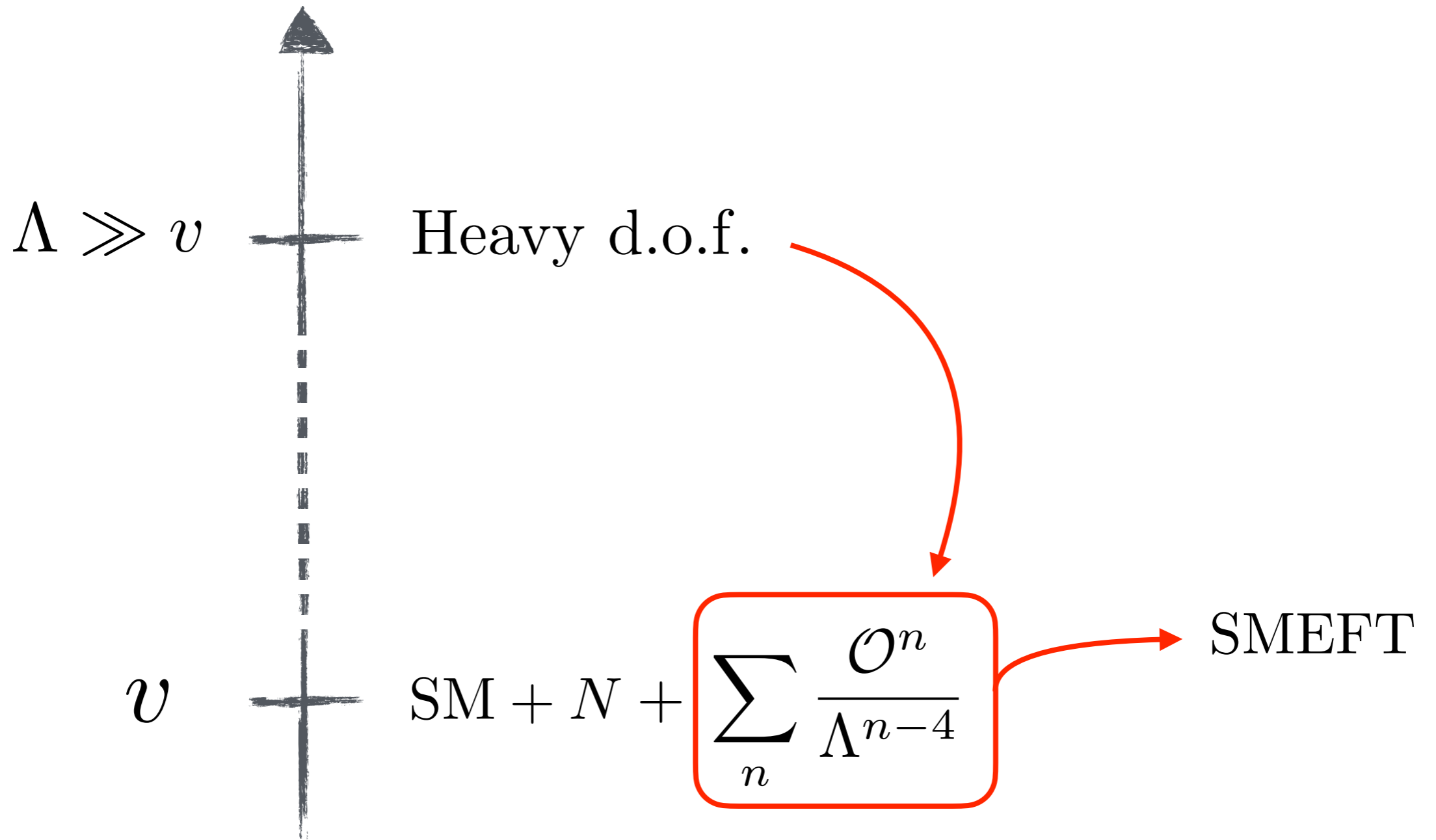




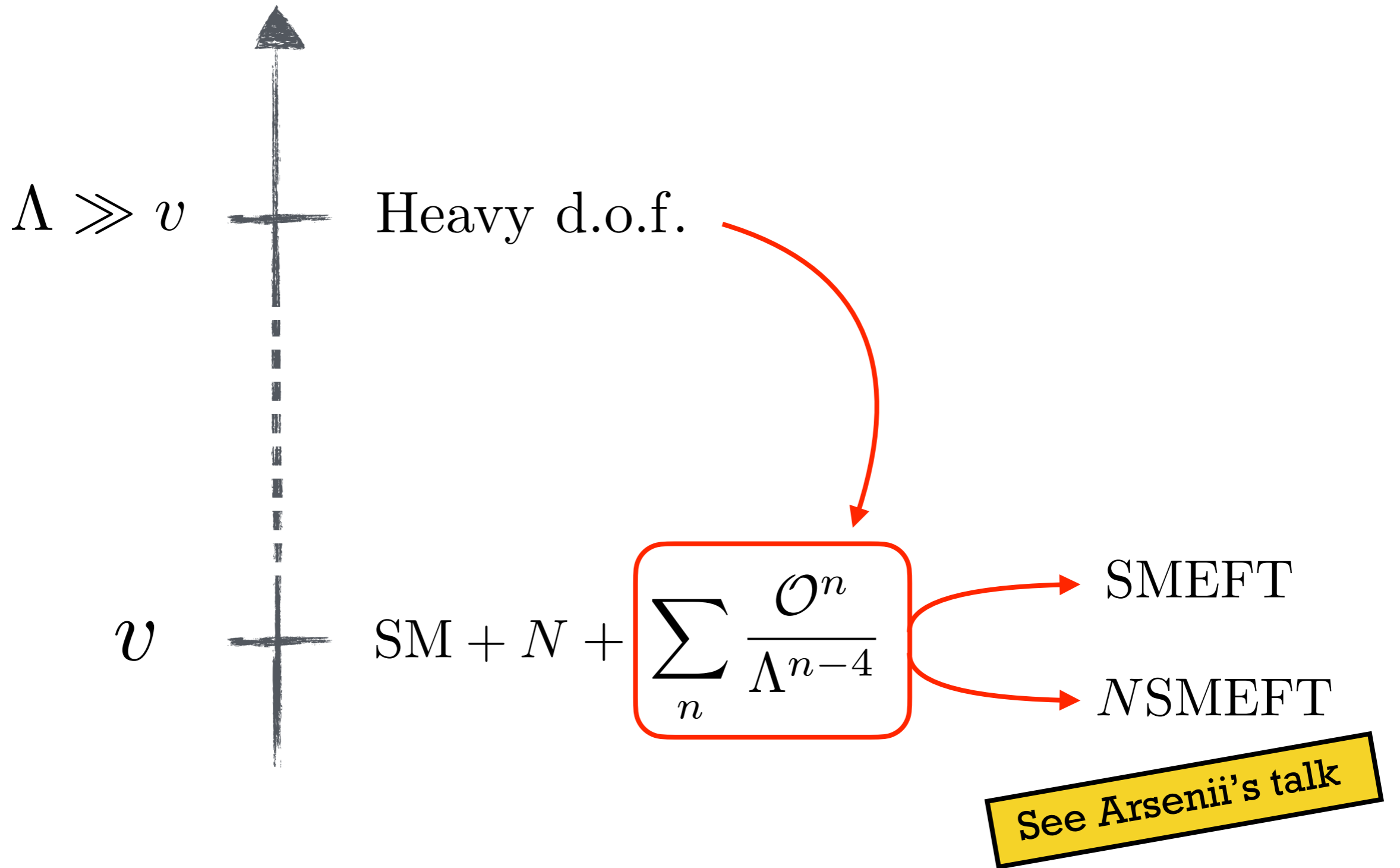
# Beyond naive see-saw



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# Beyond naive see-saw



- Non redundant basis has been worked out up to  $d = 7$  [Liao, Ma 1612.04527]
- At  $d = 5$  only two new operators exist [Graesser 0704.0438, Aparici+ 0904.3244]

$$\mathcal{O}_{NH} = |H|^2 N^2$$

$$\mathcal{O}_{NB} = N \sigma^{\mu\nu} N B_{\mu\nu}$$

Adds extra contributions to the neutrino mass matrix

Vanishes with a single right-handed neutrino

**Pheno consequences?**

# Higgs operator

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \bar{N}\not{\partial}N - \bar{L}_L Y_\nu \tilde{H} N - \frac{1}{2} M_N \bar{N}^c N + \alpha_{NH} (\bar{N}^c N) (H^\dagger H) + h.c.$$

## EWSB

$$-\frac{1}{2} \bar{n}^c \mathcal{M} n + h.c. = -\frac{1}{2} \bar{n}^c \begin{pmatrix} 0 & Y_\nu v \\ Y_\nu^T v & M_N - 2\alpha_{NH} \frac{v^2}{\Lambda} \end{pmatrix} n + h.c. \quad n = (\nu_L, N^c)$$

neglect it, see later...

- Standard see-saw mass relation

$$m_\nu \simeq v^2 Y_\nu \frac{1}{M_N} Y_\nu^T = U^* m_\nu^{(d)} U^\dagger$$

- For single RH neutrino 1-to-1 correspondence between heavy mass and mixing

$$\theta \sim \frac{yv}{M_N} \sim \sqrt{\frac{m_\nu}{M_N}} \sim 7.2 \times 10^{-6} \left( \frac{1 \text{ GeV}}{m_N} \right)^{1/2}$$

- With additional RH states extra freedom, best seen in the Casas-Ibarra formalism

$$m_\nu \simeq v^2 Y_\nu \frac{1}{M_N} Y_\nu^T = U^* m_\nu^{(d)} U^\dagger$$

**solved with**

$$Y_\nu \simeq \frac{1}{v} U^* \sqrt{\mu} \sqrt{M_N}$$

$$\sqrt{\mu} \sqrt{\mu}^T = m_\nu^{(d)}$$

- Write  $\sqrt{\mu} = \sqrt{m} \mathcal{R}$  with  $\begin{cases} \sqrt{m} \\ \mathcal{R} \end{cases}$

matrix containing physical neutrino masses  
complex orthogonal matrix

- For example, with 2 RH neutrinos

$$\sqrt{m_{NH}} = \begin{pmatrix} 0 & 0 \\ 0 & \sqrt{m_2} \\ \sqrt{m_3} & 0 \end{pmatrix}$$

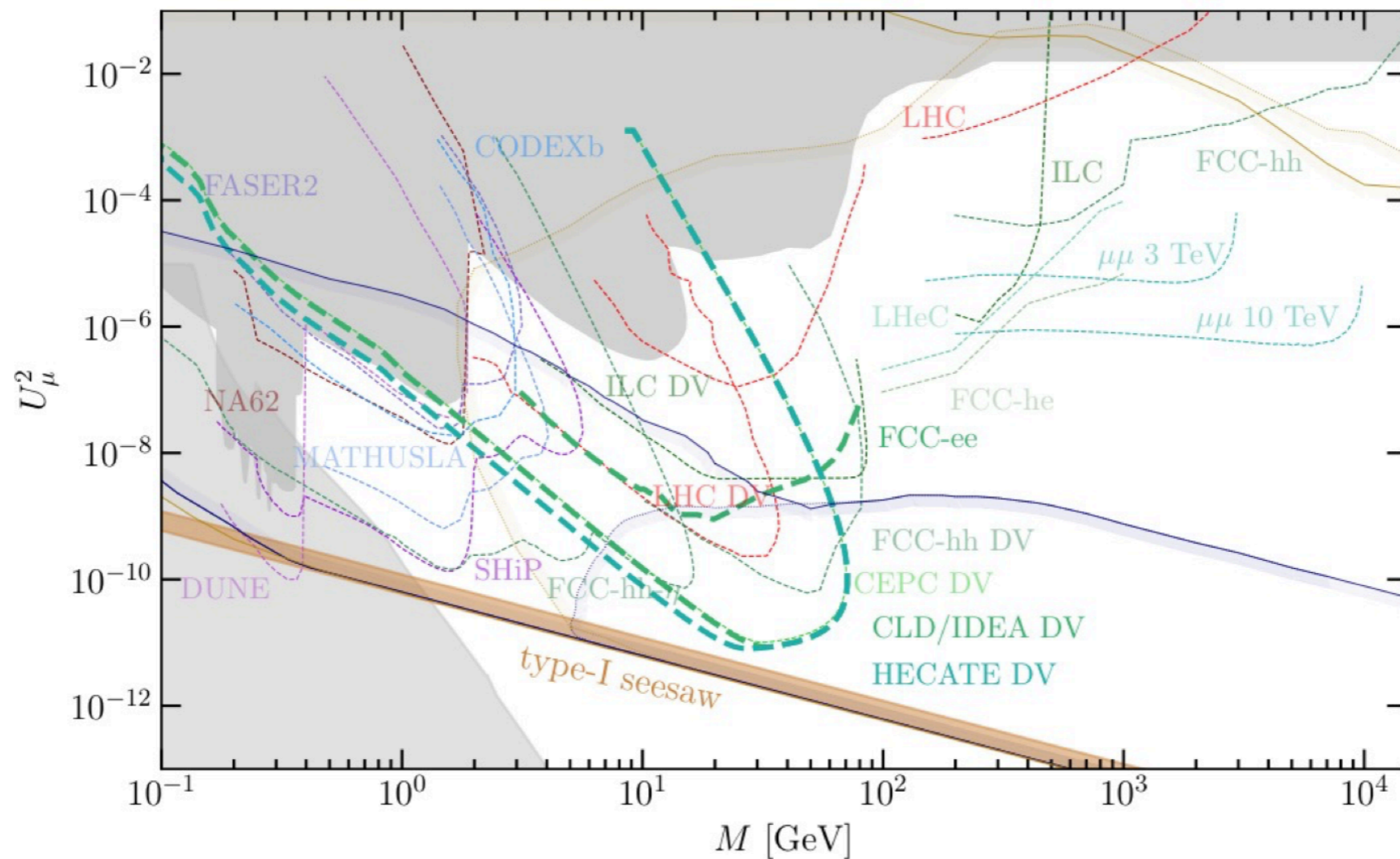
$$\mathcal{R} = \begin{pmatrix} \cos z & \pm \sin z \\ -\sin z & \pm \cos z \end{pmatrix}$$

$$z = \beta + i\gamma$$

- Complex angle in  $\mathcal{R}$  gives an exponential enhancement of the mixing

$$\theta \sim 7.2 \times 10^{-6} e^{\gamma - i\beta} \left( \frac{1 \text{ GeV}}{m_N} \right)^{1/2}$$

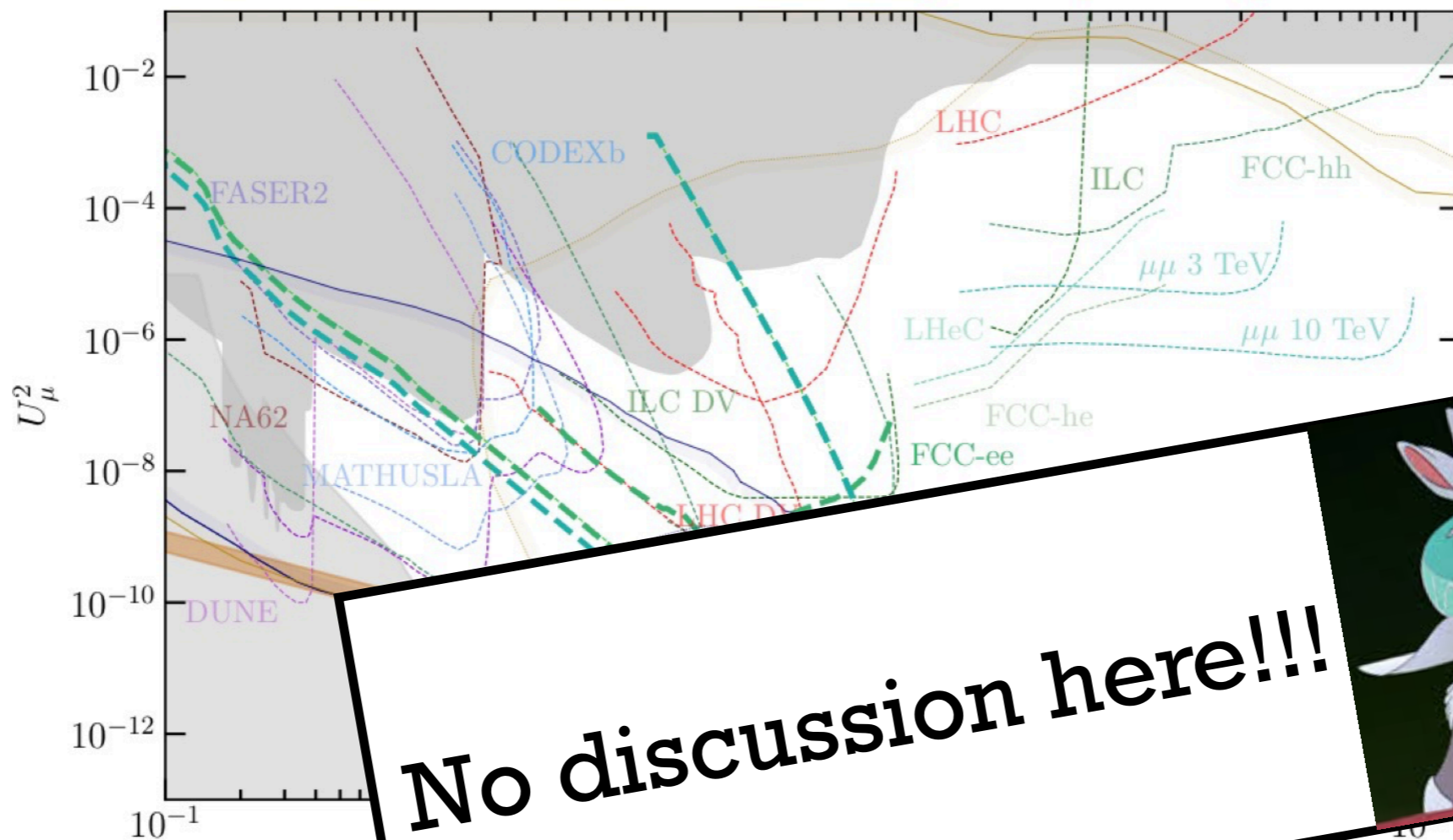
- $m_N$  and  $\theta$  can be taken almost as independent parameters - **back here**



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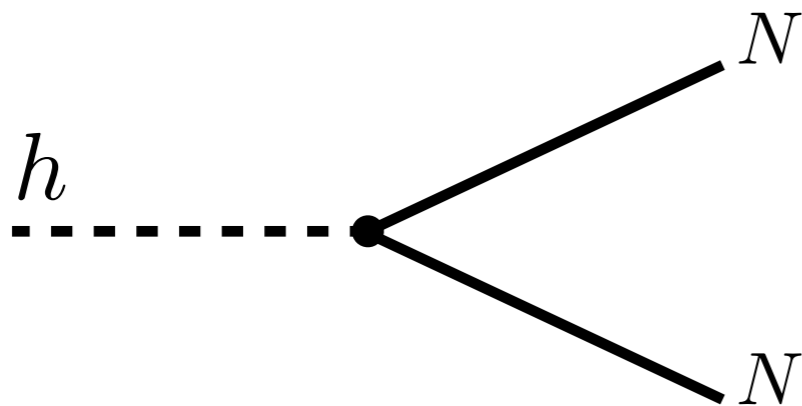
**No discussion here!!!**





- After EWSB the  $|H|^2 N^2$  operator triggers new decay mode for light  $N$

$$\frac{1}{\Lambda} |H|^2 N^2 \xrightarrow{\text{EWSB}} \frac{v}{\Lambda} h N^2$$



$$\Gamma = \frac{1}{2\pi} \frac{v^2}{\Lambda^2} m_H \left( 1 - \frac{4m_N^2}{m_H^2} \right)^{3/2}$$

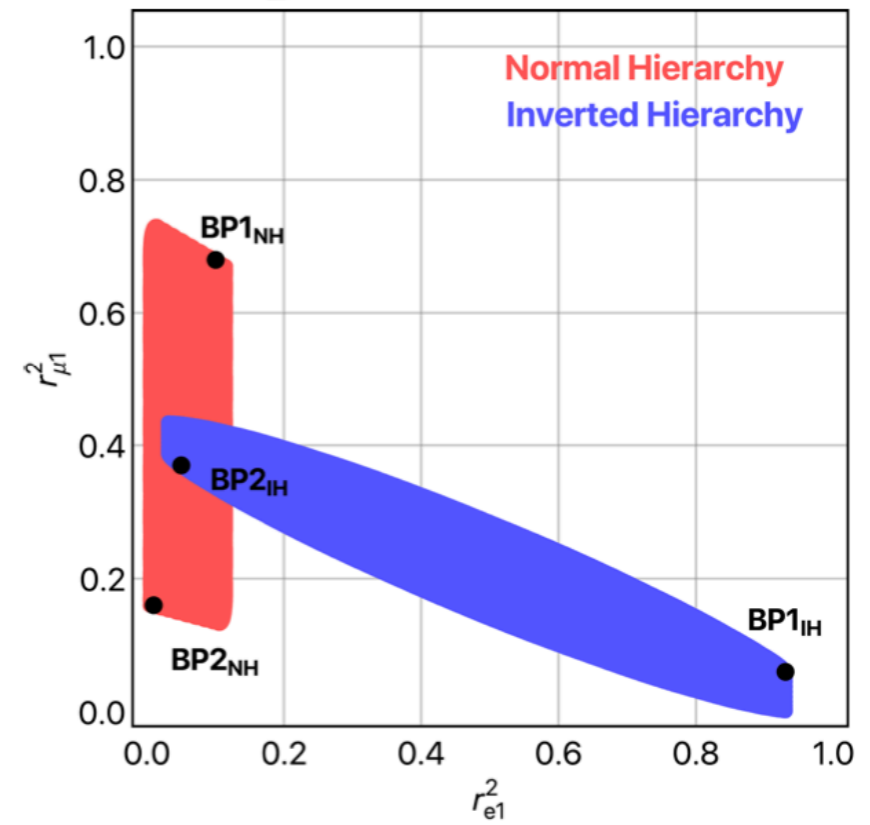
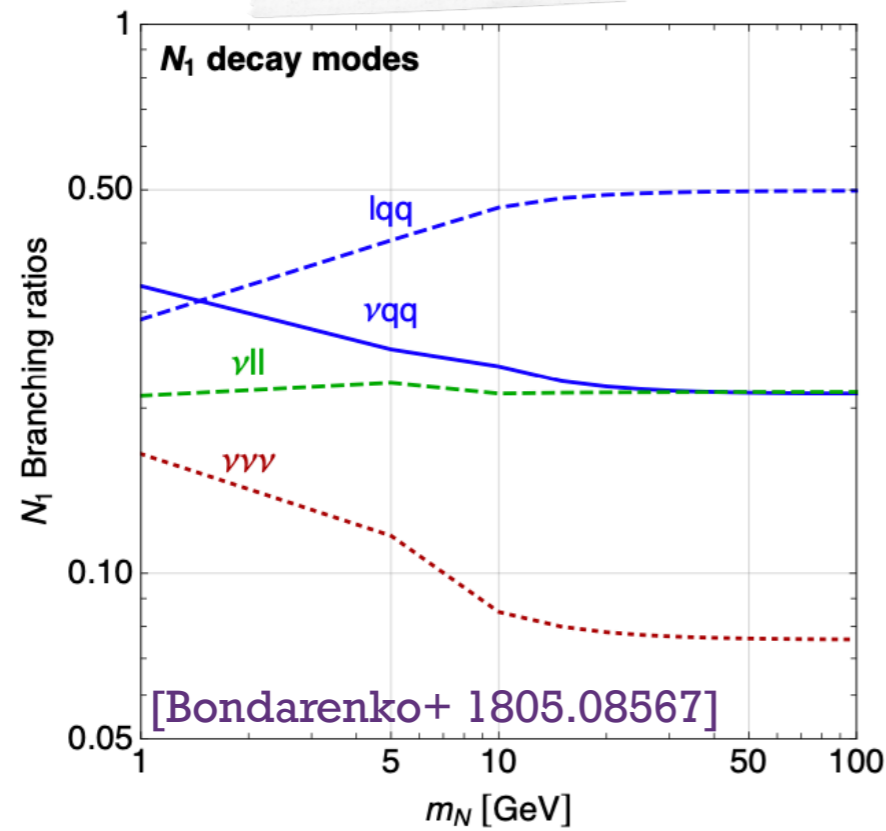
See Fabrizio's talk

### Pheno predictions

- Untagged / invisible Higgs decay if  $N$  is detector stable
- Distinctive signatures, either prompt or displaced from  $N$  decay

# Sterile neutrino decay modes

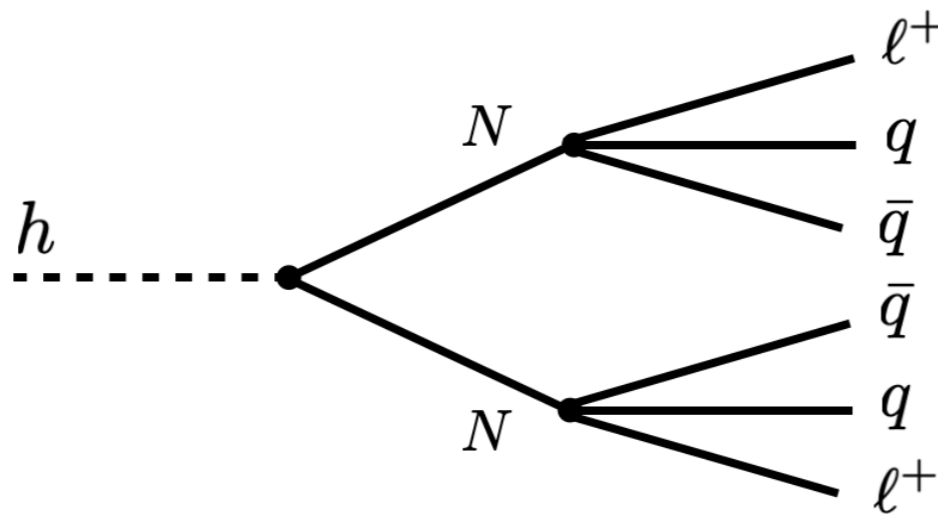
Final state	Channel	Mediator
$l'q\bar{q}$	$l'_\alpha q_i \bar{q}_j$	$W$
$\nu q\bar{q}$	$\nu_\alpha q_i \bar{q}_j$	$Z$
$\nu l' l'$	$l'_\alpha l'_\beta \nu_\beta, \alpha \neq \beta$	$W$
	$\nu_\alpha l'_\beta l'_\beta, \alpha \neq \beta$	$Z$
	$\nu_\alpha l'_\beta l'_\beta, \alpha = \beta$	$W$ and $Z$
$\nu\nu\nu$	$\nu_\alpha \nu_\beta \nu_\beta$	$Z$



	Channel	SS
Fully-leptonic	$4l \cancel{E}_T$	✓
	$2l \cancel{E}_T$	
Semi-leptonic	$3l \ 2q \ \cancel{E}_T$	✓
	$2l \ 4q$	✓
	$2l \ 2q \ \cancel{E}_T$	
	$l \ 4q \ \cancel{E}_T$	
Fully-hadronic	$4q \ \cancel{E}_T$	
	$2q \ \cancel{E}_T$	
Invisible	$\cancel{E}_T$	

	Channel	SS
Fully-leptonic	$3l \ \tau \ \cancel{E}_T$	✓
	$2l \ 2\tau \ \cancel{E}_T$	
	$l \ \tau \ \cancel{E}_T$	
	$l \ 3\tau \ \cancel{E}_T$	
	$4\tau \ \cancel{E}_T$	
	$2\tau \ \cancel{E}_T$	
Semi-leptonic	$2l \ \tau \ 2q \ \cancel{E}_T$	
	$l \ 2\tau \ 2q \ \cancel{E}_T$	
	$l \ \tau \ 4q$	
	$l \ \tau \ 2q \ \cancel{E}_T$	

	Channel	SS
Semi-leptonic	$3\tau \ 2q \ \cancel{E}_T$	
	$2\tau \ 4q$	
	$2\tau \ 2q \ \cancel{E}_T$	
	$\tau \ 2q \ \cancel{E}_T$	
	$\tau \ 4q \ \cancel{E}_T$	

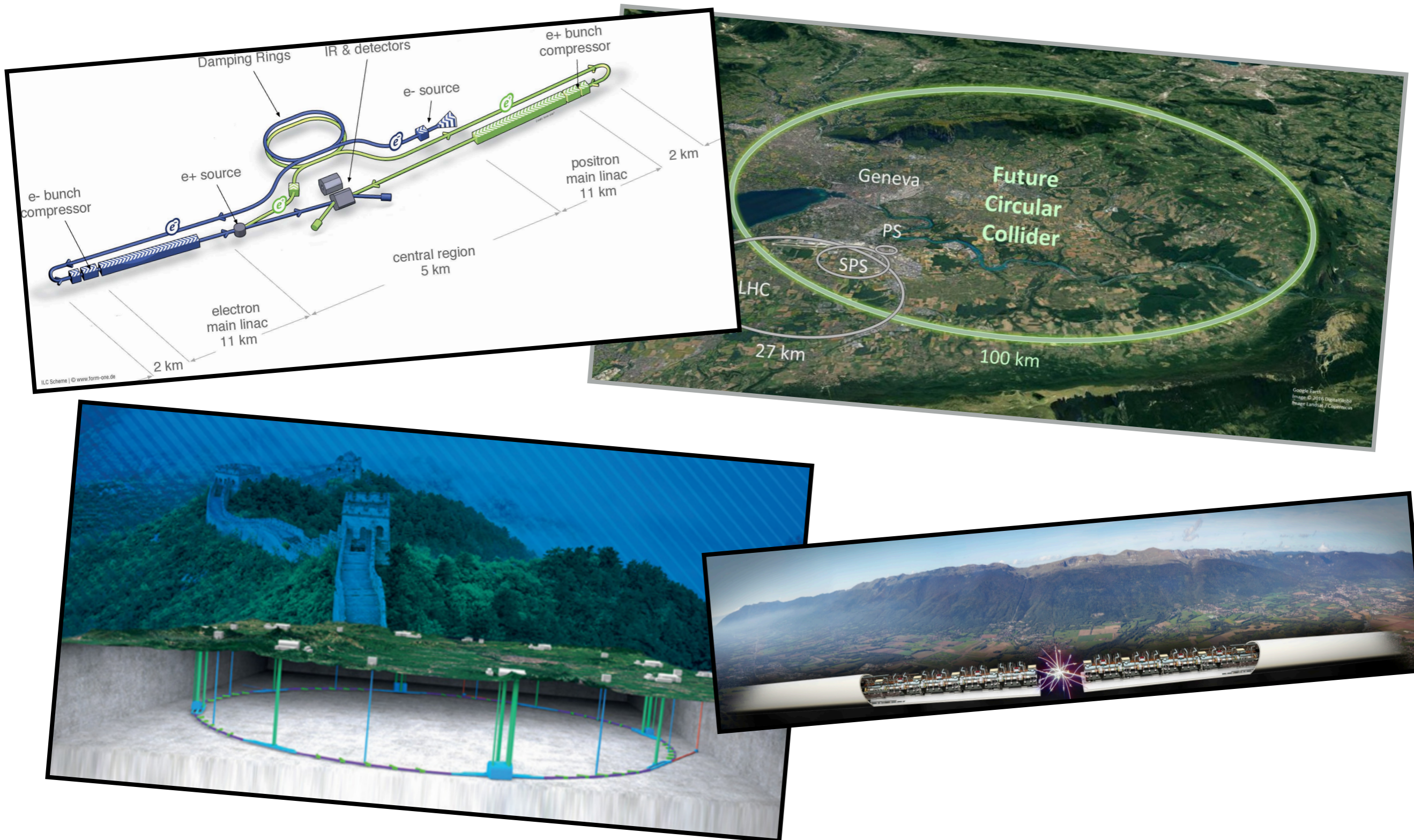


**LNV highest rate channel**

- Total width, hence lifetime, free-parameter - depends on  $\theta$ 
  - Prompt
  - Displaced
  - Stable

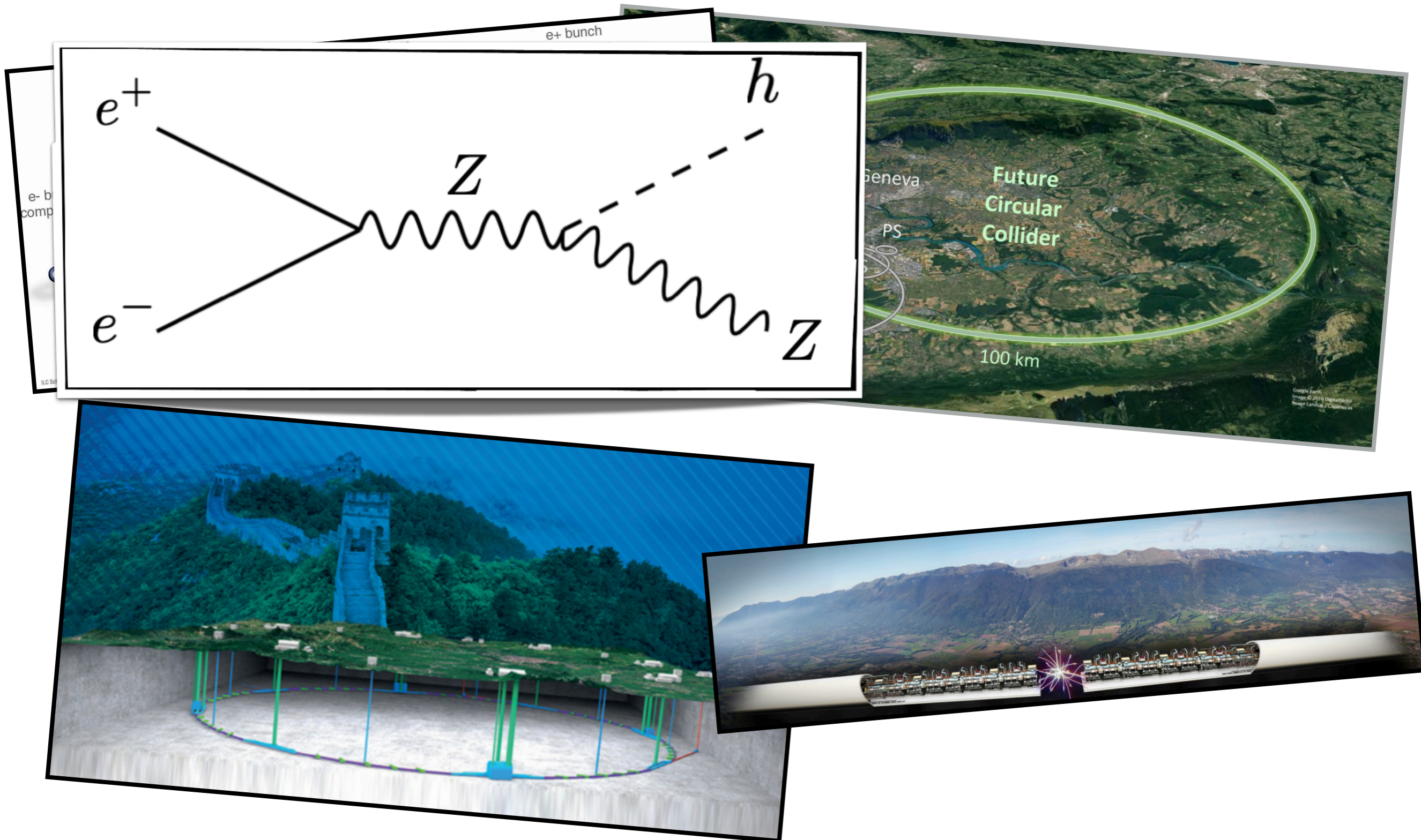
# Future Higgs / Z factories

- Heavy neutral leptons ideal target for future Higgs factories



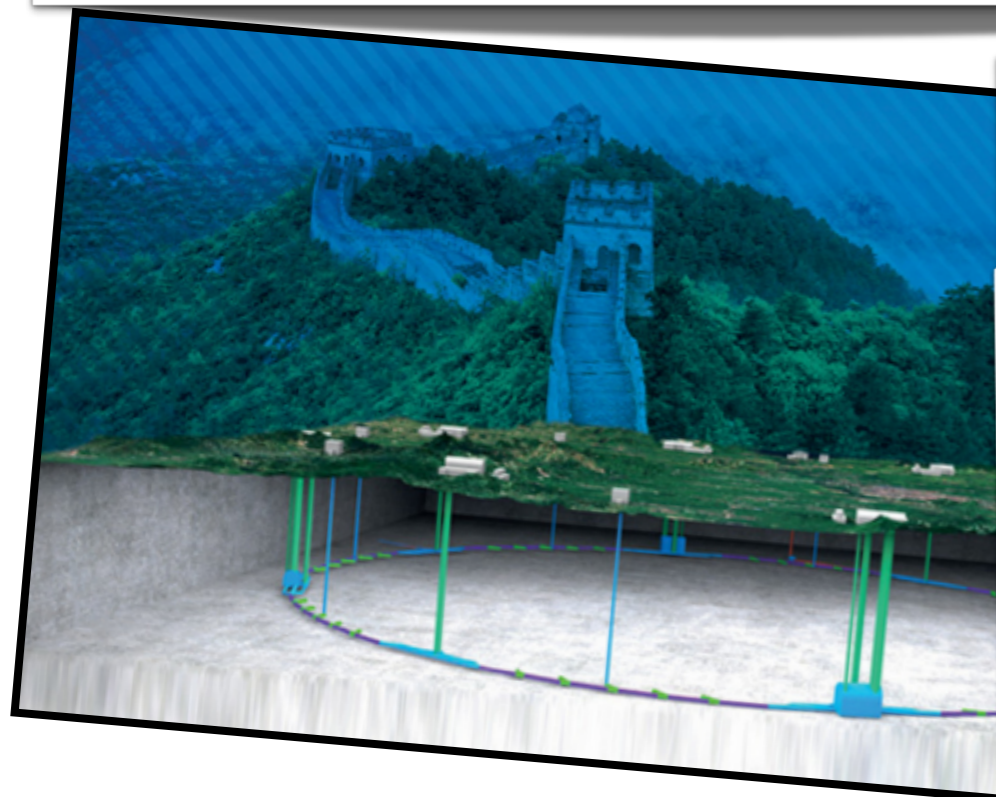
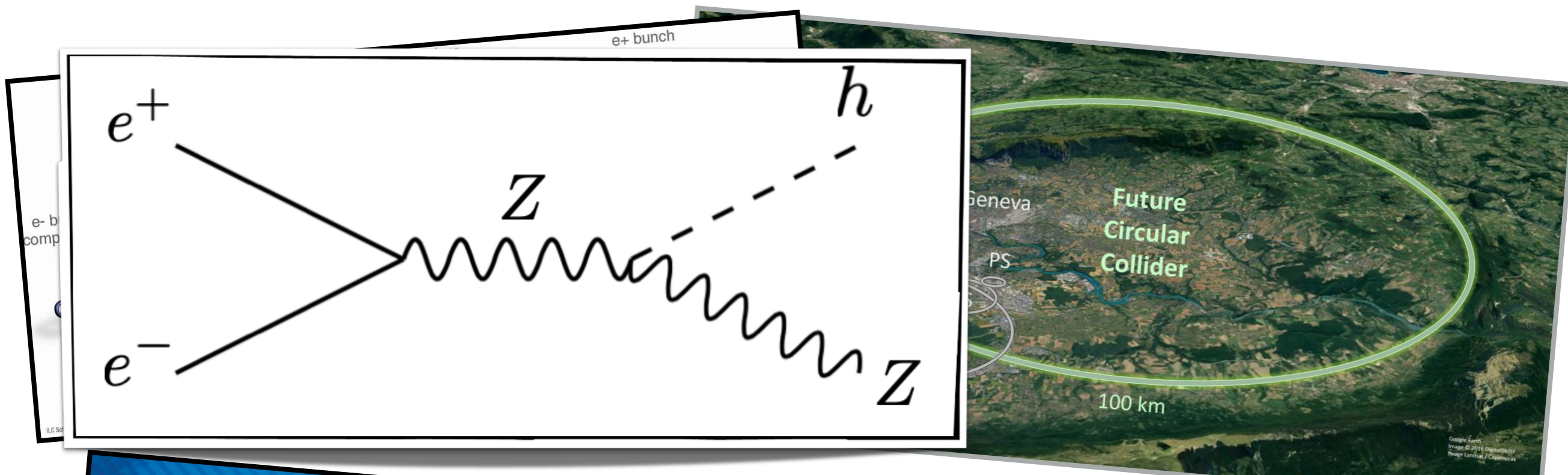
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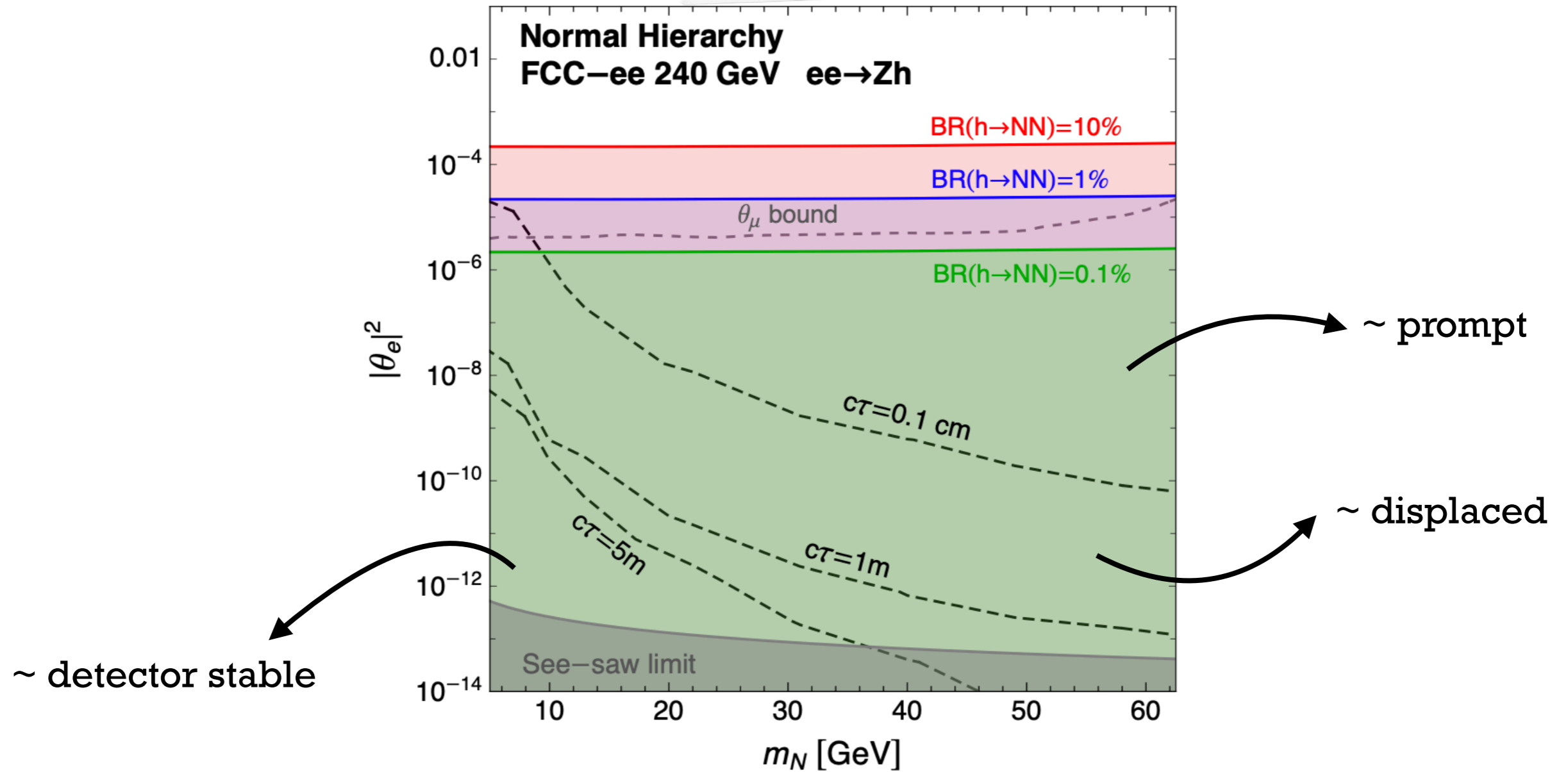
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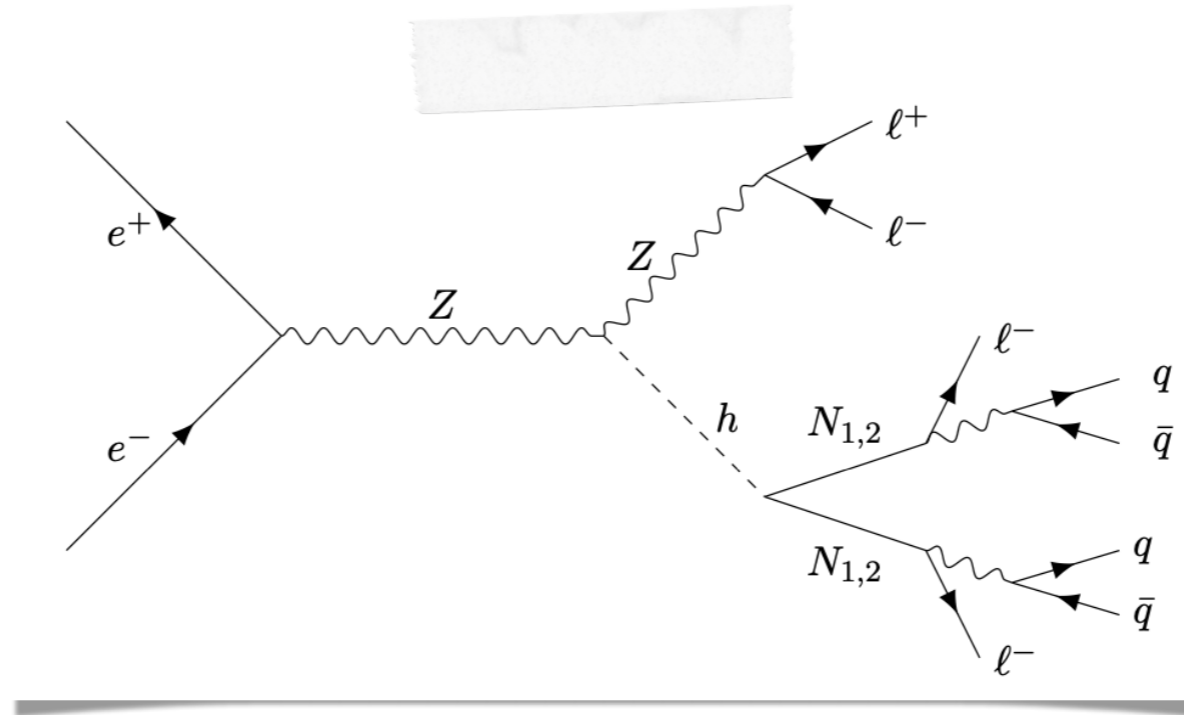
Higgs run			
Collider	$\sqrt{s}$ [GeV]	$\int \mathcal{L}$ [ $\text{ab}^{-1}$ ]	$\sigma_{Zh}$ [fb]
FCC-ee	240	5	193
ILC	250	2 (pol)	297
CLIC-380	380	1 (pol)	133
CEPC	240	5.6	193

# Prompt decay

- Need largish mixing, constrained by direct searches
- Can Higgs decay be the dominant production channel? Yes



- Consider final state with the largest BR, LNV  $\ell^\pm \ell^\pm 4j$

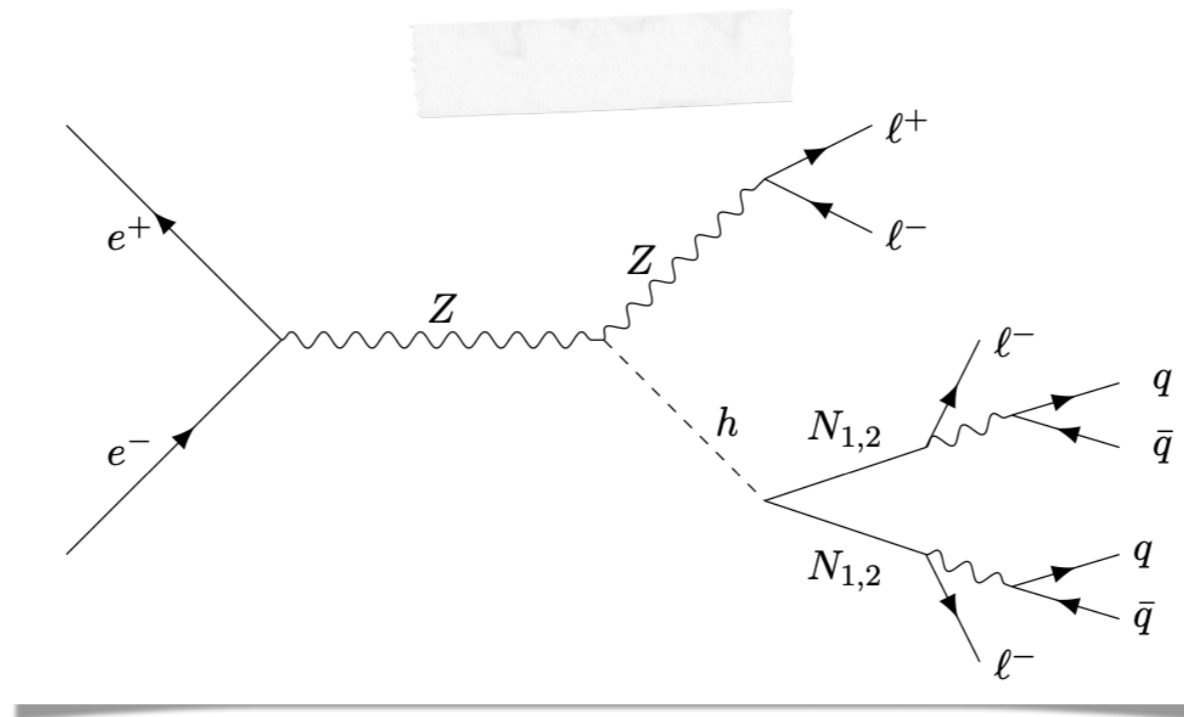


- Ask for a pair of SS leptons, Higgs-strahlung topology and leptonic  $Z$

$$\begin{aligned}
 p_T^\ell &> 2.5 \text{ GeV} & p_T^j &> 5 \text{ GeV} & |\eta^{\ell,j}| &< 2.44 & \Delta R(\ell\ell, \ell j) &> 0.15 \\
 |m_{\ell^+\ell^-} - m_Z| &< 10 \text{ GeV} & |s - 2\sqrt{s}E_{\ell^+\ell^-} + m_{\ell^+\ell^-}^2 - m_H| &< 10 \text{ GeV}
 \end{aligned}$$



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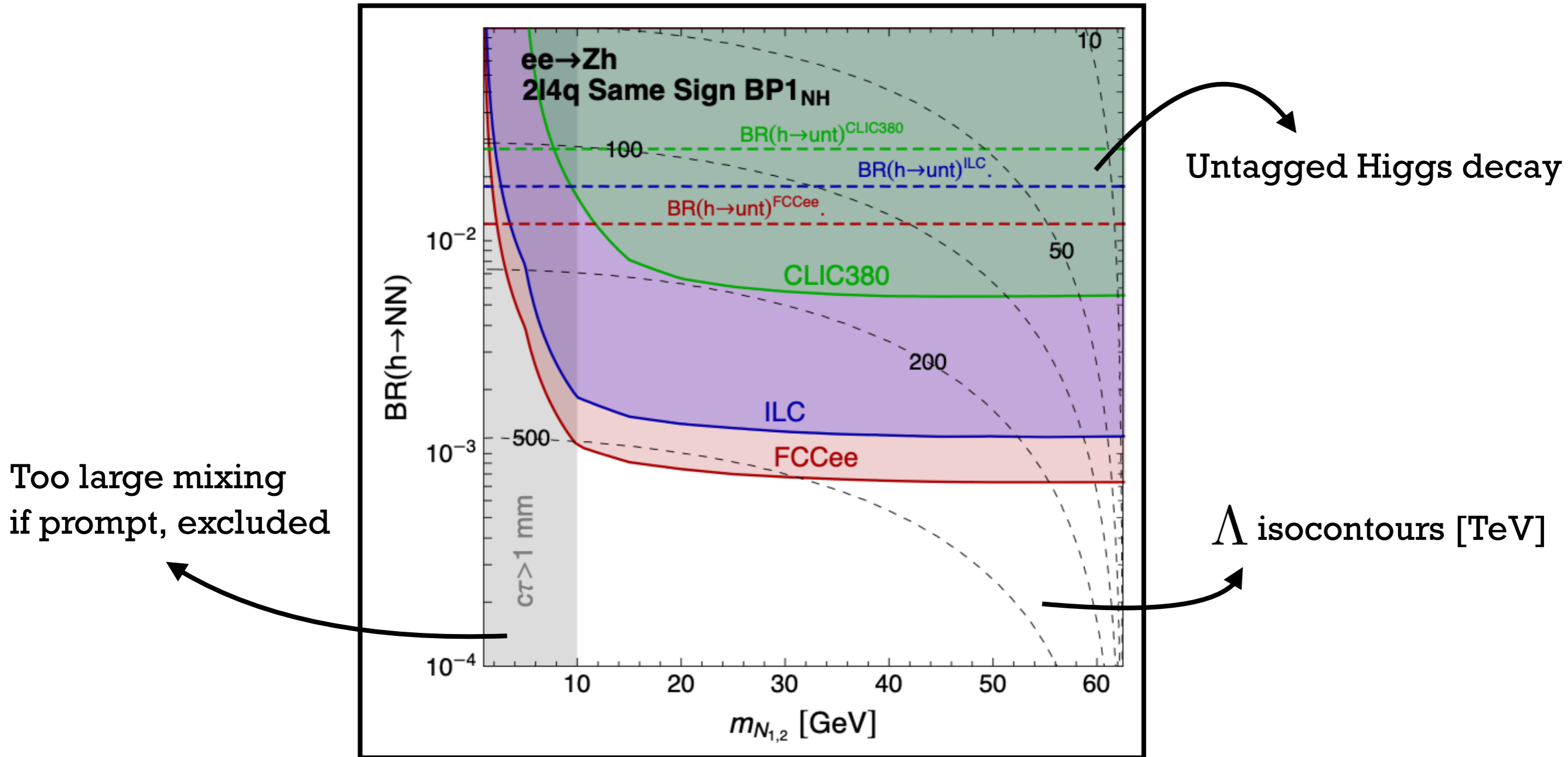
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 |m_{\ell^+\ell^-} - m_Z| < 10 \text{ GeV} & & |s - 2\sqrt{s}E_{\ell^+\ell^-} + m_{\ell^+\ell^-}^2 - m_H| < 10 \text{ GeV} & & & & 
 \end{aligned}$$

**Irreducible background** - any process giving  $(Z \rightarrow \ell_\alpha^+ \ell_\alpha^-)(h \rightarrow \ell_\beta^+ \ell_\gamma^+ + \dots)$

$L$  &  $Q_{\text{em}}$  are conserved, need  $2\nu 4q \dots (Z \rightarrow \ell_\alpha^+ \ell_\alpha^-)(h \rightarrow \ell_\beta^+ \nu_\beta \ell_\gamma^+ \nu_\gamma \bar{u} d \bar{u} d)$  **negligible**

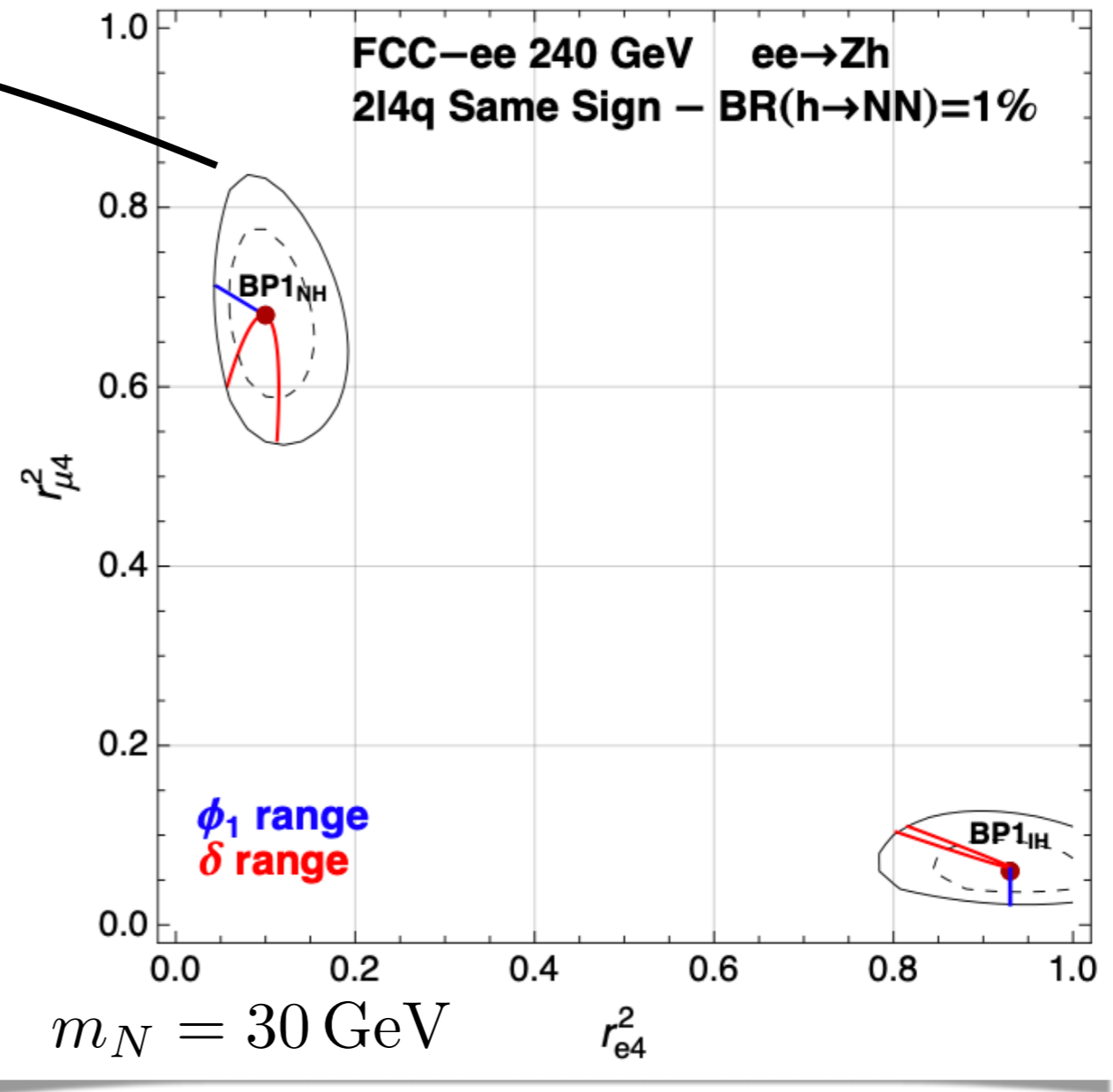
- Assume backgrounds from e.g. mis-ID to be negligible and work with zero bkg  
**[Strong assumption, but probably not too bad given the signal characteristics, potential accuracy of particle-flow reconstruction and improved analysis techniques...]**



- What can we learn if we observe a signal? Can we determine the flavor structure?
- Build  $p(n_{\text{obs}}|n_{\text{th}}) = \frac{1}{n_{\text{obs}}!} e^{-n_{\text{th}}} n_{\text{th}}^{n_{\text{obs}}}$  injecting a signal

- Determine normalized mixing up to 10%

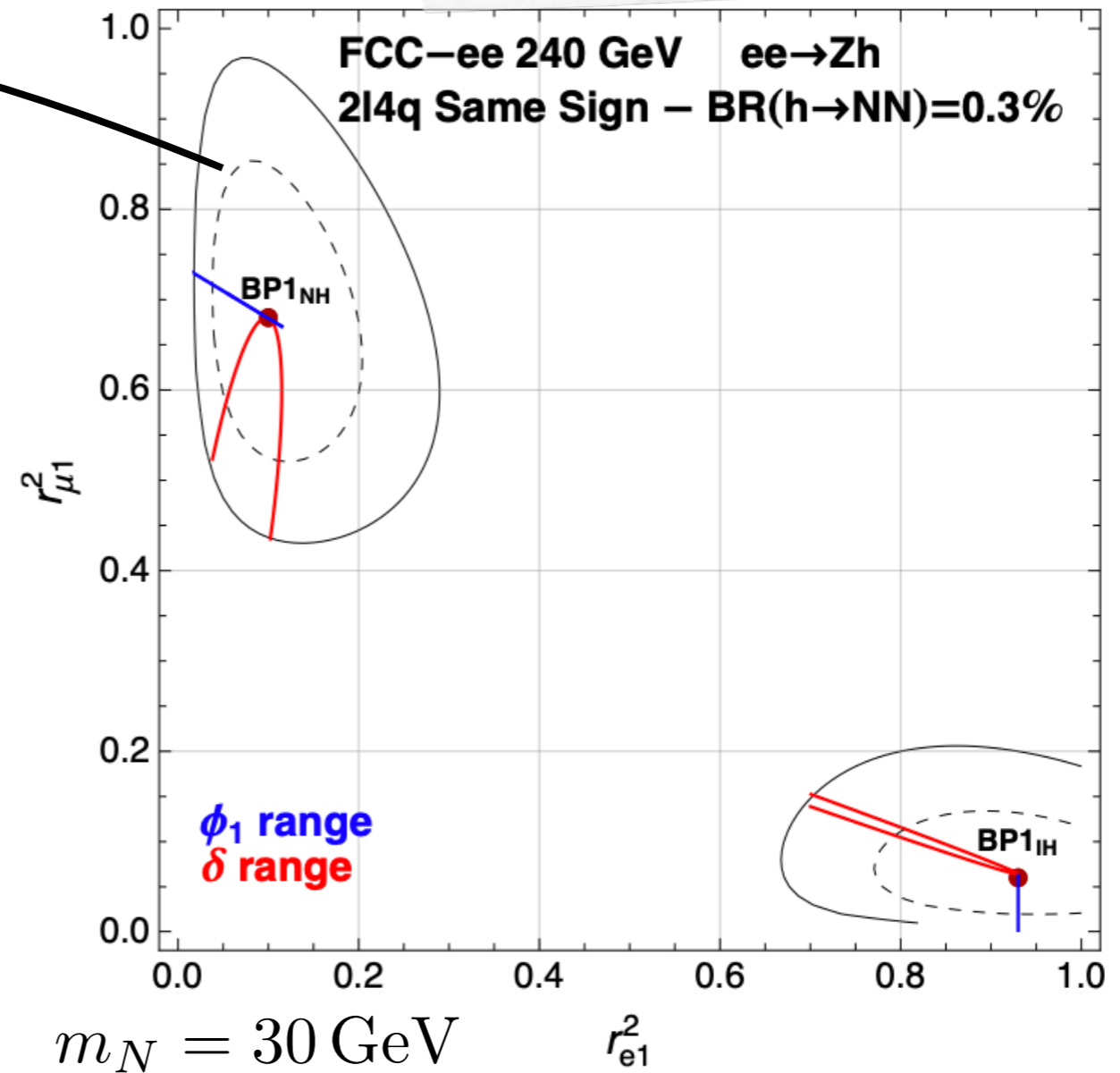
	$\text{BR}(h \rightarrow NN) = 1\%$
<b>BP1<sub>NH</sub></b>	$3.69 \leq \phi_1 \leq 5.57$ $0.78 \leq \delta \leq 1.85 \cup 4.47 \leq \delta \leq 5.55$



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- Build  $p(n_{\text{obs}}|n_{\text{th}}) = \frac{1}{n_{\text{obs}}!} e^{-n_{\text{th}}} n_{\text{th}}^{n_{\text{obs}}}$  injecting a signal

- Determine normalized mixing up to 30%

	$\text{BR}(h \rightarrow NN) = 0.3\%$
<b>BP1<sub>NH</sub></b>	$0.037 \leq \phi_1 \leq 5.95$
	$0 \leq \delta \leq 2.53 \cup 3.80 \leq \delta \leq 2\pi$



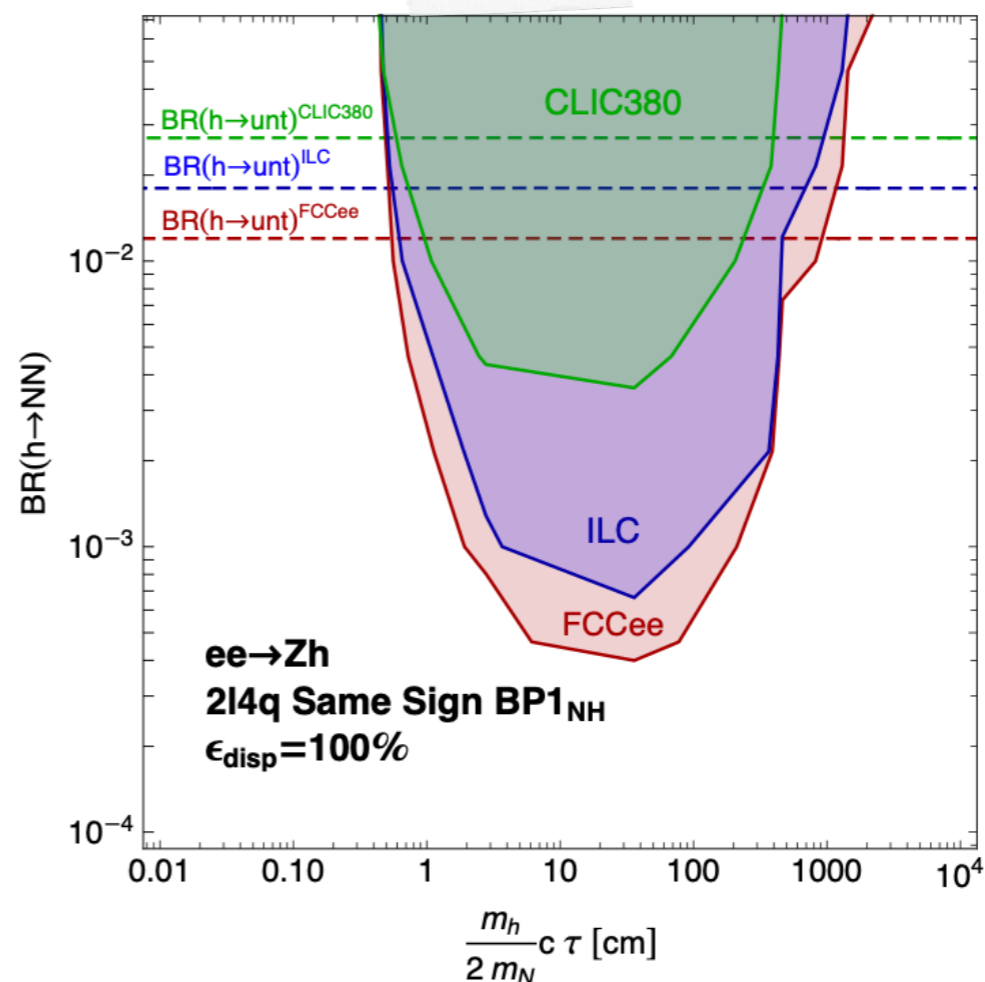
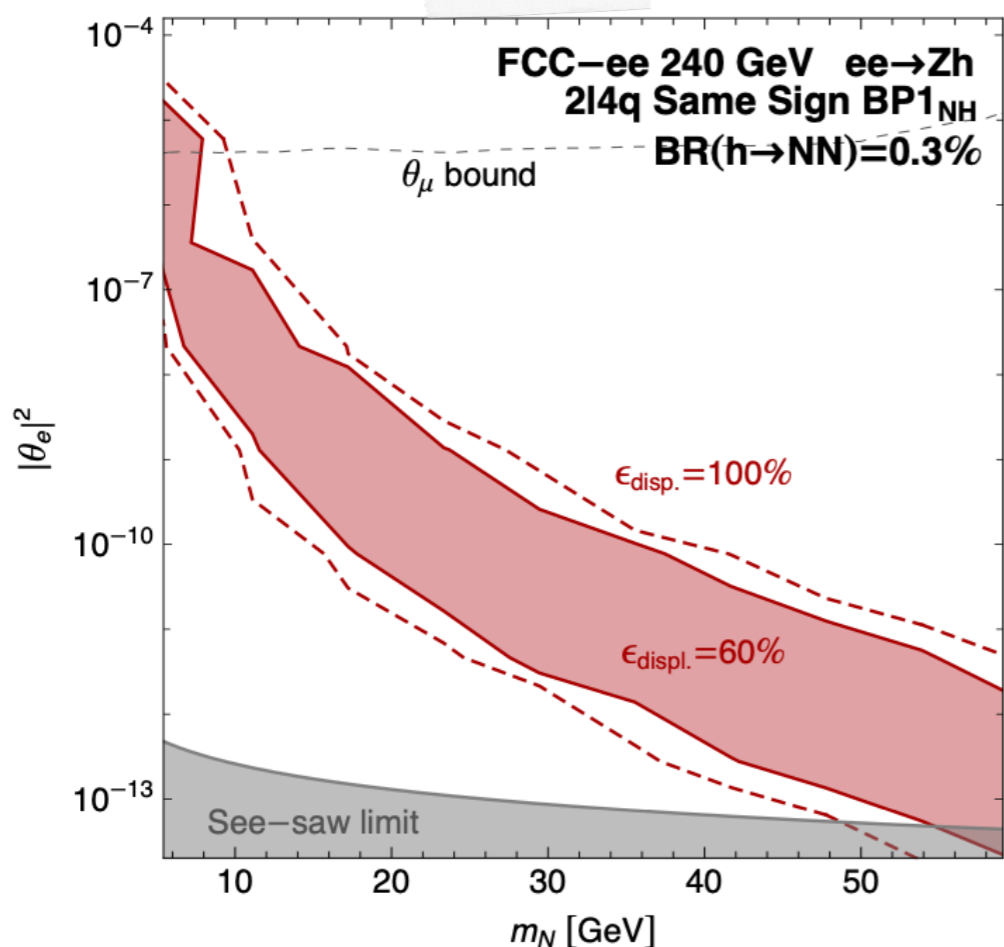
# Displaced decay

- Consider displaced a decay within  $1 \text{ cm} < L_{\text{dec}} < 1 \text{ m}$  and spherical detector
- Consider again the  $2\ell 4j$  final state, with the higher rate. Both SS and OS

$$N_s = \sigma_{Zh} \times \text{BR}(Z \rightarrow \ell^+ \ell^-) \times \text{BR}(h \rightarrow NN) \times \text{BR}(NN \rightarrow 2\ell 4q) \times \epsilon_{Zh} \times \epsilon_{P_{\Delta L}}^2 \times \epsilon_{\text{disp.}}^2 \times \mathcal{L}$$

Probability for both neutrino to decay within [1cm, 1m] ↩

$$\mathcal{P}(x_i, x_f) = e^{-\frac{x_i}{\beta\gamma c\tau}} - e^{-\frac{x_f}{\beta\gamma c\tau}} \quad \text{on event by event basis}$$



[c.f.r. 1E-2/1E-3 @ LHC, Caputo+ 1704.08721 ]

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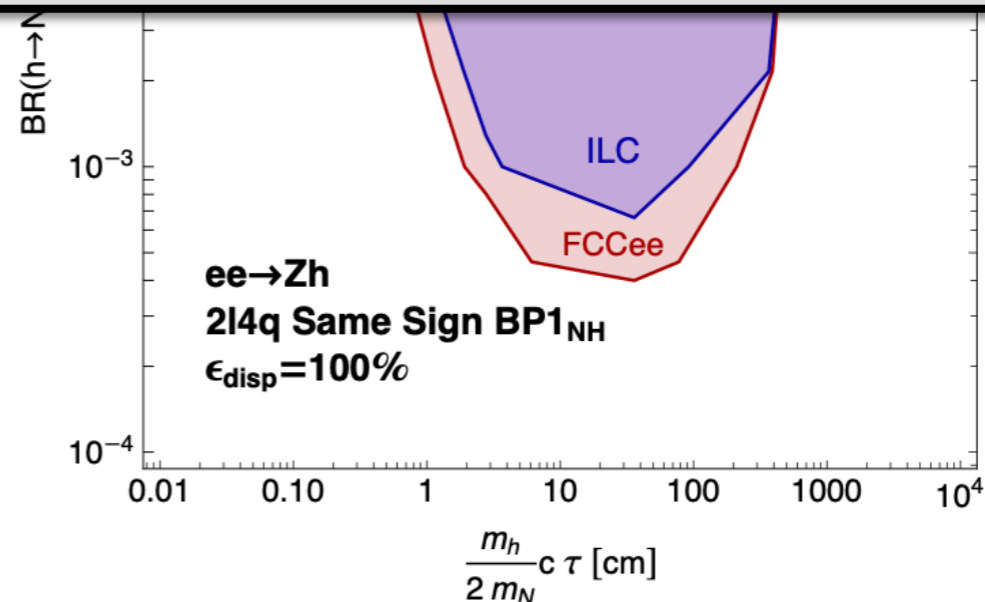
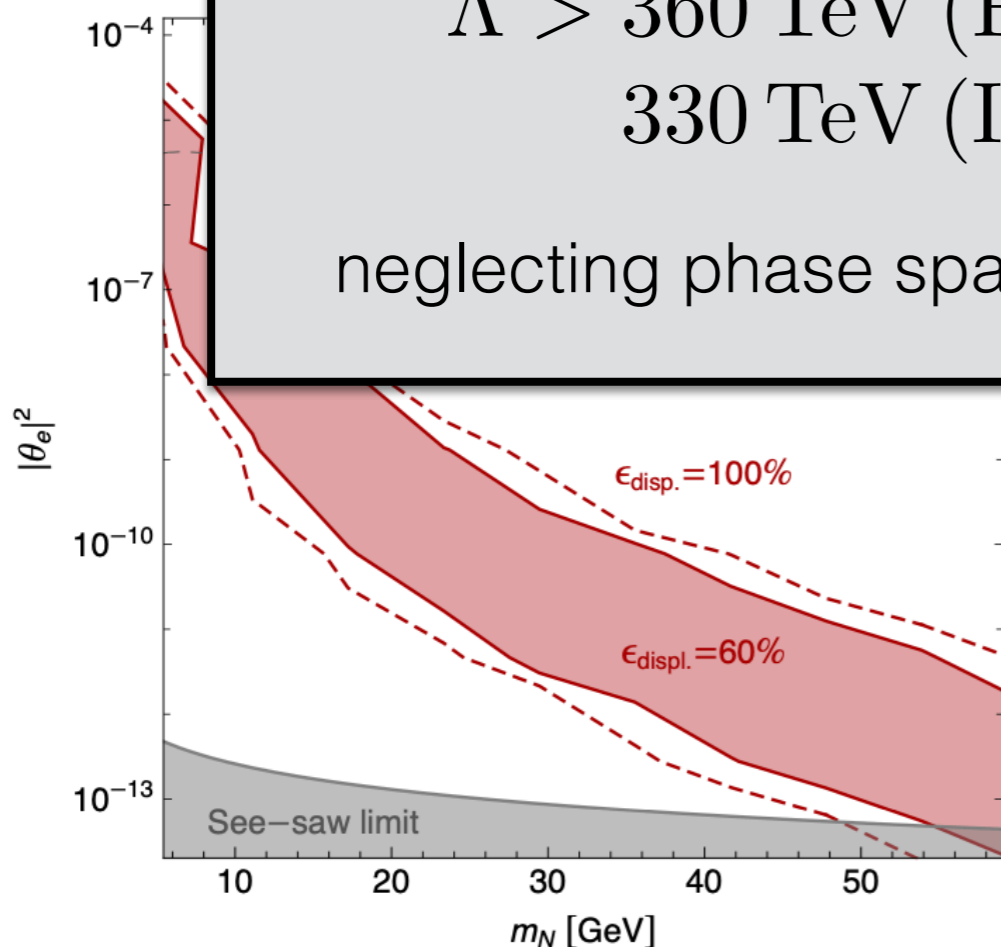
$$N_s = \sigma_{Zh} \times \text{BR}(Z \rightarrow \ell^+ \ell^-) \times \text{BR}(h \rightarrow NN) \times \text{BR}(NN \rightarrow 2\ell 4q) \times \epsilon_{Zh} \times \epsilon_{P_{\Delta T}}^2 \times \epsilon_{\text{disp}}^2 \times \mathcal{L}$$

## Detector stable

- Bounds from invisible Higgs decay, mappable in  $\Lambda$

$\Lambda > 360 \text{ TeV}$  (FCC – ee),  $320 \text{ TeV}$  (CEPC)  
 $330 \text{ TeV}$  (ILC),  $210 \text{ TeV}$  (CLIC)

neglecting phase space

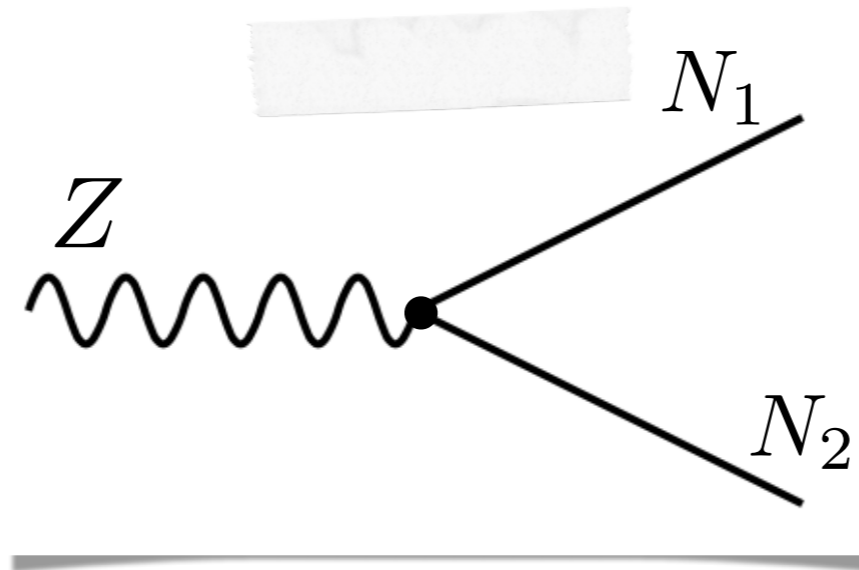


[c.f.r. 1E-2/1E-3 @ LHC, Caputo+ 1704.08721 ]

# Dipole operator

$$\mathcal{O}_{NB} = \frac{\alpha_{NB}}{\Lambda} N \sigma^{\mu\nu} N B_{\mu\nu}$$

- Antisymmetry of  $\sigma^{\mu\nu}$ , need two flavors of RH neutrino
- After EWSB generate a dipole with the  $Z$  boson and  $\gamma$



$$\Gamma_{Z \rightarrow N_1 N_2} = \frac{2}{3\pi} \frac{|\alpha_{NB}^{12}|^2}{\Lambda^2} \frac{s_w^2}{m_Z^3} \lambda^{1/2}(m_Z^2, m_{N_1}^2, m_{N_2}^2) \zeta(m_Z, m_{N_1}, m_{N_2})$$

$$\zeta(m_Z, m_{N_1}, m_{N_2}) = m_Z^2 (m_Z^2 + m_{N_1}^2 + m_{N_2}^2 - 6m_{N_1} m_{N_2} \cos 2\phi_{12}) - 2(m_{N_1}^2 - m_{N_2}^2)^2$$

$$\phi_{12} = \arg[\alpha_{NB}^{12}]$$

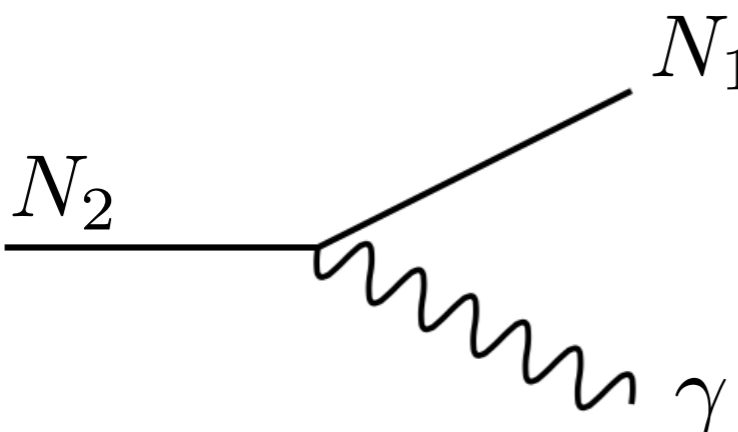
- Future colliders can produce huge numbers of  $Z$  bosons

**Z pole run**

Collider	$\sqrt{s}$ [GeV]	$\int \mathcal{L}$ [ab <sup>-1</sup> ]	$N_Z$
FCC-ee	$m_Z$	150	$6.5 \times 10^{12}$
CEPC	$m_Z$	16	$6.9 \times 10^{11}$

**What about the N decay?**

- Differently from  $\mathcal{O}_{NH}$  this operator can trigger N decay via the photon dipole

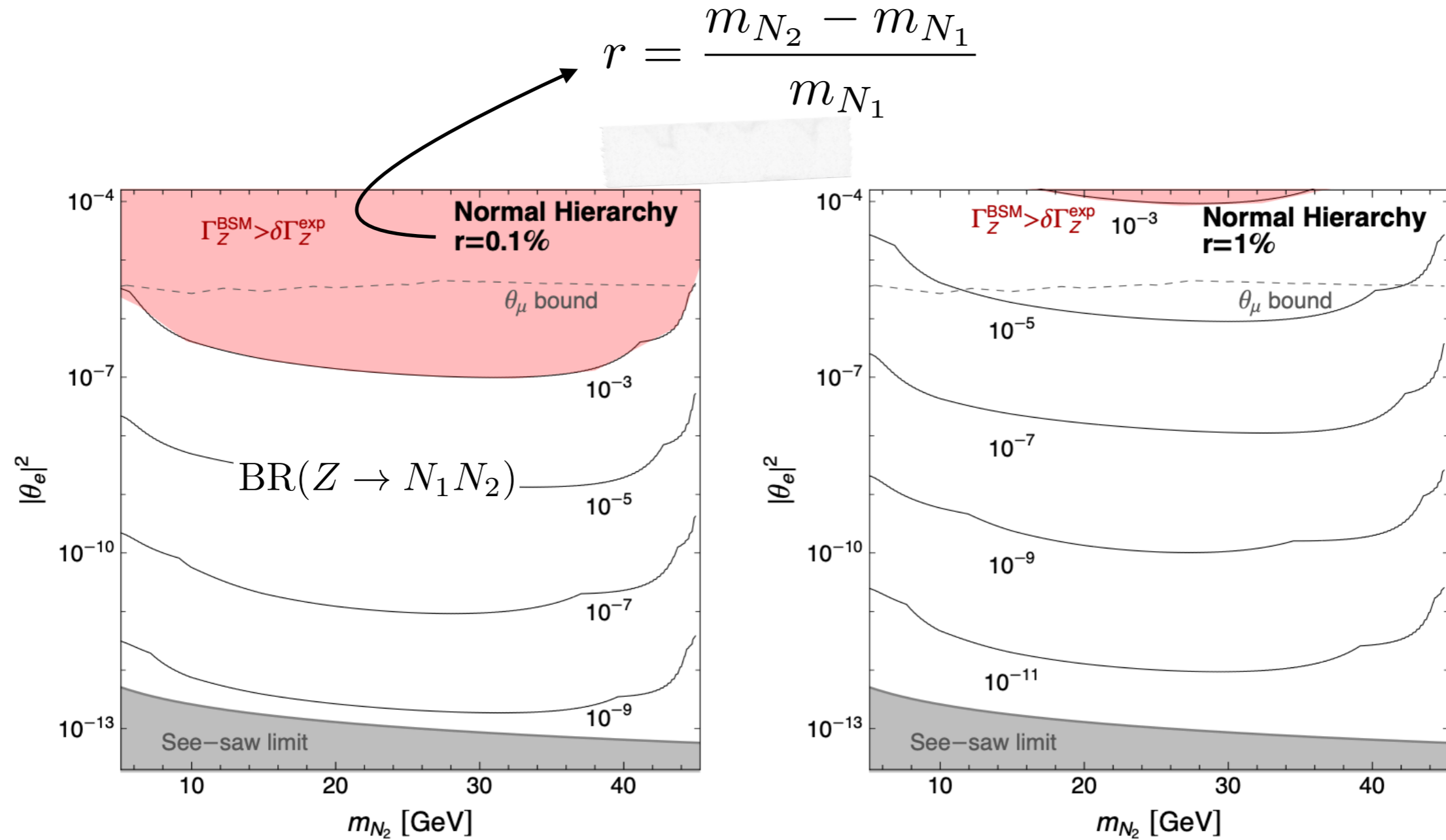


$$\Gamma(N_2 \rightarrow N_1 \gamma) = \frac{2}{\pi} c_w^2 \frac{|\alpha_{NB}|^2}{\Lambda^2} m_{N_2}^3 \left( 1 - \frac{m_{N_1}^2}{m_{N_2}^2} \right)^3$$

- Whether  $N_2$  decays via mixing or via  $\mathcal{O}_{NB}$  also depends on  $m_{N_2} - m_{N_1}$



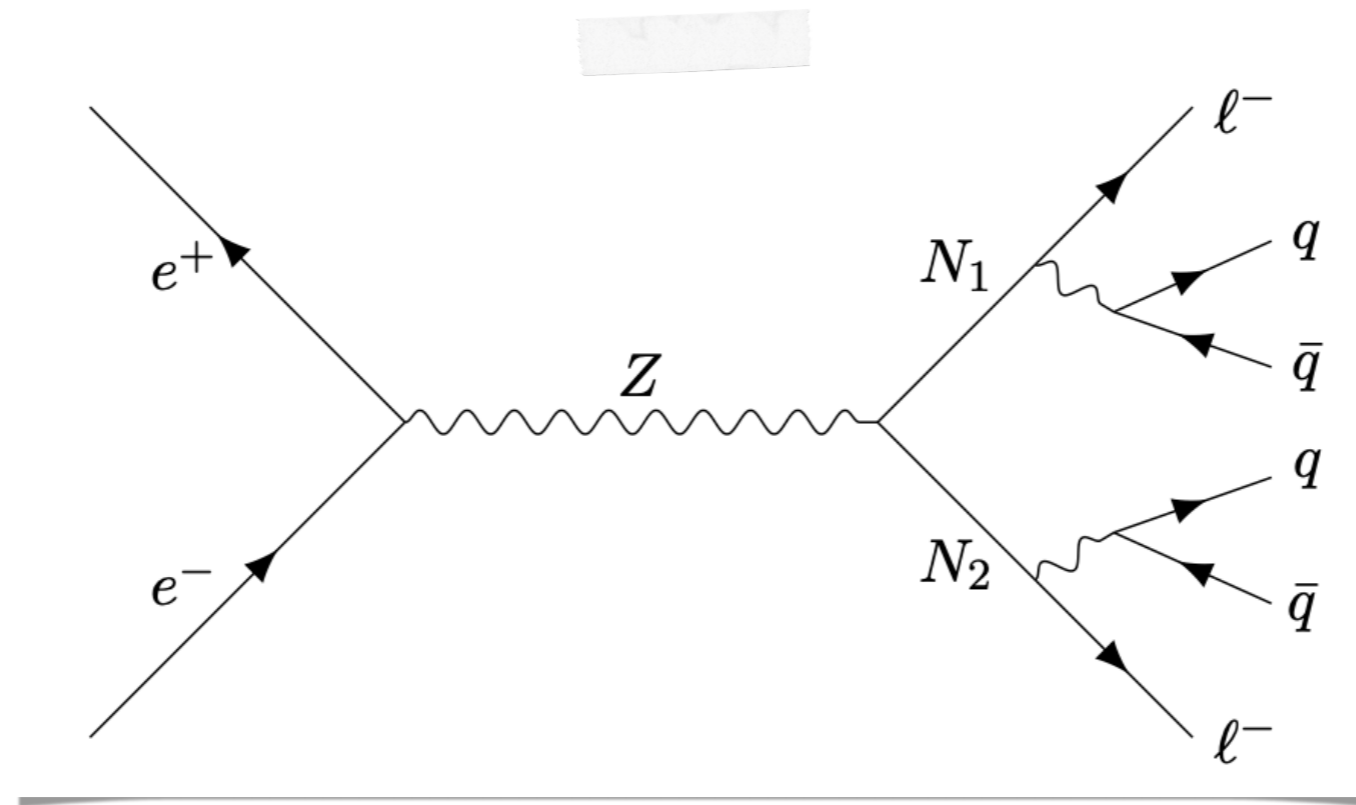
- Above the lines the decay via mixing dominates for the given  $\text{BR}(Z \rightarrow N_1 N_2)$  which fixes  $\Lambda$



- Region exists where decay is induced by the mixing and production via Z decay

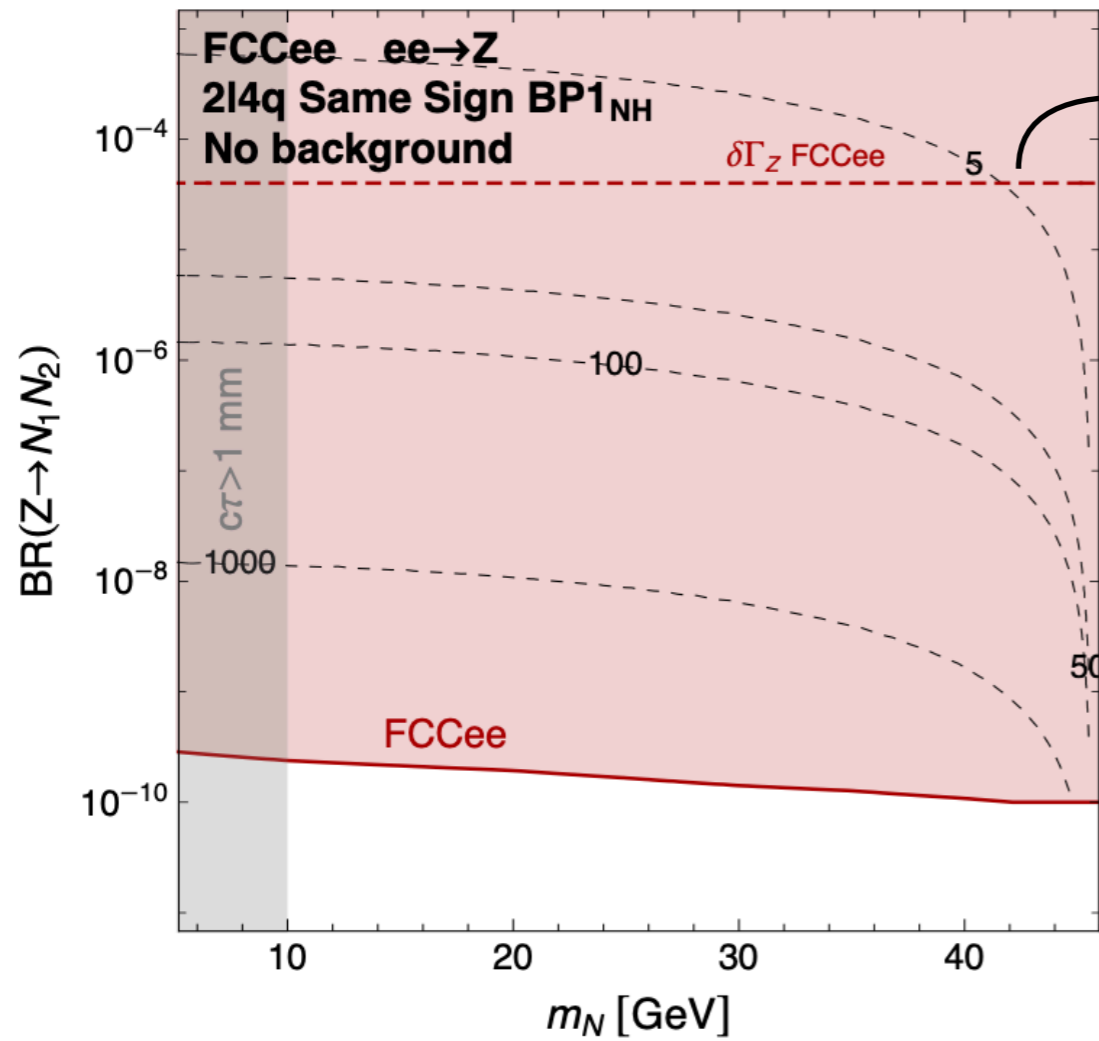
# Prompt decay

- Still use the dominant LNV  $2\ell 4j$  final state

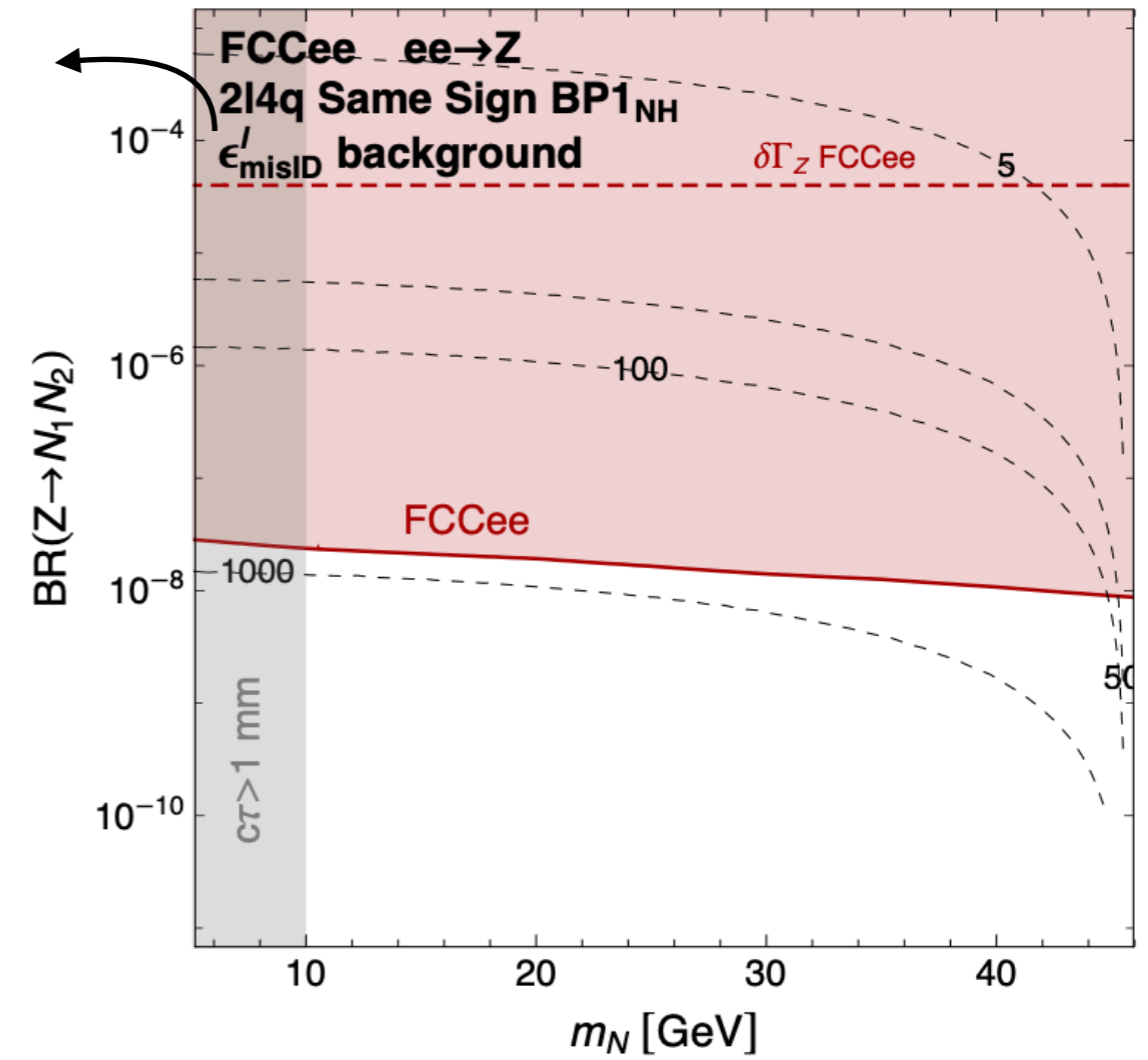


- Basic selections on  $p_T$ ,  $|\eta|$  and isolations
- Consider the reducible  $\ell^+\ell^-4j$  background with flat charge mis-ID of  $10^{-3}$

$$\sigma_{\ell^+\ell^-4j} \times 2 \times \epsilon_{\text{misID}}^{\ell} (1 - \epsilon_{\text{misID}}^{\ell}) \simeq 130 \text{ fb} \times \epsilon_{\text{misID}}^{\ell} (1 - \epsilon_{\text{misID}}^{\ell}) \simeq 0.26 \text{ fb},$$



Z width



- In the mis-ID bkg scenario can probe  $10^3$  TeV

## Caveat

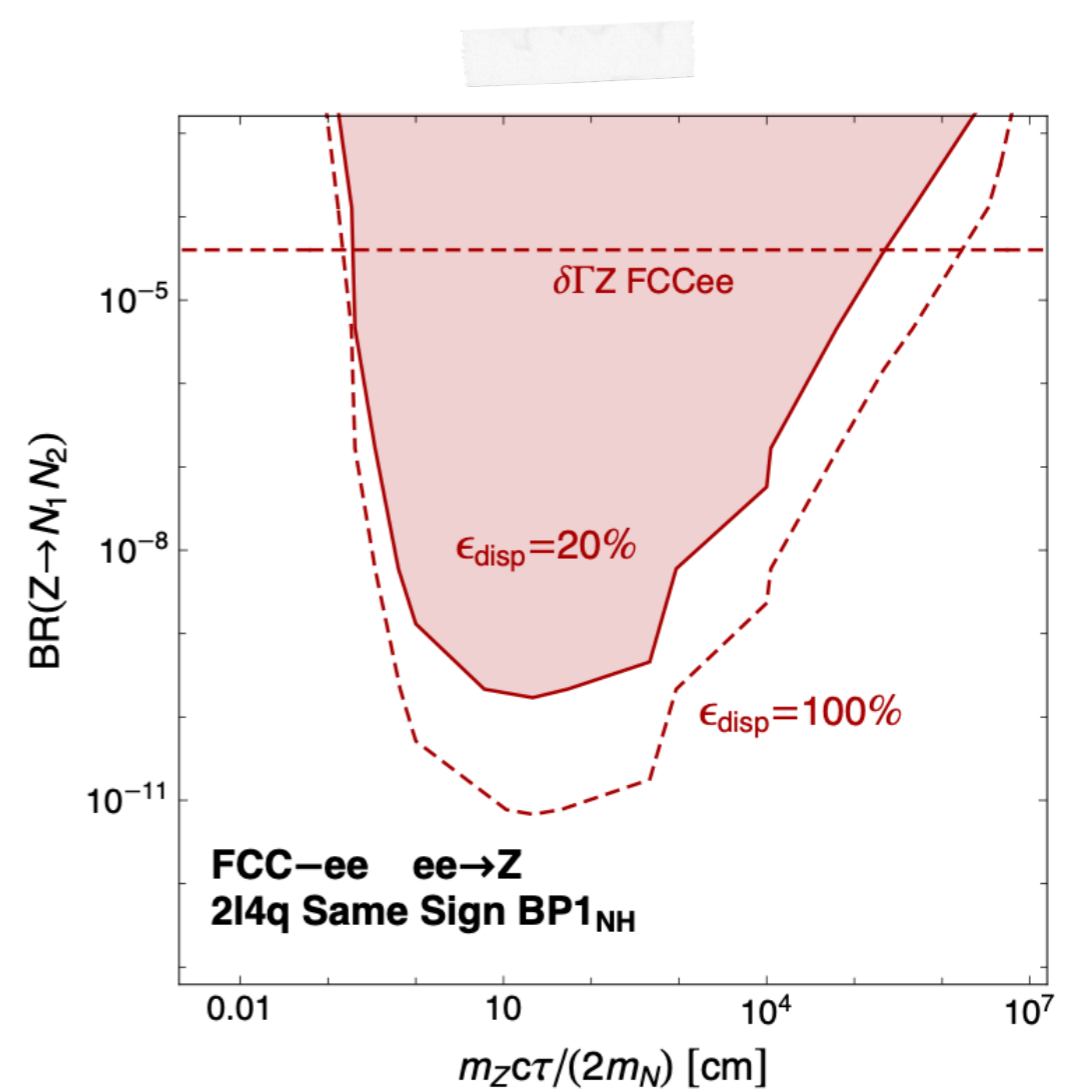
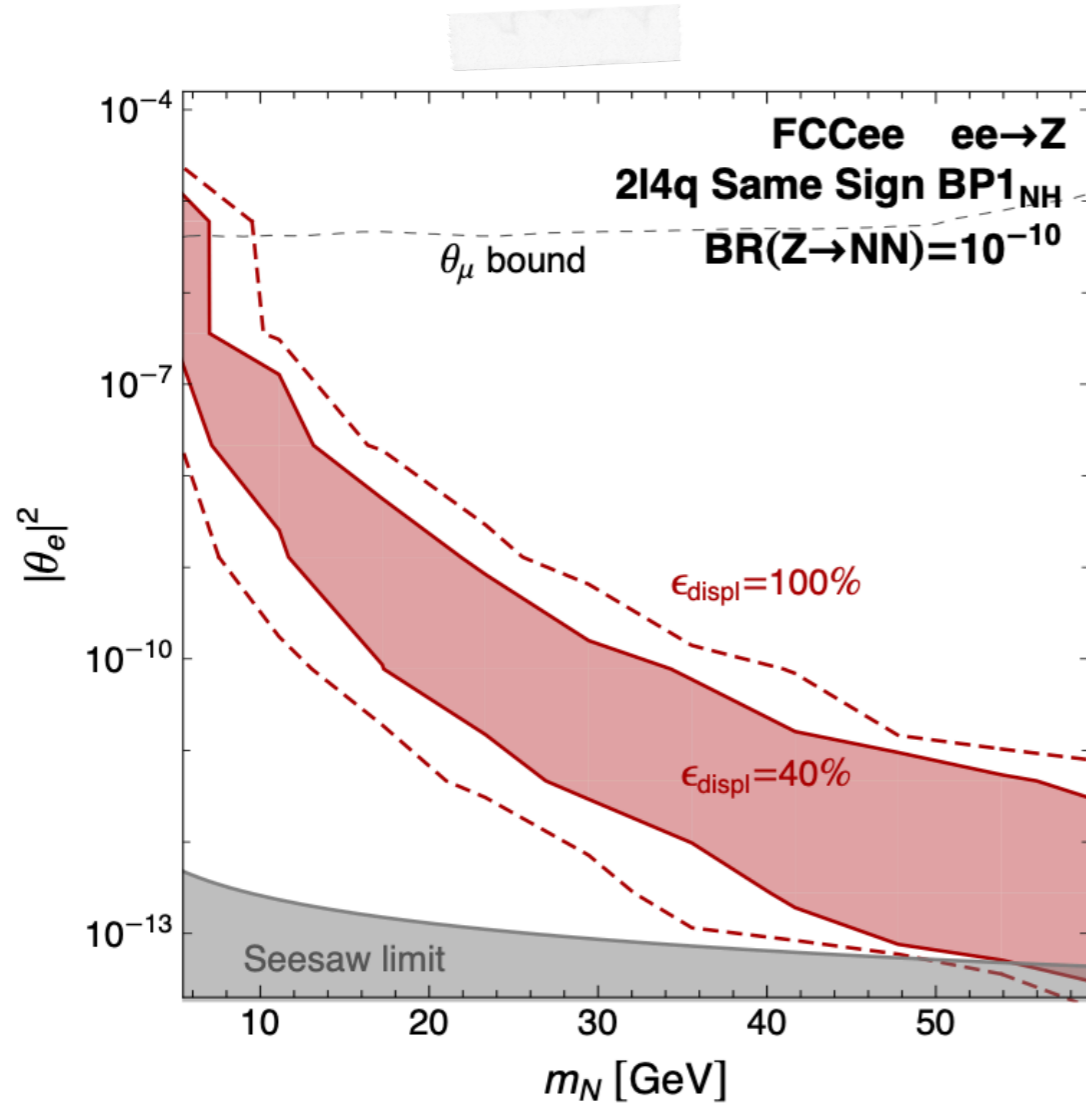
- Dipole operator can only be generated at loop level in a weakly coupled UV completion with only spin 0, 1/2, 1 states [Craig+ 2001.00017]

1000 TeV  $\longrightarrow$  10 TeV...



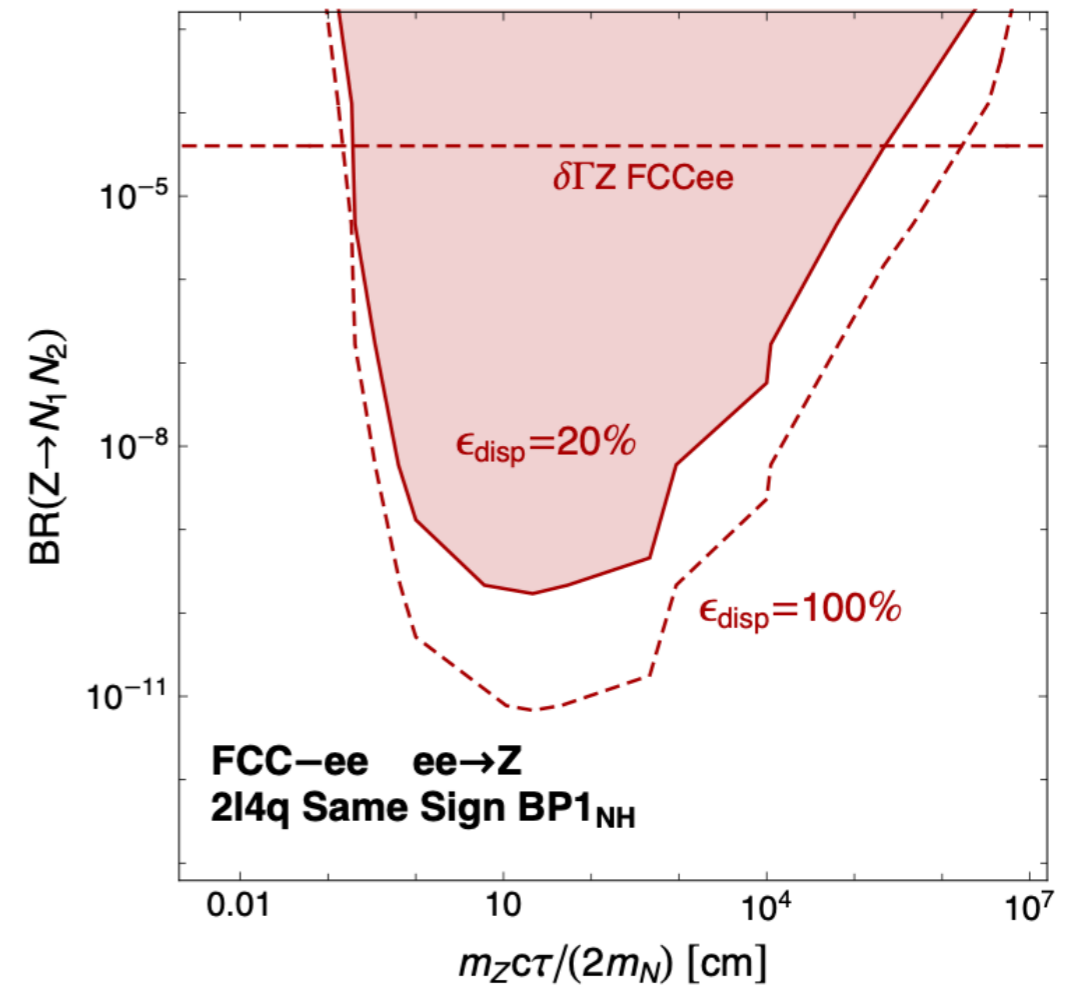
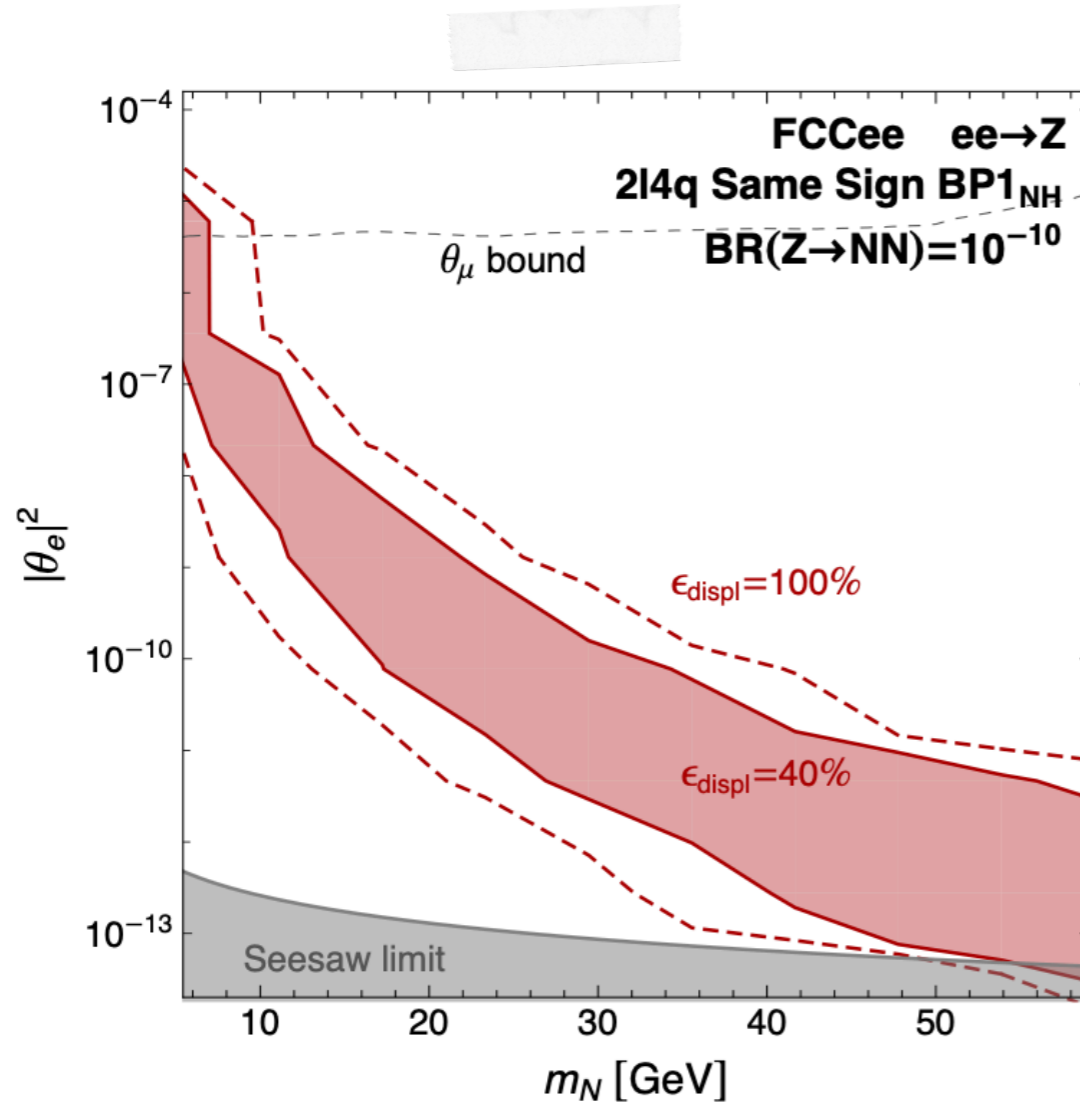
# Displaced decay

- Similar strategy than the  $\mathcal{O}_{NH}$  operator



# Displaced decay

- Similar strategy than the  $\mathcal{O}_{NH}$  operator



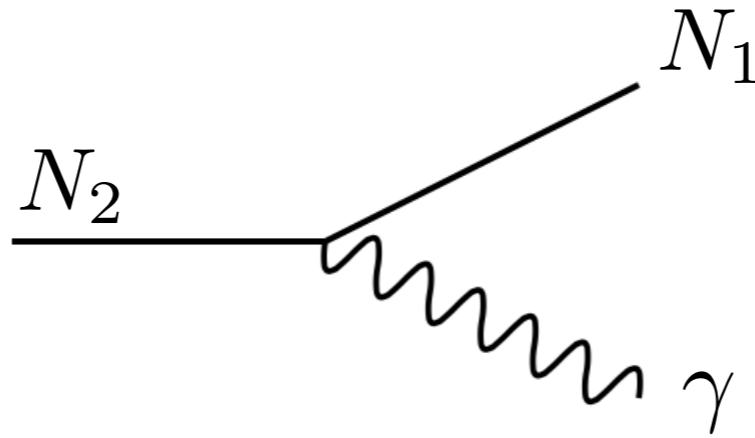
## Detector stable

- FCC-ee will measure  $R_\nu = \Gamma_{Z \rightarrow \text{inv}} / \Gamma_{Z \rightarrow \ell\ell} \quad 0.3 \times 10^{-3}$   
corresponding to  $\delta\Gamma_Z \sim 100 \text{ KeV}$

$$\Lambda \gtrsim 20 \text{ TeV}$$

# Photon dipole

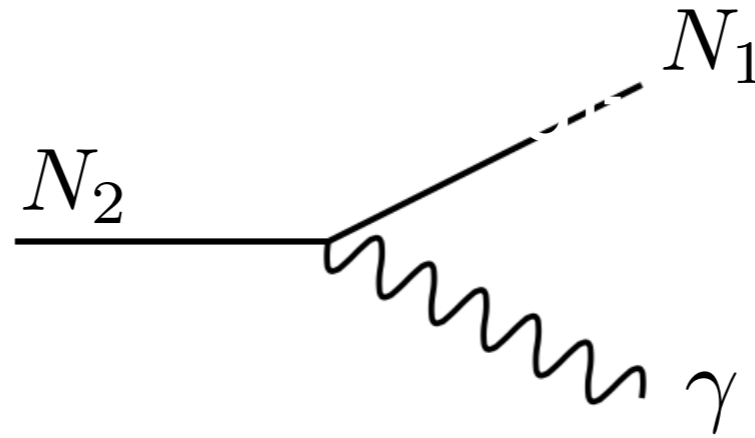
- If the mixing is negligible small, the heaviest  $N$  can decay via the photon dipole



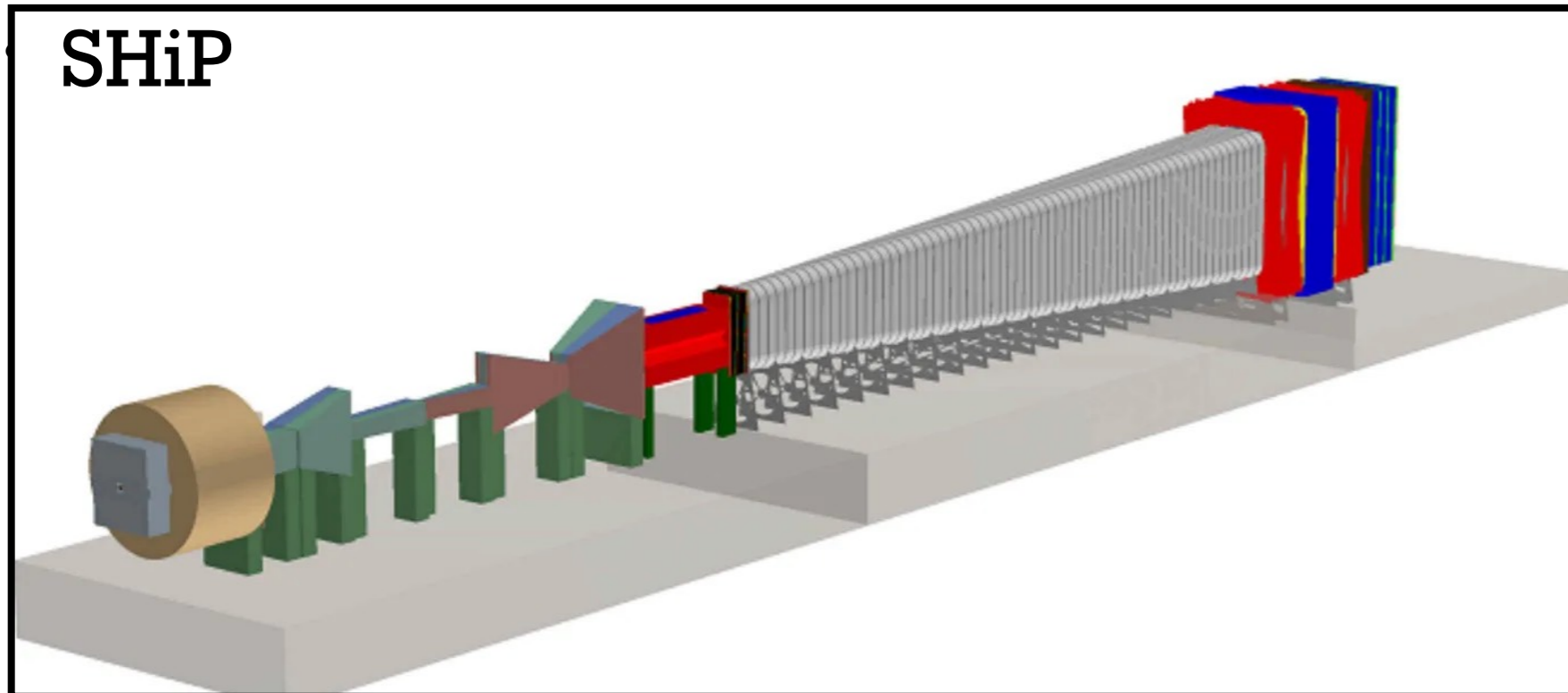
- Depending on the masses and suppression scale one can have  $\lambda_{N_2} \gg L_{\text{dec}}$
- Many experiment can be sensitive to RHN with macroscopic decay lengths...

# Photon dipole

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...pic decay lengths...

# Photon dipole

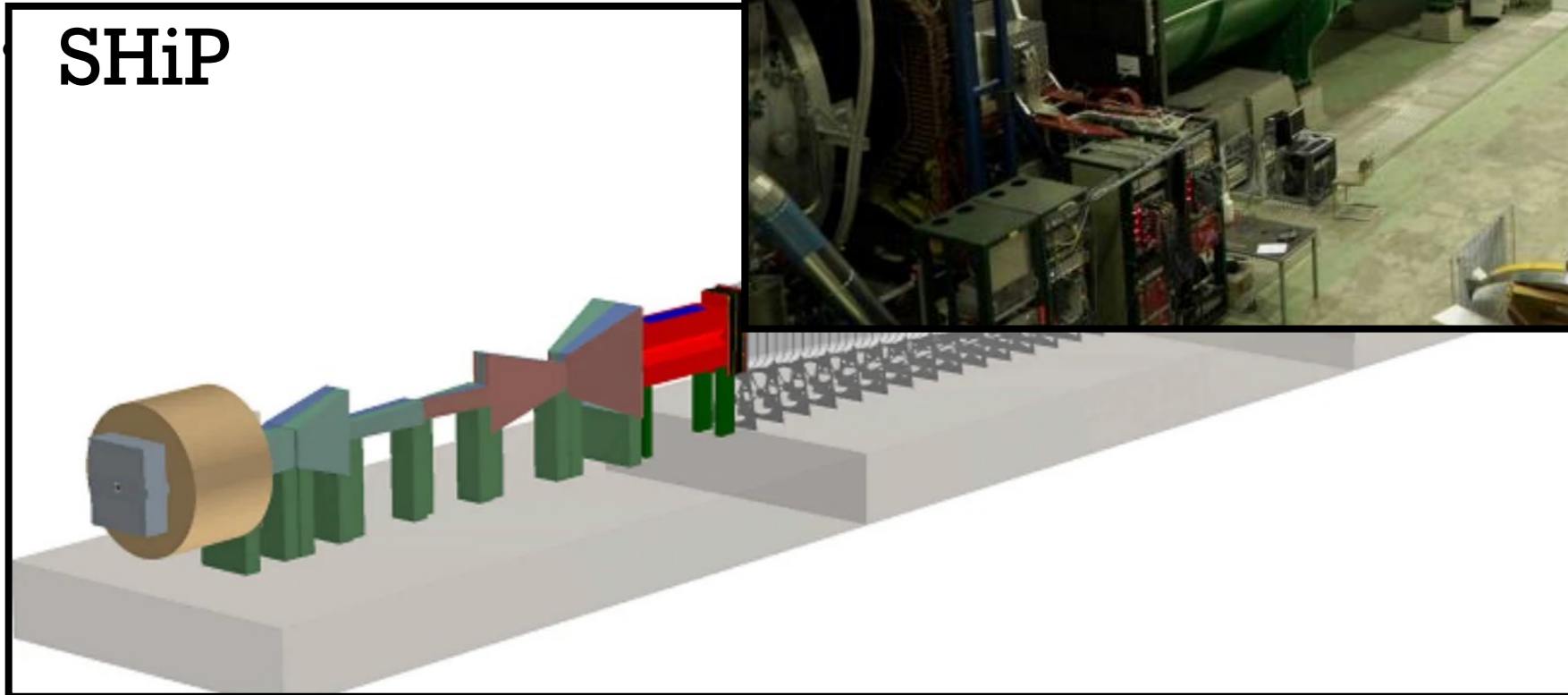
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$N$   
NA62 - beam dump



- Depending on the mass

SHiP





# Photon dipole

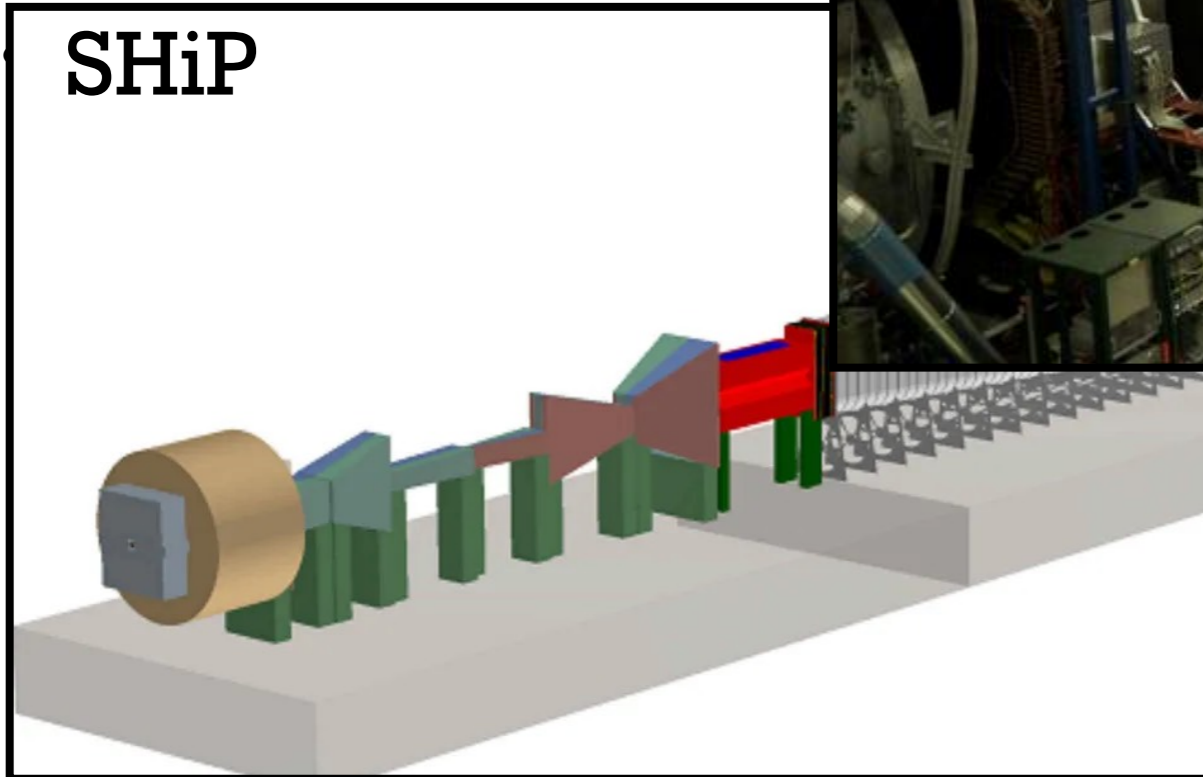
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NA62 - beam dump

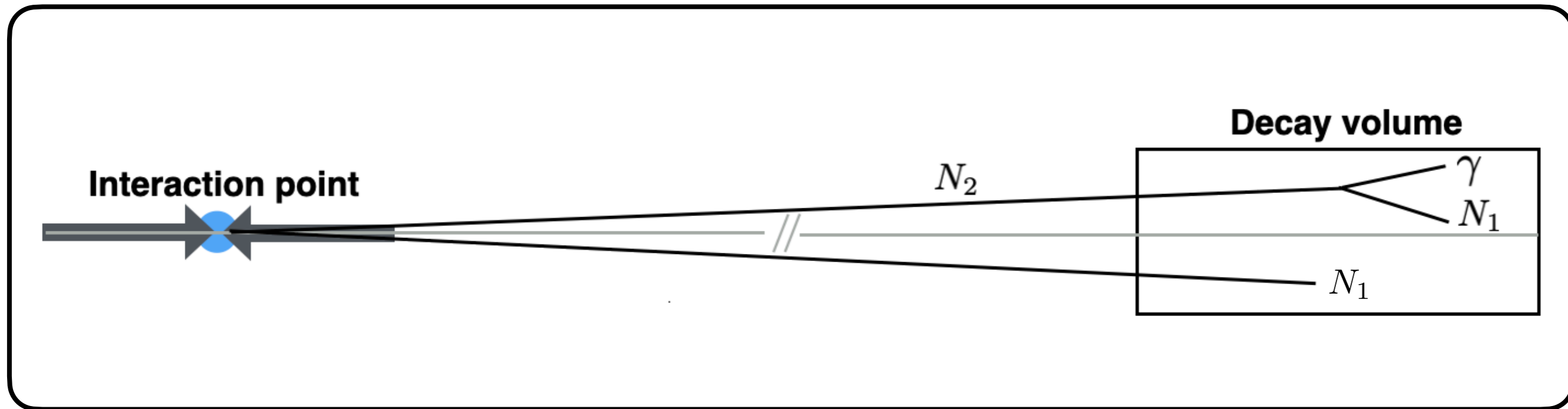


- Depending on the masses

SHiP



FASER



- The signal in the decay volume is a single photon
- In the  $N_2$  rest frame

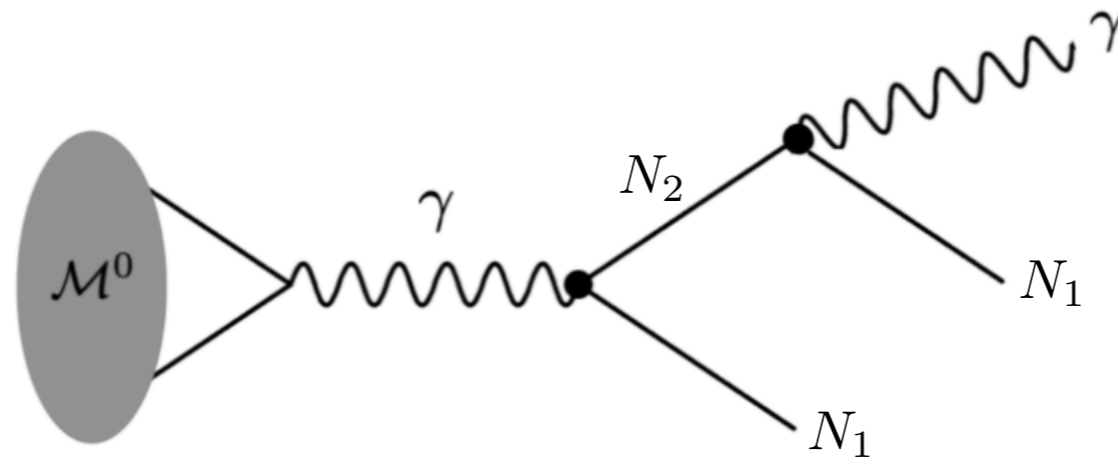
$$E_\gamma = m_{N_2} \frac{\delta}{2} \frac{2 + \delta}{(1 + \delta)^2} \quad \delta = \frac{m_{N_2} - m_{N_1}}{m_{N_1}}$$

- Boosting in the laboratory frame

$$E_\gamma^{\text{lab}} = \left( P_{N_2} + \sqrt{m_{N_2}^2 + P_{N_2}^2} \right) \frac{\delta}{2} \frac{2 + \delta}{(1 + \delta)^2} \simeq 2P_{N_2} \delta$$

Smaller  $\delta$  implies longer lifetime but softer photons...

- The dipole mediates  $N_1 N_2$  production via meson decay, either in fixed target experiments [**SHiP, NA62-dump**] or in pp collisions [**FASER**]



### Beam-dump experiment

$$N_{\text{prod}} = \sum_M N_{\text{POT}} N_M \text{BR}(M \rightarrow N_1 N_2);$$

### LHC collisions

$$N_{\text{prod}} = \sum_M \sigma_{\text{ine}} \mathcal{L} N_M \text{BR}(M \rightarrow N_1 N_2)$$

$$\sigma_{\text{ine}} = 79.5 \text{ mb}$$

$$f_{\text{dec}} = e^{-L_{\text{entry}}/L_{N_2}} - e^{-L_{\text{exit}}/L_{N_2}}$$

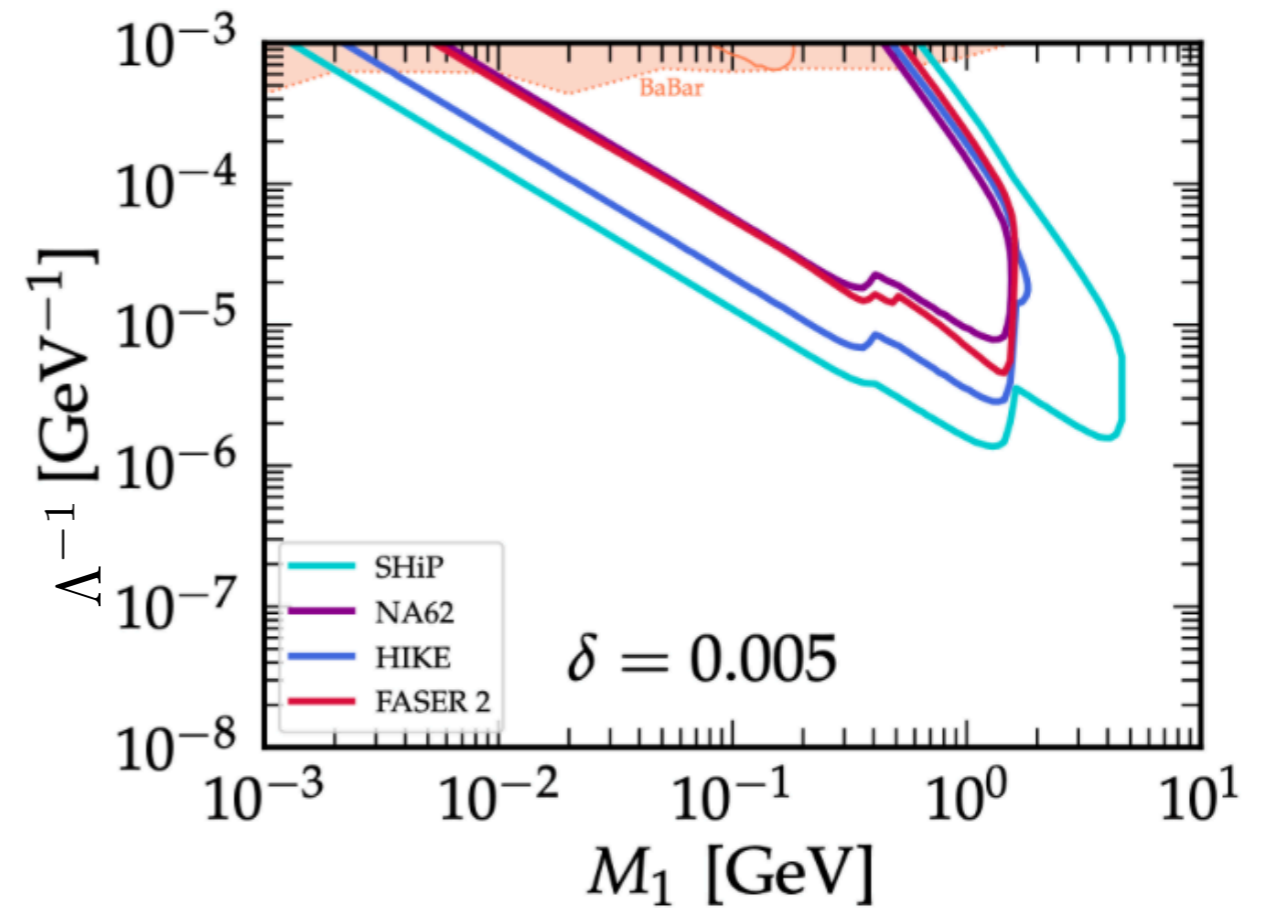
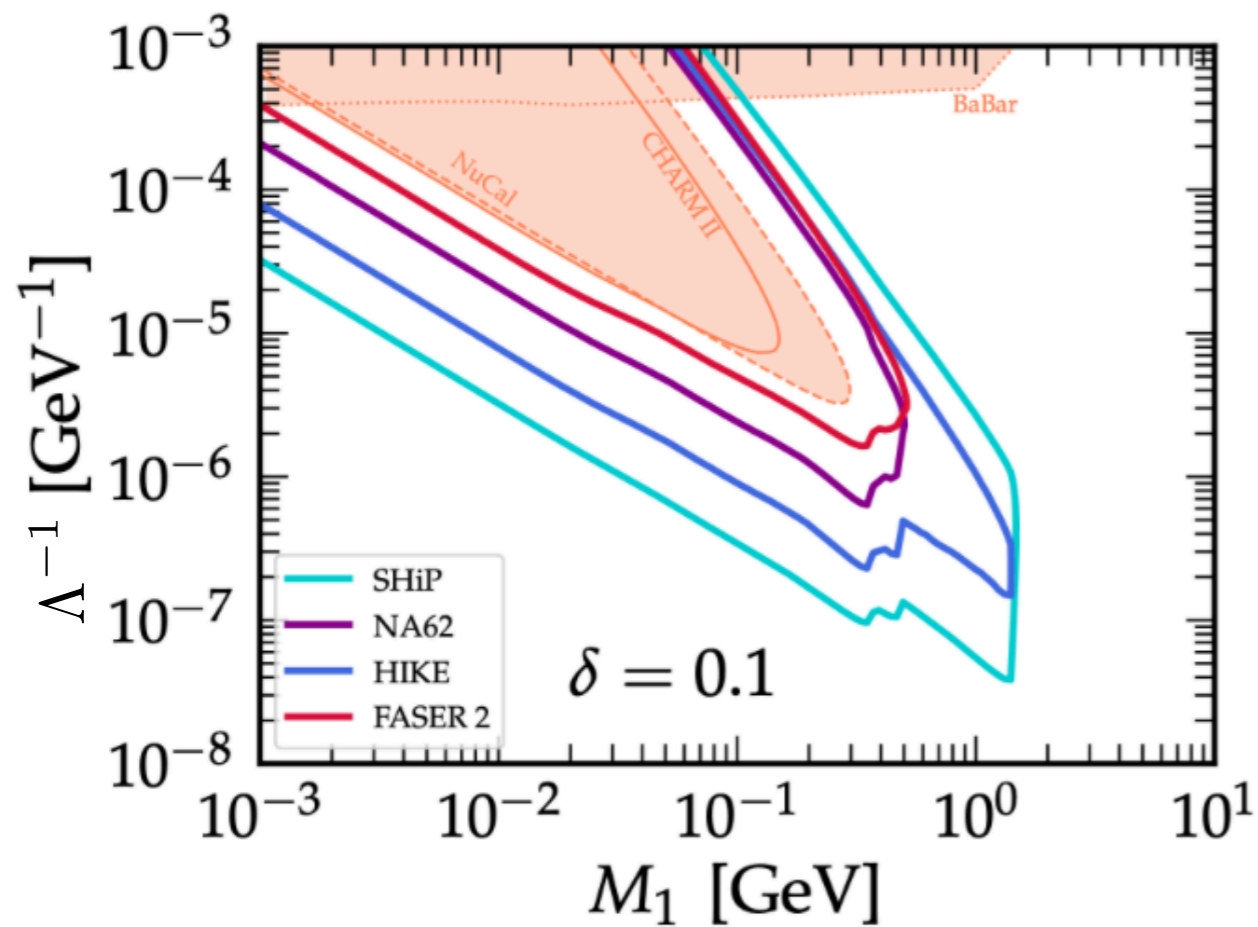
$$N_{\text{signal}} = N_{\text{prod}} \langle f_{\text{dec}} \epsilon_{\text{det}} \rangle$$

- Meson multiplicities estimated with **PYTHIA**, **FORESEE** and **SENSCalc**

$\left\{ \begin{array}{l} \text{NA62 dump} - N_{\text{POT}} = 10^{18} \\ \text{HIKE} - N_{\text{POT}} = 5 \times 10^{19} \\ \text{SHiP} - N_{\text{POT}} = 6 \times 10^{20} \end{array} \right.$

$N_{\pi^0}$	$N_{\eta}$	$N_{\eta'}$	$N_{\rho}$
4.3	0.049	0.055	0.58
$N_{\omega}$	$N_{\phi}$	$N_{J/\psi}$	$N_{\Upsilon}$
0.57	0.021	$4.7 \times 10^{-6}$	$2.2 \times 10^{-9}$

- Cut on  $E_{\gamma} > 1 \text{ GeV}$  - isocontours of  $N = 3$  signal events



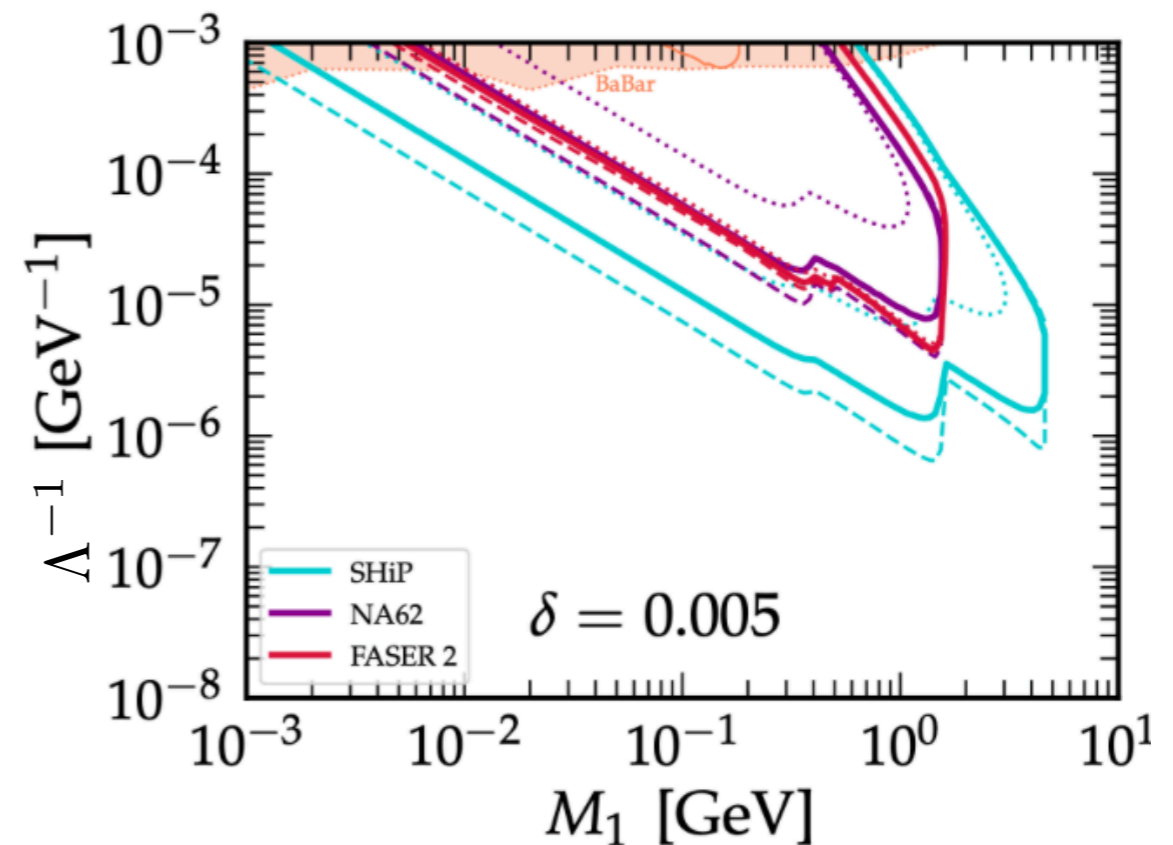
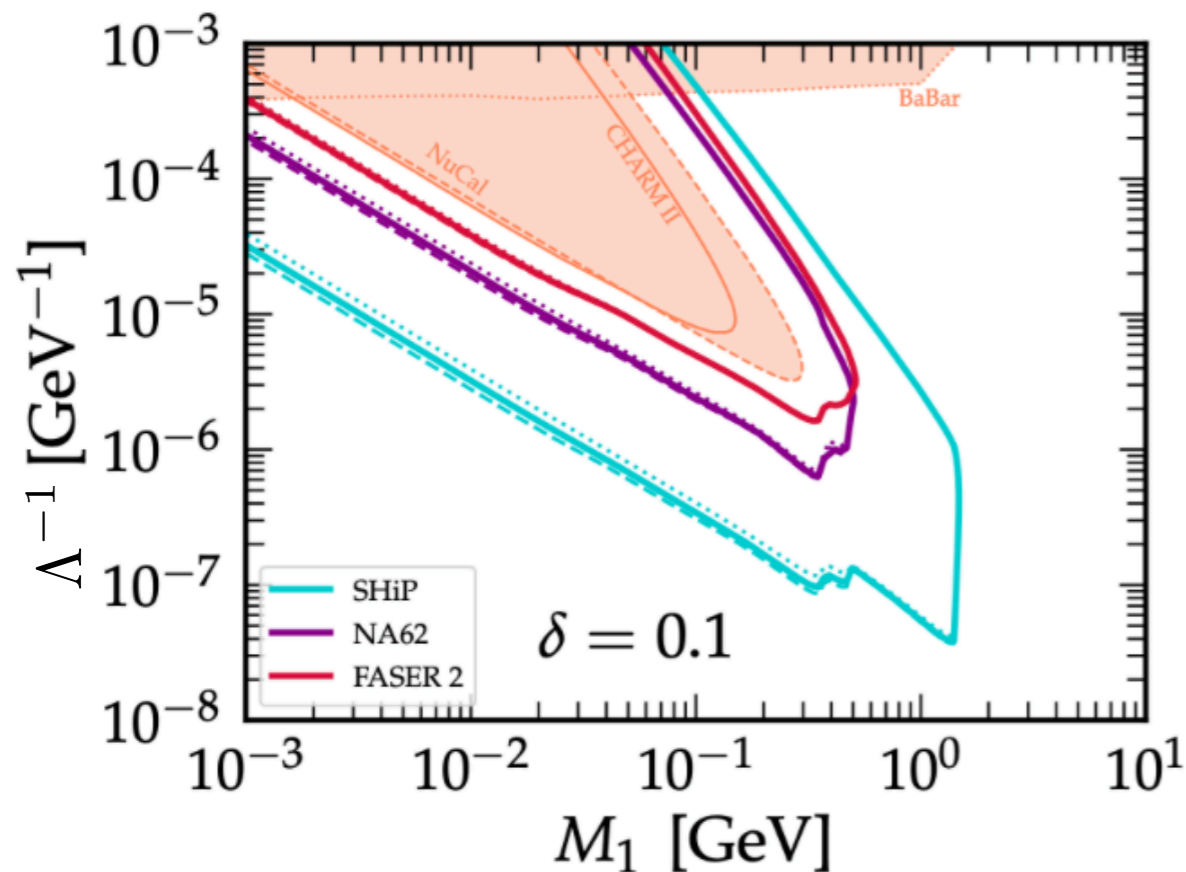
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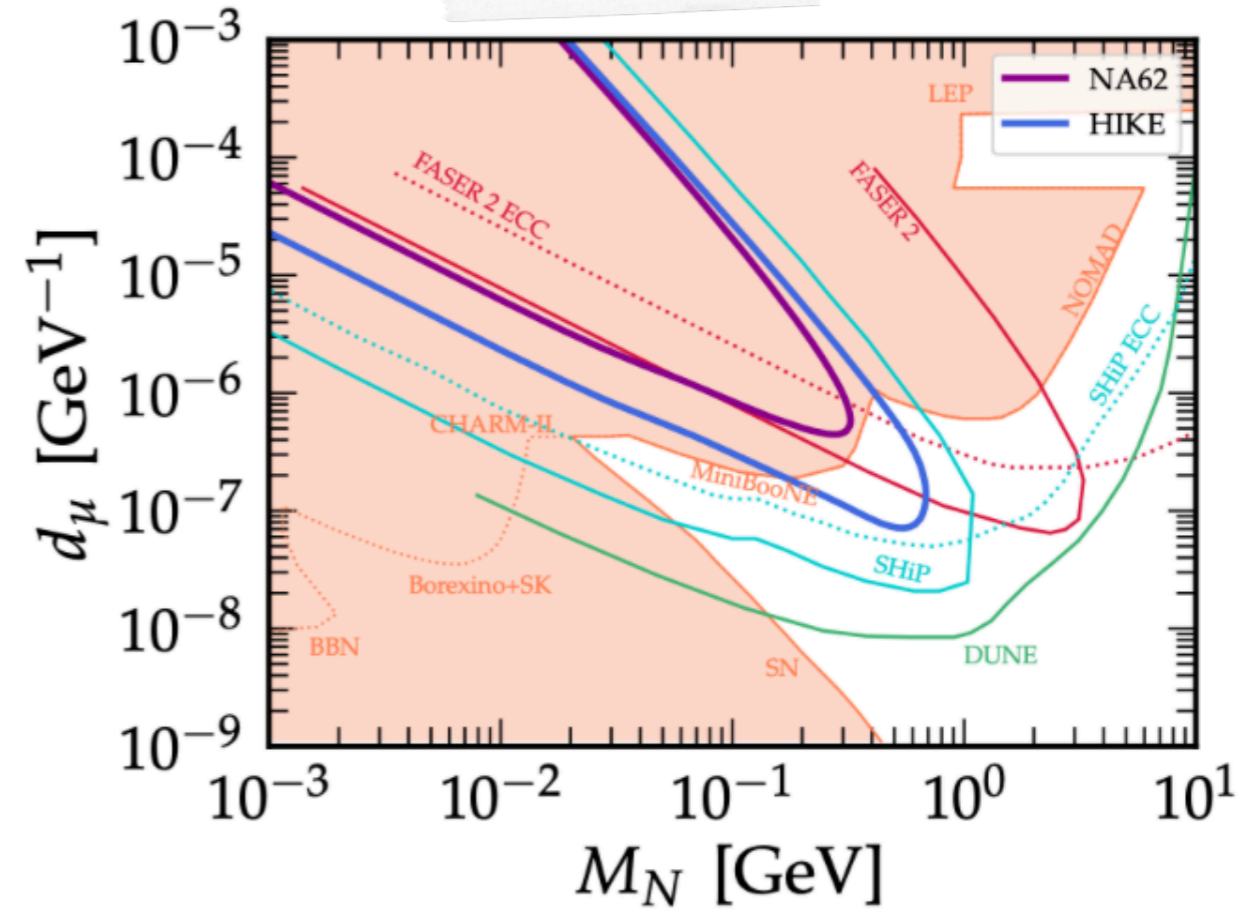
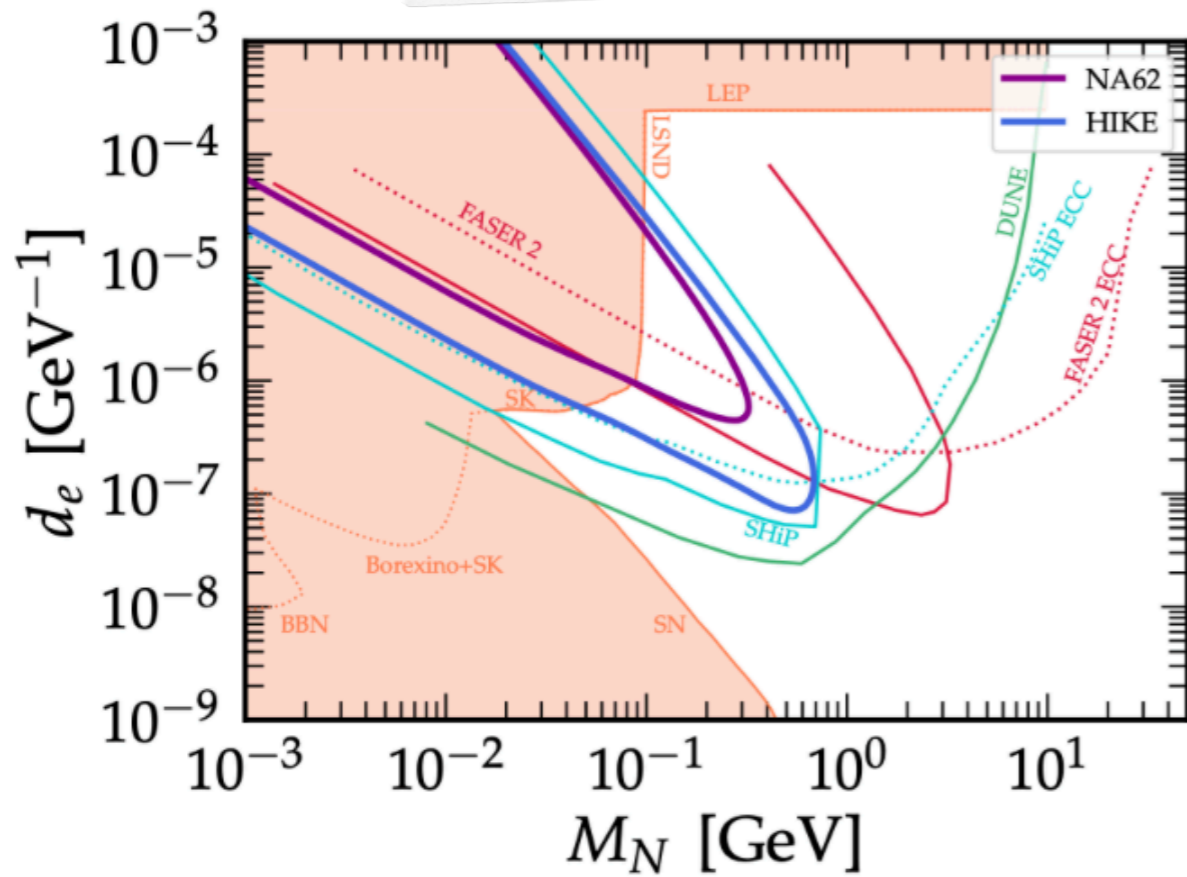
- Cut on  $E_{\gamma} > 1 \text{ GeV}$  - isocontours of  $N = 3$  signal events

Modifying the photon energy threshold: 0.5 GeV, 2 GeV



- Similar strategy applicable to active-sterile dipole

$$\mathcal{O} = d_\nu^i \bar{N} \sigma^{\mu\nu} \nu_i F_{\mu\nu}$$



Thank you



**BACKUP**



# Benchmark point choices

$$\text{BP1}_{\text{NH}} : r_{e4}^2 : r_{\mu4}^2 : r_{\tau4}^2 = 0.10 : 0.68 : 0.22$$

$$\text{BP2}_{\text{NH}} : r_{e4}^2 : r_{\mu4}^2 : r_{\tau4}^2 = 0.01 : 0.16 : 0.83$$

BR	Channel	SS	BR	Channel	SS	BR	Channel	SS	BR	Channel	SS
0.16	2l 4q	✓	0.01	3l τ E <sub>T</sub>		0.13	2τ 4q		0.01	2τ 2q E <sub>T</sub>	✓
0.09	l 4q E <sub>T</sub>		0.01	2l 2τ E <sub>T</sub>		0.09	τ 4q E <sub>T</sub>		0.01	2l 4q	
0.05	4q E <sub>T</sub>		0.01	2l E <sub>T</sub>		0.06	4q E <sub>T</sub>		0.01	l 2q E <sub>T</sub>	
0.05	2l τ 2q E <sub>T</sub>		0.01	2τ 4q		0.06	l 2τ 2q E <sub>T</sub>		0.01	E <sub>T</sub>	
0.04	3l 2q E <sub>T</sub>	✓	0.01	l τ E <sub>T</sub>		0.04	l τ 2q E <sub>T</sub>		0.01	2l 2q E <sub>T</sub>	
0.03	l 4q τ		0.01	τ 2q E <sub>T</sub>		0.03	l τ 4q		0.01	l 3τ E <sub>T</sub>	
0.03	l 2q E <sub>T</sub>		0.01	E <sub>T</sub>		0.03	τ 2q E <sub>T</sub>		0.	3l τ E <sub>T</sub>	
0.02	2l 2q E <sub>T</sub>		0.	2τ 2q E <sub>T</sub>		0.02	l 4q E <sub>T</sub>		0.	2τ E <sub>T</sub>	
0.02	l τ 2q E <sub>T</sub>		0.	l 3τ E <sub>T</sub>		0.02	2l 2τ E <sub>T</sub>		0.	3l 2q E <sub>T</sub>	✓
0.02	τ 4q E <sub>T</sub>		0.	3τ 2q E <sub>T</sub>		0.02	2l τ 2q E <sub>T</sub>		0.	2l E <sub>T</sub>	
0.02	2q E <sub>T</sub>		0.	2τ E <sub>T</sub>		0.02	2q E <sub>T</sub>		0.	4τ E <sub>T</sub>	
0.01	l 2τ 2q E <sub>T</sub>		0.	4τ E <sub>T</sub>		0.01	3τ 2q E <sub>T</sub>		0.	4l E <sub>T</sub>	✓
0.01	4l E <sub>T</sub>	✓				0.01	l τ E <sub>T</sub>				

$$\text{BP1}_{\text{IH}} : r_{e4}^2 : r_{\mu4}^2 : r_{\tau4}^2 = 0.93 : 0.06 : 0.01$$

$$\text{BP2}_{\text{IH}} : r_{e4}^2 : r_{\mu4}^2 : r_{\tau4}^2 = 0.05 : 0.37 : 0.58$$

BR	Channel	SS	BR	Channel	SS	BR	Channel	SS	BR	Channel	SS
0.24	2l 4q	✓	0.01	l τ E <sub>T</sub>		0.06	2τ 4q		0.01	2l 2q E <sub>T</sub>	
0.11	l 4q E <sub>T</sub>		0.01	2l 2τ E <sub>T</sub>		0.06	τ 4q E <sub>T</sub>		0.01	3l 2q E <sub>T</sub>	✓
0.07	3l 2q E <sub>T</sub>	✓	0.	l τ 4q		0.06	4q E <sub>T</sub>		0.01	l τ E <sub>T</sub>	
0.05	4q E <sub>T</sub>		0.	τ 4q E <sub>T</sub>		0.05	l τ 4q		0.01	3l τ E <sub>T</sub>	
0.04	l 2q E <sub>T</sub>		0.	l 2τ 2q E <sub>T</sub>		0.05	l 4q E <sub>T</sub>		0.01	E <sub>T</sub>	
0.04	2l τ 2q E <sub>T</sub>		0.	τ 2q E <sub>T</sub>		0.05	2l 4q	✓	0.01	3τ 2q E <sub>T</sub>	
0.03	2l 2q E <sub>T</sub>		0.	2τ 2q E <sub>T</sub>		0.04	2l 2τ 2q E <sub>T</sub>		0.01	2τ 2q E <sub>T</sub>	
0.02	4l E <sub>T</sub>	✓	0.	2τ E <sub>T</sub>		0.04	l 2τ 2q E <sub>T</sub>		0.01	2l E <sub>T</sub>	
0.02	2q E <sub>T</sub>		0.	l 3τ E <sub>T</sub>		0.03	l τ 2q E <sub>T</sub>		0	4l E <sub>T</sub>	✓
0.02	l τ 2q E <sub>T</sub>		0.	2τ 4q		0.02	2q τ E <sub>T</sub>		0	l 3τ E <sub>T</sub>	
0.01	2l E <sub>T</sub>		0.	3τ 2q E <sub>T</sub>		0.02	2q E <sub>T</sub>		0	2τ E <sub>T</sub>	
0.01	3l τ E <sub>T</sub>		0.	4τ E <sub>T</sub>		0.02	l 2q E <sub>T</sub>		0	4τ E <sub>T</sub>	
0.01	E <sub>T</sub>					0.02	2l 2 τ E <sub>T</sub>				

