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Long-lived HNLs at the LHC: four-fermion operators

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BLED 2024

Breaking Lepton Number in
High Energy Direct Searches

Outline

1. Motivation for right-handed (RH) neutrinos/heavy neutral leptons (HNLs)
2. NSMEFT: the effective field theory of the Standard Model extended with HNLs
3. Phenomenological signatures of stable HNLs
4. Long-lived particle detectors at the high-luminosity LHC (HL-LHC)
5. Sensitivity to long-lived HNLs produced in partonic collisions
6. Sensitivity to long-lived HNLs produced in meson decays
7. Conclusions

Motivation: new physics

No **new physics** signals at particle physics experiments (modulo several inconclusive anomalies), except for **neutrino masses**

New Physics

- very **weakly coupled**
new degrees of freedom (dofs) **below the electroweak (EW) scale v**
very likely singlets of the SM gauge group
- present **at scales $\Lambda \gg v$**
SMEFT is appropriate description
- **both**
“new dofs + SM” EFT (respecting SM gauge symmetry) required

What are these new dofs:

scalars, fermions, vectors?

Motivation: neutrino masses

In the SM neutrinos are massless

Neutrino oscillations show that (at least two) neutrinos have mass

Minimal renormalisable Lagrangian to accommodate neutrino masses:

$$\mathcal{L}_{\text{SM}+N} = \mathcal{L}_{\text{SM}} + i\bar{N}_R \not{\partial} N_R - [\bar{L}\tilde{H}Y_N N_R + \text{h.c.}]$$

N_R is right-handed (RH) neutrino

$\nu = (\nu_L, N_R)^T$ is Dirac neutrino, lepton number (LN) is conserved

$$Y_N \sim 10^{-13} \quad \Rightarrow \quad m_\nu = Y_N v / \sqrt{2} \sim 0.01 \text{ eV}$$

$$(Y_t \sim 1 \quad Y_e \sim 10^{-6} \quad \Rightarrow \quad \text{flavour problem})$$

Is LN a fundamental symmetry?

Motivation: neutrino masses

If **LN** is **violated**, then

$$-\mathcal{L}_{\text{mass}} = \bar{L}\tilde{H}Y_N N_R + \frac{1}{2}\bar{N}_R^c M N_R + \text{h.c.} \rightarrow \frac{1}{2} \begin{pmatrix} \bar{\nu}_L & \bar{N}_R^c \end{pmatrix} \begin{pmatrix} 0 & m_D \\ m_D^T & M \end{pmatrix} \begin{pmatrix} \nu_L^c \\ N_R \end{pmatrix} + \text{h.c.}$$

$\nu = (\nu_L, \nu_L^c)^T$ and $N = (N_R^c, N_R)^T$ are **Majorana** neutrinos

N is *heavy neutral lepton (HNL)*

Type I seesaw mechanism

$$m_D = Y_N v / \sqrt{2} \ll M \Rightarrow m_\nu = -m_D M^{-1} m_D^T$$

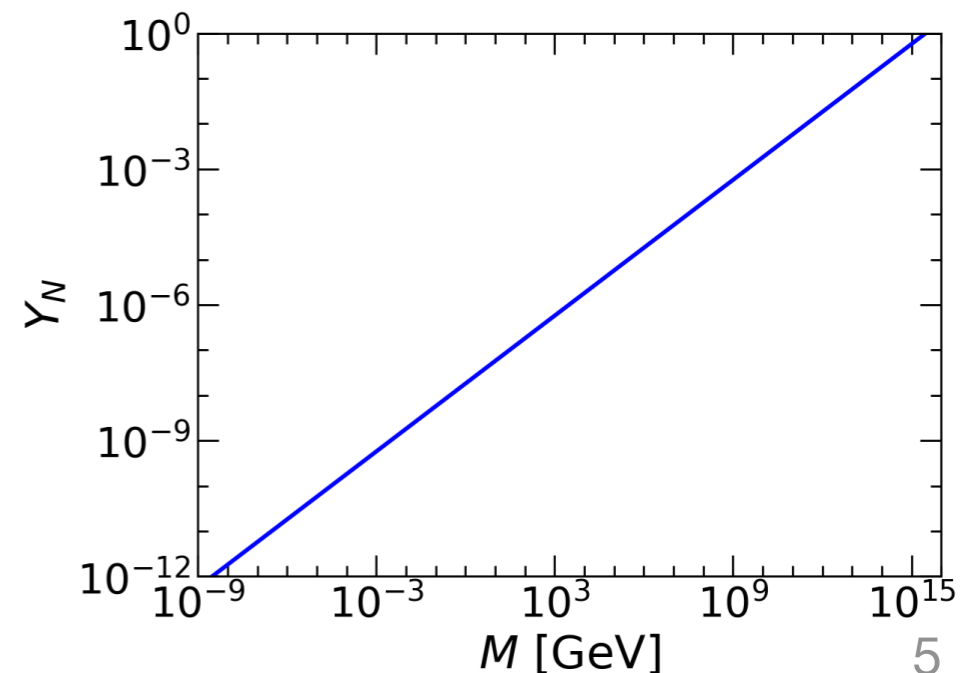
$$Y_N \sim 1, \quad M \sim 10^{15} \text{ GeV} \Rightarrow m_\nu \sim 0.01 \text{ eV}$$

For $Y_N \ll 1$, huge range of values for M

Active-heavy neutrino mixing

$$V_{\alpha N}^2 \sim \left(\frac{m_D}{M} \right)^2 \sim \frac{m_\nu}{M}$$

$$V_{\alpha N}^2 \sim 10^{-11} \div 10^{-14} \quad \text{for} \quad M \sim 1 \div 10^3 \text{ GeV}$$



Motivation: neutrino masses

There are variants of the seesaw mechanism with low M and large $V_{\alpha N}$ e.g.

Inverse seesaw mechanism

$$-\mathcal{L}_{\text{mass}} = \frac{1}{2} (\bar{\nu}_L \quad \bar{N}_R^c \quad \bar{S}_L) \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M_R^T \\ 0 & M_R & \mu \end{pmatrix} \begin{pmatrix} \nu_L^c \\ N_R \\ S_L^c \end{pmatrix} + \text{h.c.}$$

$$m_\nu = m_D M_R^{-1} \mu M_R^{-1T} m_D^T \quad \text{and} \quad V_{\alpha N}^2 \sim \left(\frac{m_D}{M_R} \right)^2 \sim \frac{m_\nu}{\mu}$$

$$m_\nu \sim 0.01 \text{ eV and } |V_{\alpha N}|^2 \sim 10^{-2} \div 10^{-8}$$

$$\text{for } Y_N \sim 10^{-3}, \quad M_R \sim 1 \div 10^3 \text{ GeV}, \quad \mu \sim 10^{-9} \div 10^{-3} \text{ GeV}$$

Small μ is technically natural, since for $\mu = 0$, LN symmetry is restored

Motivation: neutrino masses

Of course, at non-renormalisable level, the minimal way to generate **Majorana** neutrino masses is via **Weinberg dimension-5 operator**

$$\mathcal{O}_{LH} = (\bar{L}\tilde{H}) (\tilde{H}^T L^c) + \text{h.c.}$$

SMEFT accommodates **lepton-number-violating** neutrino masses

In what follows, we will assume

▶ **lepton number conservation (LNC)**

or

▶ **lepton number violation (LNV)** by $M \lesssim v$

▶ new heavy physics exists at scale $\Lambda \gg v$

Under these assumptions, N_R should be present in the EFT

⇒ **NSMEFT** (also called ν SMEFT, N_R SMEFT, SMNEFT)

NSMEFT: dim-5 operators

The effective Lagrangian

$$\mathcal{L} = \mathcal{L}_{\text{SM}+N} + \sum_{d=5}^{\infty} \frac{1}{\Lambda^{d-4}} \sum_i^{n_d} c_i^{(d)} \mathcal{O}_i^{(d)}$$

$\mathcal{O}_i^{(d)}$ are effective operators invariant under $\text{SU}(3)_C \times \text{SU}(2)_L \times \text{U}(1)_Y$

Operators of $d = 5$ (all violate LN)

$$\mathcal{O}_{LH} = (\bar{L}\tilde{H}) (\tilde{H}^T L^c) \quad \text{Weinberg, PRL 43 (1979) 1566}$$

$$\mathcal{O}_{NNH} = (\bar{N}_R^c N_R) (H^\dagger H) \quad \text{Aguila, Bar-Shalom, Soni, Wudka, 0806.0876}$$

$$\mathcal{O}_{NNB} = (\bar{N}_R^c \sigma^{\mu\nu} N_R) B_{\mu\nu} \quad \text{Aparici, Kim, Santamaria, Wudka, 0904.3244}$$

\mathcal{O}_{NNB} vanishes identically for one generation of N_R

NSMEFT: dim-6 operators

Aguila, Bar-Shalom, Soni, Wudka, 0806.0876

Liao and Ma, 1612.04527

Higgs-N operators # (+h.c.) = 5 (9)

1H	$\mathcal{O}_{NB} = \bar{L}\sigma^{\mu\nu}N_R\tilde{H}B_{\mu\nu}$	$\mathcal{O}_{NW} = \bar{L}\sigma^{\mu\nu}N_R\sigma^I\tilde{H}W_{\mu\nu}^I$
2H	$\mathcal{O}_{HN} = \bar{N}_R\gamma^\mu N_R(H^\dagger i\overleftrightarrow{D}_\mu H)$	$\mathcal{O}_{HNe} = \bar{N}_R\gamma^\mu e_R(\tilde{H}^\dagger iD_\mu H)$
3H	$\mathcal{O}_{LNH} = \bar{L}\tilde{H}N_R(H^\dagger H)$	

4-fermions 11 (16)

RRRR	$\mathcal{O}_{NN} = (\bar{N}_R\gamma_\mu N_R)(\bar{N}_R\gamma^\mu N_R)$
	$\mathcal{O}_{eN} = (\bar{e}_R\gamma_\mu e_R)(\bar{N}_R\gamma^\mu N_R)$ $\mathcal{O}_{uN} = (\bar{u}_R\gamma_\mu u_R)(\bar{N}_R\gamma^\mu N_R)$
	$\mathcal{O}_{dN} = (\bar{d}_R\gamma_\mu d_R)(\bar{N}_R\gamma^\mu N_R)$ $\mathcal{O}_{duNe} = (\bar{d}_R\gamma_\mu u_R)(\bar{N}_R\gamma^\mu e_R)$
LLRR	$\mathcal{O}_{LN} = (\bar{L}\gamma_\mu L)(\bar{N}_R\gamma^\mu N_R)$ $\mathcal{O}_{QN} = (\bar{Q}\gamma_\mu Q)(\bar{N}_R\gamma^\mu N_R)$
LRLR	$\mathcal{O}_{LNLe} = (\bar{L}N_R)\epsilon(\bar{L}e_R)$ $\mathcal{O}_{LNQd} = (\bar{L}N_R)\epsilon(\bar{Q}d_R)$
	$\mathcal{O}_{LdQN} = (\bar{L}d_R)\epsilon(\bar{Q}N_R)$
LRRL	$\mathcal{O}_{QuNL} = (\bar{Q}u_R)(\bar{N}_RL)$

2 (4)

\cancel{L}	$\mathcal{O}_{NNNN} = (\bar{N}_R^c N_R)(\bar{N}_R^c N_R)$
\cancel{L} & \cancel{B}	$\mathcal{O}_{QQdN} = (\bar{Q}^c\epsilon Q)(\bar{d}_R^c N_R)$
	$\mathcal{O}_{uddN} = (\bar{u}_R^c d_R)(\bar{d}_R^c N_R)$

$n_f = 1$ [3] : 29 [1614]
operators including h.c.

4-fermions and (almost) stable N

Dirac $\nu = (\nu_L, N_R)^T$ or Majorana $N = (N_R^c, N_R)^T$ with $m_N \lesssim 0.1$ GeV

Alcaide, Banerjee, Chala, AT, 1905.11375

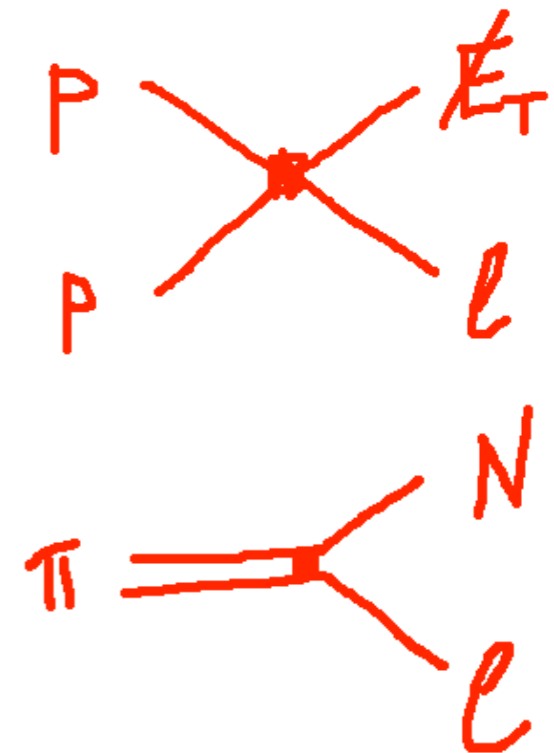
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LRLR	$\mathcal{O}_{LNLe} = (\overline{L} N_R) \epsilon(\overline{L} e_R) \quad \mathcal{O}_{LNQd} = (\overline{L} N_R) \epsilon(\overline{Q} d_R)$ $\mathcal{O}_{LdQN} = (\overline{L} d_R) \epsilon(\overline{Q} N_R)$
LRRL	$\mathcal{O}_{QuNL} = (\overline{Q} u_R)(\overline{N_R} L)$

4-fermions and (almost) stable N

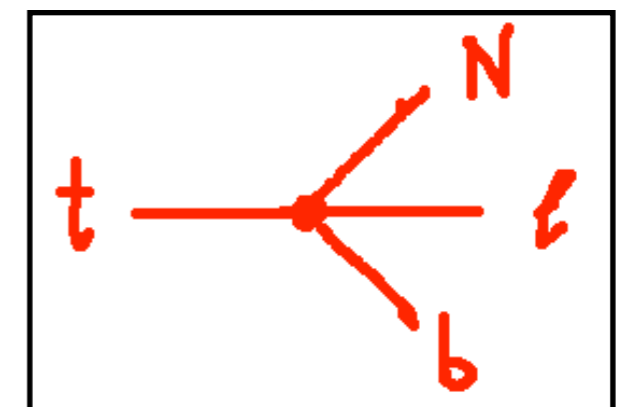
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Alcaide, Banerjee, Chala, AT, 1905.11375

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New top decay

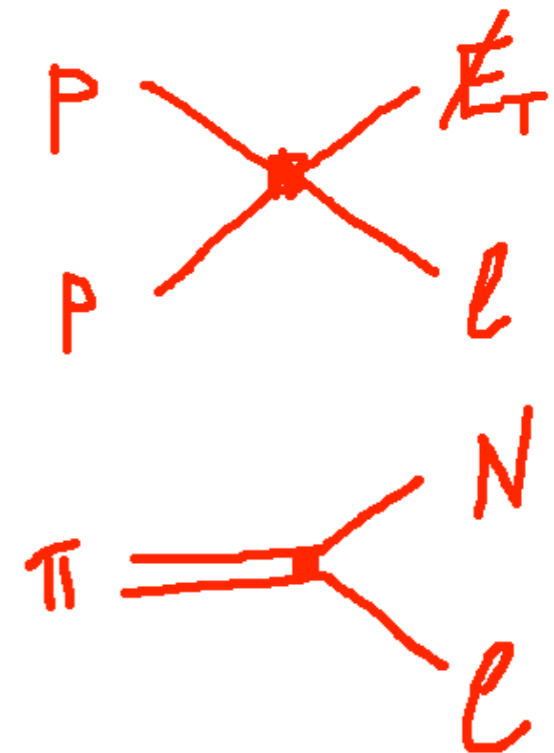


4-fermions and (almost) stable N

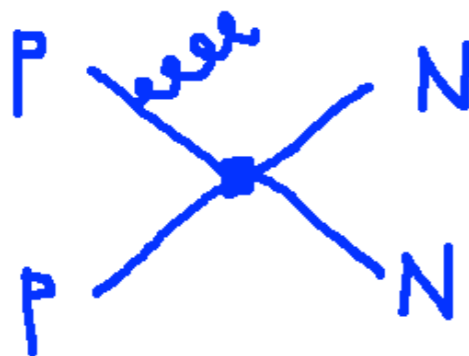
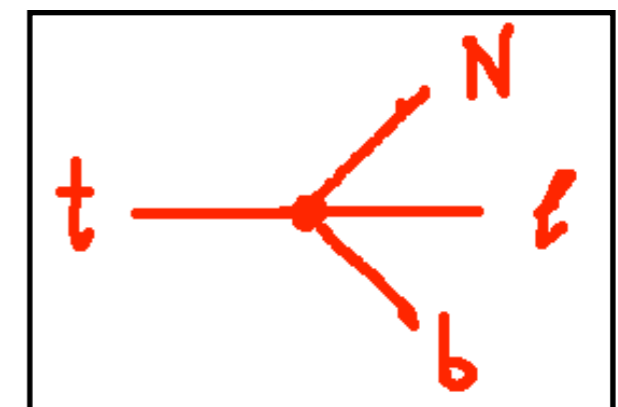
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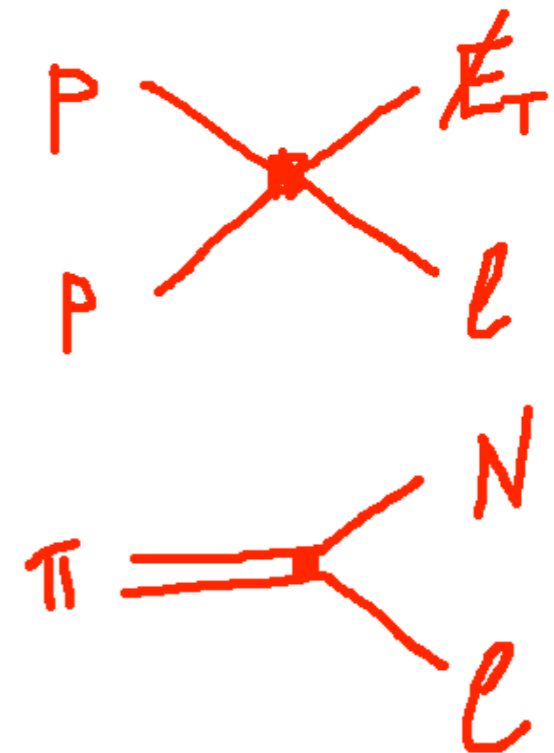


4-fermions and (almost) stable N

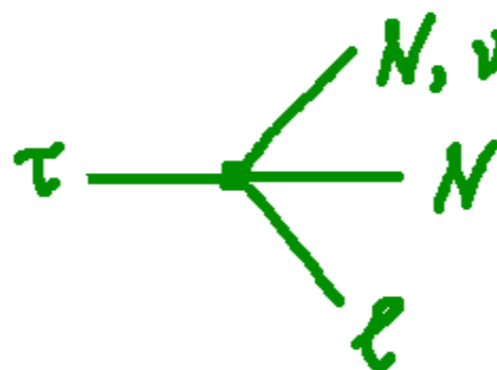
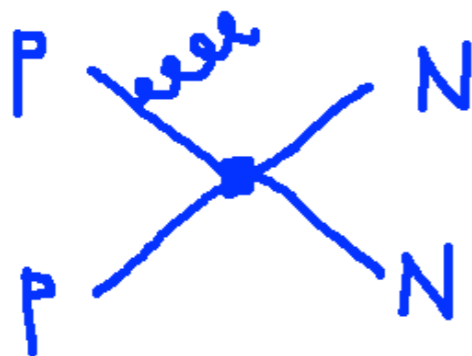
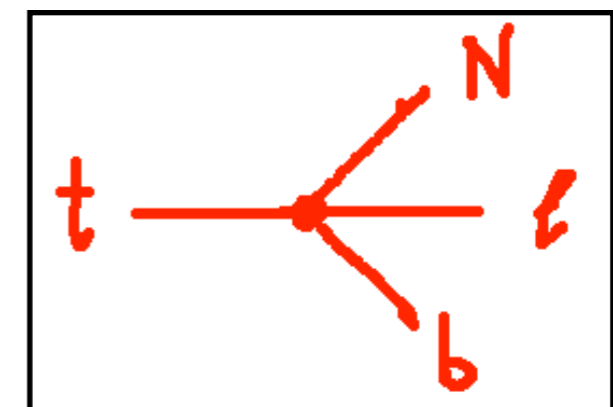
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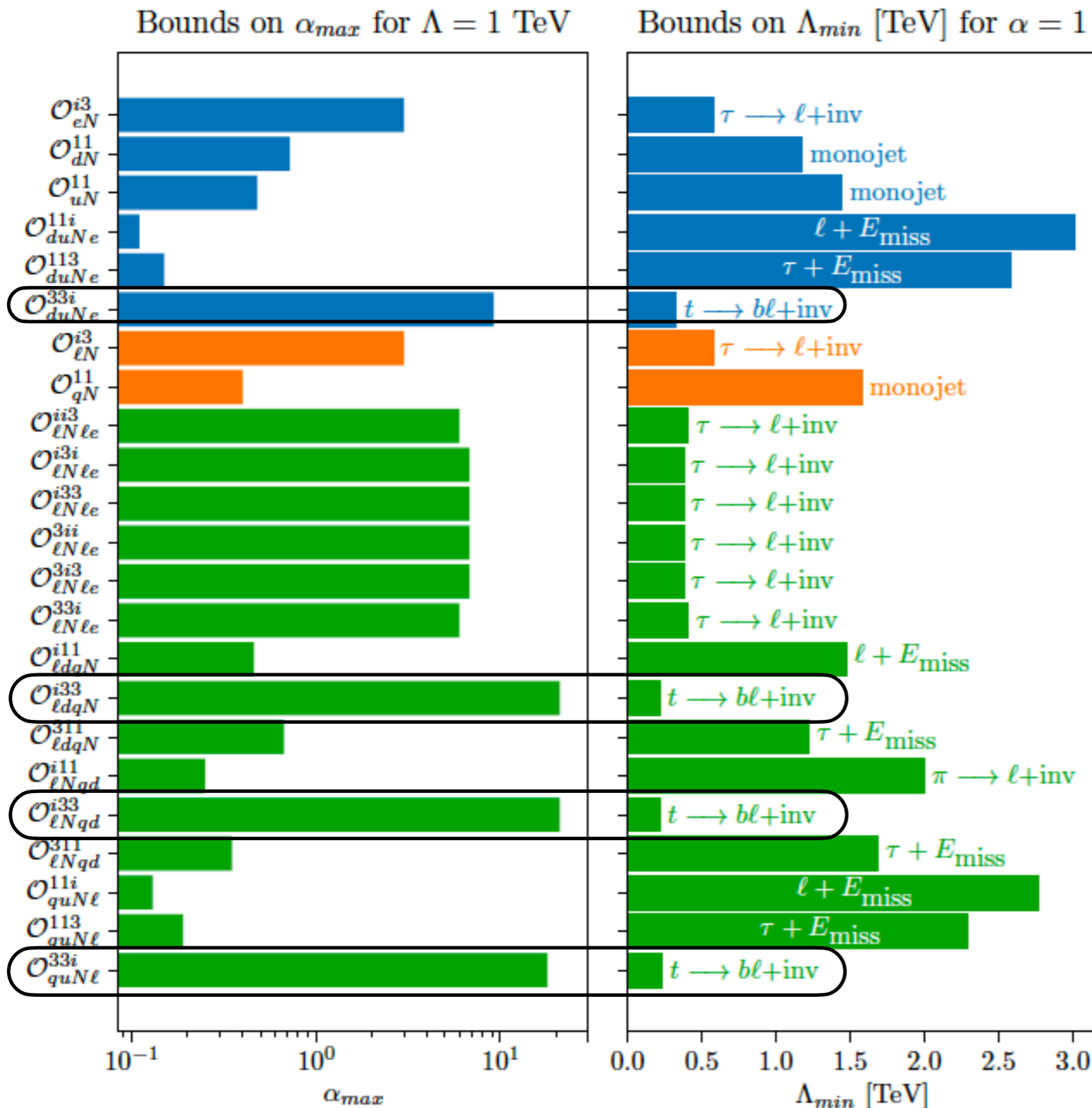


New top decay



4-fermions and (almost) stable N

RRRR
LLLL
LRRL and LRLR



Alcaide, Banerjee, Chala, AT, 1905.11375

Figure from J. Alcaide's PhD thesis

$$pp \rightarrow \ell + E_T^{\text{miss}}$$

ATLAS, 1706.04786

$$pp \rightarrow j + E_T^{\text{miss}} \text{ (monojet)}$$

CMS, 1712.02345

$$\Gamma_{\pi \rightarrow e + \text{inv}} = (310 \pm 1) \times 10^{-23} \text{ GeV}$$

$$\Gamma_{\tau \rightarrow e + \text{inv}} = (4.03 \pm 0.02) \times 10^{-13} \text{ GeV}$$

PDG, RPP 2018

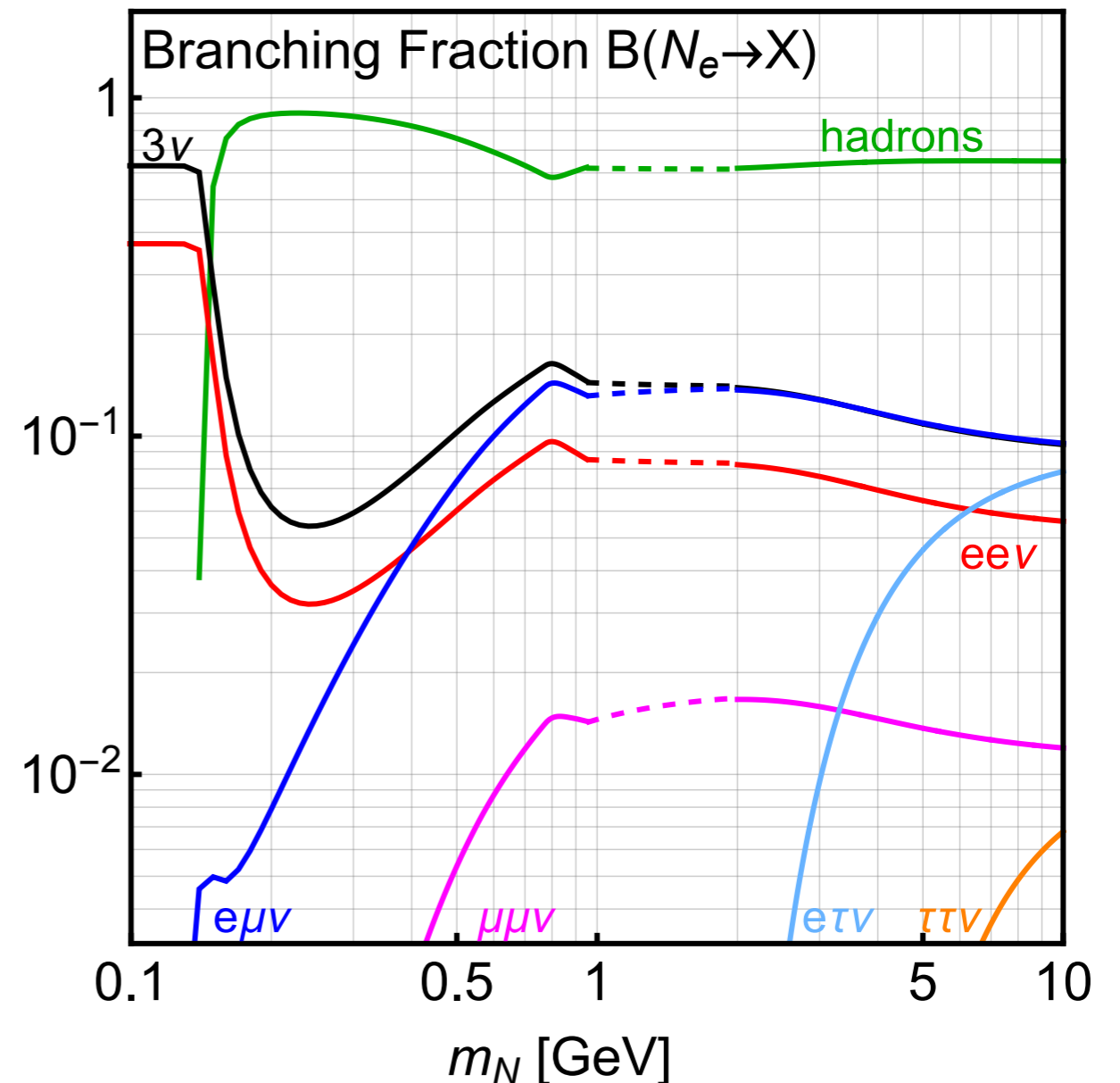
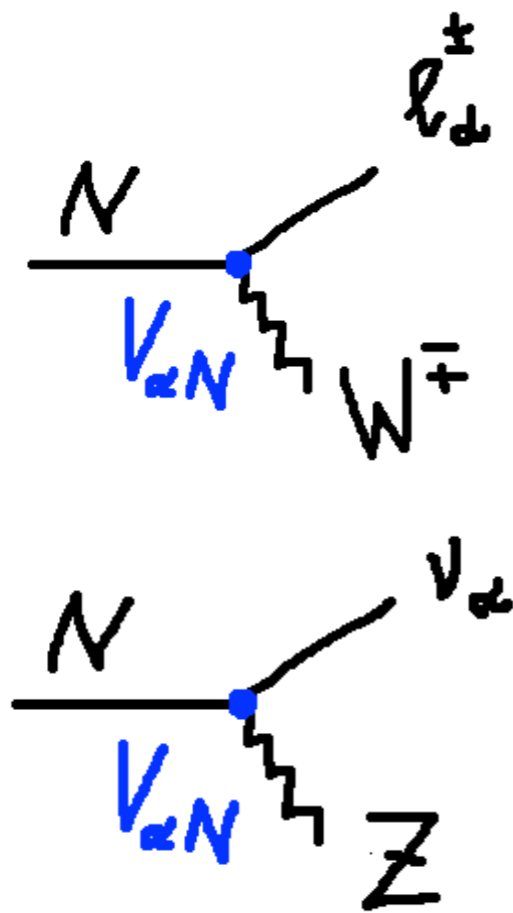
$$t \rightarrow b\ell + \text{inv} @ \text{HL-LHC}$$

Alcaide, Banerjee, Chala, AT, 1905.11375

HNL decay via active-heavy mixing

$$\mathcal{L}_{\min} = -\frac{g}{\sqrt{2}} V_{\alpha N} \bar{\ell}_{\alpha} \gamma^{\mu} P_L N W_{\mu} - \frac{g}{2 \cos \theta_W} V_{\alpha N} \bar{\nu}_{\alpha} \gamma^{\mu} P_L N Z_{\mu} + \text{h.c.}$$

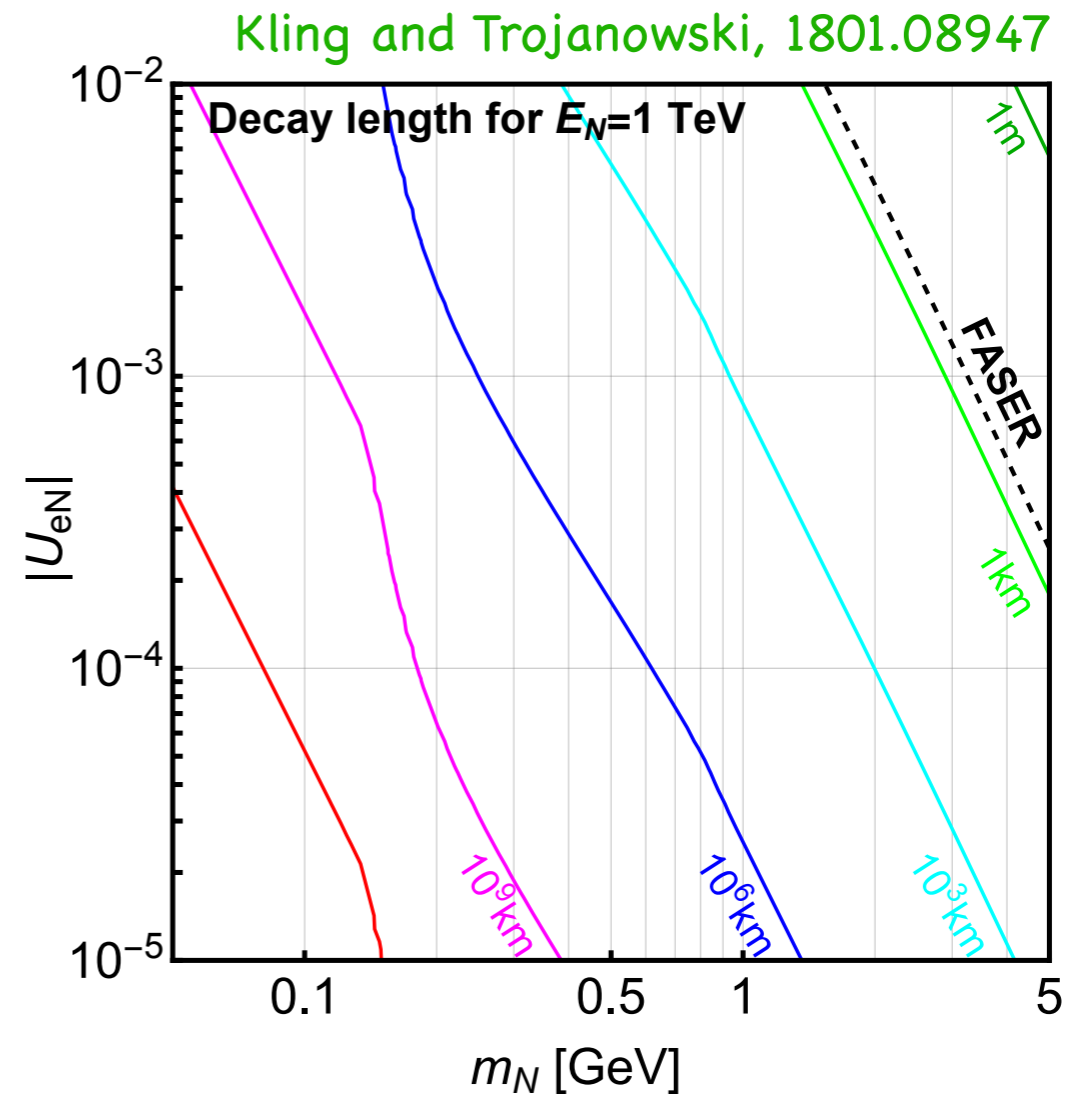
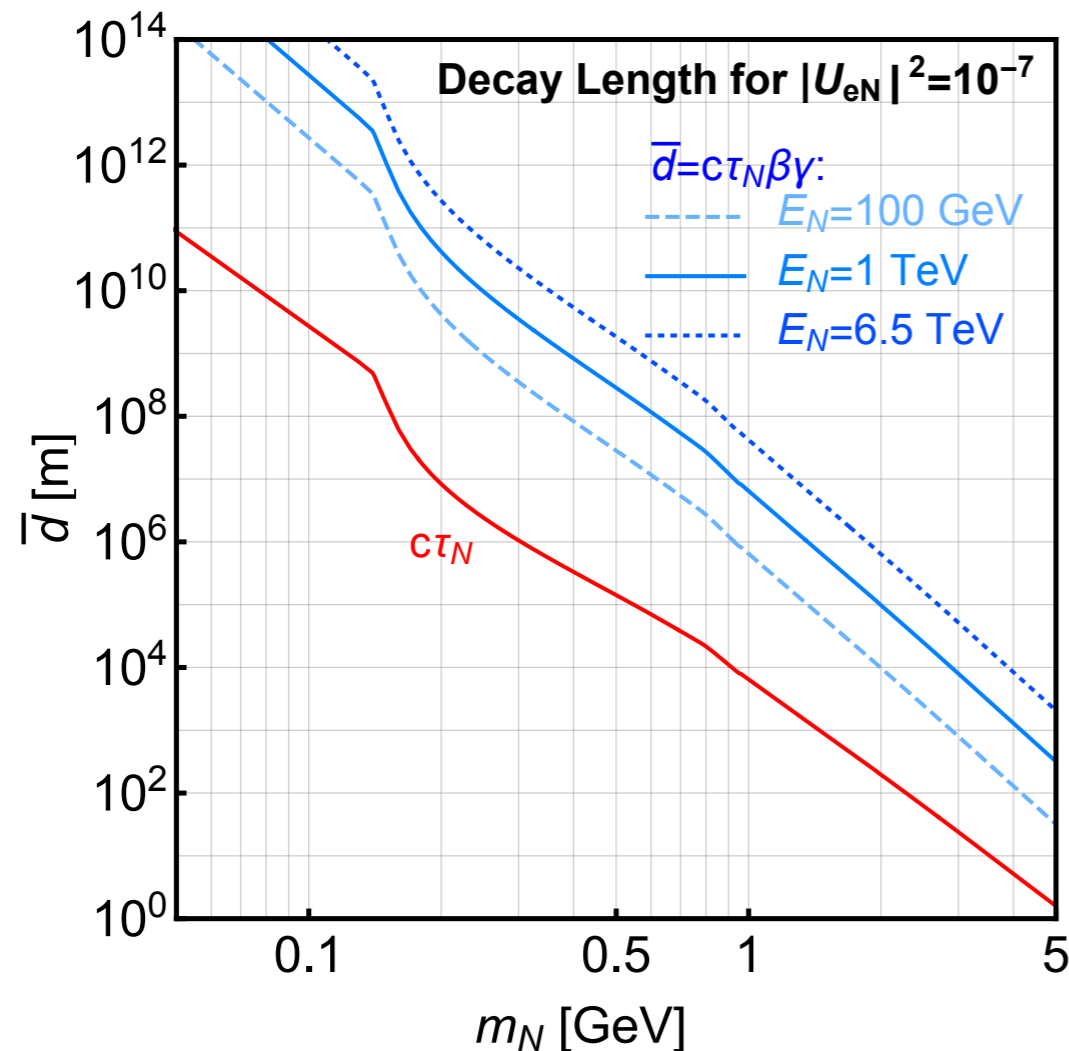
Kling and Trojanowski, 1801.08947



Long-lived HNLs

Proper decay length: $c\tau_N = \frac{1}{\Gamma_N} \propto \frac{1}{|V_{\alpha N}|^2}$

Decay length in the *lab frame*: $\bar{d} = \beta \gamma c \tau_N$



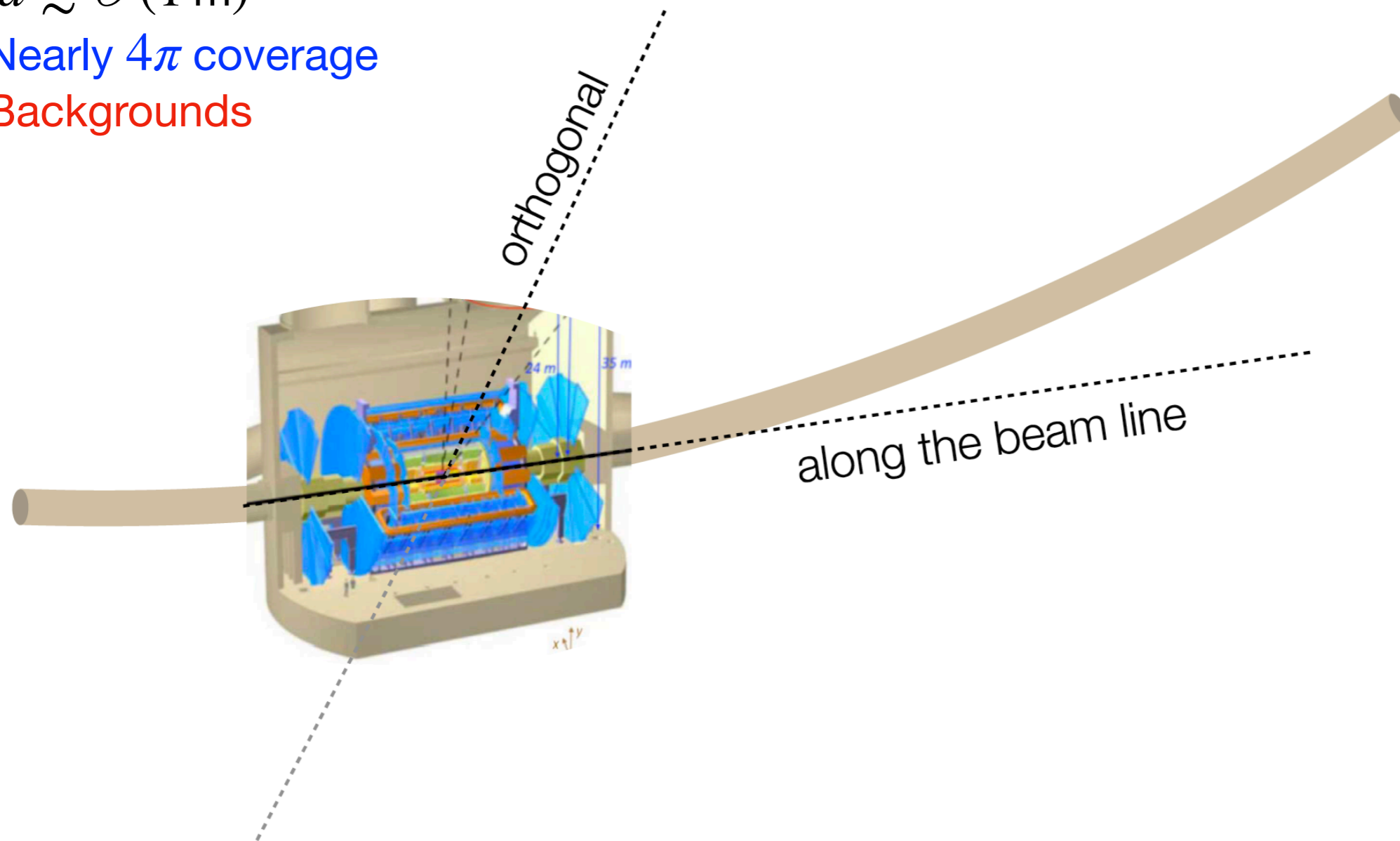
Local detectors at HL-LHC

ATLAS and CMS

$$\bar{d} \lesssim \mathcal{O}(1 \text{ m})$$

Nearly 4π coverage

Backgrounds



Images from [O. Brandt's talk at Oxford Particle Physics Seminar](#) on 9/6/2020

FASER: ForwArD Search ExpeRiment

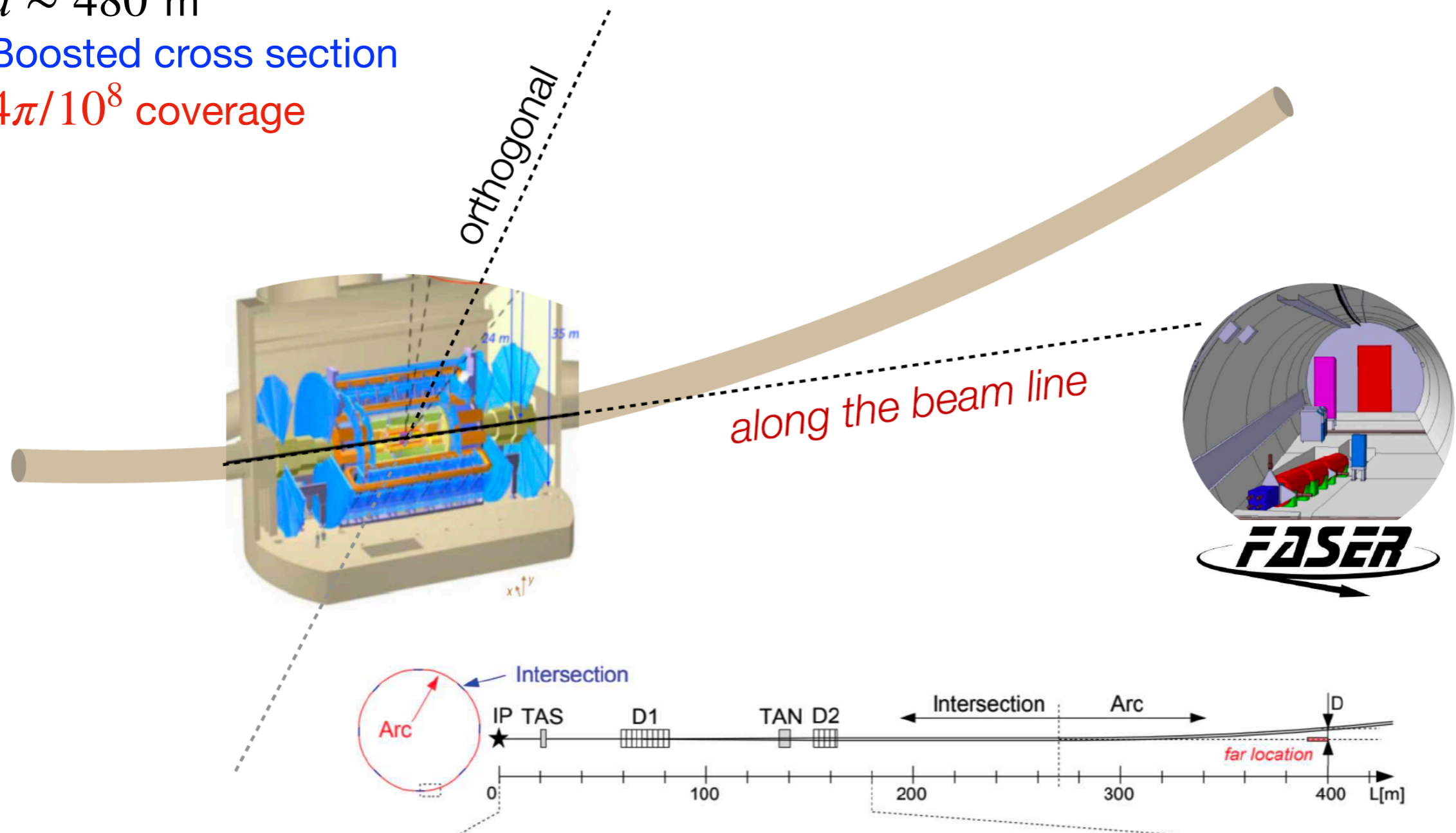
Cylinder with $r = 10$ cm and $\ell = 1.5$ m

Started data taking in 2022

$\bar{d} \sim 480$ m

Boosted cross section

$4\pi/10^8$ coverage



Images from [O. Brandt's talk at Oxford Particle Physics Seminar](#) on 9/6/2020

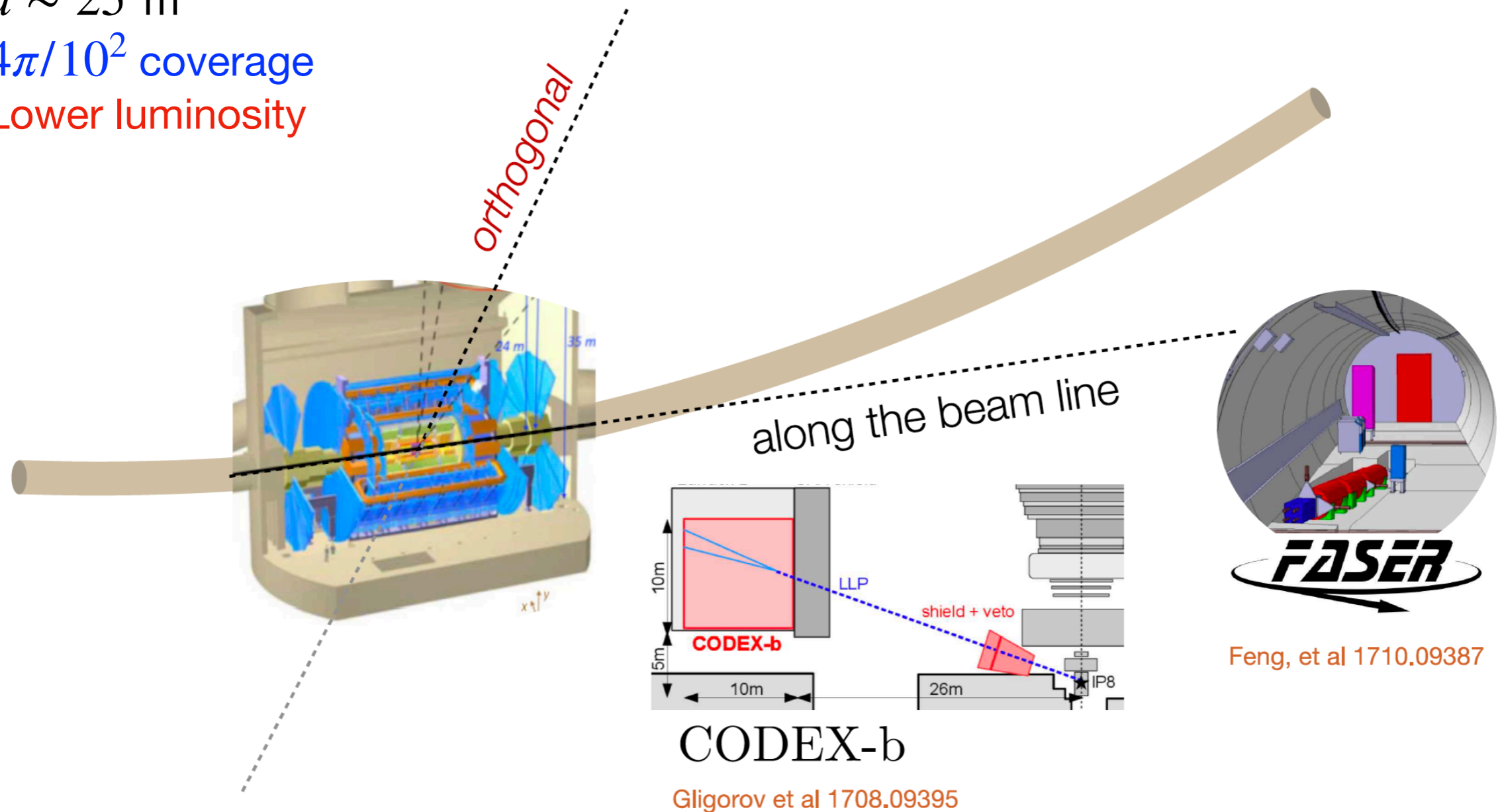
CODEX-b: COmpact Detector for EXotics at LHCb

Box of 10 m × 10 m × 10 m

$\bar{d} \sim 25$ m

$4\pi/10^2$ coverage

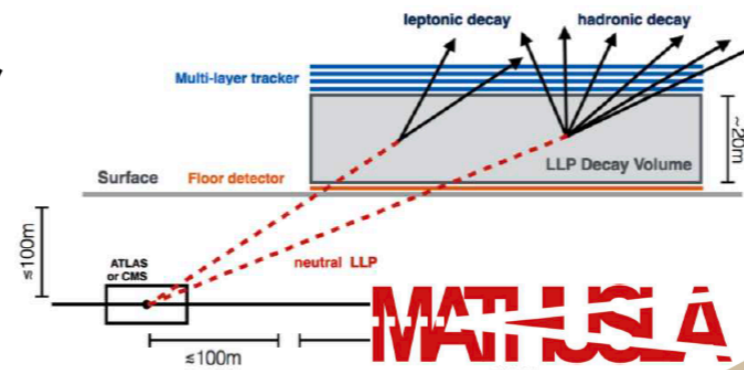
Lower luminosity



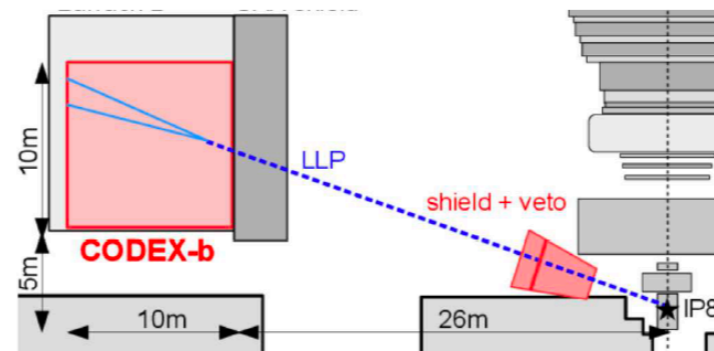
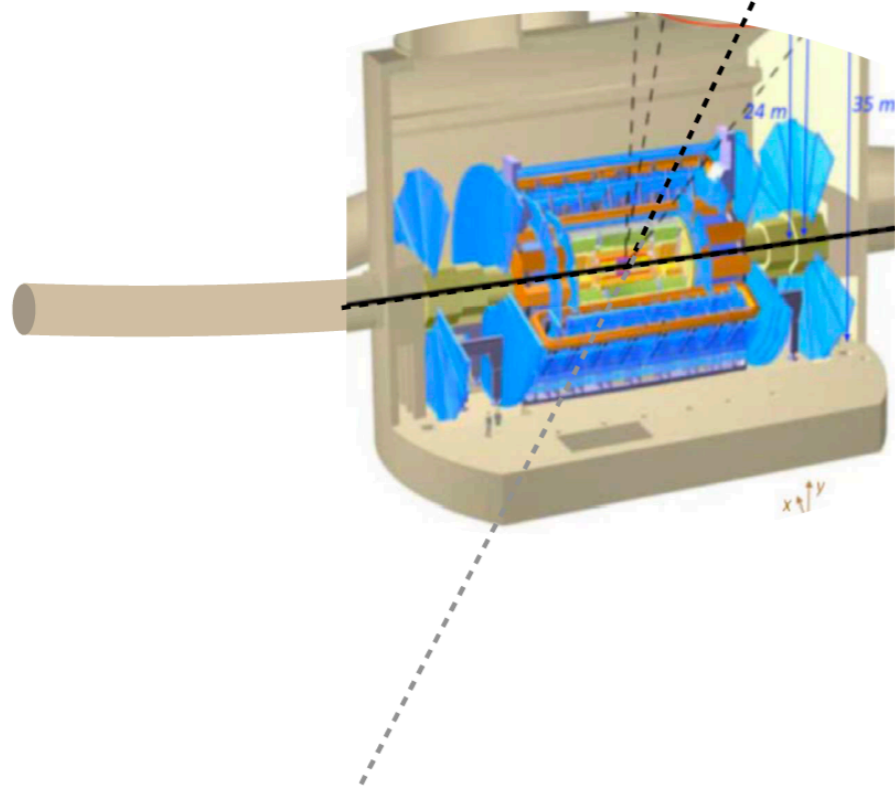
Images from [O. Brandt's talk at Oxford Particle Physics Seminar](#) on 9/6/2020

MATHUSLA: MAssive Timing Hodoscope for Ultra Stable neutral pArticles

Box of 100 m × 100 m × 25 m
 $\bar{d} \sim \mathcal{O}(100 \text{ m})$
 $4\pi/25$ coverage

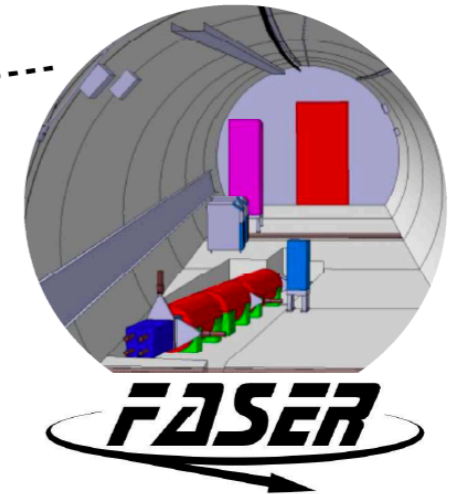


Chou et al 1606.06298



CODEX-b

Gligorov et al 1708.09395

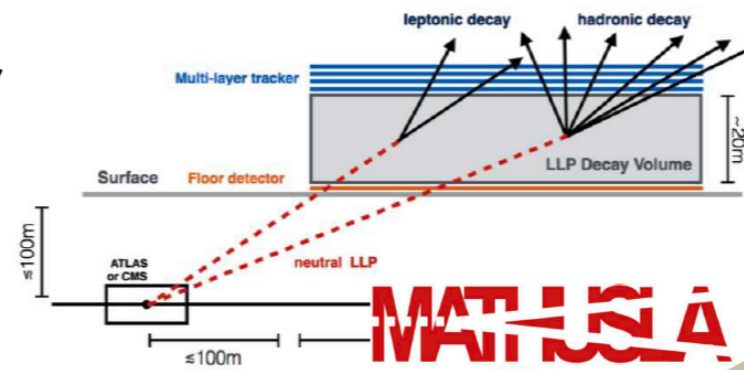
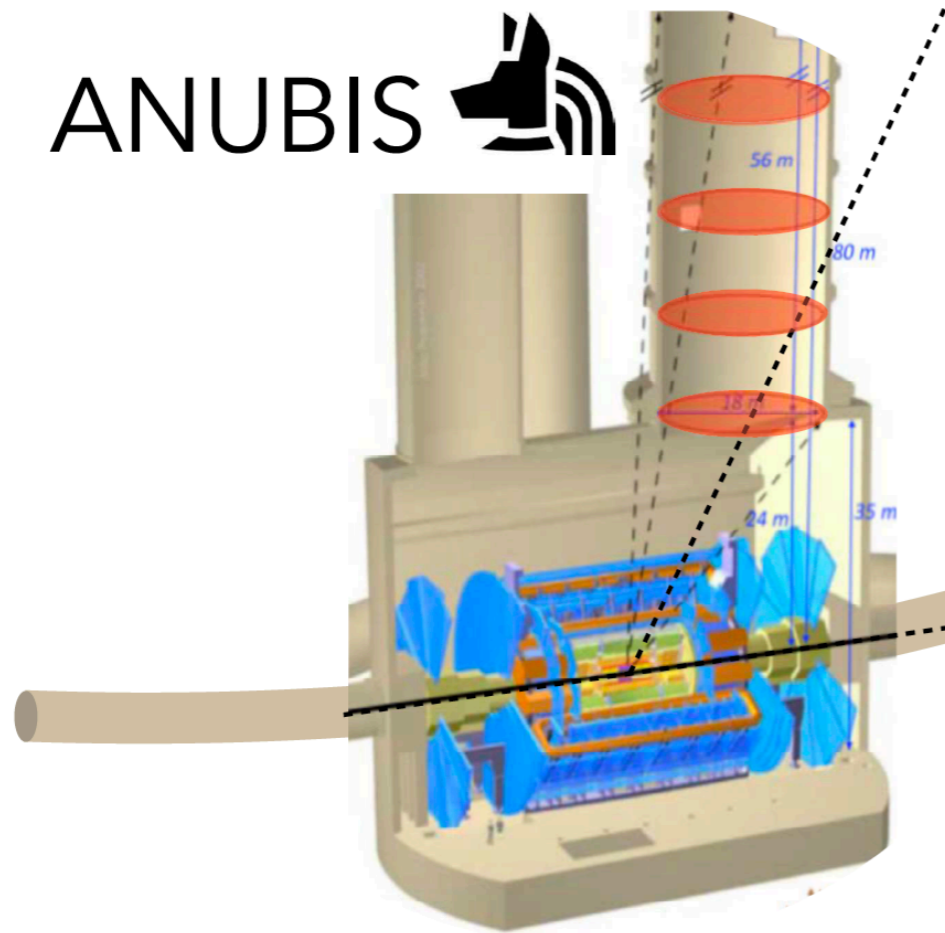


Feng, et al 1710.09387

Images from O. Brandt's talk at Oxford Particle Physics Seminar on 9/6/2020

ANUBIS: AN Underground Belayed In-Shaft search experiment

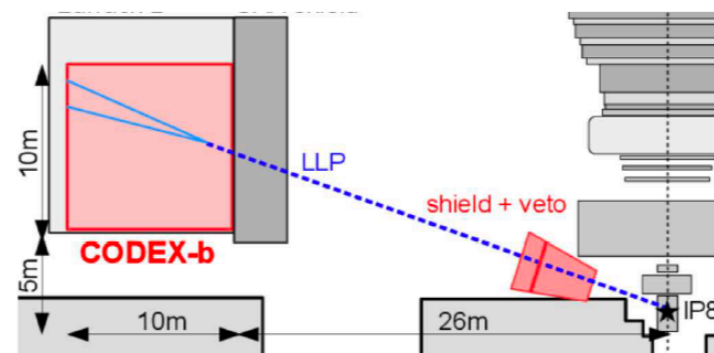
ANUBIS 



Chou et al 1606.06298

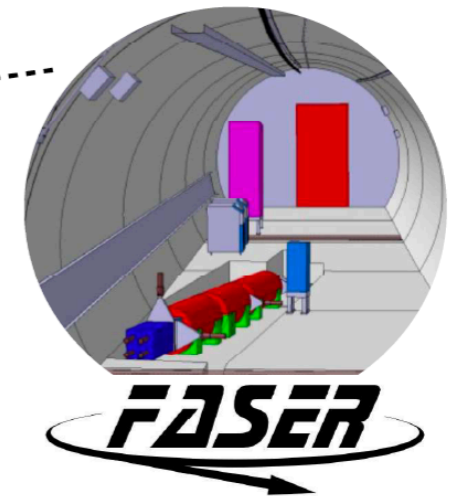
Cylinder with $r = 9$ m and $h = 56$ m
 $\bar{d} \sim$ few 10 m
 $4\pi/50$ coverage

Bauer, OB, Lee, Ohm 1909.13022



CODEX-b

Gligorov et al 1708.09395

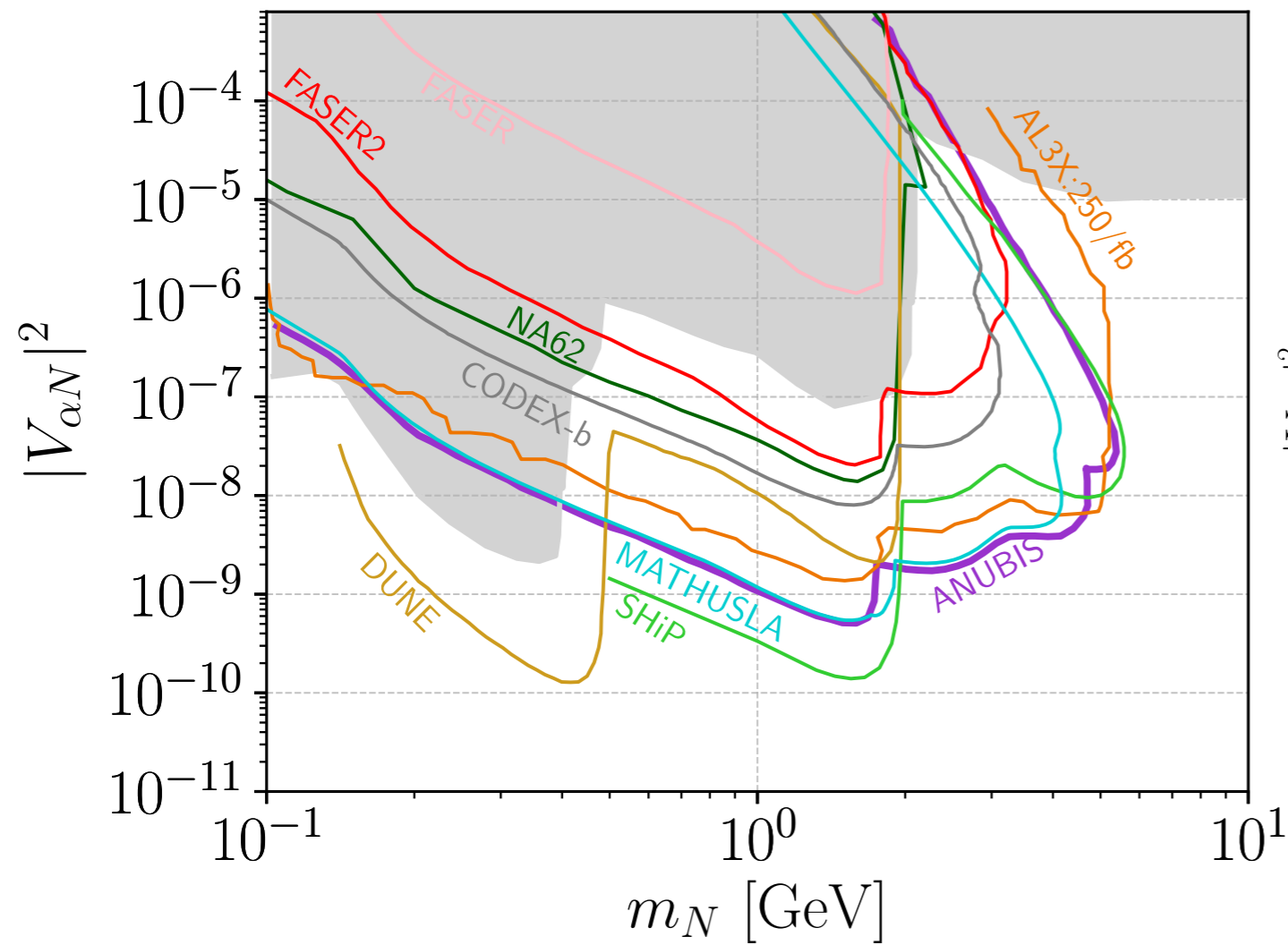


Feng, et al 1710.09387

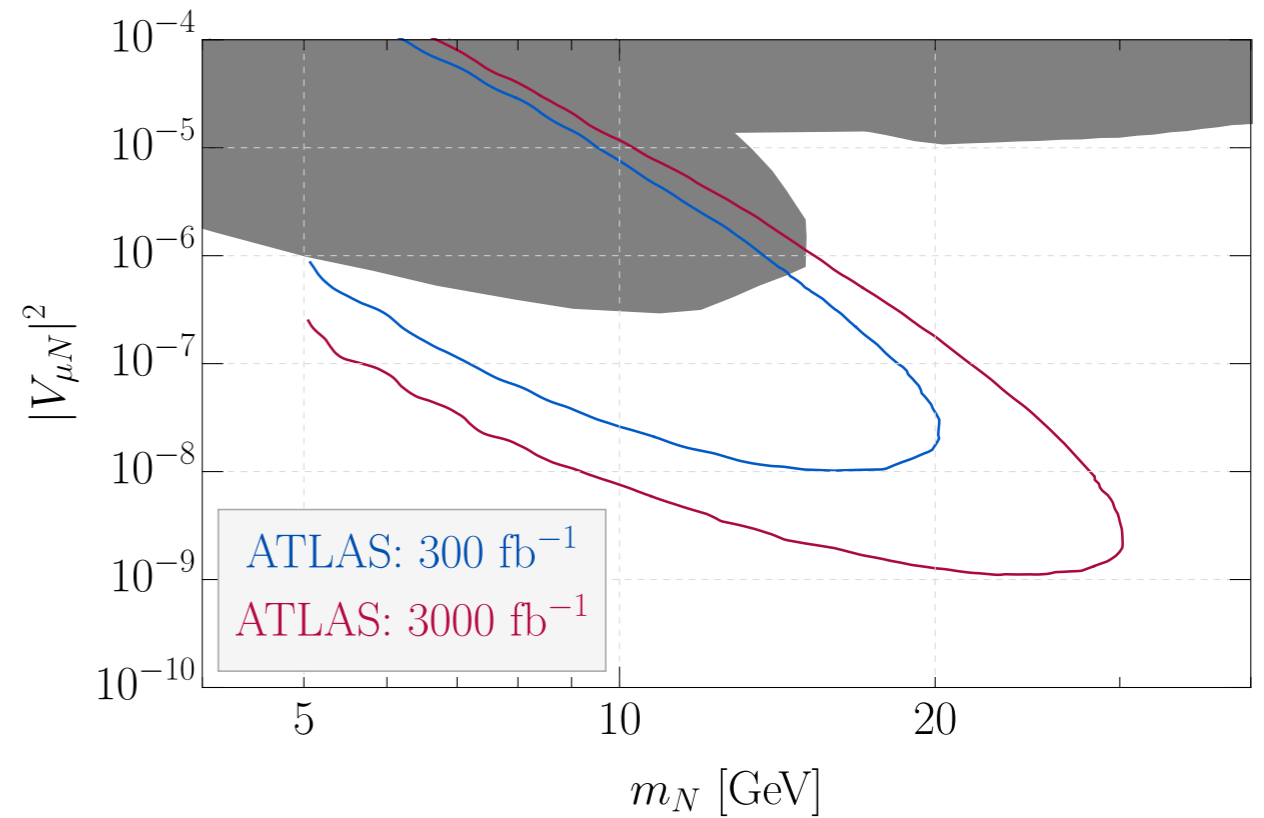
Images from O. Brandt's talk at Oxford Particle Physics Seminar on 9/6/2020

Minimal mixing scenario at HL-LHC

Hirsch and Wang, 1801.08947



Beltrán, Cottin, Helo, Hirsch, AT, Wang, 2110.15096
(update of Cottin, Helo, Hirsch, 1806.05191)



4-fermion pair-N operators

Name	Structure	$n_N = 1$	$n_N = 3$
\mathcal{O}_{dN}	$(\bar{d}_R \gamma^\mu d_R) (\bar{N}_R \gamma_\mu N_R)$	9	81
\mathcal{O}_{uN}	$(\bar{u}_R \gamma^\mu u_R) (\bar{N}_R \gamma_\mu N_R)$	9	81
\mathcal{O}_{QN}	$(\bar{Q} \gamma^\mu Q) (\bar{N}_R \gamma_\mu N_R)$	9	81
\mathcal{O}_{eN}	$(\bar{e}_R \gamma^\mu e_R) (\bar{N}_R \gamma_\mu N_R)$	9	81
\mathcal{O}_{NN}	$(\bar{N}_R \gamma_\mu N_R) (\bar{N}_R \gamma_\mu N_R)$	1	36
\mathcal{O}_{LN}	$(\bar{L} \gamma^\mu L) (\bar{N}_R \gamma_\mu N_R)$	9	81

Examples of UV completions

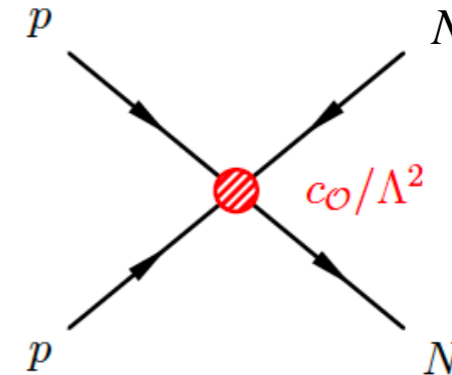
LQ state	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	Coupling	Operator
S_d	3	1	$-1/3$	g_{dN}	\mathcal{O}_{dN}
S_u	3	1	$2/3$	g_{uN}	\mathcal{O}_{uN}
S_Q	3	2	$1/6$	g_{qN}	\mathcal{O}_{qN}

$$\mathcal{L}_{S_d} = g_{dN} \bar{d}_R N_R^c S_d + g_{ue} \bar{u}_R e_R^c S_d + g_{QL} \bar{Q} \epsilon L^c S_d + \text{h.c.}$$

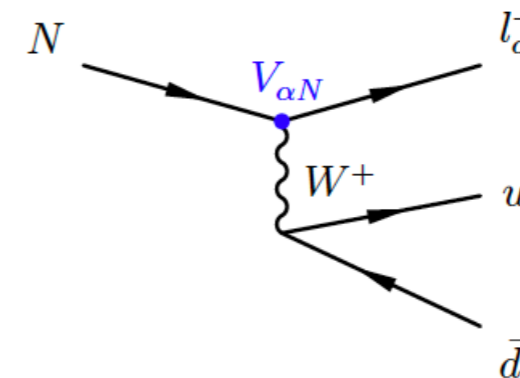
$$\mathcal{L}_{S_u} = g_{uN} \bar{u}_R N_R^c S_u + \text{h.c.}$$

$$\mathcal{L}_{S_Q} = g_{qN} \bar{Q} N_R S_Q + g_{dL} \bar{d}_R L \epsilon S_Q + \text{h.c.}$$

- HNLs are pair produced via pair- N_R operators



- Lightest HNL cannot decay via these operators; it decays via mixing



$$\frac{c_{qN}}{\Lambda^2} = \frac{g_{qN}^2}{2m_{S_q}^2}, \quad q = d, u, Q$$

4-fermion pair-N operators

Name	Structure	$n_N = 1$	$n_N = 3$
\mathcal{O}_{dN}	$(\bar{d}_R \gamma^\mu d_R) (\bar{N}_R \gamma_\mu N_R)$	9	81
\mathcal{O}_{uN}	$(\bar{u}_R \gamma^\mu u_R) (\bar{N}_R \gamma_\mu N_R)$	9	81
\mathcal{O}_{QN}	$(\bar{Q} \gamma^\mu Q) (\bar{N}_R \gamma_\mu N_R)$	9	81
\mathcal{O}_{eN}	$(\bar{e}_R \gamma^\mu e_R) (\bar{N}_R \gamma_\mu N_R)$	9	81
\mathcal{O}_{NN}	$(\bar{N}_R \gamma_\mu N_R) (\bar{N}_R \gamma_\mu N_R)$	1	36
\mathcal{O}_{LN}	$(\bar{L} \gamma^\mu L) (\bar{N}_R \gamma_\mu N_R)$	9	81

Examples of UV completions

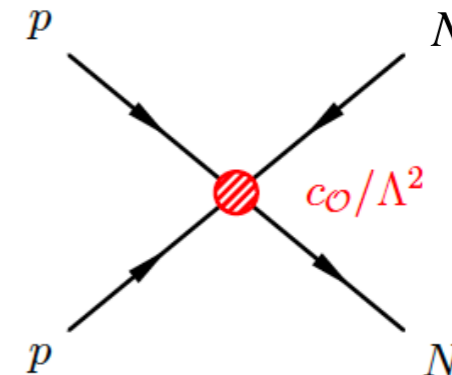
LQ state	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	Coupling	Operator
S_d	3	1	$-1/3$	g_{dN}	\mathcal{O}_{dN}
S_u	3	1	$2/3$	g_{uN}	\mathcal{O}_{uN}
S_Q	3	2	$1/6$	g_{QN}	\mathcal{O}_{QN}

$$\mathcal{L}_{S_d} = g_{dN} \bar{d}_R N_R^c S_d + g_{ue} \bar{u}_R e_R^c S_d + g_{QL} \bar{Q} \epsilon L^c S_d + \text{h.c.}$$

$$\mathcal{L}_{S_u} = g_{uN} \bar{u}_R N_R^c S_u + \text{h.c.}$$

$$\mathcal{L}_{S_Q} = g_{QN} \bar{Q} N_R S_Q + g_{dL} \bar{d}_R L \epsilon S_Q + \text{h.c.}$$

- HNLs are pair produced via pair- N_R operators

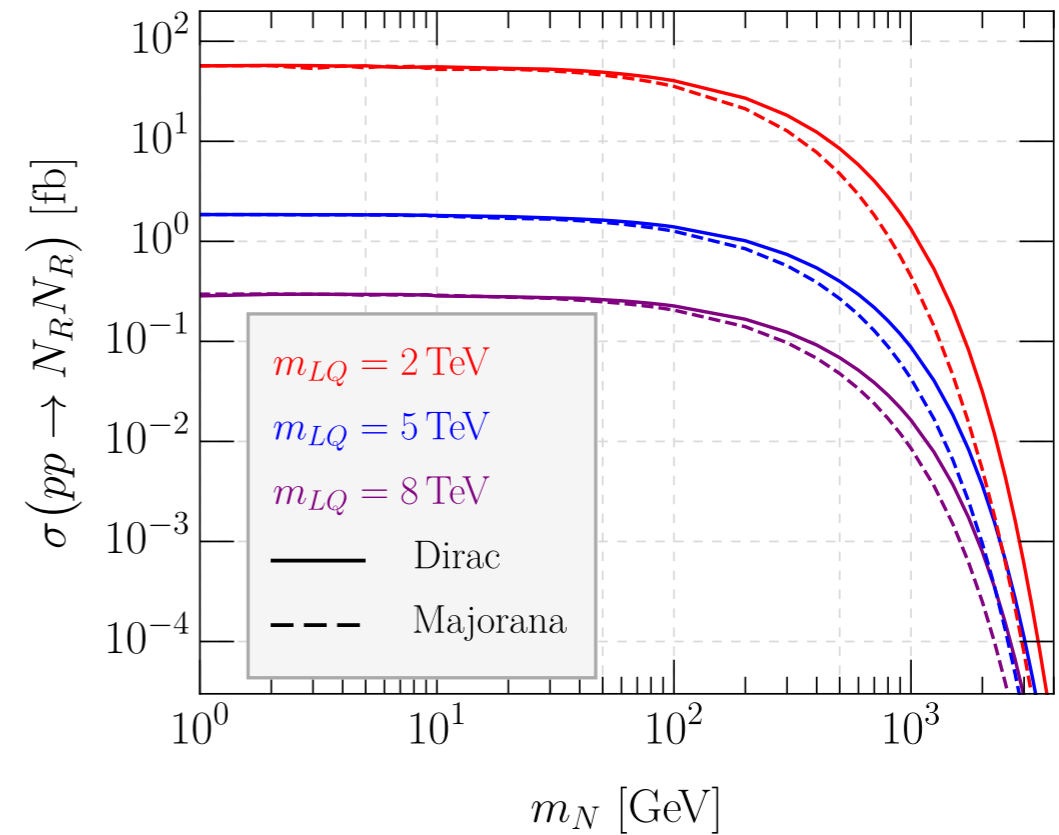
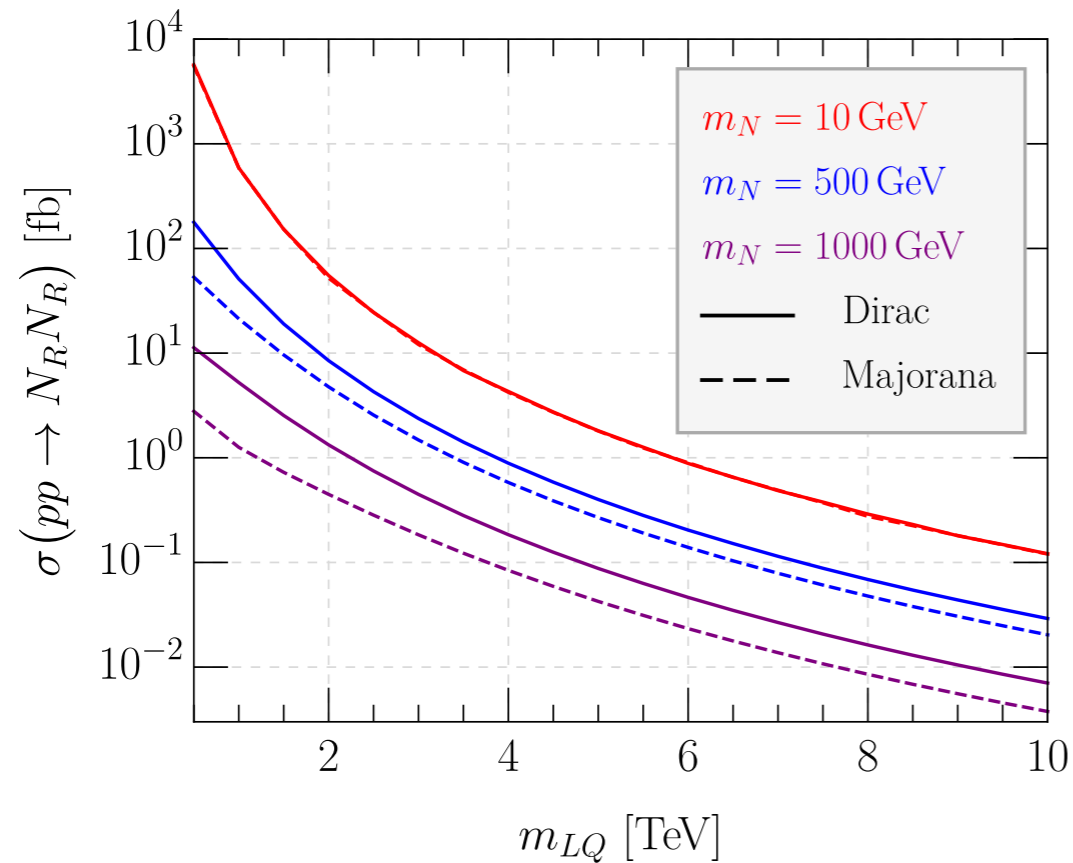


- Lightest HNL cannot decay via these operators; it decays via mixing

- MadGraph5 cannot handle Majorana fermions in operators with more than 2 fermions; renormalisable completions are needed to effectively implement such operators

4-fermion pair-N operators

Examples of HNL pair production cross section for \mathcal{O}_{dN} ($g_{dN} = \sqrt{2} \Leftrightarrow c_{dN}^{11} = 1$)



$$\sigma_D(d\bar{d} \rightarrow N\bar{N}) = \frac{c_{dN}^2}{192\pi\Lambda^4} s \sqrt{1 - \frac{4m_N^2}{s}} \left[1 + \frac{1}{3} \left(1 - \frac{4m_N^2}{s} \right) \right]$$

$$\sigma_M(d\bar{d} \rightarrow NN) = \frac{c_{dN}^2}{144\pi\Lambda^4} s \left(1 - \frac{4m_N^2}{s} \right)^{3/2} \Rightarrow \text{suppression for } m_N \gtrsim 100 \text{ GeV}$$

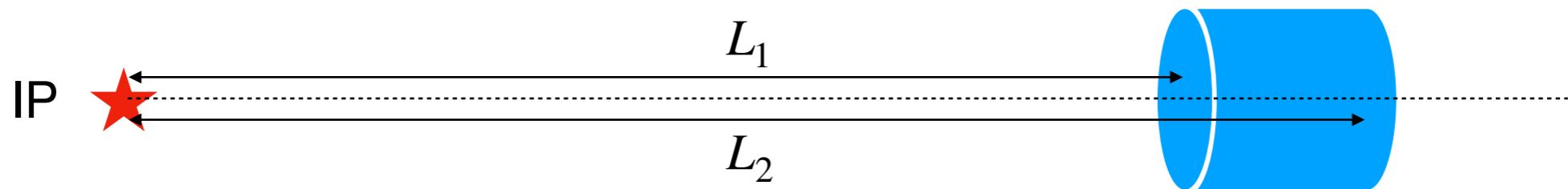
Number of events

Projected number of signal events at ATLAS:

$$N_S^{\text{ATLAS}} = \underbrace{\sigma(pp \rightarrow NN)}_{\text{MadGraph5}} \cdot \mathcal{L} \cdot \underbrace{\text{BR}(N \rightarrow \ell jj)}_{\text{MadSpin+Pythia8}} \cdot 2 \cdot \epsilon$$

Decay probability of an HNL in a far detector (approximately):

$$P[N \text{ decay}] = e^{-L_1/\beta\gamma c\tau} - e^{-L_2/\beta\gamma c\tau}$$

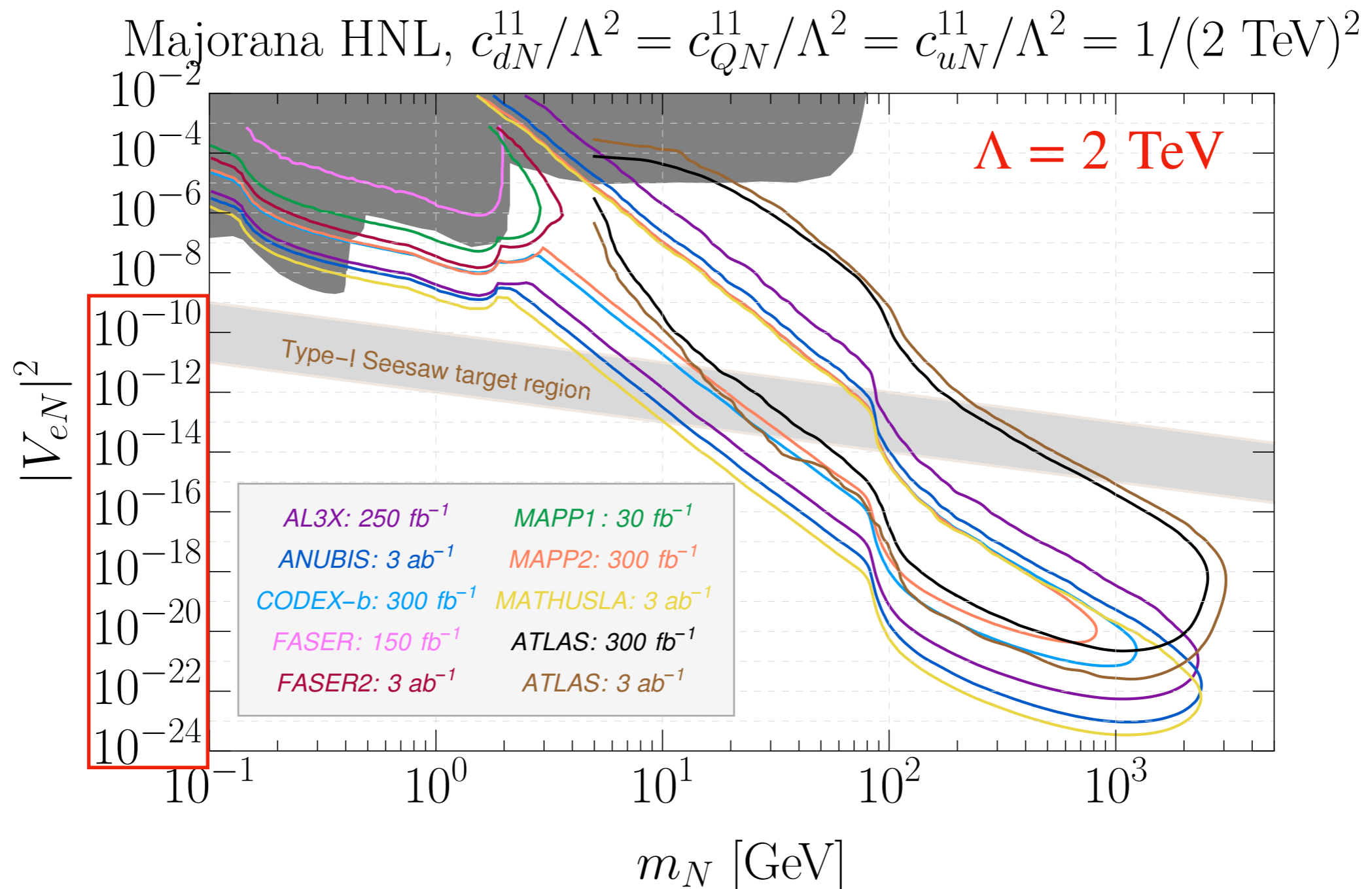


Projected number of signal events at a far detector:

$$N_S^{\text{FD}} = 2 \cdot \underbrace{\sigma(pp \rightarrow NN)}_{\text{MadGraph5}} \cdot \mathcal{L} \cdot \underbrace{\langle P[N \text{ decay in f.v.}] \rangle}_{\text{Pythia8}} \cdot \underbrace{\text{BR}(N \rightarrow \text{vis.})}_{\text{analytical}}$$

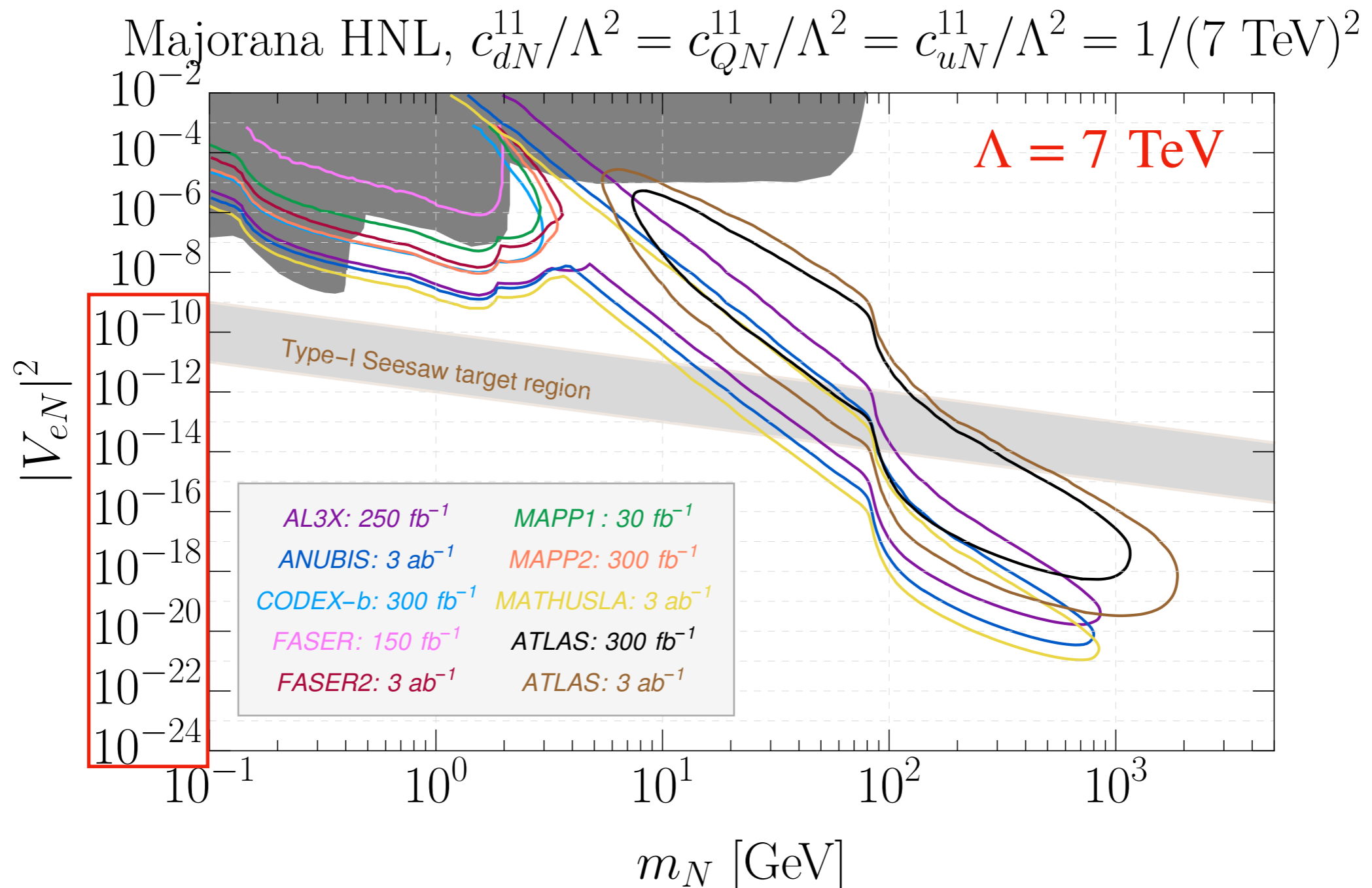
4-fermion pair-N operators at HL-LHC

Reach on active-heavy neutrino mixing (for fixed new physics scale)



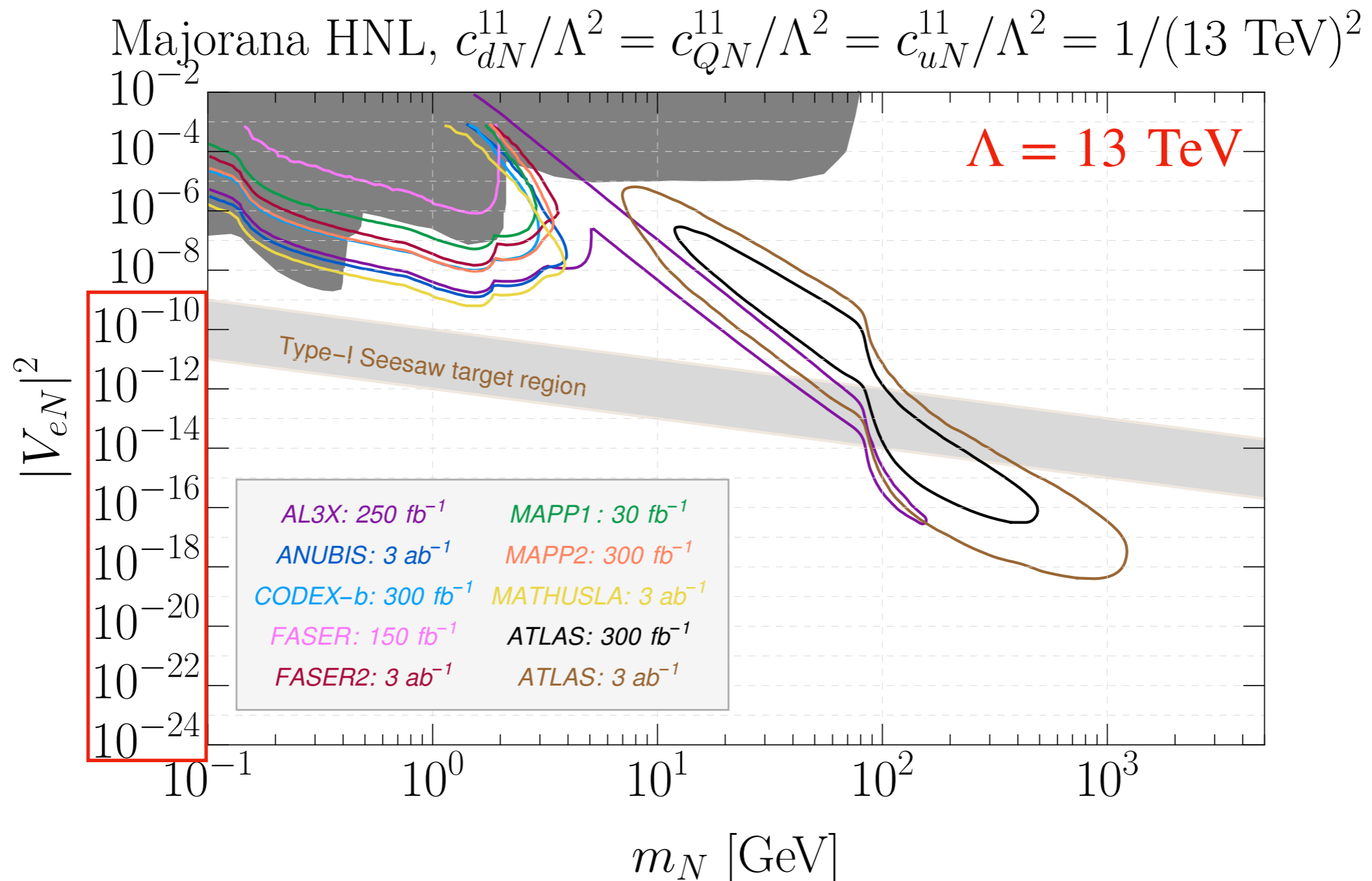
4-fermion pair-N operators at HL-LHC

Reach on active-heavy neutrino mixing (for fixed new physics scale)



4-fermion pair-N operators at HL-LHC

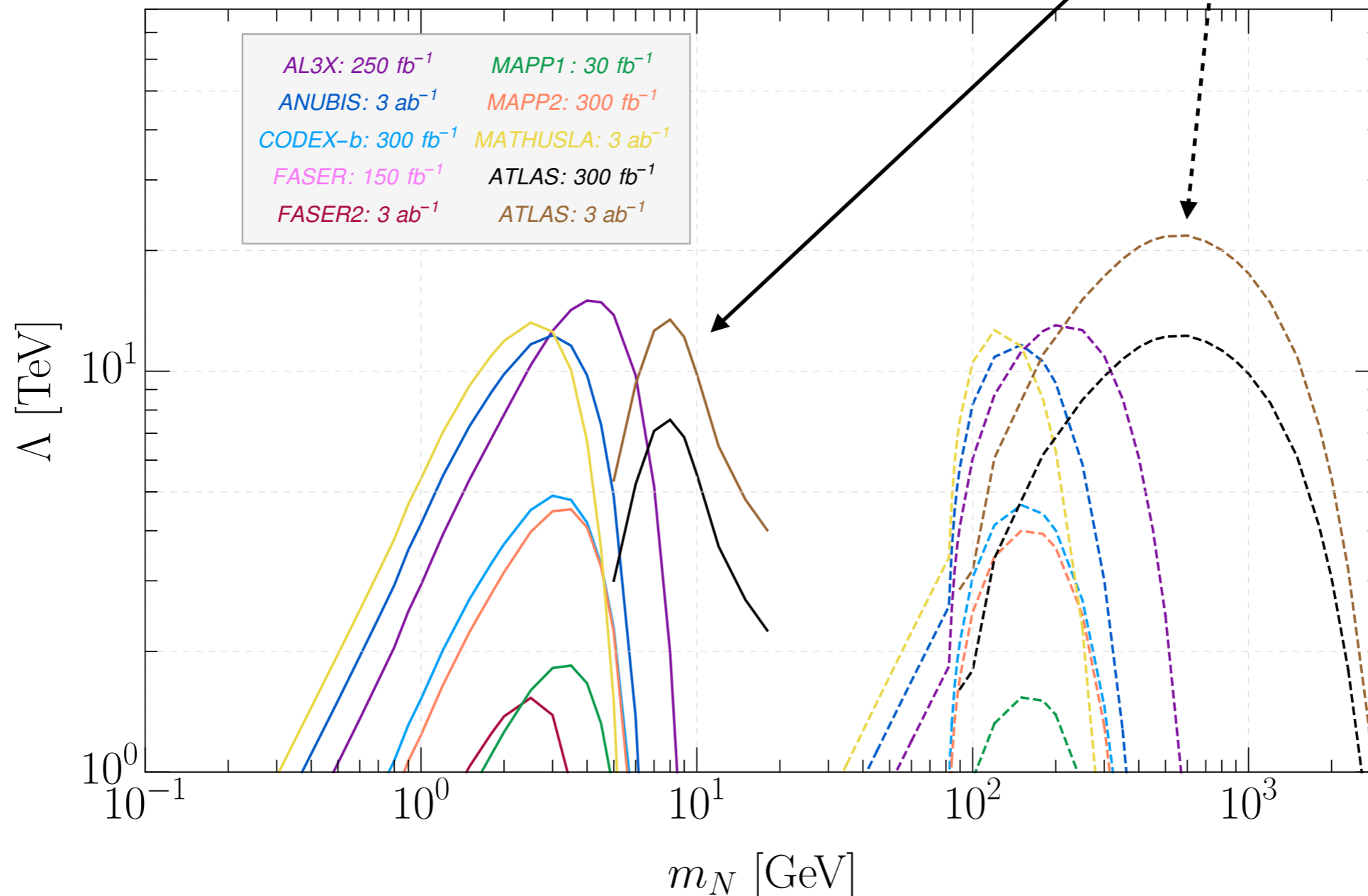
Reach on active-heavy neutrino mixing (for fixed new physics scale)



4-fermion pair-N operators at HL-LHC

Reach on new physics scale (for fixed active-heavy neutrino mixing)

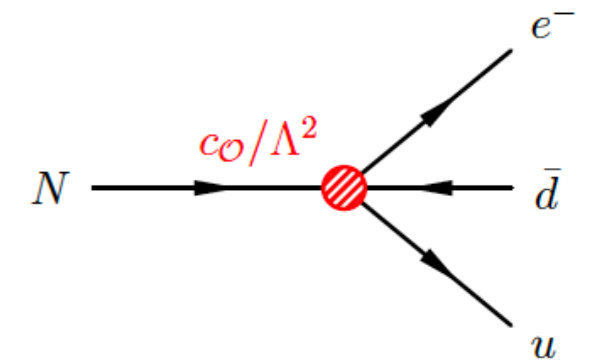
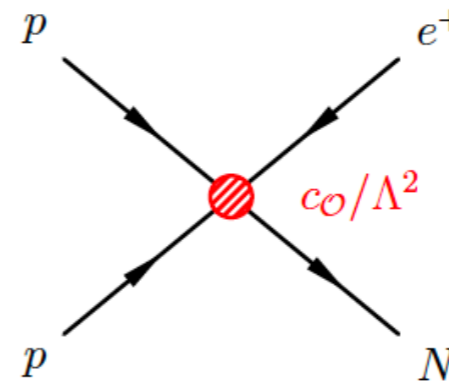
Dirac HNL, $c_{dN}^{11} = c_{QN}^{11} = c_{uN}^{11} = 1$, $|V_{eN}|^2 = 10^{-5}, 10^{-17}$



4-fermion single-N operators

Name	Structure (+ h.c.)	$n_N = 1$	$n_N = 3$
\mathcal{O}_{duNe}	$(\bar{d}_R \gamma^\mu u_R) (\bar{N}_R \gamma_\mu e_R)$	54	162
\mathcal{O}_{LNQd}	$(\bar{L} N_R) \epsilon (\bar{Q} d_R)$	54	162
\mathcal{O}_{LdQN}	$(\bar{L} d_R) \epsilon (\bar{Q} N_R)$	54	162
\mathcal{O}_{QuNL}	$(\bar{Q} u_R) (\bar{N}_R L)$	54	162
\mathcal{O}_{LNLe}	$(\bar{L} N_R) \epsilon (\bar{L} e_R)$	54	162

- Both HNL production and decay can be dominated by the operator



Examples of UV completions

Heavy scalar	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	Operator	Matching relation
Leptoquark S_d	3	1	-1/3	\mathcal{O}_{duNe}	$\frac{c_{duNe}}{\Lambda^2} = \frac{g_{dN} g_{ue}}{2m_{S_d}^2}$
Leptoquark S_Q	3	2	1/6	\mathcal{O}_{LdQN}	$\frac{c_{LdQN}}{\Lambda^2} = \frac{g_{dL} g_{QN}}{m_{S_Q}^2}$
Inert doublet Φ	1	2	1/2	\mathcal{O}_{LNQd}	$\frac{c_{LNQd}}{\Lambda^2} = \frac{g_{LN} g_{Qd}}{m_\Phi^2}$
				\mathcal{O}_{QuNL}	$\frac{c_{QuNL}}{\Lambda^2} = \frac{g_{Qu} g_{LN}}{m_\Phi^2}$

$$\mathcal{L}_\Phi = g_{Qd} \bar{Q} \Phi d_R + g_{Qu} \bar{Q} \tilde{\Phi} u_R + g_{LN} \bar{L} \tilde{\Phi} N_R + \text{h.c.}$$

4-fermion single-N operators

Example of HNL single production cross sections

$$\sqrt{s} = 14 \text{ TeV}, \quad \Lambda = 5 \text{ TeV}, \quad |V_{eN}|^2 = 10^{-5}$$

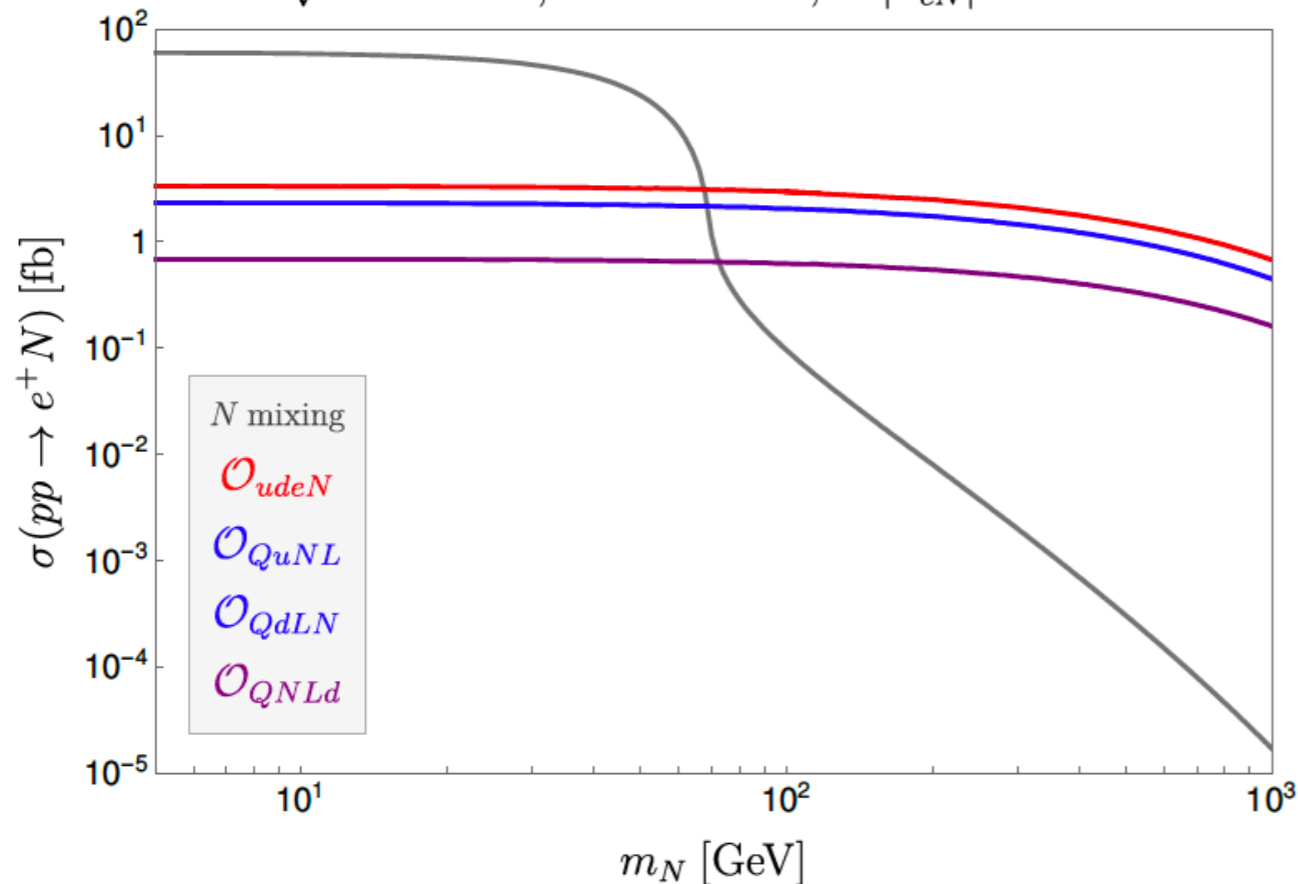


Figure from R. Beltrán's master thesis

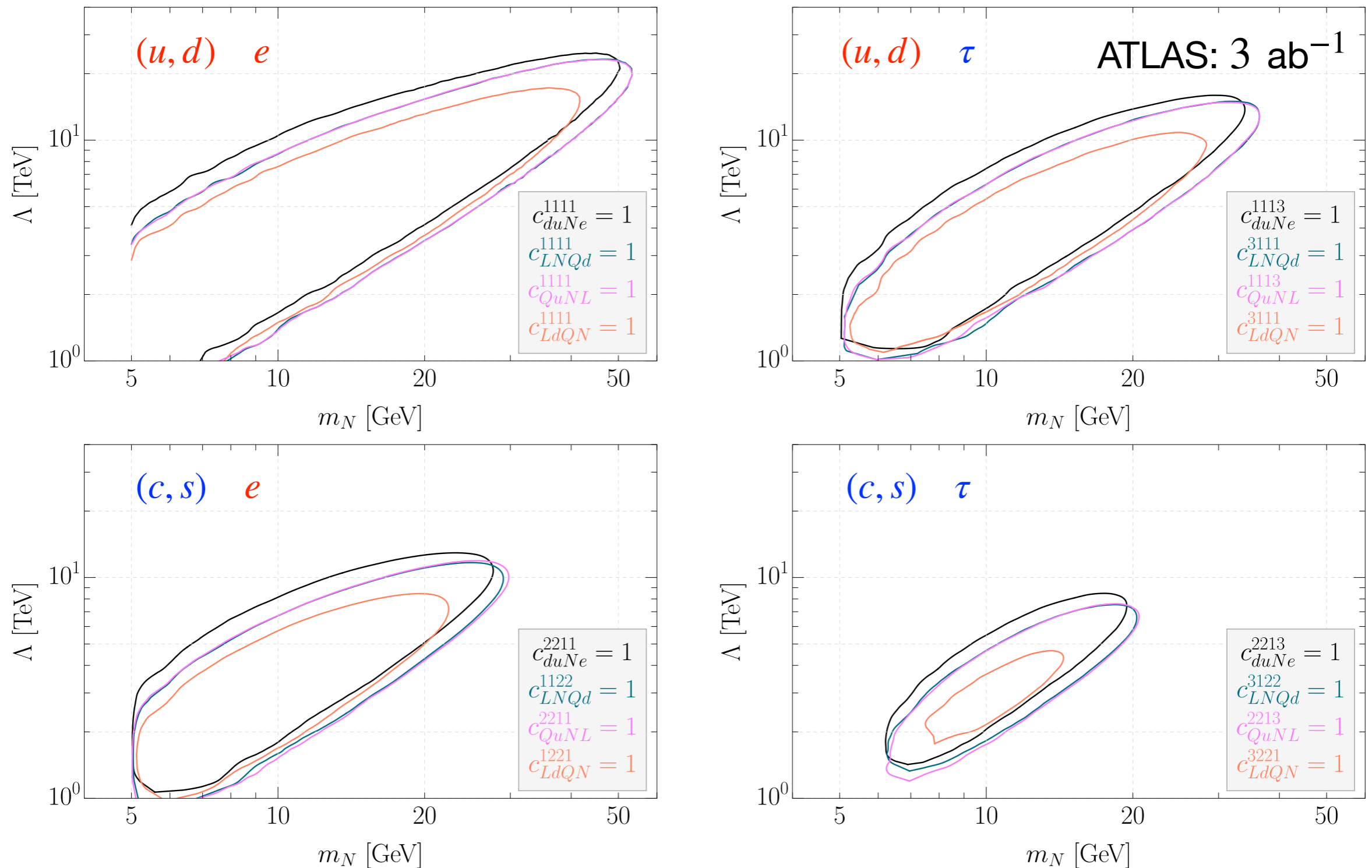
$$\sigma^{\text{mix}} \propto |V_{eN}|^2$$

$$\sigma^{\mathcal{O}} \propto \Lambda^{-4}$$

Partial decay width of HNL

$$\Gamma(N \rightarrow \ell qq') = \frac{c_{\mathcal{O}}^2 m_N^5}{f_{\mathcal{O}} 512 \pi^3 \Lambda^4}, \quad f_{\mathcal{O}} = 1 \quad (4) \quad \text{for} \quad \mathcal{O}_{duNe} \quad (3 \text{ remaining operators})$$

4-fermion single-N operators at HL-LHC



Assumption: both HNL production and decay are dominated by the operator
 (fulfilled everywhere in the plots if $|V_{\alpha N}|^2 \lesssim 10^{-9}$)

Beltrán, Cottin, Helo, Hirsch, AT, Wang, 2110.15096

NLEFT: low-energy EFT with N

For low-energy processes at energies $E \ll v$ and GeV-scale HNLs, the appropriate EFT is the low-energy EFT extended with N_R (NLEFT), which does not contain t , H , Z , W^\pm

$$\mathcal{L}_{\text{NLEFT}} = \mathcal{L}_{\text{ren}} + \sum_{d \geq 5} \sum_i c_i^{(d)} \mathcal{O}_i^{(d)}$$

$$\mathcal{L}_{\text{ren}} = \mathcal{L}_{\text{QCD+QED}} + i \bar{N}_R \not{\partial} N_R - \left[\frac{1}{2} \bar{\nu}_L M_\nu \nu_L^c + \frac{1}{2} \bar{N}_R^c M_N N_R + \bar{\nu}_L M_D N_R + \text{h.c.} \right]$$

$\mathcal{O}_i^{(d)}$ are effective operators invariant under $\text{SU}(3)_C \times \text{U}(1)_{\text{em}}$

$d \leq 6$ operators with SM fields: [Jenkins, Manohar, Stoffer, 1709.04486](#)

$d \leq 6$ operators with N_R : [Chala, AT, 2001.07732](#); [Li, Ma, Schmidt, 2005.01543](#)

$d \leq 9$ operators with N_R : [Li et al., 2105.09329](#)

Neutral current quark- N 4-fermion operators

NLEFT pair- N_R operators					NLEFT single- N_R operators						
		Name	Structure	$n_N = 1$	$n_N = 3$			Name	Structure	$n_N = 1$	$n_N = 3$
LNC	$\mathcal{O}_{dN}^{V,RR}$	$(\bar{d}_R \gamma_\mu d_R)$	$(\bar{N}_R \gamma^\mu N_R)$	9	81	LNC	$\mathcal{O}_{d\nu N}^{S,RR}$	$(\bar{d}_L d_R)$	$(\bar{\nu}_L N_R)$	54	162
	$\mathcal{O}_{uN}^{V,RR}$	$(\bar{u}_R \gamma_\mu u_R)$	$(\bar{N}_R \gamma^\mu N_R)$	4	36		$\mathcal{O}_{d\nu N}^{T,RR}$	$(\bar{d}_L \sigma_{\mu\nu} d_R)$	$(\bar{\nu}_L \sigma^{\mu\nu} N_R)$	54	162
	$\mathcal{O}_{dN}^{V,LR}$	$(\bar{d}_L \gamma_\mu d_L)$	$(\bar{N}_R \gamma^\mu N_R)$	9	81		$\mathcal{O}_{wN}^{S,RR}$	$(\bar{u}_L u_R)$	$(\bar{\nu}_L N_R)$	24	72
	$\mathcal{O}_{uN}^{V,LR}$	$(\bar{u}_L \gamma_\mu u_L)$	$(\bar{N}_R \gamma^\mu N_R)$	4	36		$\mathcal{O}_{wN}^{T,RR}$	$(\bar{u}_L \sigma_{\mu\nu} u_R)$	$(\bar{\nu}_L \sigma^{\mu\nu} N_R)$	24	72
LNV	$\mathcal{O}_{dN}^{S,RR}$	$(\bar{d}_L d_R)$	$(\bar{N}_R^c N_R)$	18	108	$\mathcal{O}_{d\nu N}^{S,LR}$	$(\bar{d}_R d_L)$	$(\bar{\nu}_L N_R)$	54	162	
	$\mathcal{O}_{dN}^{T,RR}$	$(\bar{d}_L \sigma_{\mu\nu} d_R)$	$(\bar{N}_R^c \sigma^{\mu\nu} N_R)$	0	54	$\mathcal{O}_{wN}^{S,LR}$	$(\bar{u}_R u_L)$	$(\bar{\nu}_L N_R)$	24	72	
	$\mathcal{O}_{uN}^{S,RR}$	$(\bar{u}_L u_R)$	$(\bar{N}_R^c N_R)$	8	48	LNV	$\mathcal{O}_{d\nu N}^{V,RR}$	$(\bar{d}_R \gamma_\mu d_R)$	$(\bar{\nu}_L^c \gamma^\mu N_R)$	54	162
	$\mathcal{O}_{uN}^{T,RR}$	$(\bar{u}_L \sigma_{\mu\nu} u_R)$	$(\bar{N}_R^c \sigma^{\mu\nu} N_R)$	0	24		$\mathcal{O}_{wN}^{V,RR}$	$(\bar{u}_R \gamma_\mu u_R)$	$(\bar{\nu}_L^c \gamma^\mu N_R)$	24	72
	$\mathcal{O}_{dN}^{S,LR}$	$(\bar{d}_R d_L)$	$(\bar{N}_R^c N_R)$	18	108		$\mathcal{O}_{d\nu N}^{V,LR}$	$(\bar{d}_L \gamma_\mu d_L)$	$(\bar{\nu}_L^c \gamma^\mu N_R)$	54	162
	$\mathcal{O}_{uN}^{S,LR}$	$(\bar{u}_R u_L)$	$(\bar{N}_R^c N_R)$	8	48		$\mathcal{O}_{wN}^{V,LR}$	$(\bar{u}_L \gamma_\mu u_L)$	$(\bar{\nu}_L^c \gamma^\mu N_R)$	24	72

In the NLEFT, $n_d = 3$ and $n_u = 2$ (no top quark)

Charged current quark- N_R operators have been studied in [De Vries et al., 2010.07305](#)

Matching to NSMEFT: pair- N_R operators

NSMEFT pair- N_R operators				
	Name	Structure	$n_N = 1$	$n_N = 3$
$d = 6$ (LNC)	\mathcal{O}_{dN}	$(\bar{d}_R \gamma_\mu d_R) (\bar{N}_R \gamma^\mu N_R)$	9	81
	\mathcal{O}_{uN}	$(\bar{u}_R \gamma_\mu u_R) (\bar{N}_R \gamma^\mu N_R)$	9	81
	\mathcal{O}_{QN}	$(\bar{Q} \gamma_\mu Q) (\bar{N}_R \gamma^\mu N_R)$	9	81
	\mathcal{O}_{HN}	$(H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{N}_R \gamma^\mu N_R)$	1	9
$d = 7$ (LNV)	\mathcal{O}_{QNdH}	$(\bar{Q} N_R) (\bar{N}_R^c d_R) H$	18	162
	\mathcal{O}_{dQNH}	$H^\dagger (\bar{d}_R Q) (\bar{N}_R^c N_R)$	18	108
	\mathcal{O}_{QNuH}	$(\bar{Q} N_R) (\bar{N}_R^c u_R) \tilde{H}$	18	162
	\mathcal{O}_{uQNH}	$\tilde{H}^\dagger (\bar{u}_R Q) (\bar{N}_R^c N_R)$	18	108

$d = 6$ LNC in NLEFT $\Leftrightarrow d = 6$ in NSMEFT

$$c_{dN,ij}^{V,RR} = C_{dN}^{ij} - \frac{g_Z^2}{m_Z^2} Z_{d_R}^{ij} Z_N$$

$$c_{uN,ij}^{V,RR} = C_{uN}^{ij} - \frac{g_Z^2}{m_Z^2} Z_{u_R}^{ij} Z_N$$

$$c_{dN,ij}^{V,LR} = V_{ki}^* V_{lj} C_{QN}^{kl} - \frac{g_Z^2}{m_Z^2} Z_{d_L}^{ij} Z_N$$

$$c_{uN,ij}^{V,LR} = C_{QN}^{ij} - \frac{g_Z^2}{m_Z^2} Z_{u_L}^{ij} Z_N$$

$d = 6$ LNV in NLEFT $\Leftrightarrow d = 7$ in NSMEFT

$$c_{dN,ij}^{S,RR} = -\frac{v}{2\sqrt{2}} V_{ki}^* C_{QNdH}^{kj} \quad c_{uN,ij}^{S,RR} = -\frac{v}{2\sqrt{2}} C_{QNuH}^{ij}$$

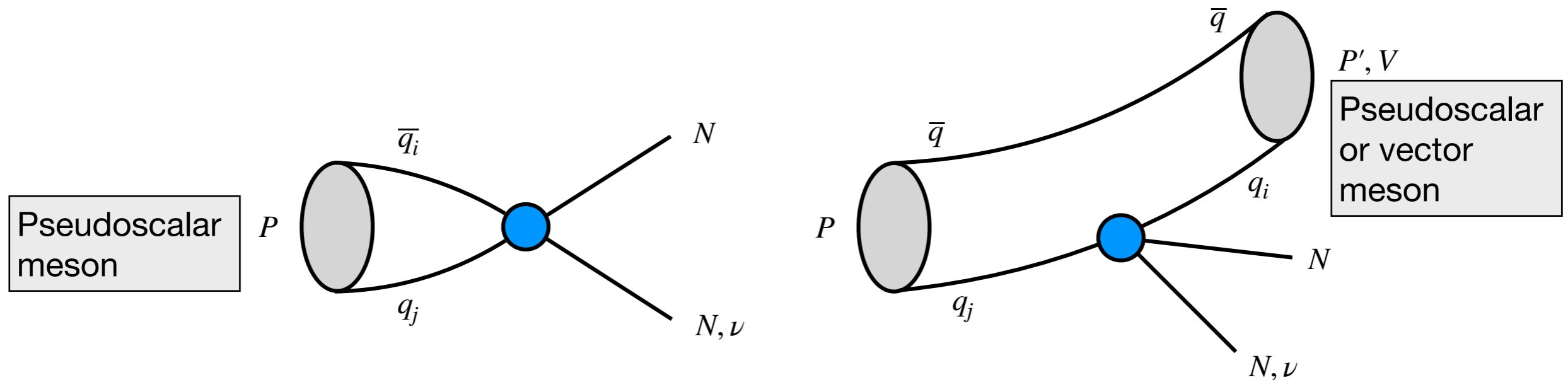
$$c_{dN,ij}^{S,LR} = \frac{v}{\sqrt{2}} V_{kj} C_{dQNH}^{ik} \quad c_{uN,ij}^{S,LR} = \frac{v}{\sqrt{2}} C_{uQNH}^{ij}$$

$$g_Z \equiv \frac{e}{s_W c_W}$$

$$Z_\psi^{ij} \equiv \left(T_\psi^3 - Q_\psi s_W^2 \right) \delta^{ij}$$

$$Z_N \equiv -\frac{v^2}{2} C_{HN}$$

HNL production in meson decays



• $c \rightarrow u$ $D^0 \rightarrow NN (\nu N)$

$D^0 \rightarrow \pi^0, \eta, \eta' (\rho^0, \omega)$ for $q = u$

$D^+ \rightarrow \pi^+ (\rho^+)$ for $q = d$

$D_s^+ \rightarrow K^+ (K^{*+})$ for $q = s$

$\eta_c \rightarrow \bar{D}^0 (\bar{D}^{*0})$ for $q = c$

$B_c^+ \rightarrow B^+ (B^{*+})$ for $q = b$

• $b \rightarrow d$ $B^0 \rightarrow NN (\nu N)$

...

• $b \rightarrow s$ $B_s^0 \rightarrow NN (\nu N)$

...

• $s \rightarrow d$ $K_{S/L} \rightarrow NN (\nu N)$

...

HNLs from D - and B -meson decays: [Beltrán, Cottin, Helo, Hirsch, AT, Wang, 2210.02461](#)

HNLs from K -meson decays: [Beltrán, Günther, Hirsch, AT, Wang, 2309.11546](#)

Partial meson decay widths

Two-body decay:

$$\Gamma(P \rightarrow NN) = \frac{m_P}{32\pi} \sqrt{1 - \frac{4m_N^2}{m_P^2}} \left[2 |f_P|^2 \left| c_{qN,ij}^{V,RR} - c_{qN,ij}^{V,LR} \right|^2 m_N^2 \right. \\ \left. + |f_P^S|^2 \left\{ \left(\left| c_{qN,ij}^{S,RR} - c_{qN,ij}^{S,LR} \right|^2 + \left| c_{qN,ji}^{S,RR} - c_{qN,ji}^{S,LR} \right|^2 \right) \left(1 - \frac{2m_N^2}{m_P^2} \right) \right. \right. \\ \left. \left. + 2 \left[\left(c_{qN,ij}^{S,RR} - c_{qN,ij}^{S,LR} \right) \left(c_{qN,ji}^{S,RR} - c_{qN,ji}^{S,LR} \right) + \text{h.c.} \right] \frac{m_N^2}{m_P^2} \right\} \right. \\ \left. + f_P f_P^S \left\{ \left(c_{qN,ij}^{V,RR} - c_{qN,ij}^{V,LR} \right) \left(c_{qN,ij}^{S,RR*} - c_{qN,ij}^{S,LR*} + c_{qN,ji}^{S,RR} - c_{qN,ji}^{S,LR} \right) m_N + \text{h.c.} \right\} \right]$$

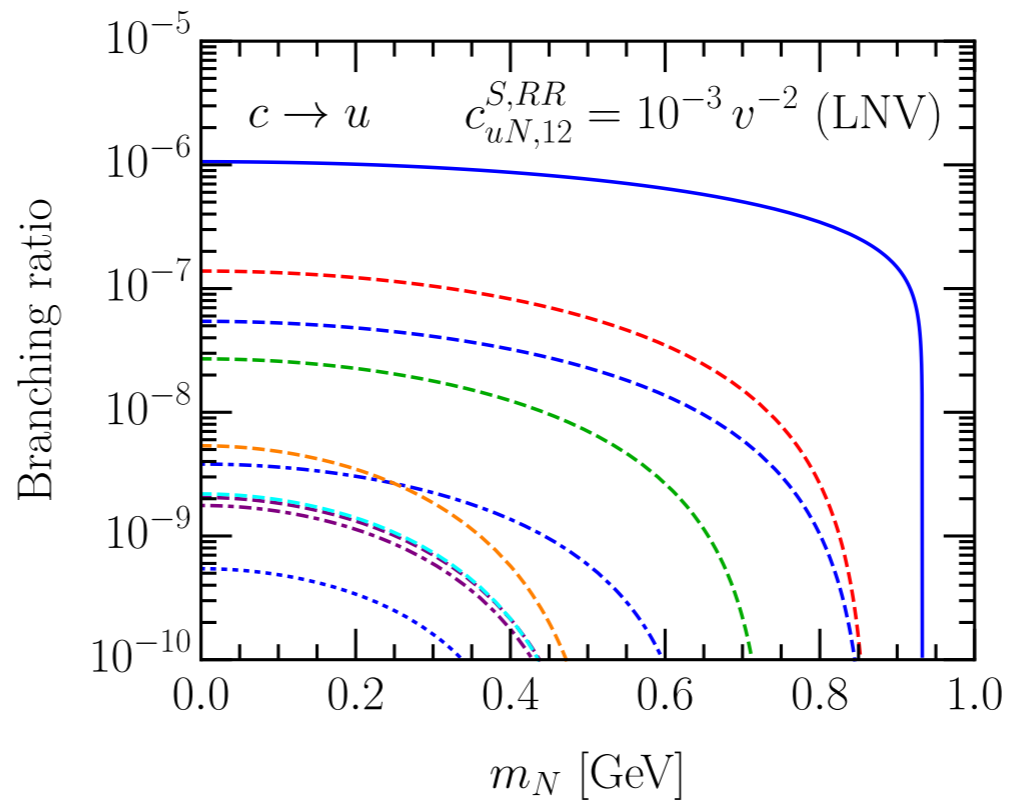
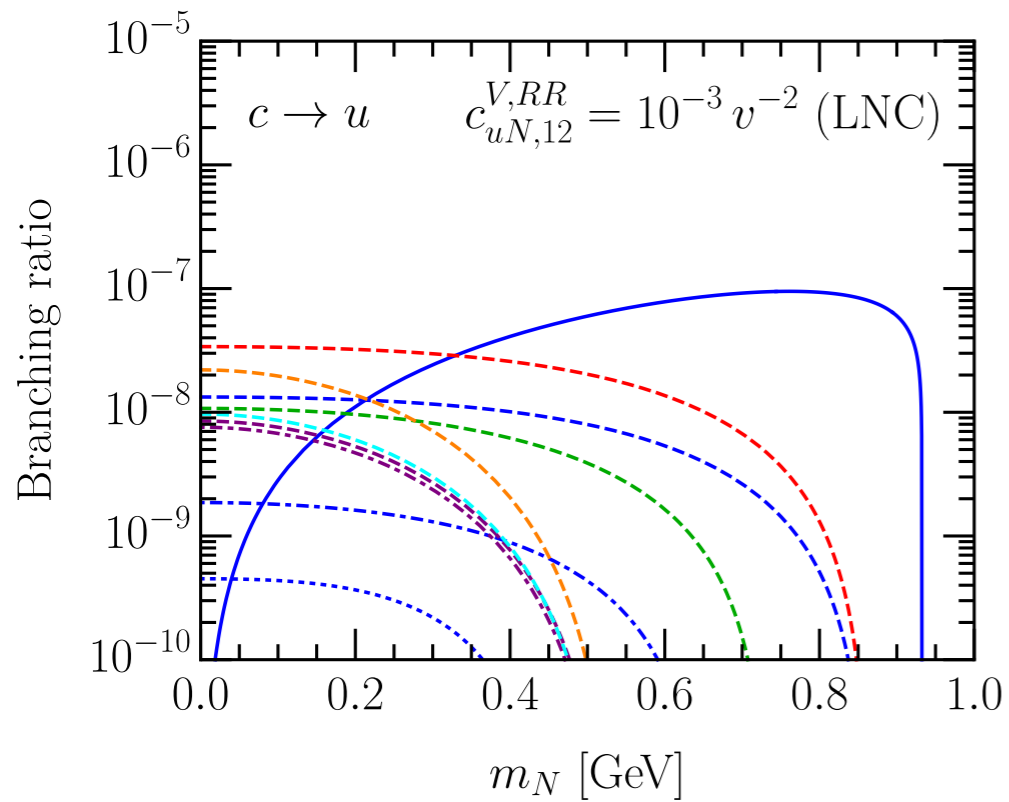
$$\langle 0 | \bar{q}_i \gamma^\mu \gamma_5 q_j | P(p) \rangle = if_P p^\mu \quad \langle 0 | \bar{q}_i \gamma_5 q_j | P(p) \rangle = i \frac{m_P^2}{m_{q_i} + m_{q_j}} f_P \equiv if_P^S$$

Three-body decays require the knowledge of transition form factors:

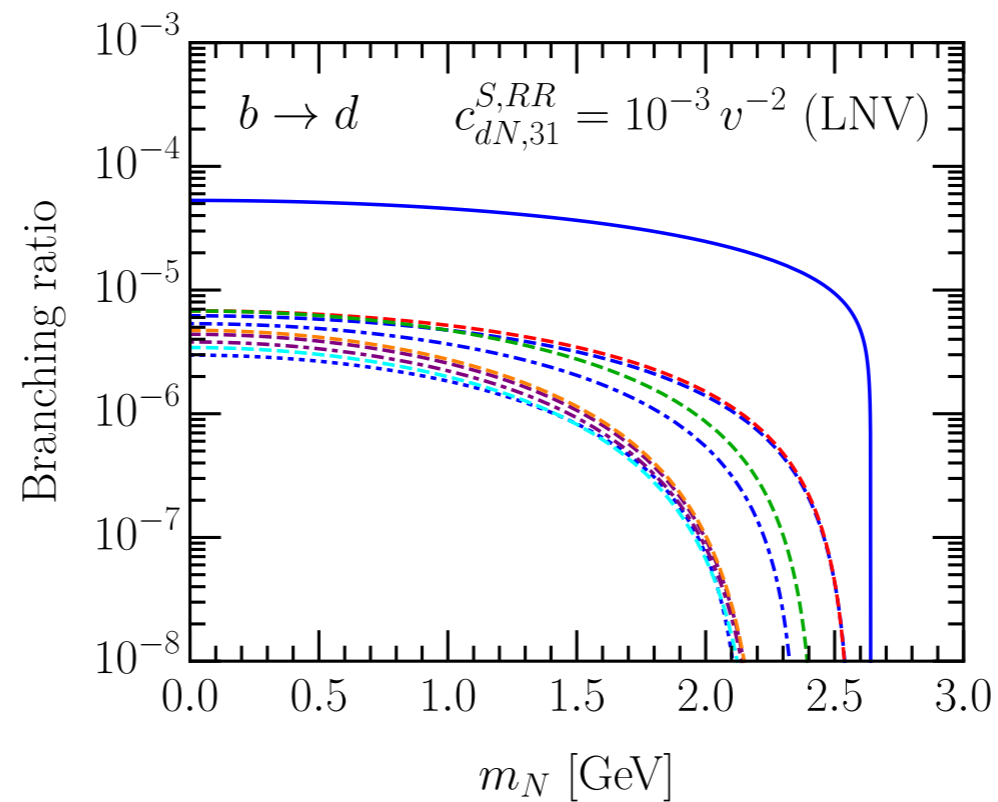
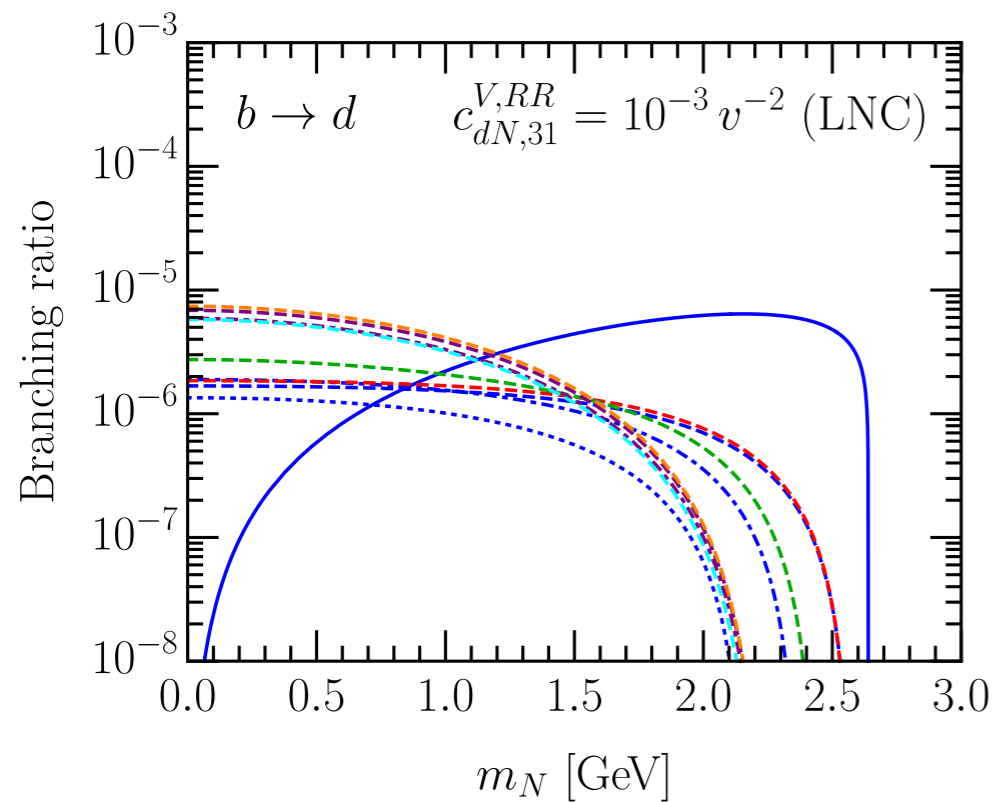
$$\langle P'(p') | \mathcal{F} | P(p) \rangle \quad \text{and} \quad \langle V(p', \epsilon) | \mathcal{F} | P(p) \rangle$$

$$\mathcal{F} \in \{ \bar{q}_i \gamma^\mu q_j, \bar{q}_i \gamma^\mu \gamma_5 q_j, \bar{q}_i q_j, \bar{q}_i \gamma_5 q_j, \bar{q}_i \sigma^{\mu\nu} q_j \}$$

Branching ratios of D and B meson decays



- $D^0 \rightarrow N + N$
- - - $D^0 \rightarrow \pi^0 + N + N$
- · - · $D^0 \rightarrow \eta + N + N$
- · · $D^0 \rightarrow \eta' + N + N$
- - - $D^+ \rightarrow \pi^+ + N + N$
- - - $D_s^+ \rightarrow K^+ + N + N$
- - - $D^0 \rightarrow \rho^0 + N + N$
- - - $D^0 \rightarrow \omega + N + N$
- - - $D^+ \rightarrow \rho^+ + N + N$
- · - · $D_s^+ \rightarrow K^{*+} + N + N$



- $B^0 \rightarrow N + N$
- - - $B^0 \rightarrow \pi^0 + N + N$
- · - · $B^0 \rightarrow \eta + N + N$
- · · $B^0 \rightarrow \eta' + N + N$
- - - $B^+ \rightarrow \pi^+ + N + N$
- - - $B_s^0 \rightarrow \bar{K}^0 + N + N$
- - - $B^0 \rightarrow \rho^0 + N + N$
- - - $B^0 \rightarrow \omega + N + N$
- - - $B^+ \rightarrow \rho^+ + N + N$
- · - · $B_s^0 \rightarrow \bar{K}^{*0} + N + N$

Number of events

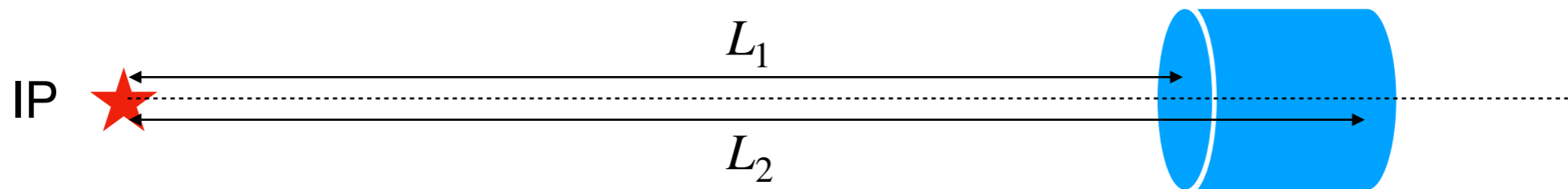
Projected number of signal events:

$$N_S = \sum_i 2 \cdot N_{M_i} \cdot \text{BR}(M_i \rightarrow NN + \text{anything}) \cdot \langle P[N \text{ decay}] \rangle \cdot \text{BR}(N \rightarrow \text{vis.})$$

analytical
Pythia8
analytical

Decay probability of an HNL in a far detector (approximately):

$$P[N \text{ decay}] = e^{-L_1/\beta\gamma c\tau} - e^{-L_2/\beta\gamma c\tau}$$

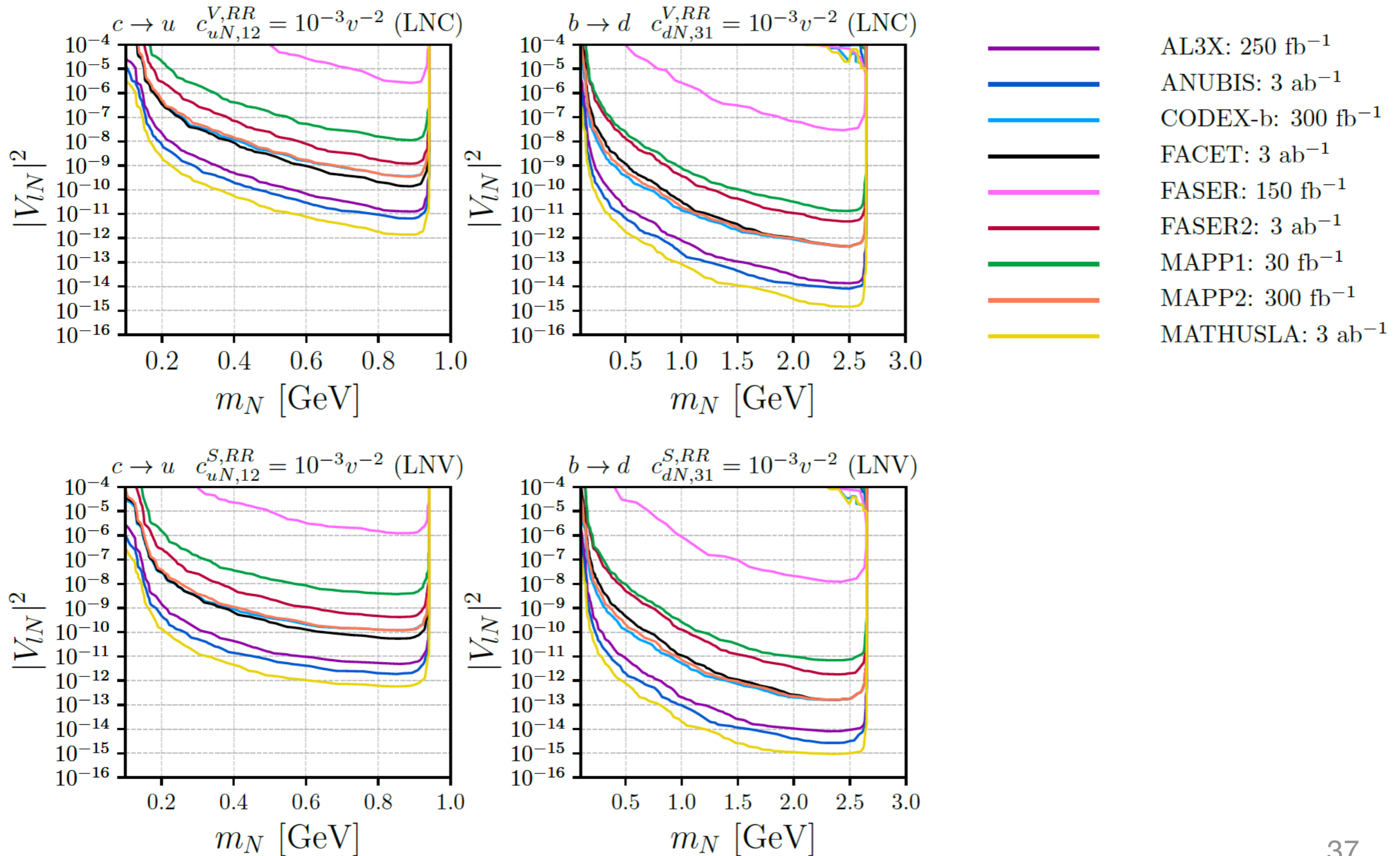


Inclusive production numbers of D and B mesons at the HL-LHC with $\sqrt{s} = 14$ TeV and $\mathcal{L} = 3 \text{ ab}^{-1}$:

D^0	D^\pm	D_s^\pm	B^0	B^\pm	B_s^0
4.12×10^{16}	2.16×10^{16}	7.02×10^{15}	1.58×10^{15}	1.58×10^{15}	2.73×10^{14}

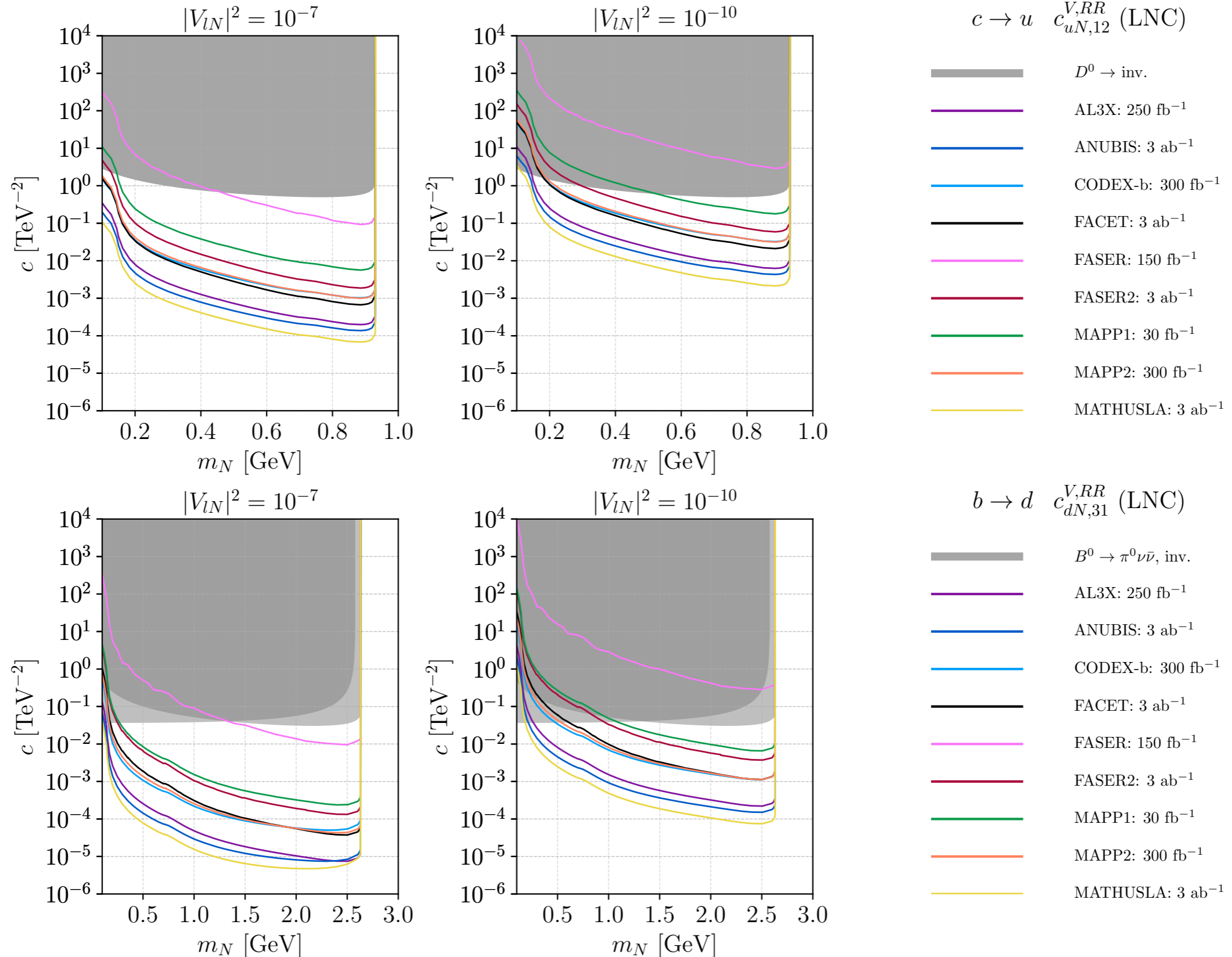
4-fermion NLEFT operators at HL-LHC

Reach on active-heavy neutrino mixing (for fixed Wilson coefficient)



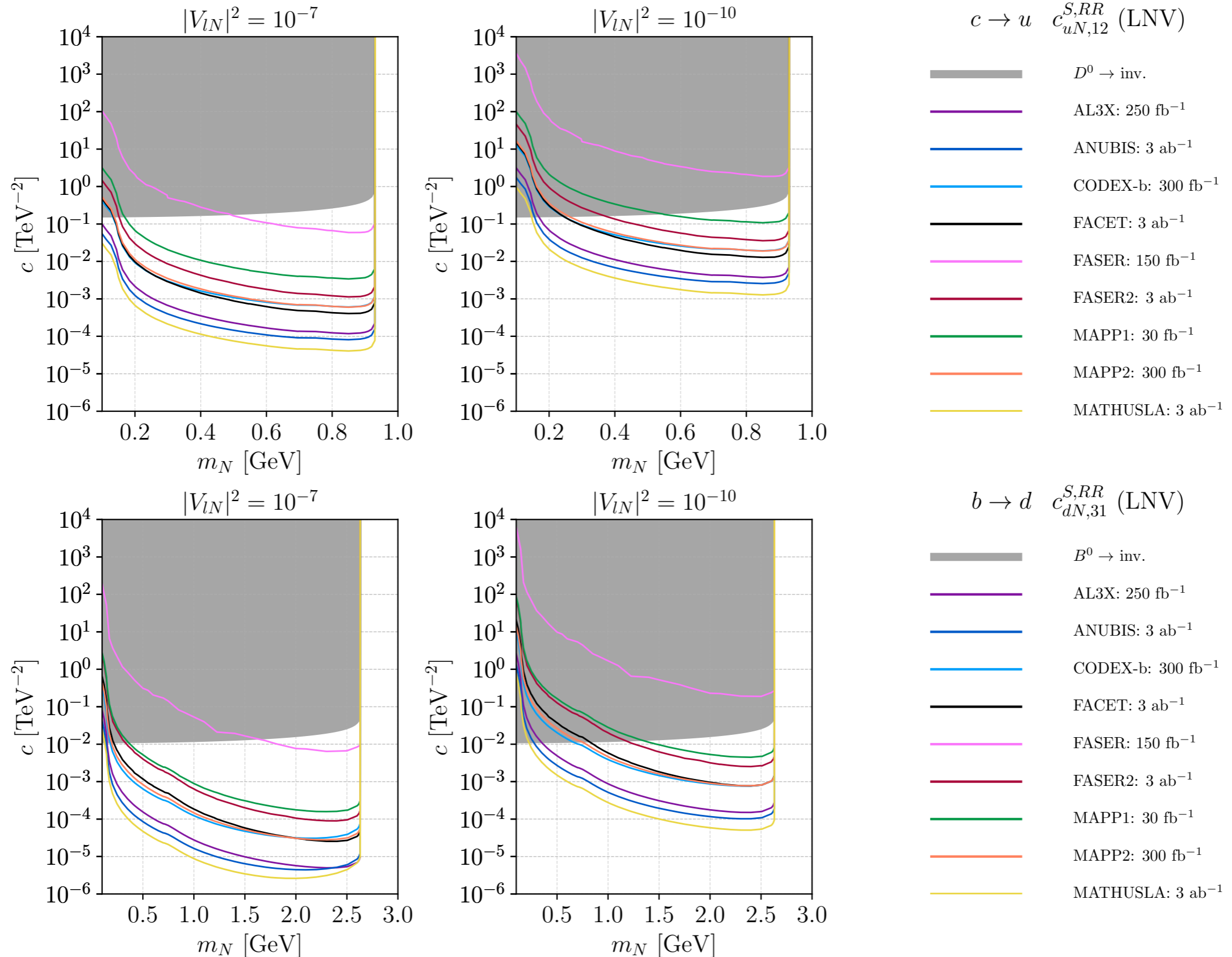
4-fermion NLEFT operators at HL-LHC

Reach on Wilson coefficients (for fixed active-heavy neutrino mixing)



4-fermion NLEFT operators at HL-LHC

Reach on Wilson coefficients (for fixed active-heavy neutrino mixing)



New physics scales

LNC operators:

$$c_{\text{NLEFT}}^{(6)} \sim C_{\text{NSMEFT}}^{(6)} \sim \frac{1}{\Lambda^2} \Rightarrow \Lambda \sim \left[\frac{1}{c_{\text{NLEFT}}^{(6)}} \right]^{1/2}$$

$$c_{\text{NLEFT}}^{(6)} \lesssim 10^{-4} \quad (10^{-5}) \Rightarrow \Lambda \gtrsim 100 \quad (316) \text{ TeV}$$

LNV operators:

$$c_{\text{NLEFT}}^{(6)} \sim \frac{v}{2\sqrt{2}} C_{\text{NSMEFT}}^{(7)} \sim \frac{1}{2\sqrt{2}} \frac{v}{\Lambda^3} \Rightarrow \Lambda \sim \left[\frac{1}{2\sqrt{2}} \frac{v}{c_{\text{NLEFT}}^{(6)}} \right]^{1/3}$$

$$c_{\text{NLEFT}}^{(6)} \lesssim 10^{-4} \quad (10^{-5}) \Rightarrow \Lambda \gtrsim 10 \quad (21) \text{ TeV}$$

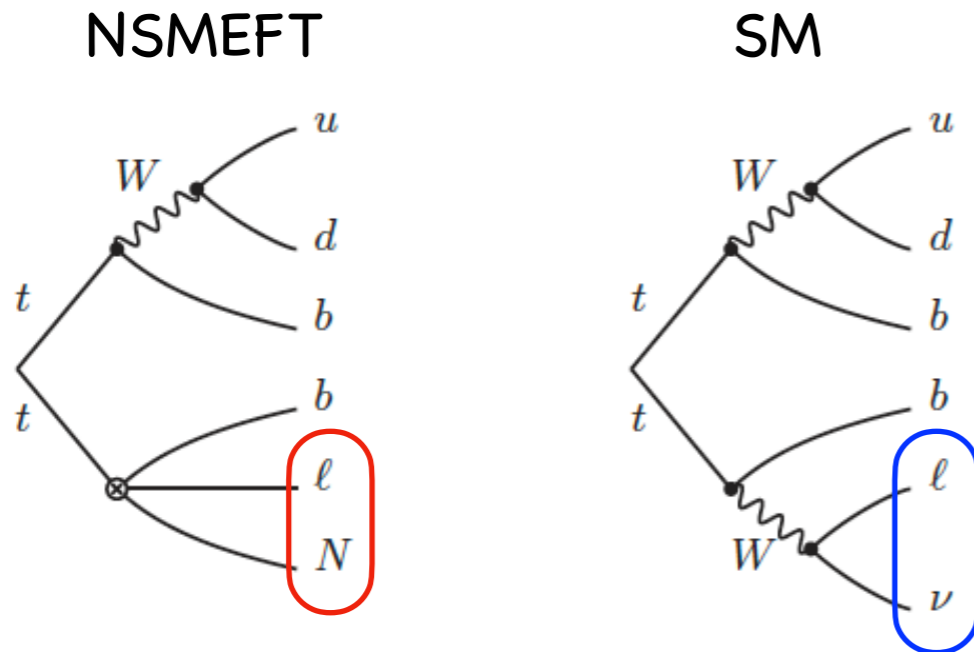
Conclusions

- ▶ Neutrino masses may be pointing towards the existence of **HNLs**
- ▶ HNLs may have masses below the EW scale and new heavy physics may exist at scales $\Lambda \gg v$, hence **NSMEFT (NLEFT)**
- ▶ HNLs may be **long-lived** (in a broad mass range)
- ▶ In addition to active-heavy mixing, they can be produced through **new effective interactions** directly in **partonic collisions** or in **meson decays**
- ▶ Rich programme for **LLP searches at HL-LHC**:
 - ATLAS, CMS
 - AL3X, ANUBIS, CODEX-b, FACET, FASER, MATHUSLA, MoEDAL-MAPP
- ▶ New physics scales up to
 - **20 TeV** for LNC operators could be probed through **direct HNL production**
 - **300 (20) TeV** for LNC (LNV) operators via **meson decays**

Backup slides

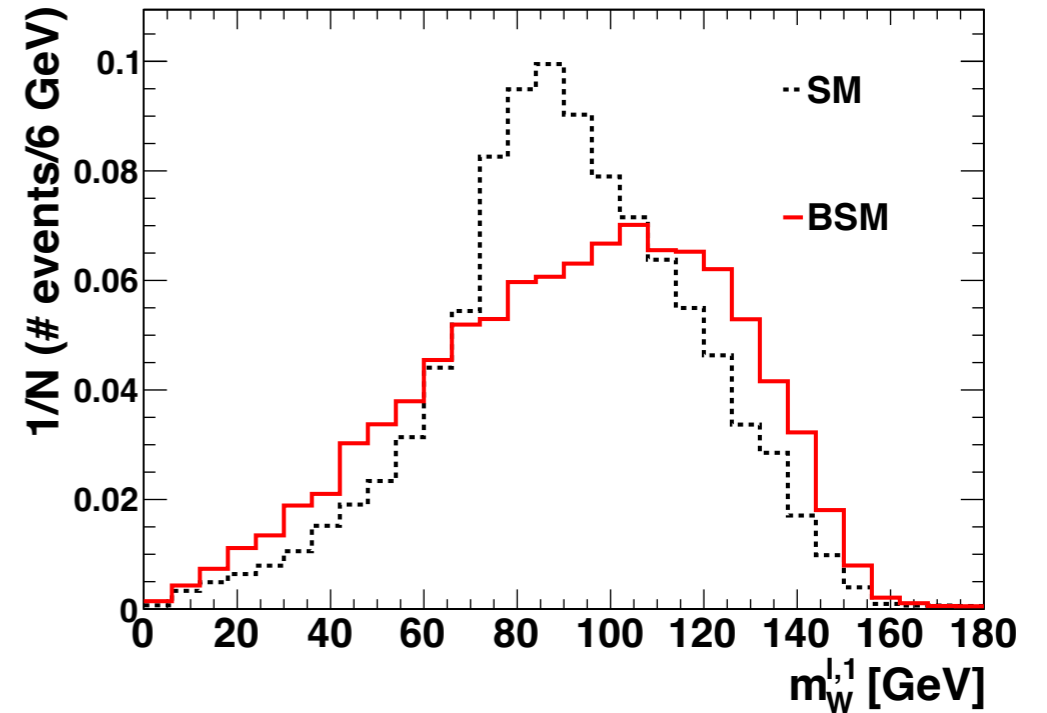
Novel LHC analysis for $t \rightarrow b\ell + \text{inv}$

Alcaide, Banerjee, Chala, AT, 1905.11375

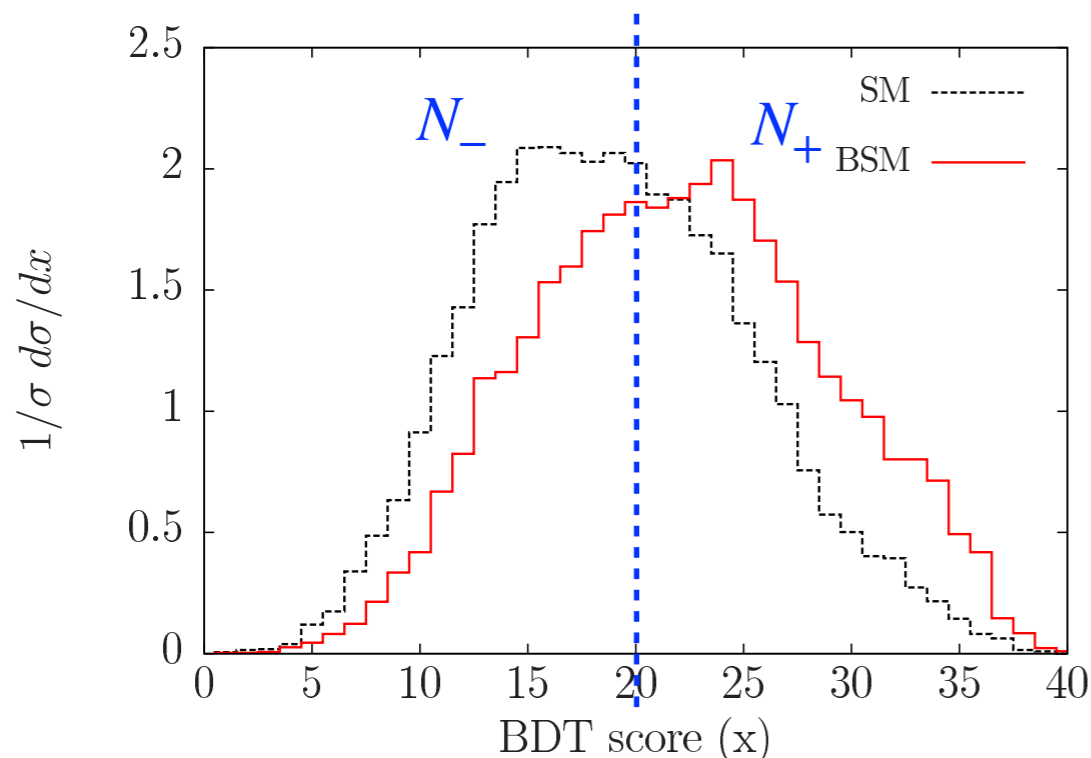


do not reconstruct m_W

reconstruct m_W



A multivariate analysis based on a BDT classifier ($p_T^{b_i}, p_T^{j_i}, m_W, \Delta R_{ij}$)



$$A = \frac{N_+ - N_-}{N_+ + N_-} \quad \begin{cases} A < 0 & \text{in SM} \\ A > 0 & \text{in NSMEFT} \end{cases}$$

$$\mathcal{B}(t \rightarrow b\ell N) \sim 2 \times 10^{-4}$$

@ HL-LHC with $\mathcal{L} = 3 \text{ ab}^{-1}$

Matching to NSMEFT: single- N_R operators

NSMEFT single- N_R operators

	Name	Structure	$n_N = 1$	$n_N = 3$
$d = 6$ (LNC)	\mathcal{O}_{LNQd}	$\epsilon_{ab} (\bar{L}^a N_R) (\bar{Q}^b d_R)$	54	162
	\mathcal{O}_{LdQN}	$\epsilon_{ab} (\bar{L}^a d_R) (\bar{Q}^b N_R)$	54	162
	\mathcal{O}_{QuNL}	$(\bar{Q} u_R) (\bar{N}_R L)$	54	162
$d = 7$ (LNV)	\mathcal{O}_{dNLH}	$\epsilon_{ab} (\bar{d}_R \gamma_\mu d_R) (\bar{N}_R^c \gamma^\mu L^a) H^b$	54	162
	\mathcal{O}_{uNLH}	$\epsilon_{ab} (\bar{u}_R \gamma_\mu u_R) (\bar{N}_R^c \gamma^\mu L^a) H^b$	54	162
	\mathcal{O}_{QNLH1}	$\epsilon_{ab} (\bar{Q} \gamma_\mu Q) (\bar{N}_R^c \gamma^\mu L^a) H^b$	54	162
	\mathcal{O}_{QNLH2}	$\epsilon_{ab} (\bar{Q} \gamma_\mu Q^a) (\bar{N}_R^c \gamma^\mu L^b) H$	54	162
	\mathcal{O}_{NL1}	$\epsilon_{ab} (\bar{N}_R^c \gamma_\mu L^a) (iD^\mu H^b) (H^\dagger H)$	6	18
	\mathcal{O}_{NL2}	$\epsilon_{ab} (\bar{N}_R^c \gamma_\mu L^a) H^b (H^\dagger i\overleftrightarrow{D}^\mu H)$	6	18

$d = 6$ LNC in NLEFT $\Leftrightarrow d = 6$ in NSMEFT

$$c_{d\nu N,ija}^{S,RR} = V_{ki}^* \left(C_{LNQd}^{akj} - \frac{1}{2} C_{LdQN}^{ajk} \right)$$

$$c_{d\nu N,ija}^{T,RR} = -\frac{1}{8} V_{ki}^* C_{LdQN}^{ajk}$$

$$c_{u\nu N,ija}^{S,RR} = c_{u\nu N,ija}^{T,RR} = c_{d\nu N,ija}^{S,LR} = 0$$

$$c_{u\nu N,ija}^{S,LR} = C_{QuNL}^{jia*}$$

$d = 6$ LNV in NLEFT $\Leftrightarrow d = 7$ in NSMEFT

$$c_{d\nu N,ija}^{V,RR} = -\frac{v}{\sqrt{2}} C_{dNLH}^{ija} - \frac{g_Z^2}{m_Z^2} Z_{dR}^{ij} Z_{\nu N}^\alpha$$

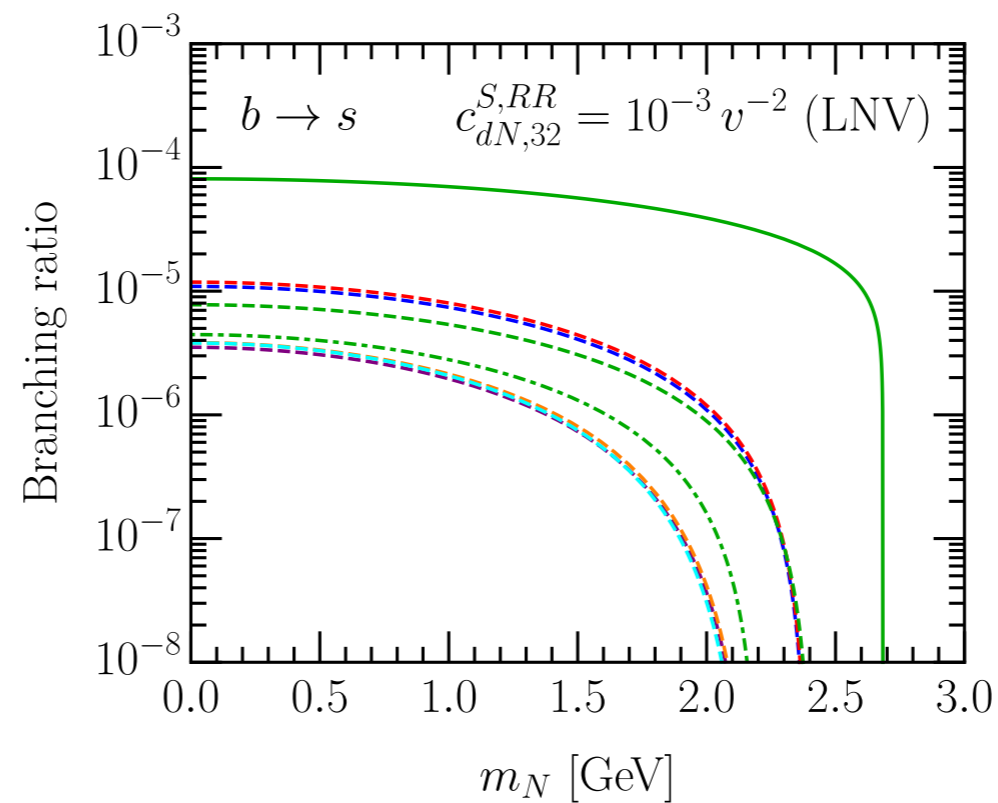
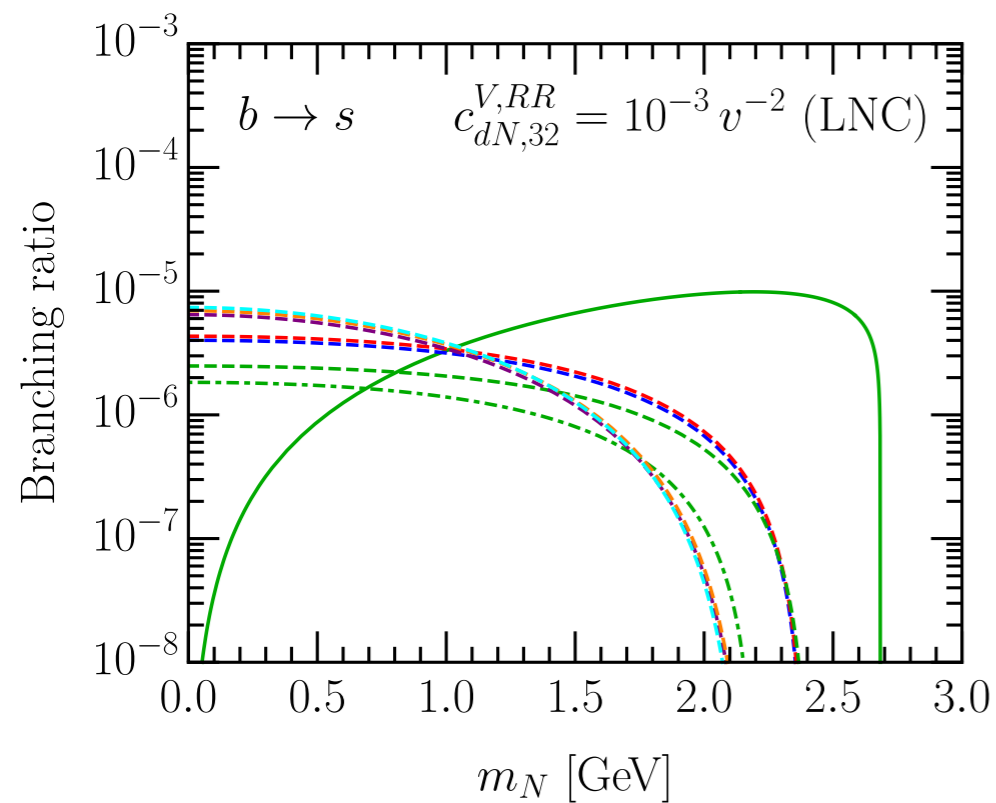
$$c_{d\nu N,ija}^{V,LR} = -\frac{v}{\sqrt{2}} V_{ki}^* V_{lj} \left(C_{QNLH1}^{kla} - C_{QNLH2}^{kla} \right) - \frac{g_Z^2}{m_Z^2} Z_{dL}^{ij} Z_{\nu N}^\alpha$$

$$c_{u\nu N,ija}^{V,RR} = -\frac{v}{\sqrt{2}} C_{uNLH}^{ija} - \frac{g_Z^2}{m_Z^2} Z_{uR}^{ij} Z_{\nu N}^\alpha$$

$$c_{u\nu N,ija}^{V,LR} = -\frac{v}{\sqrt{2}} C_{QNLH1}^{ija} - \frac{g_Z^2}{m_Z^2} Z_{uL}^{ij} Z_{\nu N}^\alpha$$

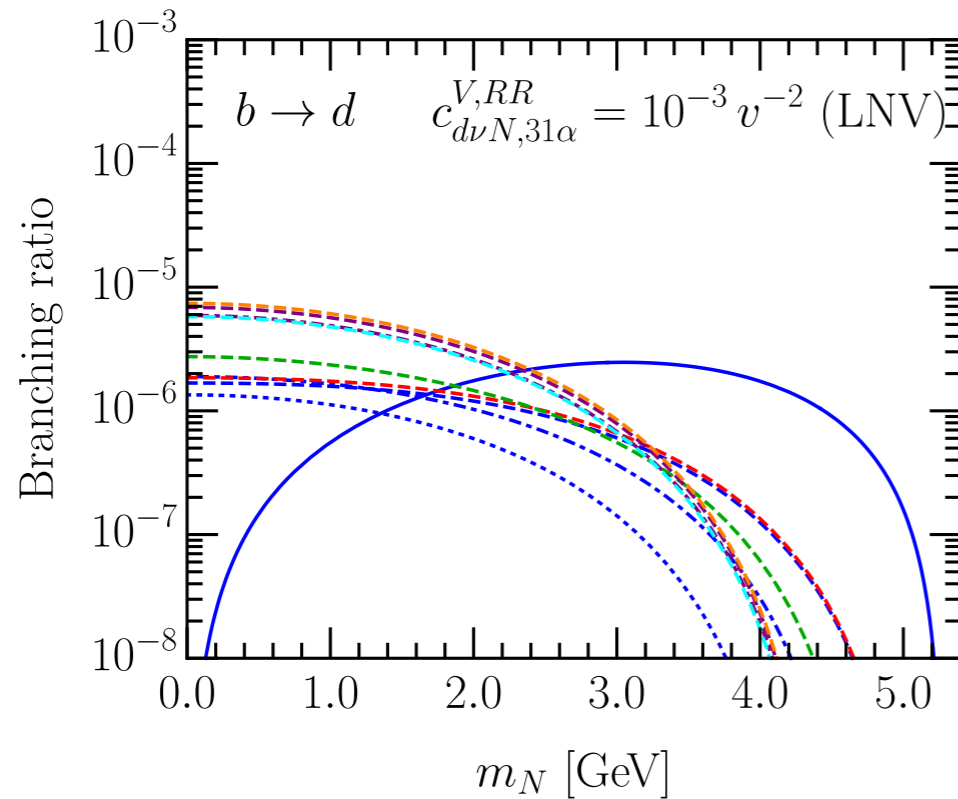
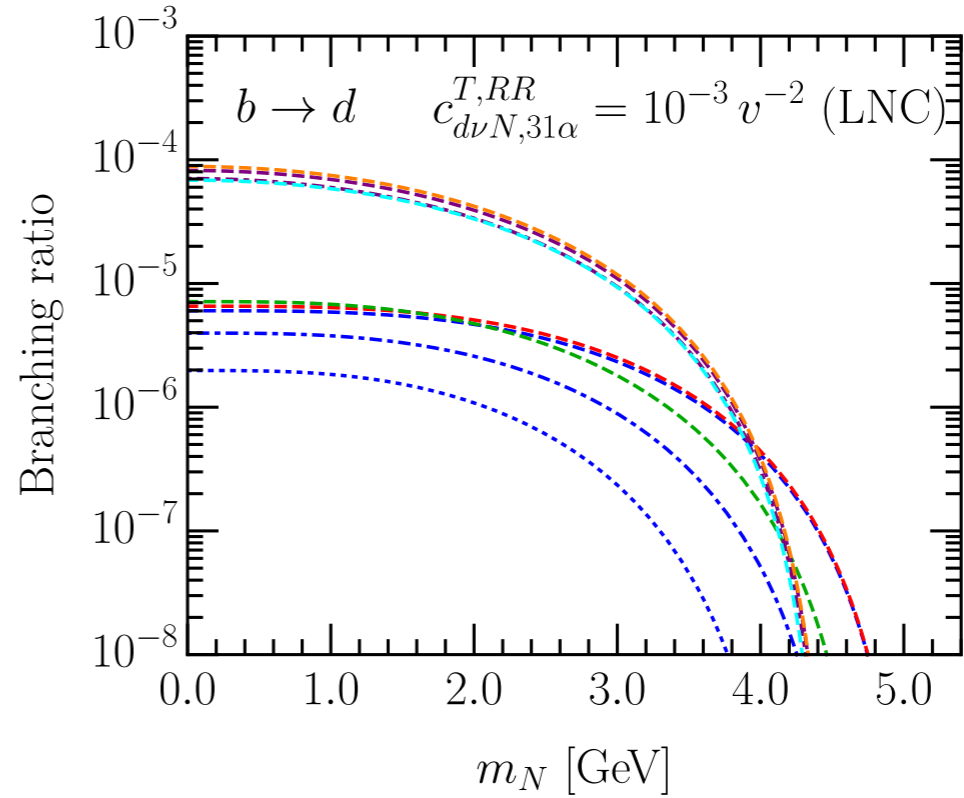
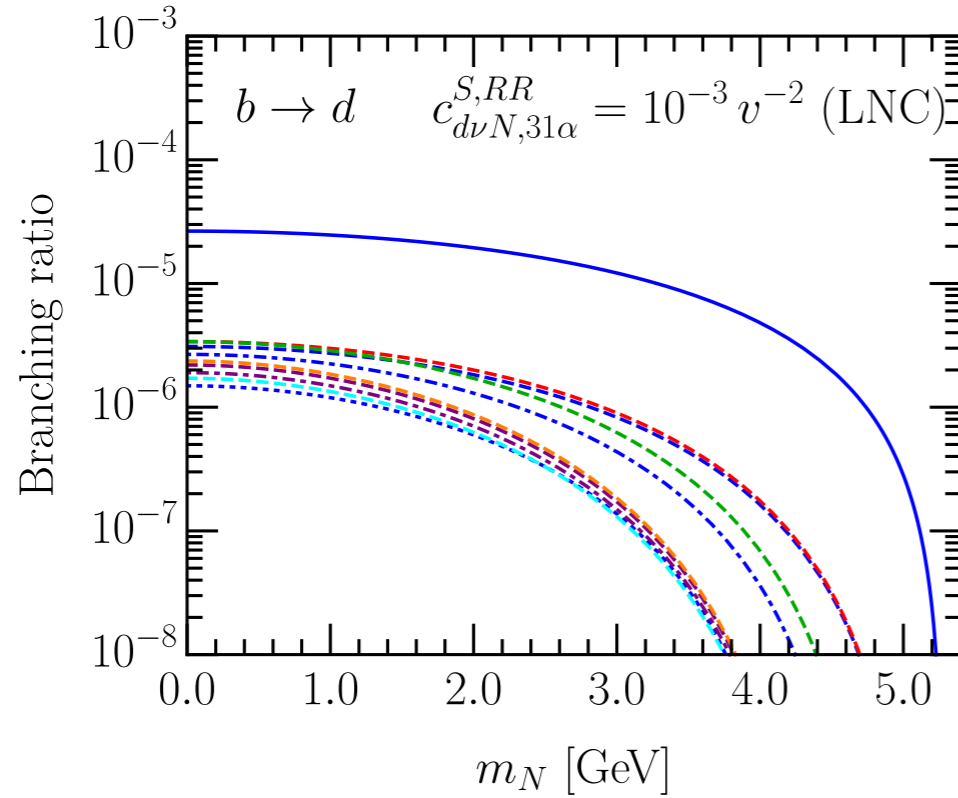
$$Z_{\nu N}^\alpha \equiv \frac{v^3}{4\sqrt{2}} (C_{NL1}^\alpha + 2C_{NL2}^\alpha)$$

Branching ratios: $b \rightarrow s$ scenario



- $B_s^0 \rightarrow N + N$
- - - $B^0 \rightarrow K^0 + N + N$
- - - $B^+ \rightarrow K^+ + N + N$
- - - $B_s^0 \rightarrow \eta + N + N$
- - - $B_s^0 \rightarrow \eta' + N + N$
- - - $B^0 \rightarrow K^{*0} + N + N$
- - - $B^+ \rightarrow K^{*+} + N + N$
- - - $B_s^0 \rightarrow \phi + N + N$

Branching ratios: single-N operators



- $B^0 \rightarrow \nu_\alpha + N$
- - - $B^0 \rightarrow \pi^0 + \nu_\alpha + N$
- · · $B^0 \rightarrow \eta + \nu_\alpha + N$
- · · $B^0 \rightarrow \eta' + \nu_\alpha + N$
- - - $B^+ \rightarrow \pi^+ + \nu_\alpha + N$
- - - $B_s^0 \rightarrow \bar{K}^0 + \nu_\alpha + N$
- - - $B^0 \rightarrow \rho^0 + \nu_\alpha + N$
- - - $B^0 \rightarrow \omega + \nu_\alpha + N$
- - - $B^+ \rightarrow \rho^+ + \nu_\alpha + N$
- - - $B_s^0 \rightarrow \bar{K}^{*0} + \nu_\alpha + N$

Other experiments

AL3X: A Laboratory for Long-Lived eXotics
@ALICE

Cylinder with $0.85 \text{ m} < r < 5 \text{ m}$ and $\ell = 12 \text{ m}$
 $c\tau \sim 10 \text{ m}$

FACET: Forward-Aperture CMS ExTension
@CMS

Cylinder with $r = 0.5 \text{ m}$ and $\ell = 18 \text{ m}$
 $c\tau \sim 100 \text{ m}$

MoEDAL-MAPP: MoEDAL's Apparatus for Penetrating Particles
(MoEDAL: Monopole and Exotics Detector at the LHC)
@LHCb

MAPP1: $\sim 130 \text{ m}^3$

MAPP2: $\sim 430 \text{ m}^3$

$c\tau \sim 50 \text{ m}$

Existing constraints on BRs

PDG 2022

Decay	Limit on BR	Decay	Limit on BR	Decay	Limit on BR
$D^0 \rightarrow \text{inv.}$	9.4×10^{-5}	$B^0 \rightarrow \text{inv.}$	2.4×10^{-5}	$B_s^0 \rightarrow \phi \nu \bar{\nu}$	5.4×10^{-3}
		$B^0 \rightarrow \pi^0 \nu \bar{\nu}$	9.0×10^{-6}	$B^0 \rightarrow K^0 \nu \bar{\nu}$	2.6×10^{-5}
		$B^0 \rightarrow \rho^0 \nu \bar{\nu}$	4.0×10^{-5}	$B^0 \rightarrow K^{*0} \nu \bar{\nu}$	1.8×10^{-5}
		$B^+ \rightarrow \pi^+ \nu \bar{\nu}$	1.4×10^{-5}	$B^+ \rightarrow K^+ \nu \bar{\nu}$	1.6×10^{-5}
		$B^+ \rightarrow \rho^+ \nu \bar{\nu}$	3.0×10^{-5}	$B^+ \rightarrow K^{*+} \nu \bar{\nu}$	4.0×10^{-5}

BELL'17

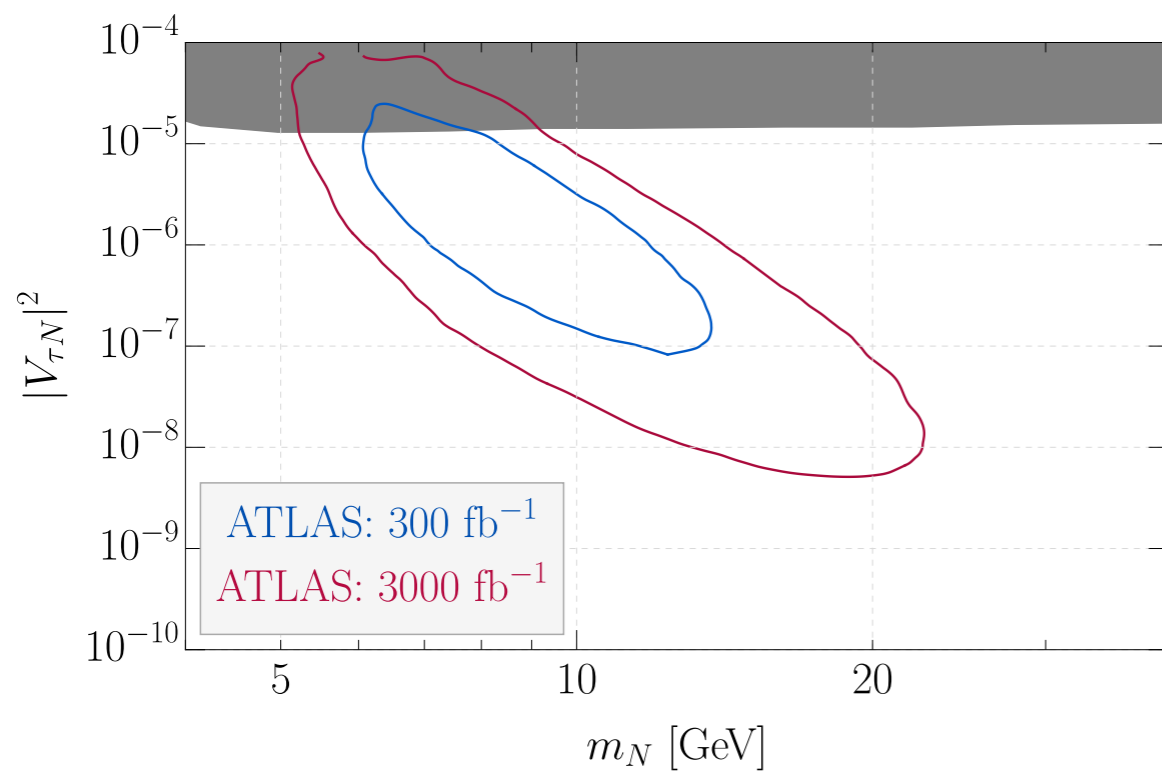
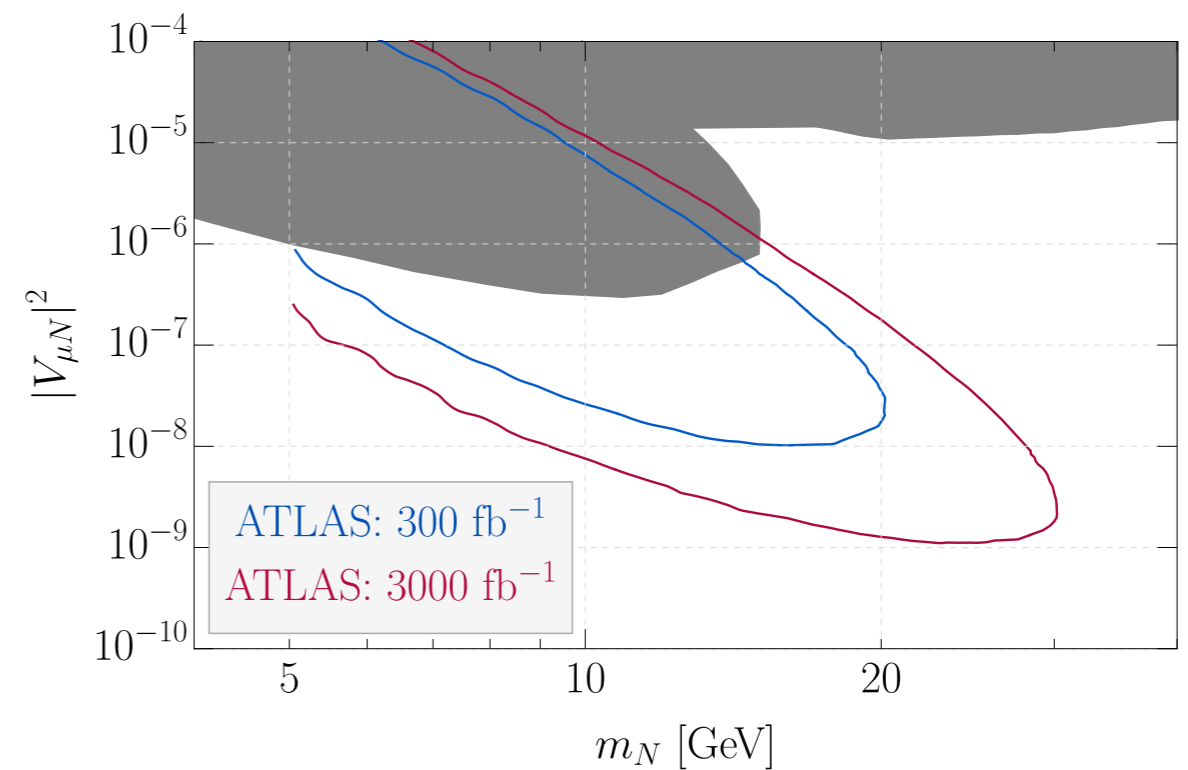
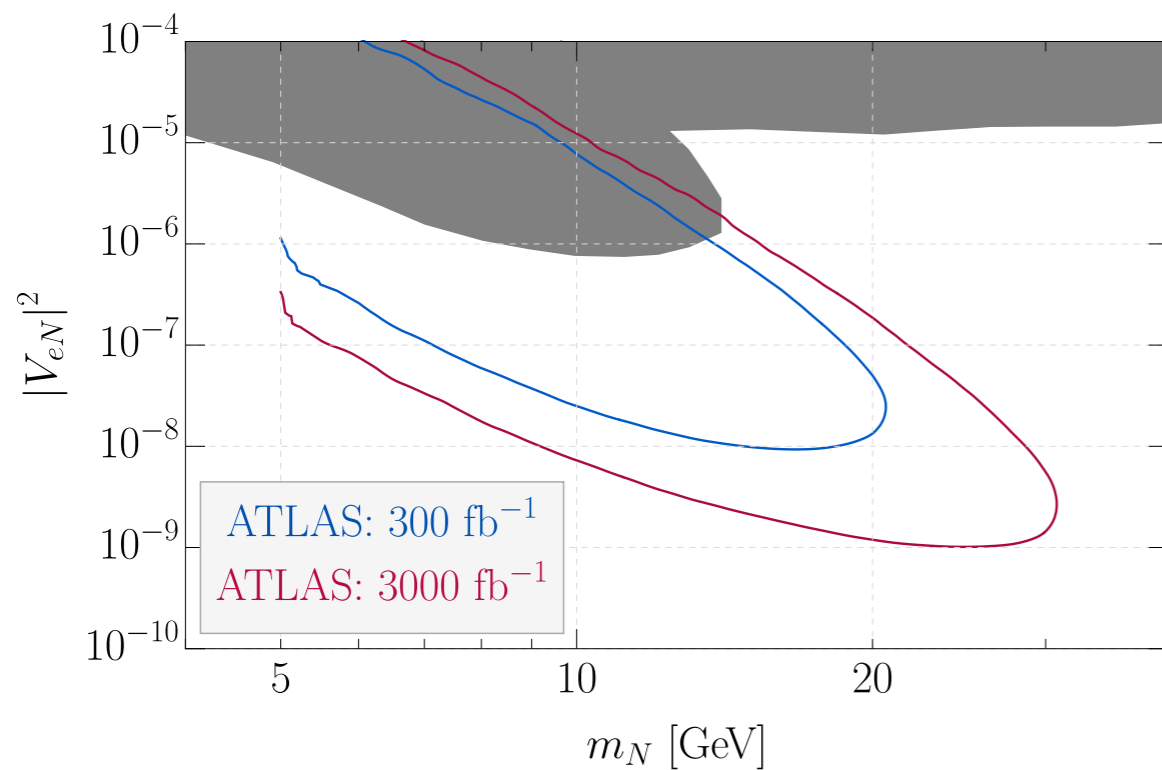
BABAR'12
BELL'17

BABAR'13

Decay	Branching ratio
$K_L \rightarrow \pi^0 \nu \bar{\nu}$	$< 3.0 \times 10^{-9}$ at 90% C.L.
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	$(1.14_{-0.33}^{+0.40}) \times 10^{-10}$

Decay	Branching ratio
$K^+ \rightarrow e^+ \nu_e$	$(1.582 \pm 0.007) \times 10^{-5}$
$K^+ \rightarrow \pi^0 e^+ \nu_e$	$(5.07 \pm 0.04) \times 10^{-2}$
$K_S \rightarrow \pi^\pm e^\mp \nu_e$	$(7.04 \pm 0.08) \times 10^{-4}$
$K_L \rightarrow \pi^\pm e^\mp \nu_e$	$(40.55 \pm 0.11) \times 10^{-2}$

Minimal 3+1 scenario



Beltrán et al., 2110.15096
(update of Cottin, Helo, Hirsch, 1806.05191)

Long-lived HNLs

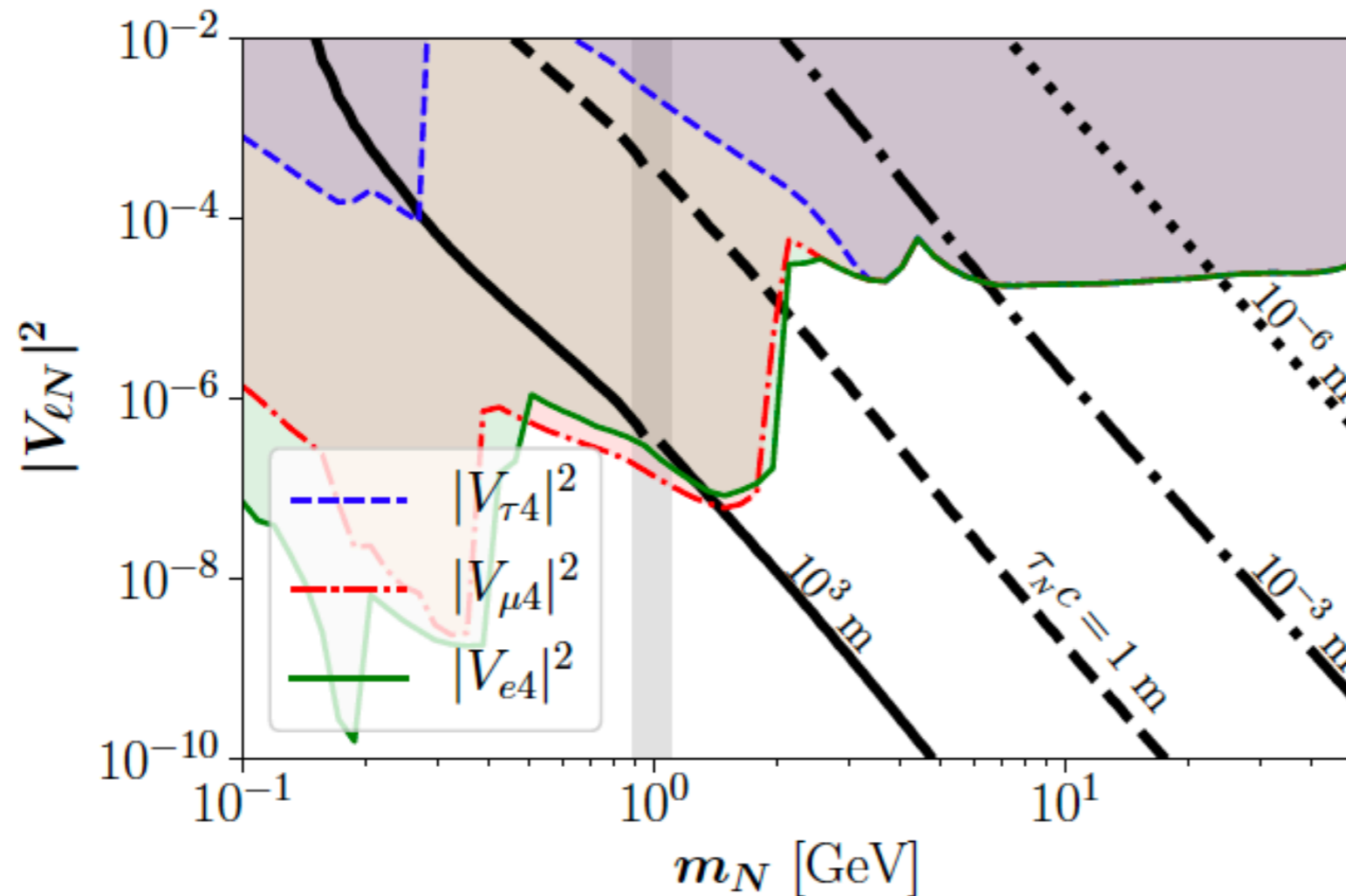


Figure from
Abada, Bernal, Losada, Marcano,
1807.10024

HNLs can be long-lived particles (LLPs)

HNL decay width calculation:

Atre, Han, Pascoli, Zhang, 0901.3589

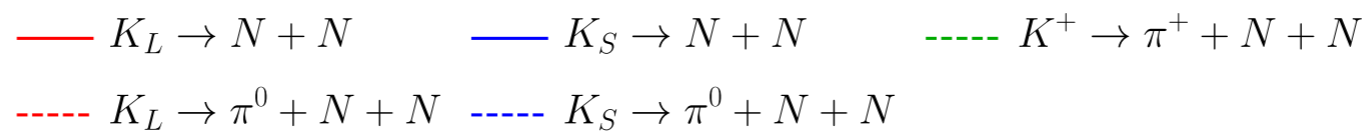
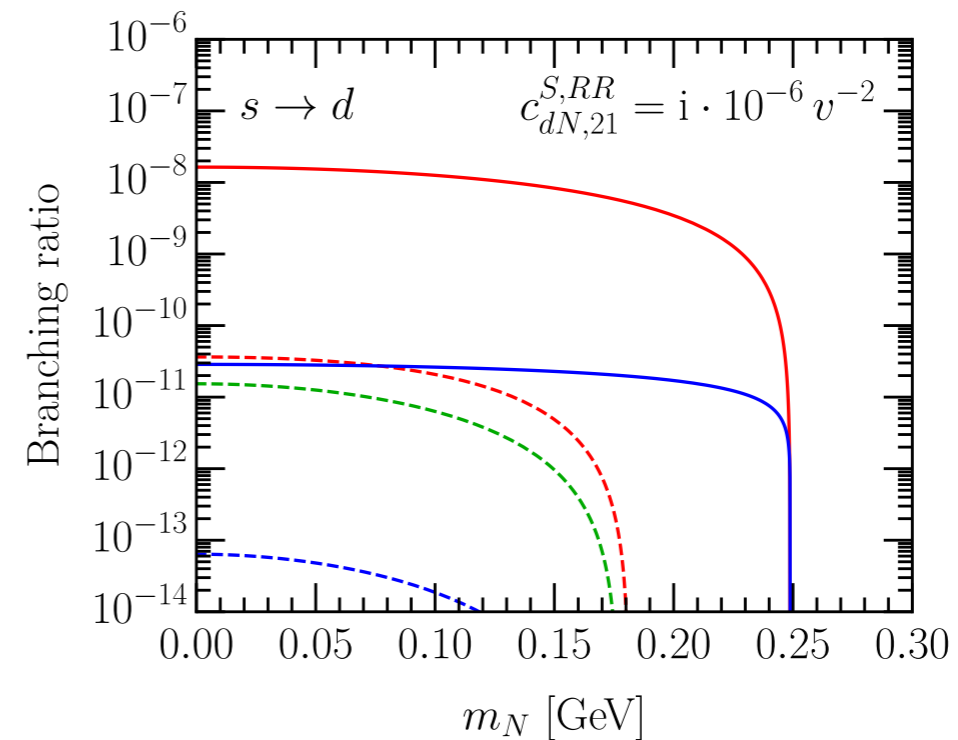
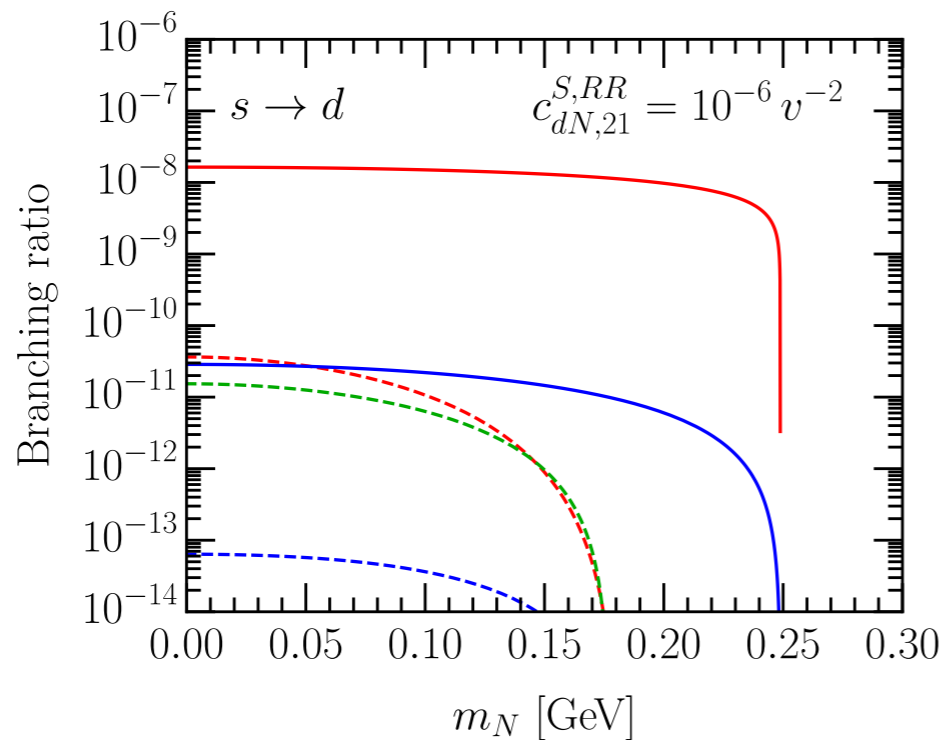
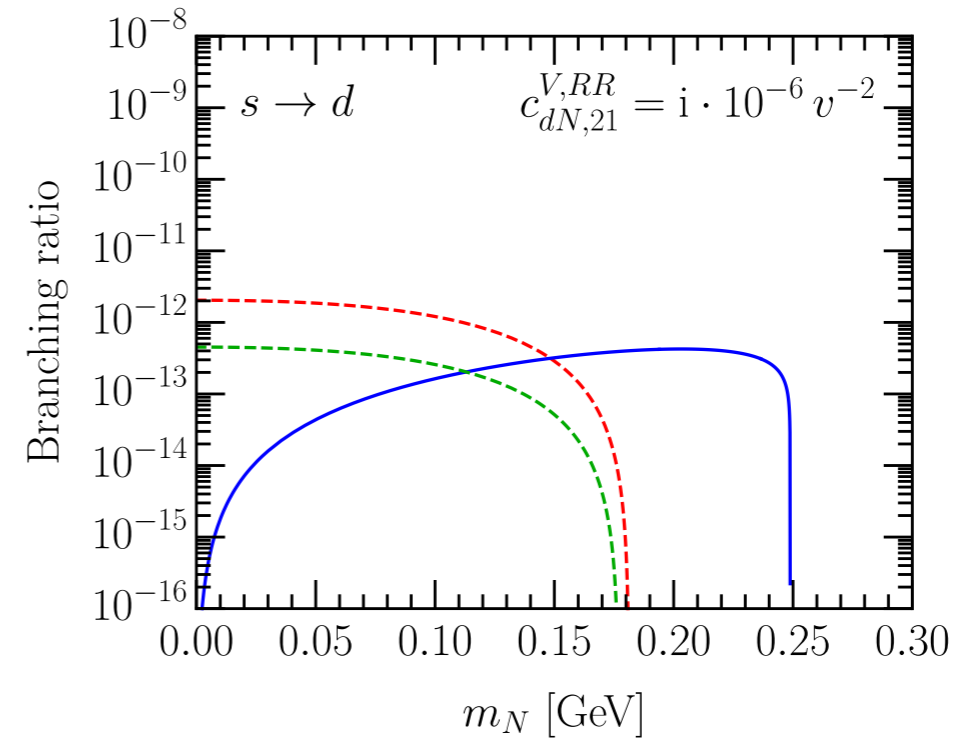
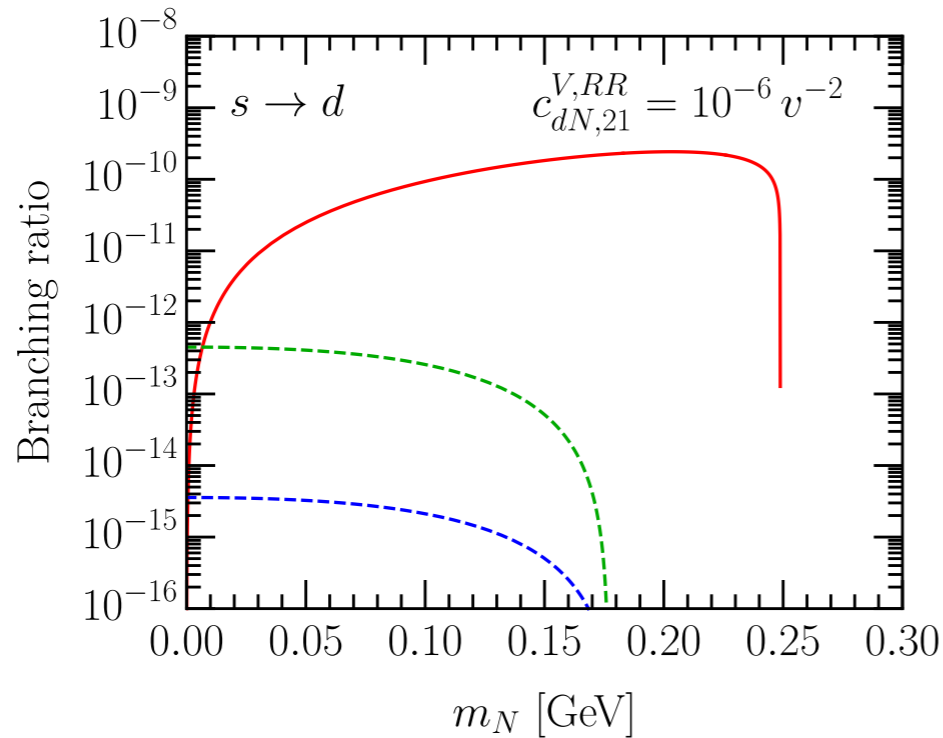
Bondarenko, Boyarsky, Gorbunov, Ruchayskiy, 1805.08567

4-fermion quark-N operators (kaons)

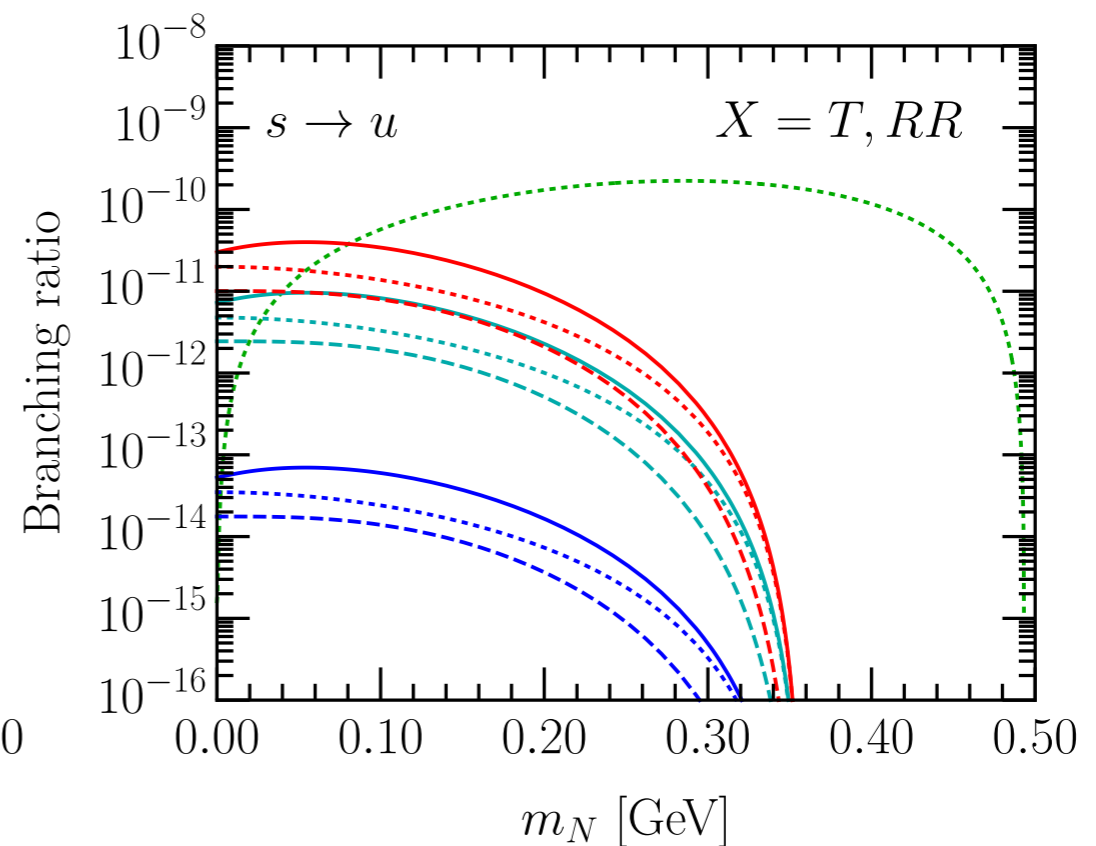
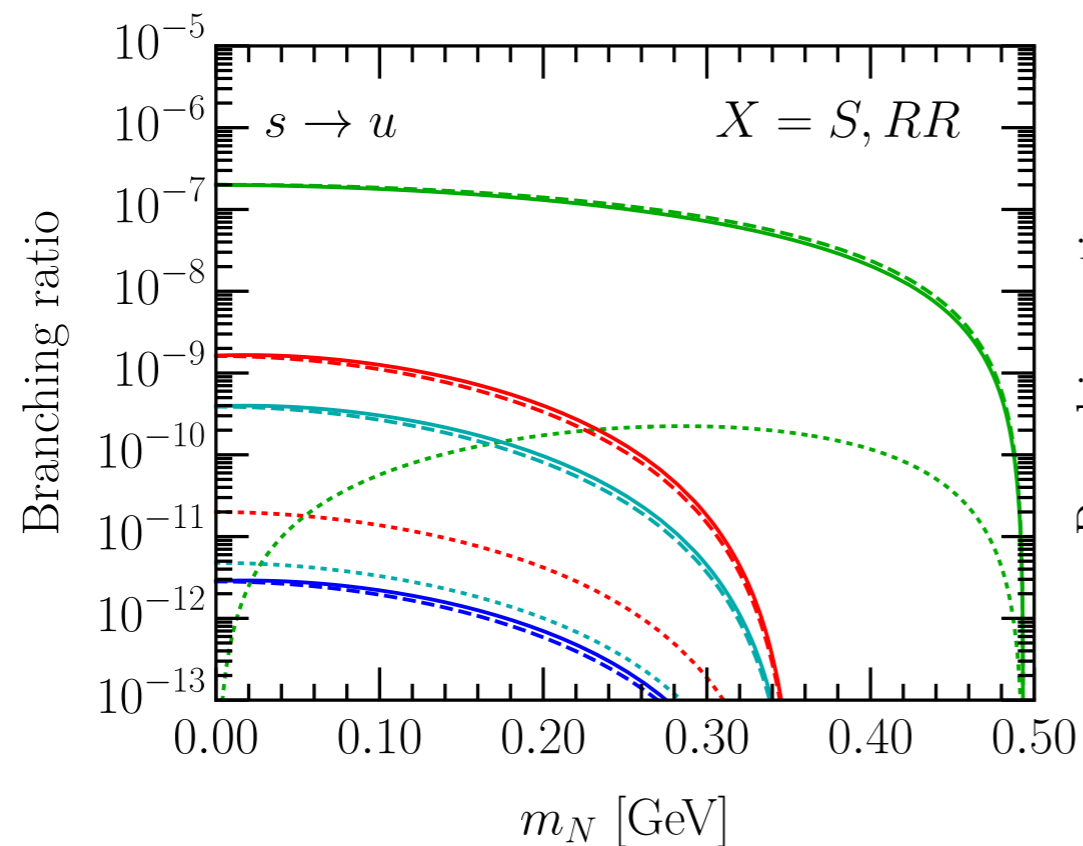
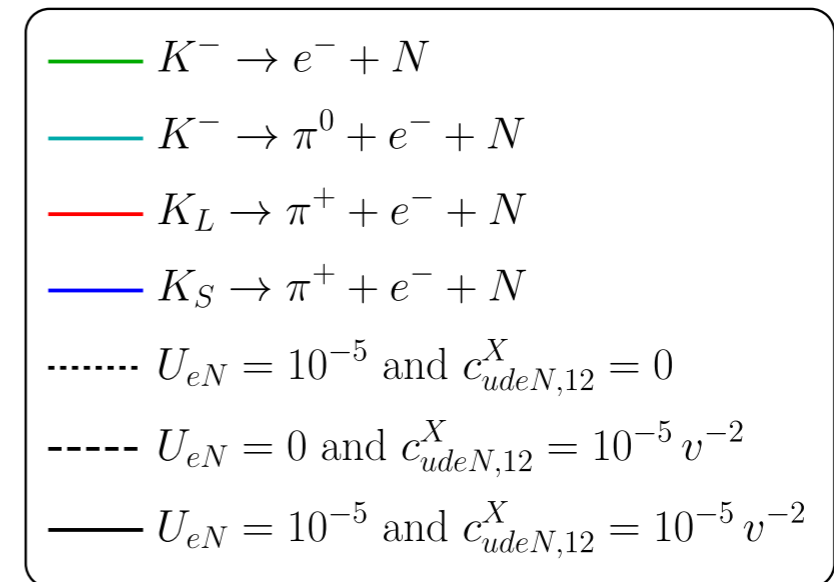
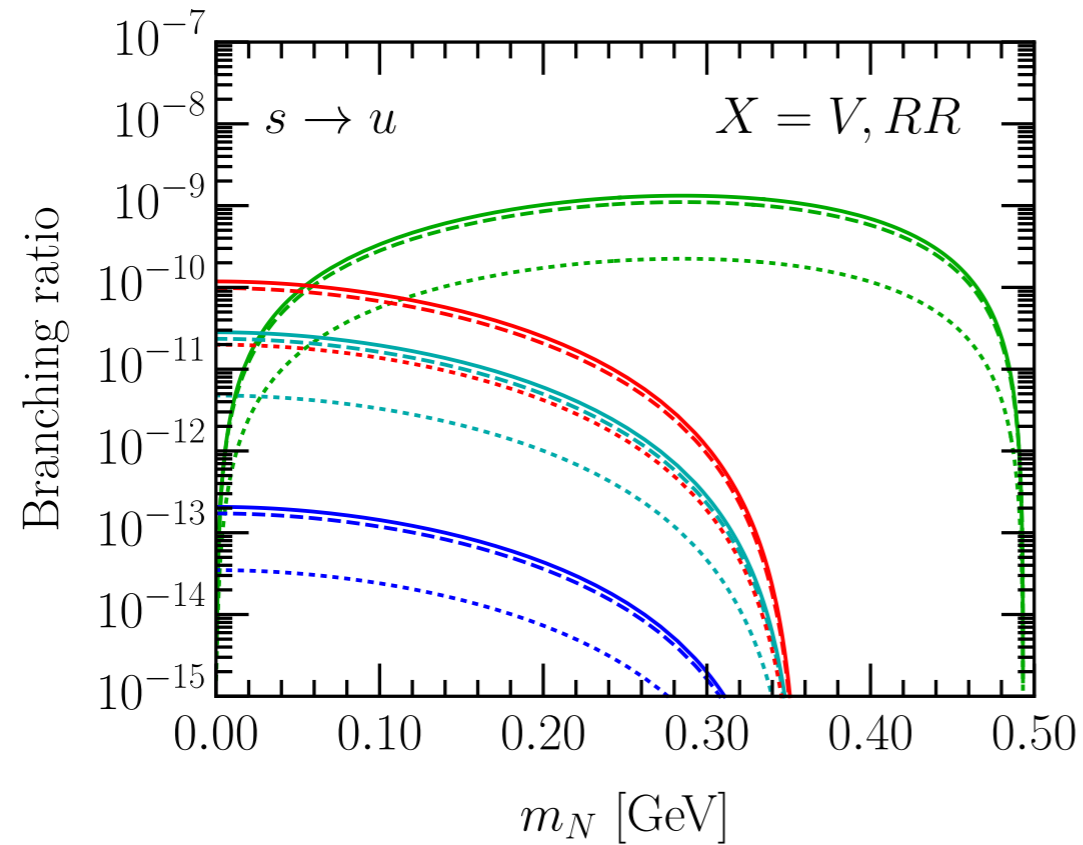
NLEFT pair- N_R operators (NC)		
LNC operators		
Name	Structure	N_{pars}
$\mathcal{O}_{dN}^{V,RR}$	$(\bar{d}_R \gamma_\mu d_R) (\bar{N}_R \gamma^\mu N_R)$	9
$\mathcal{O}_{uN}^{V,RR}$	$(\bar{u}_R \gamma_\mu u_R) (\bar{N}_R \gamma^\mu N_R)$	4
$\mathcal{O}_{dN}^{V,LR}$	$(\bar{d}_L \gamma_\mu d_L) (\bar{N}_R \gamma^\mu N_R)$	9
$\mathcal{O}_{uN}^{V,LR}$	$(\bar{u}_L \gamma_\mu u_L) (\bar{N}_R \gamma^\mu N_R)$	4
LNV operators		
Name	Structure	N_{pars}
$\mathcal{O}_{dN}^{S,RR}$	$(\bar{d}_L d_R) (\bar{N}_R^c N_R)$	18
$\mathcal{O}_{uN}^{S,RR}$	$(\bar{u}_L u_R) (\bar{N}_R^c N_R)$	8
$\mathcal{O}_{dN}^{S,LR}$	$(\bar{d}_R d_L) (\bar{N}_R^c N_R)$	18
$\mathcal{O}_{uN}^{S,LR}$	$(\bar{u}_R u_L) (\bar{N}_R^c N_R)$	8

NLEFT single- N_R operators (CC)	
LNC operators	
Name	Structure
$\mathcal{O}_{udeN}^{V,RR}$	$(\bar{u}_R \gamma_\mu d_R) (\bar{e}_R \gamma^\mu N_R)$
$\mathcal{O}_{udeN}^{V,LR}$	$(\bar{u}_L \gamma_\mu d_L) (\bar{e}_R \gamma^\mu N_R)$
$\mathcal{O}_{udeN}^{S,RR}$	$(\bar{u}_L d_R) (\bar{e}_L N_R)$
$\mathcal{O}_{udeN}^{T,RR}$	$(\bar{u}_L \sigma_{\mu\nu} d_R) (\bar{e}_L \sigma^{\mu\nu} N_R)$
$\mathcal{O}_{udeN}^{S,LR}$	$(\bar{u}_R d_L) (\bar{e}_L N_R)$
LNV operators	
Name	Structure
$\mathcal{O}_{udeN}^{V,LL}$	$(\bar{u}_L \gamma_\mu d_L) (\bar{e}_L \gamma^\mu N_R^c)$
$\mathcal{O}_{udeN}^{V,RL}$	$(\bar{u}_R \gamma_\mu d_R) (\bar{e}_L \gamma^\mu N_R^c)$
$\mathcal{O}_{udeN}^{S,LL}$	$(\bar{u}_R d_L) (\bar{e}_R N_R^c)$
$\mathcal{O}_{udeN}^{T,LL}$	$(\bar{u}_R \sigma_{\mu\nu} d_L) (\bar{e}_R \sigma^{\mu\nu} N_R^c)$
$\mathcal{O}_{udeN}^{S,RL}$	$(\bar{u}_L d_R) (\bar{e}_R N_R^c)$

Branching ratios: pair-N operators



Branching ratios: single-N operators

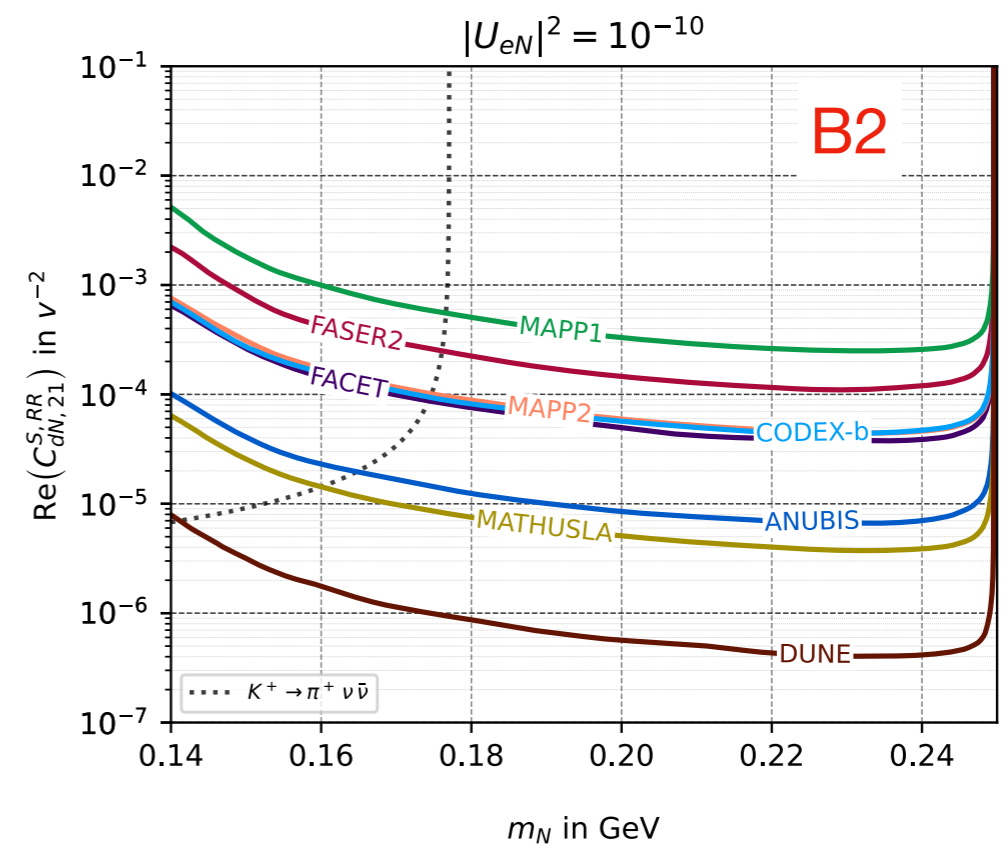
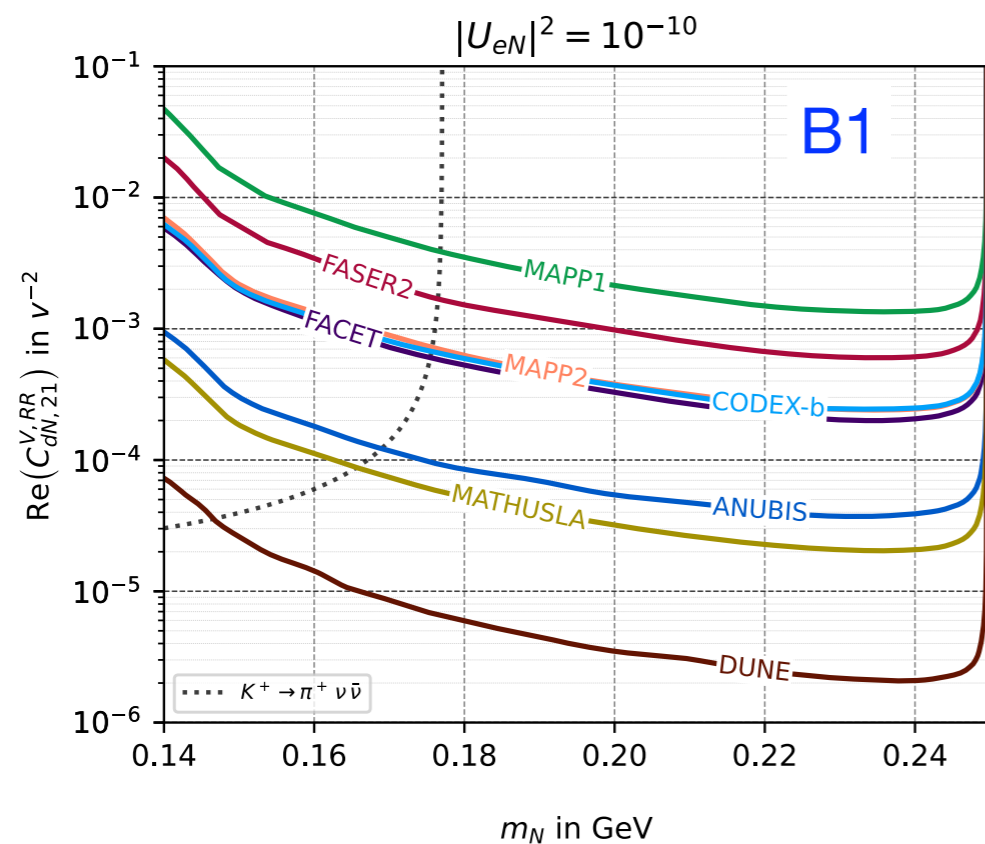
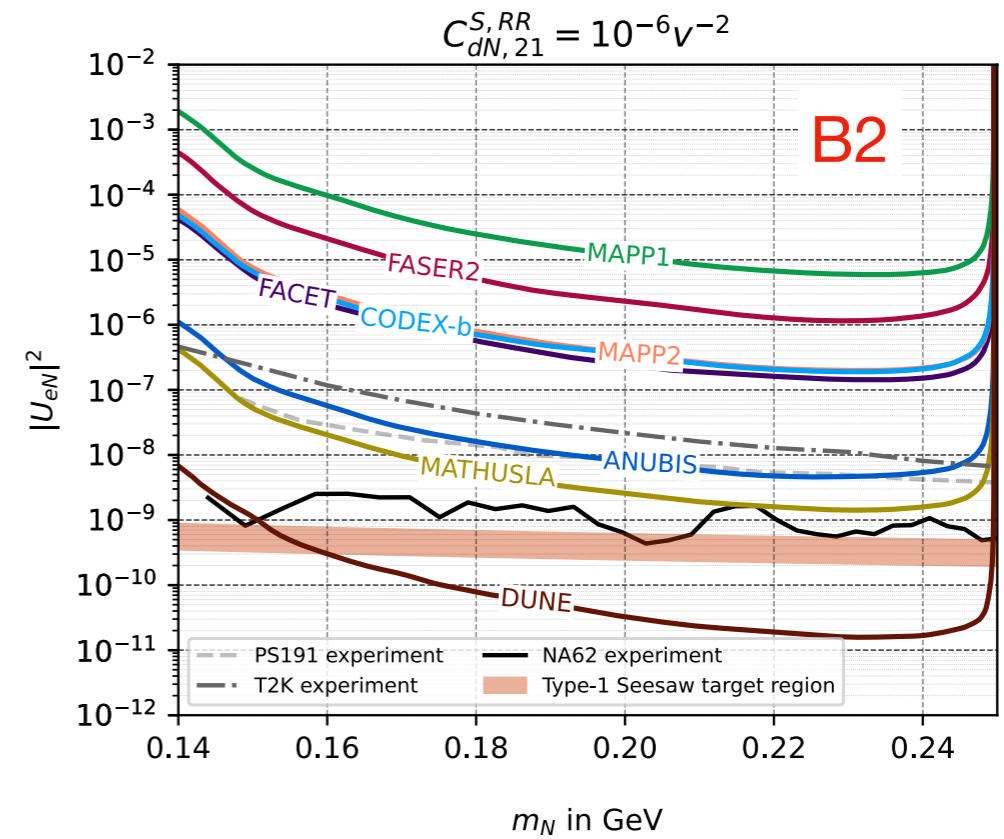
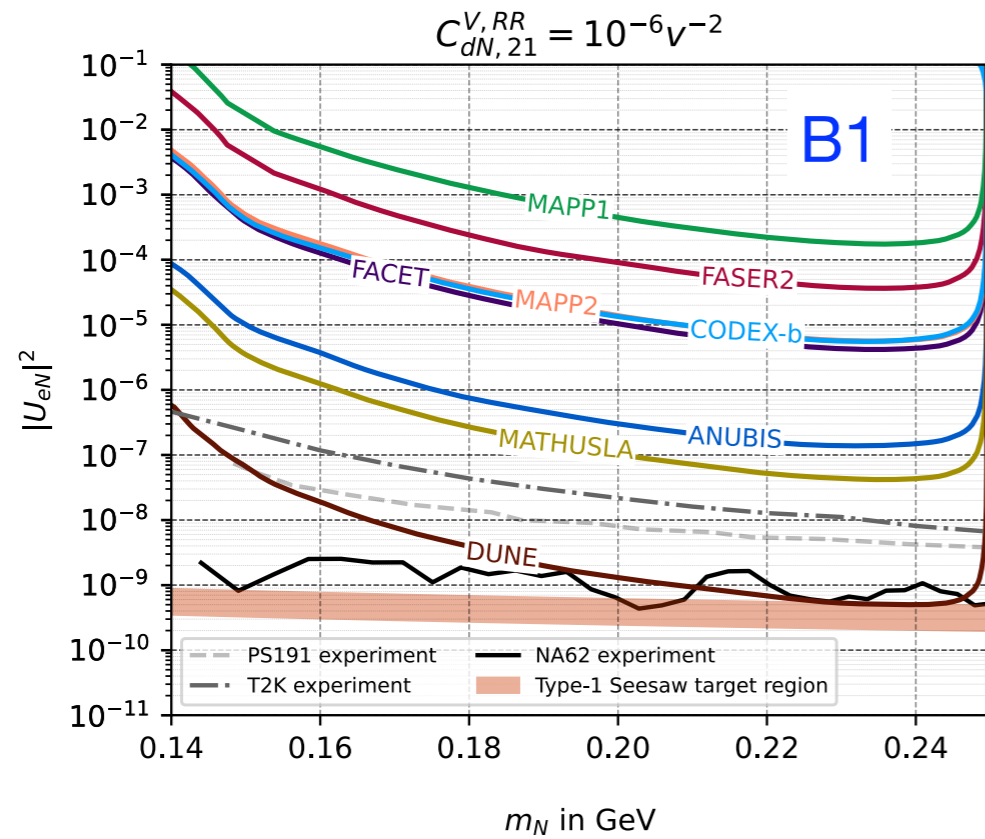


Benchmark scenarios

Benchmark	Production	Decay
B1.1	$c_{dN,21}^{V,RR} \in \mathbb{R}$	U_{eN}
B1.2	$c_{dN,21}^{V,RR} \in i\mathbb{R}$	U_{eN}
B2.1	$c_{dN,21}^{S,RR} \in \mathbb{R}$	U_{eN}
B2.2	$c_{dN,21}^{S,RR} \in i\mathbb{R}$	U_{eN}

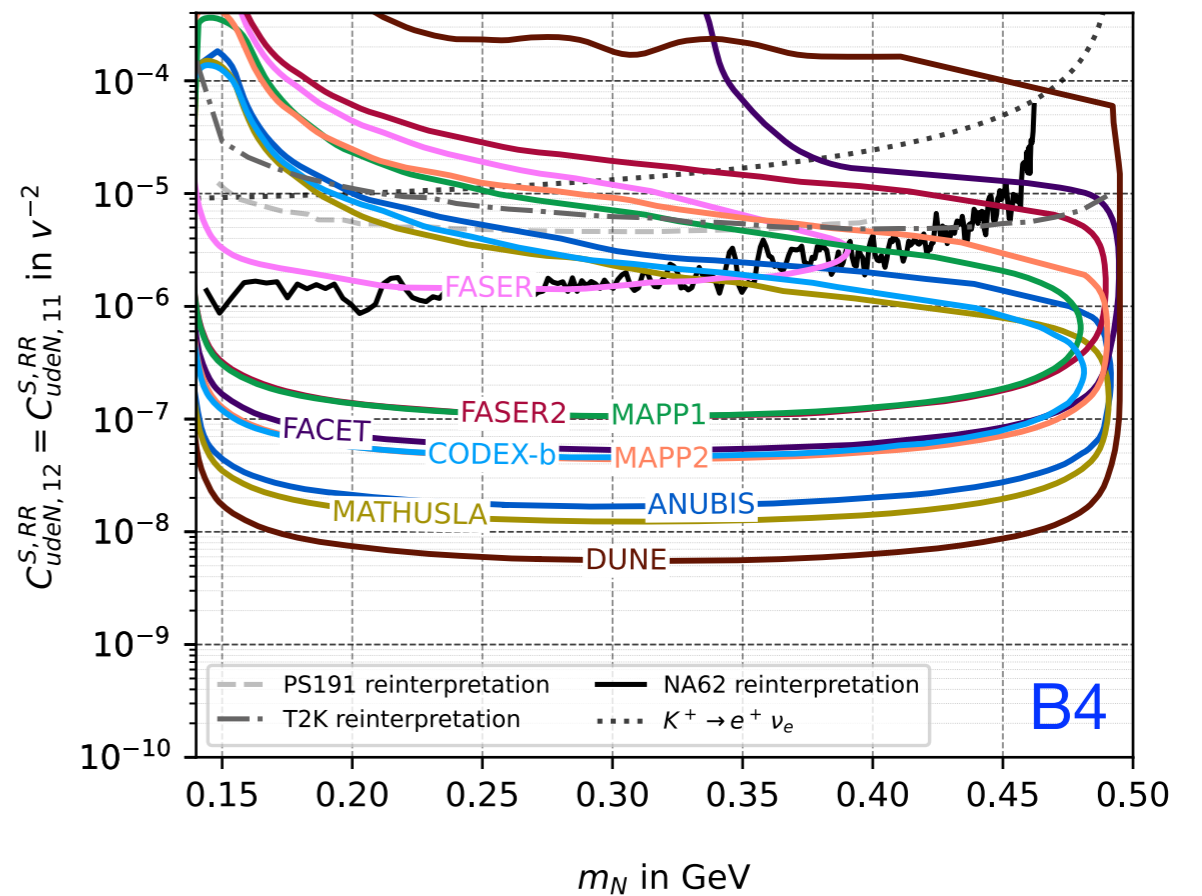
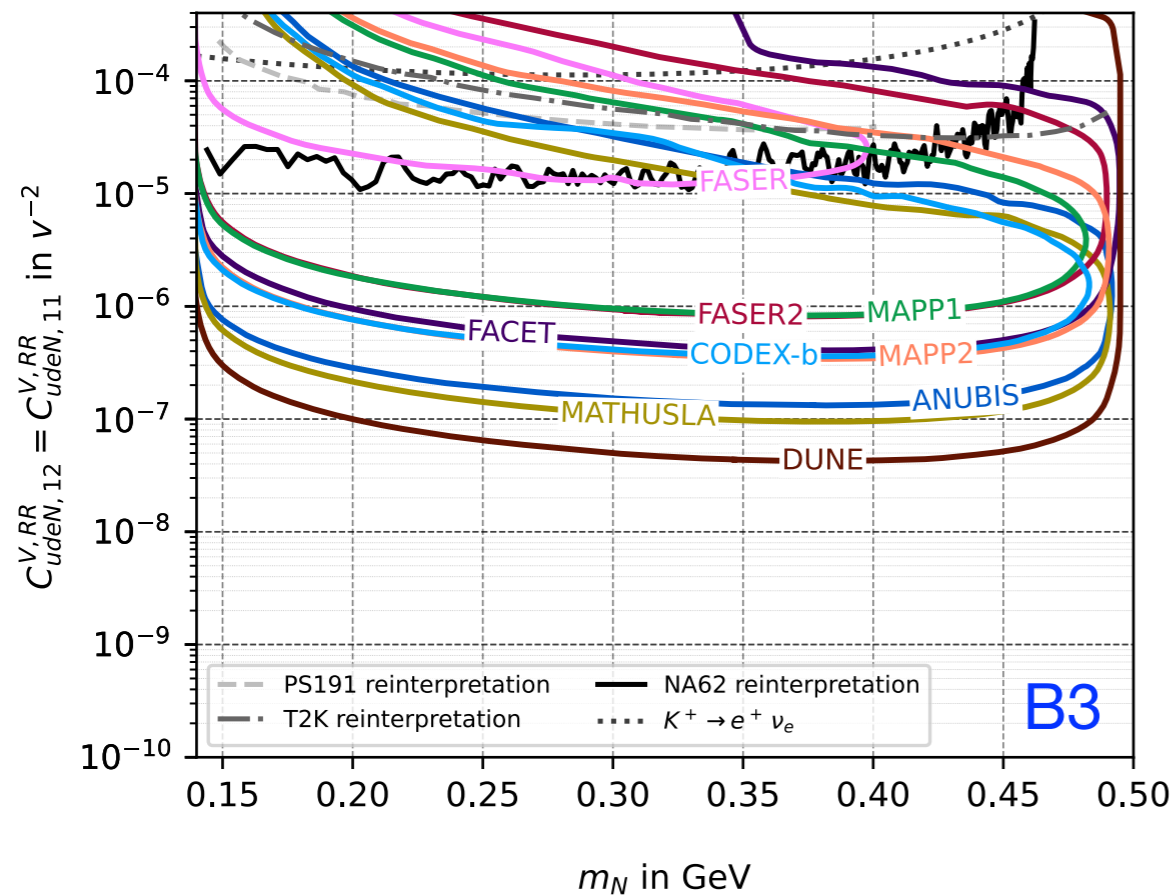
Benchmark	Production	Decay
B3	$c_{udeN,12}^{V,RR}$	$c_{udeN,11}^{V,RR}$
B4	$c_{udeN,12}^{S,RR}$	$c_{udeN,11}^{S,RR}$
B5	$c_{udeN,12}^{V,RR}$ and U_{eN}	U_{eN}
B6	$c_{udeN,12}^{S,RR}$ and U_{eN}	U_{eN}
B7	$c_{udeN,12}^{V,RL}$ and U_{eN}	U_{eN}
B8	$c_{udeN,12}^{S,RL}$ and U_{eN}	U_{eN}

Pair-N benchmarks B1 and B2



Single-N benchmarks B3 and B4

Production and decay of N through the same operator structure $\mathcal{O}_{udeN}^{VIS,RR}$, but with different quark flavour indices: 12 (for production) vs. 11 (for decay)



Single-N benchmarks B5 and B7

