

# LNV beyond dim-5 Weinberg Operator



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Breaking Lepton Number in High Energy Direct Searches



**BLED 2024**



**Incredible Hulk**



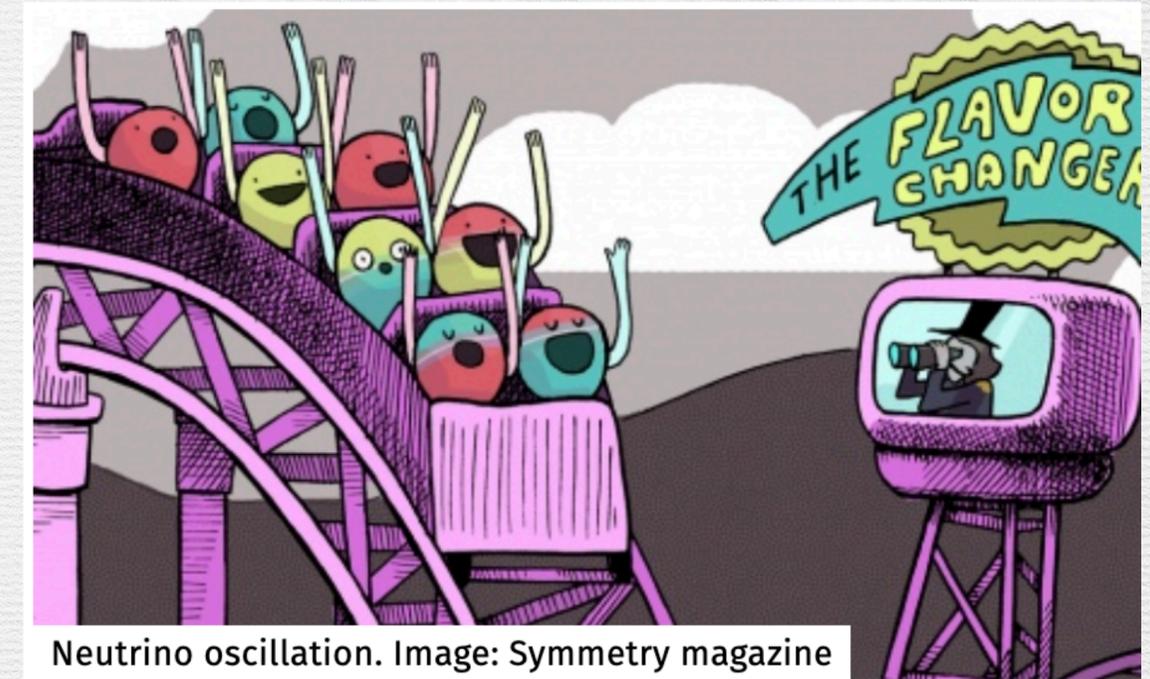
**Credible Hulk**



**Very rich literature on the topic!  
I am sure I have missed many relevant citations**

# Neutrino masses and Lepton Number Violation

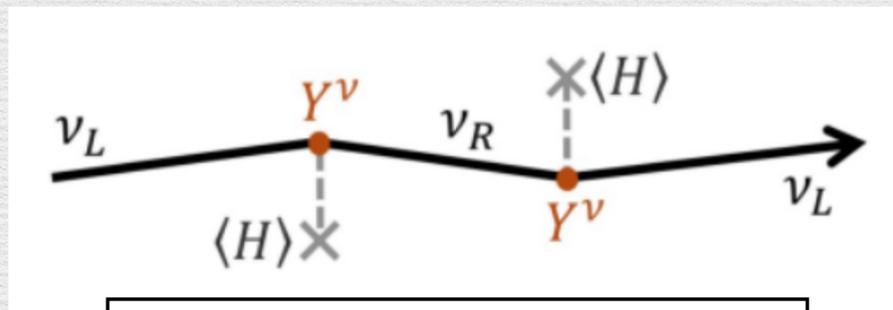
The only laboratory evidence of BSM physics : **Neutrino Oscillations**



Purely SM:

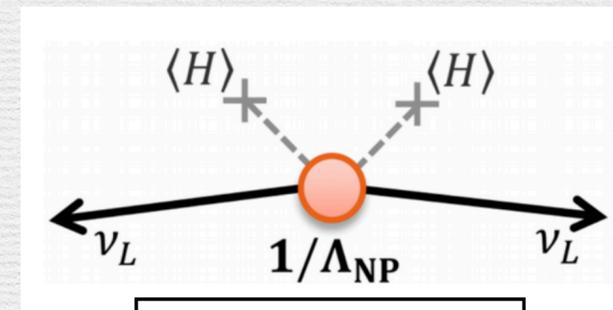
- **strictly massless neutrinos**
- **conservation of lepton number and flavours**

Two possibilities for neutrino masses:



$$m_D \nu_L \nu_R^c \subset y_\nu L H \nu_R^c$$

VS.



$$m_M \bar{\nu}_L \nu_L^c$$

**Dirac:** like other fermions,

but tiny Yukawa couplings  $\sim 10^{-12}$

finetuning, symmetry, ...?

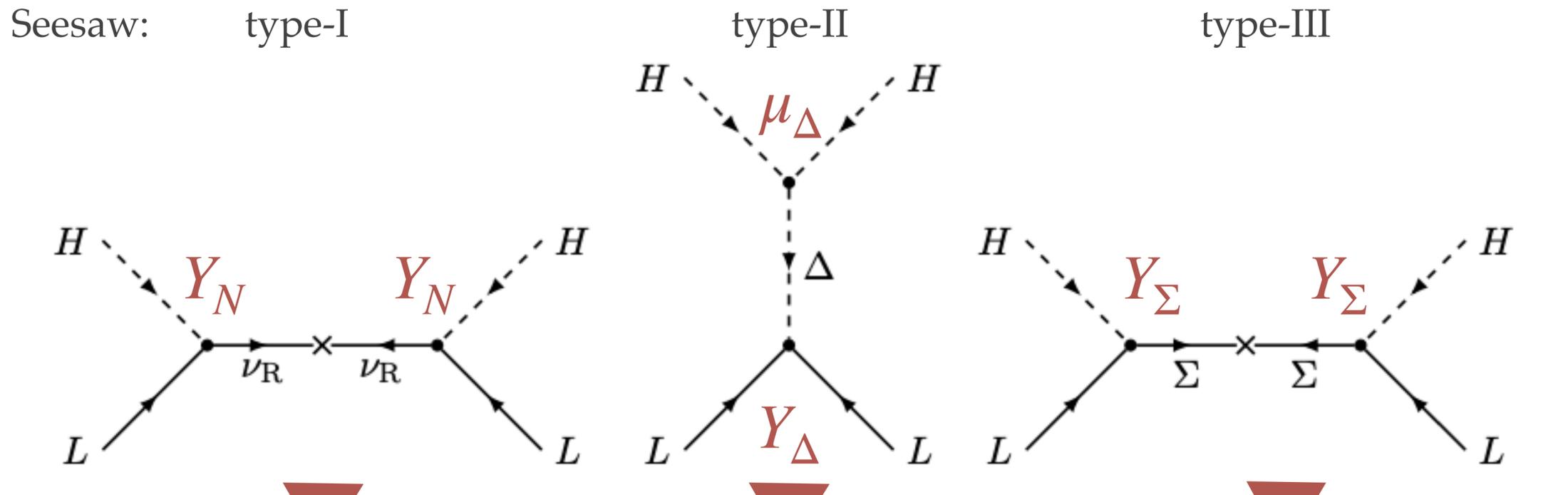
**Majorana:**  $\nu = \nu^c$  : **Lepton Number Violation!**

Phenomenologically very interesting!

Connection to Leptogenesis?

# Minimal neutrino mass models: "Bauhaus"

Minimal possibilities for Majorana mass  $\rightarrow$  Tree-level dimension-5:



$$m_\nu = Y_N^T \frac{v^2}{M_N} Y_N$$

$$m_\nu = Y_\Delta \frac{v^2}{M_\Delta^2} \mu_\Delta$$

$$m_\nu = Y_\Sigma^T \frac{v^2}{M_\Sigma} Y_\Sigma$$

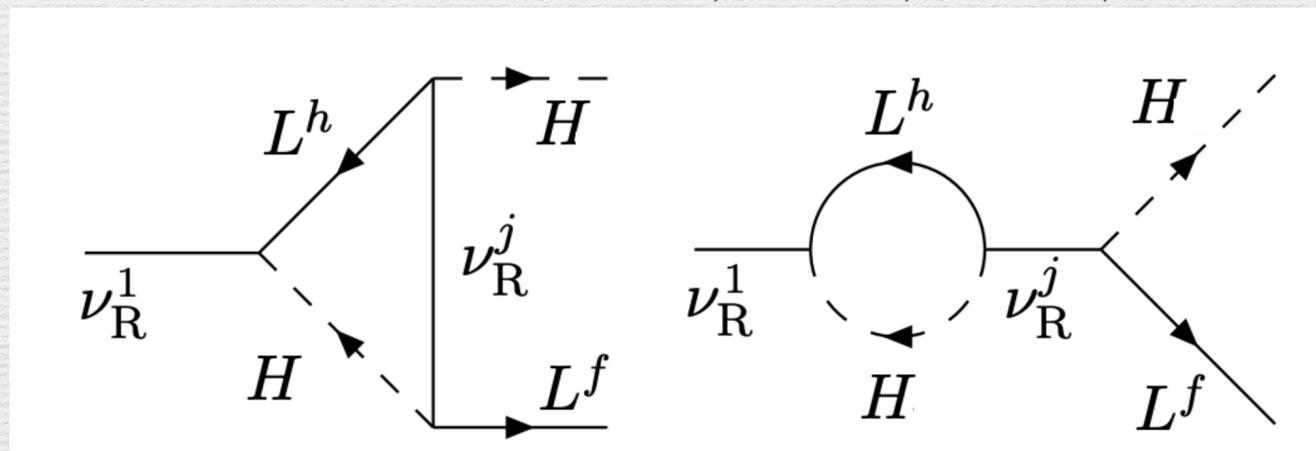


Minkowski; Gell-Mann, Ramond, Slansky; Mohapatra, Senjanovic; Schechter, Valle; Ma, Sarkar; Magg, Wetterich; Cheng, Li; Lazarides, Shafi; Foot, Lew, Joshi; Ma; Ma, Roy; Hambye, Lin, Notari, Papucci, Strumia; Bajc, nemevsek, Senjanovic; Dorsner, Fileviez-Perez ++

Liu, Segré; Flanz, Paschos, Sarkar; Covi, Roulet, Vissani; Pilaftsis

Fukugida, Yanagida

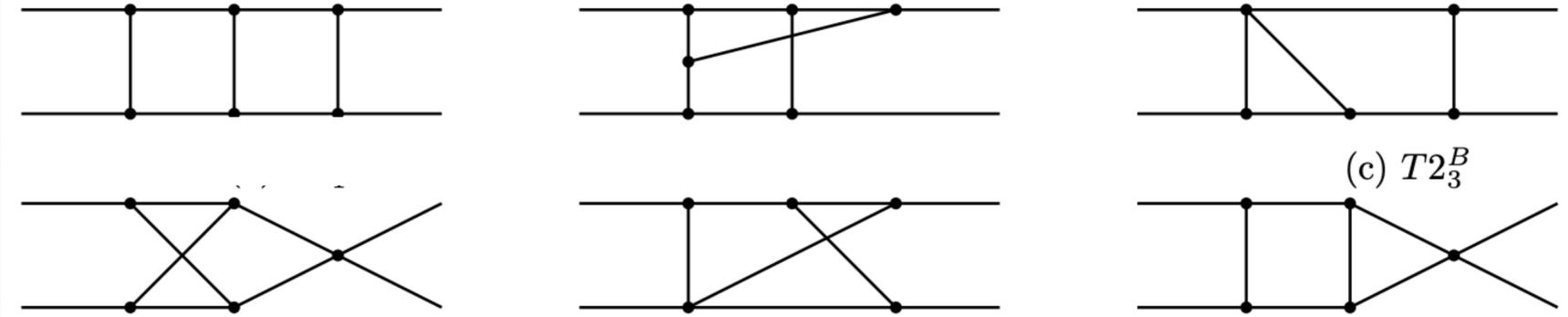
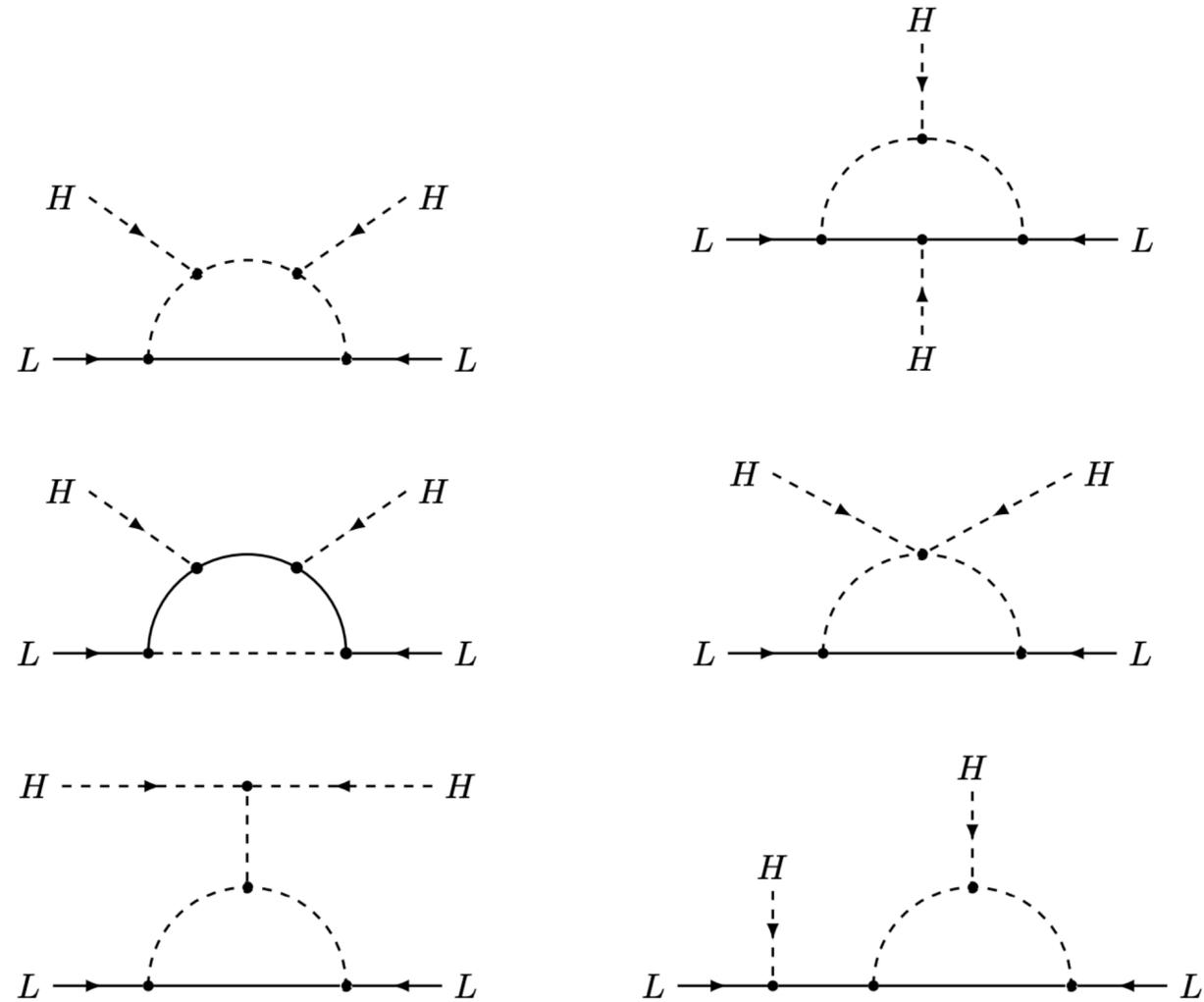
Bonus: gateway to explain baryon asymmetry of the Universe  
Shakarov's conditions  $\Rightarrow$  Leptogenesis



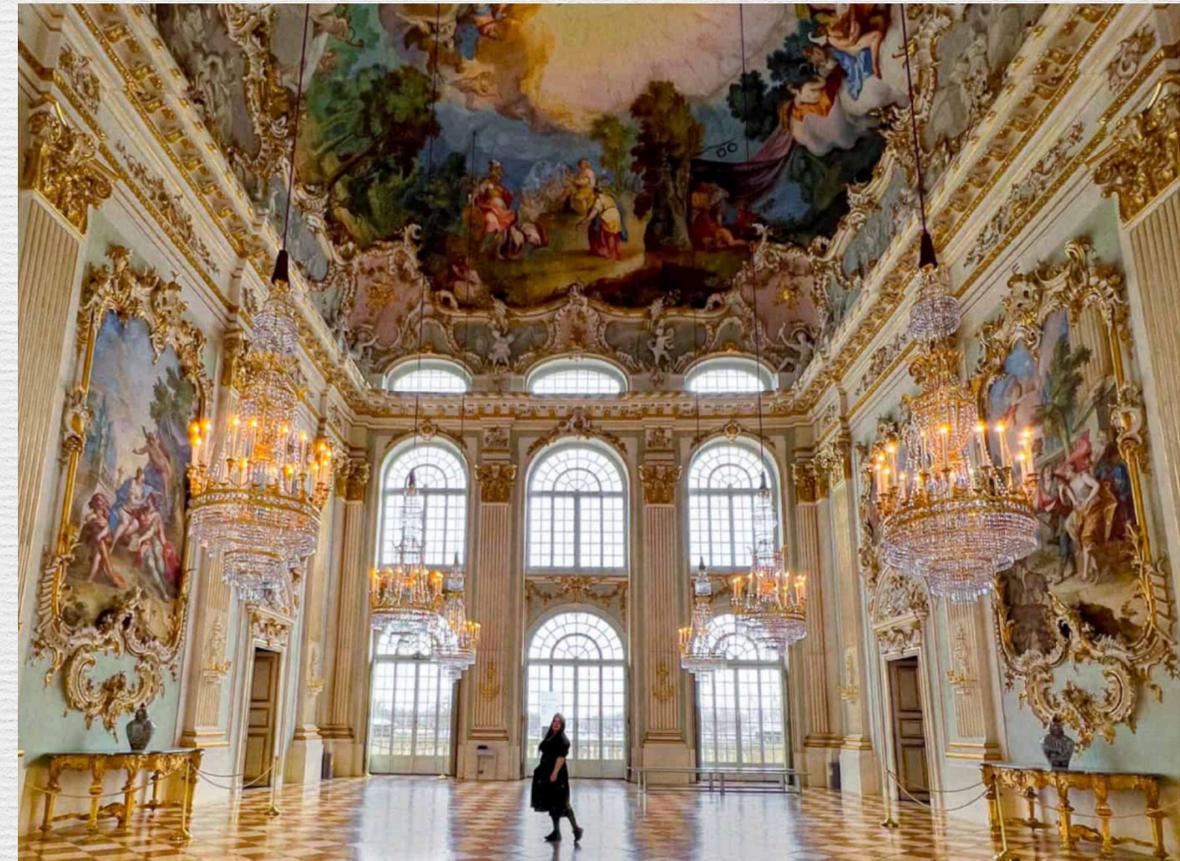
# Neutrino mass models: “Baroque”

One-loop@ dimension-5:

Two-loop@ dimension-5:



Things only get more baroque from here!



# How to probe neutrino mass mechanisms?

Too many possibilities of realising the Majorana neutrino masses

type I, II, III seesaw, low-scale seesaws, n-loop radiative models, Left-Right Symmetric Model, 3-3-1 Model ++



**High-scale:  $10^{(10-15)}$  GeV**

theoretically natural  $Y_\nu \lesssim \mathcal{O}(1)$  + unification

Vanilla high-scale leptogenesis

New states decoupled: hard to test!

**Low-scale: KeV - tens of TeV**

small  $Y_\nu$  / approximate LNC/ loop suppression

Leptogenesis via resonant/oscillation

New states within experimental reach

**How to probe so many different neutrino mass model possibilities?**

Effective Field Theory approach “dim by dim” provides a robust option

✓ **Model Independent**

✗ **Direct NP signatures**

e.g. **Resonant NP production:**  
**simplified model approach**

# Effective Field Theory

An EFT is the set of all “**allowed**” local operators with mass dimension less than some maximum one

$$\mathcal{L} = \sum_i c_i O_i$$

$$[O_i] = d_i$$

→

$$c_i \sim \frac{1}{\Lambda^{d_i-4}}$$

Consider a nonrenormalisable operator ( $d > 4$ ) :  $\mathcal{O}_5$  with  $d = 5$

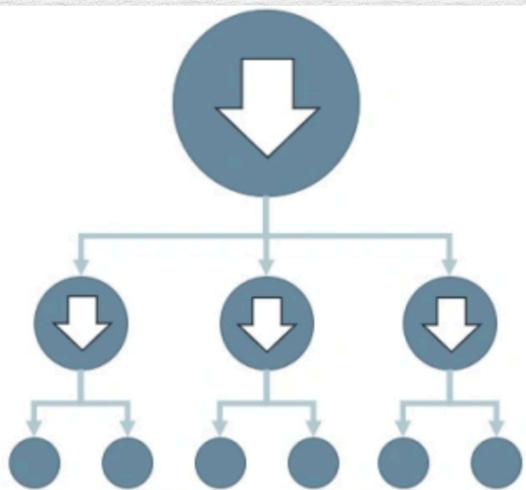
It will generate divergences at higher dimension. Example: a loop with two insertions of  $\mathcal{O}_5$  will diverge as  $\left(\frac{p^2}{\Lambda^2}\right) \Rightarrow$  requiring a counter-term with  $d=6$ .

$\Rightarrow$  we need an infinite # of operators to absorb all the divergences

Appelquist, Carrazzone ++

**Fortunately nature decouples:** (i) there are no “+ve” powers of heavy scale ( $M$ ), except in log’s  
(ii)  $\log M$  can be absorbed into  $c_i$ ’s

# Connecting EFTs to Experiments



Top-down

UV known:  
match onto the EFT **1**

set constraints  
with this simplified  
parameterization **2**

**1**

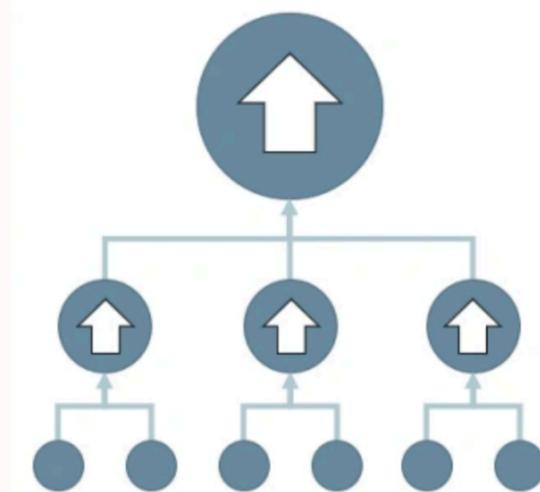
**2**



Bottom-up

**2** infer properties  
of the UV sector  
(unknown)

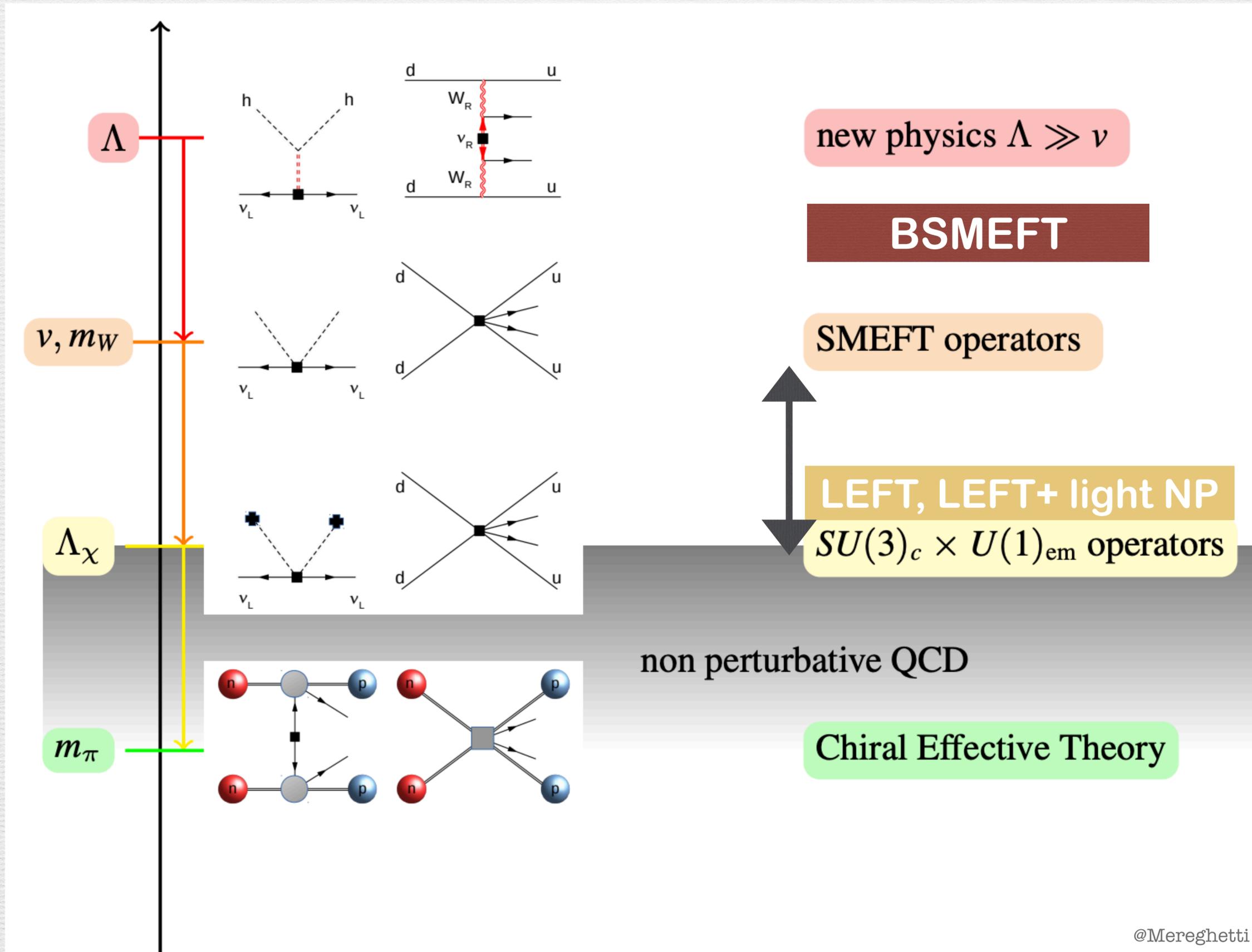
**1** constrain the EFT in a  
model independent way



accessible  $E$

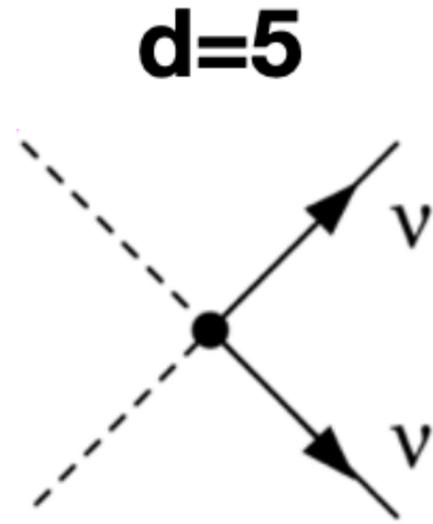
$(\bar{e}_L \gamma_\mu e_L)(\bar{e}_L \gamma^\mu e_L)$	$(\bar{\psi} \psi)^2$	$(\bar{\psi} \psi)(\bar{l}_R e_R)$	$(\bar{\psi} \psi)(\bar{\psi} \psi)$
$(\bar{u}_L \gamma_\mu u_L)(\bar{u}_L \gamma^\mu u_L)$	$(\bar{b}_L c_L)(\bar{d}_L d_L)$	$(\bar{\psi} \psi)(\bar{b}_L u_L)$	$(\bar{\psi} D^\mu \psi)^* (\bar{\psi} D_\mu \psi)$
$(\bar{d}_L \gamma_\mu d_L)(\bar{d}_L \gamma^\mu d_L)$	$(\bar{q}_L^c u_L) c_{23} (\bar{q}_L^c d_L)$	$(\bar{\psi} \psi)(\bar{q}_L d_L)$	$(\bar{l}_R \gamma_\mu l_R)(\bar{l}_R \gamma^\mu l_R)$
$(\bar{e}_L \gamma_\mu e_L)(\bar{u}_L \gamma^\mu u_L)$	$(\bar{q}_L^c T^A u_L) c_{23} (\bar{q}_L^c T^A d_L)$	$f^{ABC} C_{\mu\nu}^A C_{\nu\rho}^B C_{\rho\mu}^C$	$(\bar{q}_L \gamma_\mu \bar{q}_L)(\bar{q}_L \gamma^\mu \bar{q}_L)$
$(\bar{e}_L \gamma_\mu e_L)(\bar{d}_L \gamma^\mu d_L)$	$(\bar{b}_L c_L) c_{23} (\bar{q}_L^c u_L)$	$f^{ABC} \bar{C}_{\mu\nu}^A C_{\nu\rho}^B C_{\rho\mu}^C$	$(\bar{l}_R \gamma_\mu l_R)(\bar{l}_R \gamma^\mu l_R)$
$(\bar{u}_L \gamma_\mu u_L)(\bar{d}_L \gamma^\mu d_L)$	$(\bar{l}_L^c \sigma_{\mu\nu} e_L) (\bar{l}_L^c \sigma^{\mu\nu} u_L)$	$f^{ABC} W_{\mu\nu}^A W_{\nu\rho}^B W_{\rho\mu}^C$	$(\bar{l}_R \gamma_\mu l_R)(\bar{q}_L \gamma^\mu \bar{q}_L)$
$(\bar{l}_R \sigma^{\mu\nu} e_R) \bar{l}_R W_{\mu\nu}^I$	$(\bar{\psi} i \bar{D}_\mu \psi) (\bar{l}_R \gamma^\mu l_R)$	$\psi^\dagger \psi W_{\mu\nu}^A W^{\mu\nu A}$	$(\bar{l}_R \gamma_\mu l_R)(\bar{e}_L \gamma^\mu e_L)$
$(\bar{l}_R \sigma^{\mu\nu} e_R) \bar{l}_R B_{\mu\nu}$	$(\bar{\psi} i \bar{D}_\mu \psi) (\bar{q}_L \gamma^\mu q_L)$	$\psi^\dagger \psi C_{\mu\nu}^A C^{\mu\nu A}$	$(\bar{l}_R \gamma_\mu l_R)(\bar{u}_L \gamma^\mu u_L)$
$(\bar{q}_L \sigma^{\mu\nu} T^A u_L) \bar{q}_L C_{\mu\nu}^A$	$(\bar{\psi} i \bar{D}_\mu \psi) (\bar{e}_L \gamma^\mu e_L)$	$\psi^\dagger \psi W_{\mu\nu}^A W^{\mu\nu A}$	$(\bar{l}_R \gamma_\mu l_R)(\bar{d}_L \gamma^\mu d_L)$
$(\bar{q}_L \sigma^{\mu\nu} u_L) \bar{q}_L W_{\mu\nu}^I$	$(\bar{\psi} i \bar{D}_\mu \psi) (\bar{q}_L \gamma^\mu \bar{q}_L)$	$\psi^\dagger \psi \bar{W}_{\mu\nu}^I W^{\mu\nu I}$	$(\bar{q}_L \gamma_\mu \bar{q}_L)(\bar{e}_L \gamma^\mu e_L)$
$(\bar{q}_L \sigma^{\mu\nu} u_L) \bar{q}_L B_{\mu\nu}$	$(\bar{\psi} i \bar{D}_\mu \psi) (\bar{q}_L \gamma^\mu u_L)$	$\psi^\dagger \psi B_{\mu\nu} B^{\mu\nu}$	$(\bar{q}_L \gamma_\mu \bar{q}_L)(\bar{u}_L \gamma^\mu u_L)$
$(\bar{q}_L \sigma^{\mu\nu} T^A d_L) \bar{q}_L C_{\mu\nu}^A$	$(\bar{\psi} i \bar{D}_\mu \psi) (\bar{u}_L \gamma^\mu u_L)$	$\psi^\dagger \psi \bar{B}_{\mu\nu} B^{\mu\nu}$	$(\bar{q}_L \gamma_\mu \bar{q}_L)(\bar{u}_L \gamma^\mu T^A u_L)$
$(\bar{q}_L \sigma^{\mu\nu} d_L) \bar{q}_L W_{\mu\nu}^I$	$(\bar{\psi} i \bar{D}_\mu \psi) (\bar{d}_L \gamma^\mu d_L)$	$\psi^\dagger \psi W_{\mu\nu}^I B^{\mu\nu I}$	$(\bar{q}_L \gamma_\mu \bar{q}_L)(\bar{d}_L \gamma^\mu d_L)$
$(\bar{q}_L \sigma^{\mu\nu} d_L) \bar{q}_L B_{\mu\nu}$	$i(\bar{\psi} D_\mu \psi) (\bar{u}_L \gamma^\mu d_L)$	$\psi^\dagger \psi W_{\mu\nu}^I B^{\mu\nu I}$	$(\bar{q}_L \gamma_\mu \bar{q}_L)(\bar{d}_L \gamma^\mu T^A d_L)$

# Some popular EFTs for BSM Phenomenology

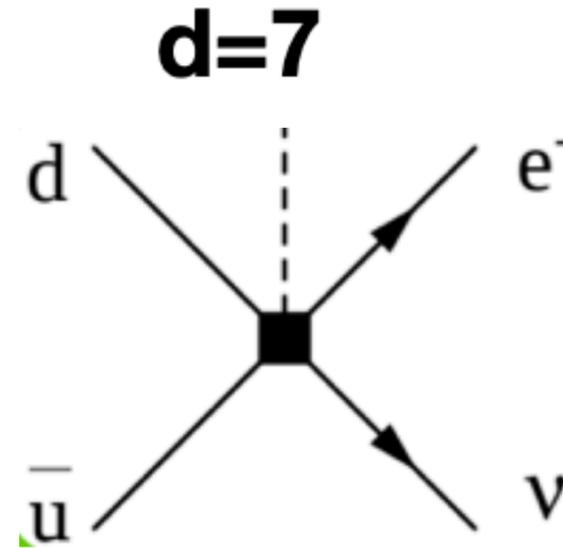


# Lepton Number Violation and SMEFT

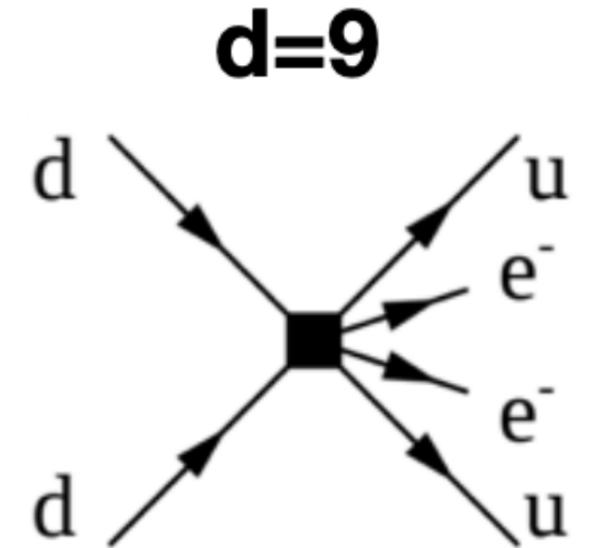
## LNV SMEFT:



Weinberg '79



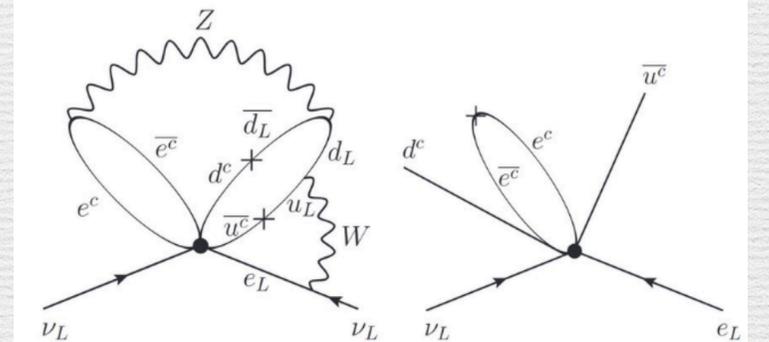
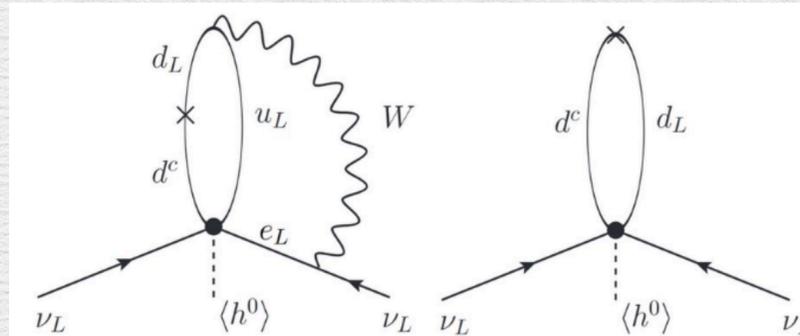
Babu and Leung '01  
de Gouvea and Jenkins '08  
Lehman '14



M. Graesser '16  
Y. Liao and X. D. Ma '20

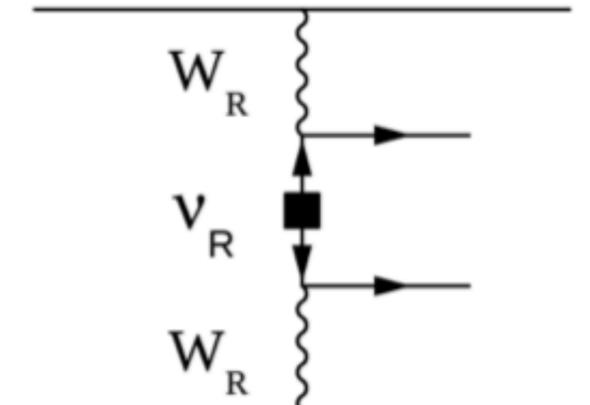
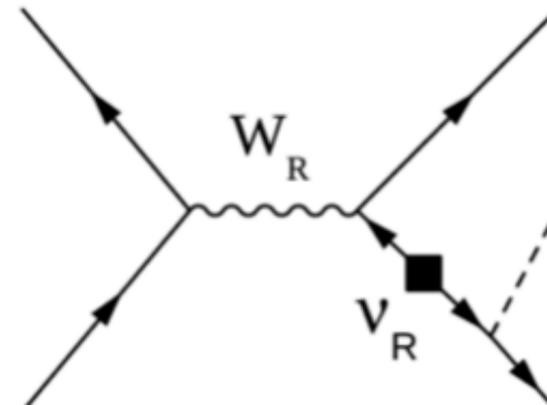
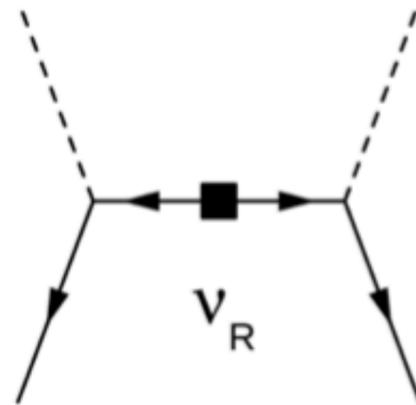
## Neutrino mass:

$$\frac{1}{\Lambda} \epsilon_{ij} \epsilon_{mn} L_i^T C L_m H_j H_n \rightarrow \frac{v^2}{\Lambda} \nu_L^T C \nu_L$$



## UV example:

LRSM: (L $\leftrightarrow$ R) at high scale  
*Mohapatra and Pati '75*  
*Senjanovic and Mohapatra '75*



# Lepton Number Violating dimension-7 SMEFT operators

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + C_5 \mathcal{O}_5 + \sum_i C_7^i \mathcal{O}_7^i + \sum_i C_9^i \mathcal{O}_9^i + \dots$$

d=7: 12 Independent operator with  $\Delta L = 2$

First systematic analysis:

Lehman '14

-> 20 independent operators

13 conserving B but  $\Delta L = 2$

7 violating both  $\Delta B = -\Delta L = -1$

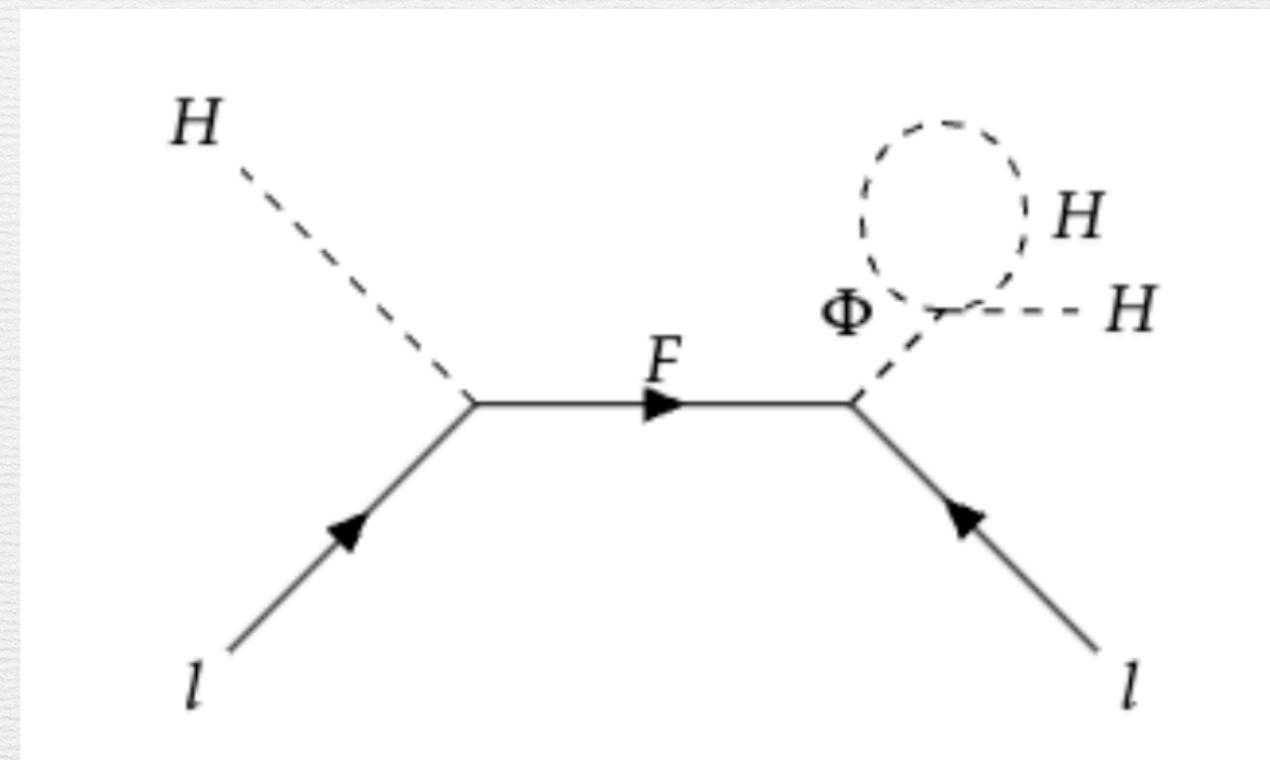
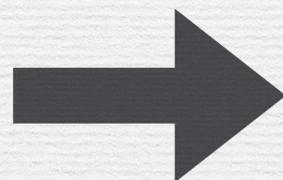
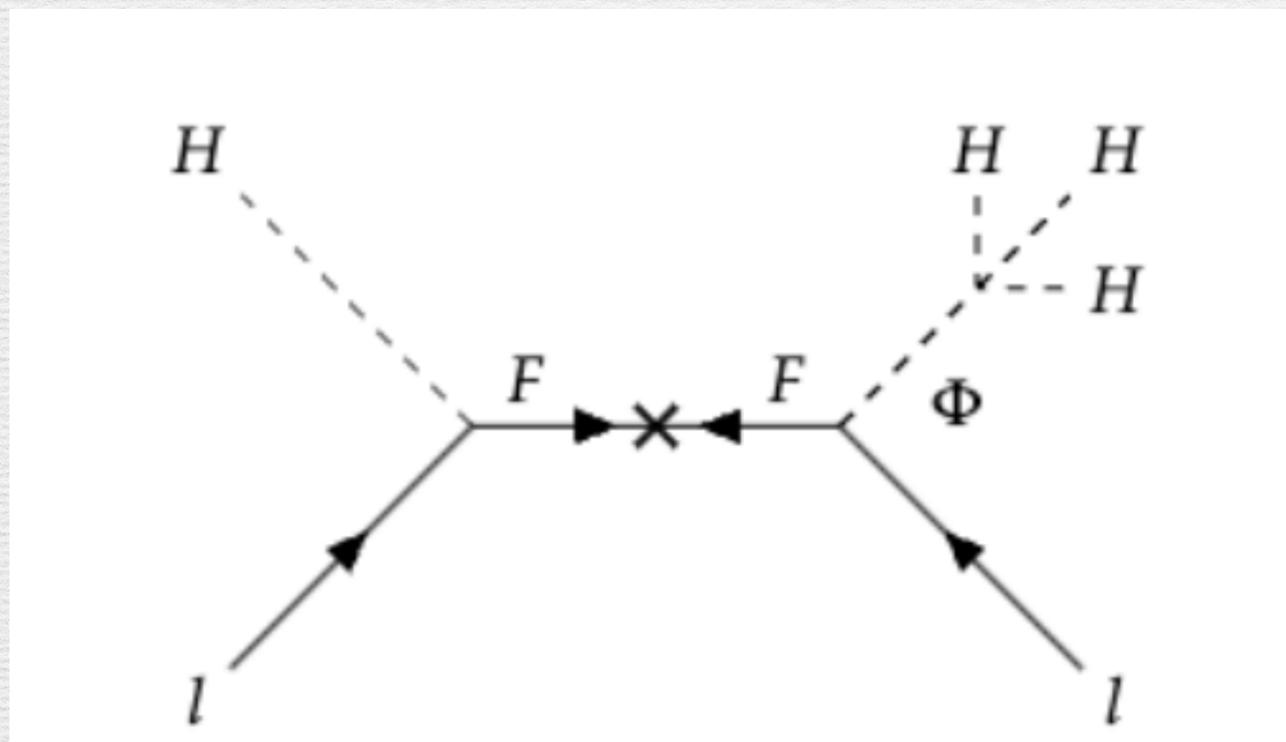
Further reduced in

Liao, Ma '17

18 = 12+6 (indept. structures)

Type	$\mathcal{O}$	Operator
$\Psi^2 H^4$	$\mathcal{O}_{LH}^{pr}$	$\epsilon_{ij}\epsilon_{mn} (\overline{L}_p^{ci} L_r^m) H^j H^n (H^\dagger H)$
$\Psi^2 H^3 D$	$\mathcal{O}_{LeHD}^{pr}$	$\epsilon_{ij}\epsilon_{mn} (\overline{L}_p^{ci} \gamma_\mu e_r) H^j (H^m i D^\mu H^n)$
$\Psi^2 H^2 D^2$	$\mathcal{O}_{LHD1}^{pr}$	$\epsilon_{ij}\epsilon_{mn} (\overline{L}_p^{ci} D_\mu L_r^j) (H^m D^\mu H^n)$
	$\mathcal{O}_{LHD2}^{pr}$	$\epsilon_{im}\epsilon_{jn} (\overline{L}_p^{ci} D_\mu L_r^j) (H^m D^\mu H^n)$
$\Psi^2 H^2 X$	$\mathcal{O}_{LHB}^{pr}$	$g\epsilon_{ij}\epsilon_{mn} (\overline{L}_p^{ci} \sigma_{\mu\nu} L_r^m) H^j H^n B^{\mu\nu}$
	$\mathcal{O}_{LHW}^{pr}$	$g'\epsilon_{ij} (\epsilon\tau^I)_{mn} (\overline{L}_p^{ci} \sigma_{\mu\nu} L_r^m) H^j H^n W^{I\mu\nu}$
$\Psi^4 D$	$\mathcal{O}_{\bar{d}uLLD}^{prst}$	$\epsilon_{ij} (\overline{d}_p \gamma_\mu u_r) (\overline{L}_s^{ci} i D^\mu L_t^j)$
$\Psi^4 H$	$\mathcal{O}_{\bar{e}LLLH}^{prst}$	$\epsilon_{ij}\epsilon_{mn} (\overline{e}_p L_r^i) (\overline{L}_s^{cj} L_t^m) H^n$
	$\mathcal{O}_{\bar{d}LueH}^{prst}$	$\epsilon_{ij} (\overline{d}_p L_r^i) (\overline{u}_s^c e_t) H^j$
	$\mathcal{O}_{\bar{d}LQLH1}^{prst}$	$\epsilon_{ij}\epsilon_{mn} (\overline{d}_p L_r^i) (\overline{Q}_s^{cj} L_t^m) H^n$
	$\mathcal{O}_{\bar{d}LQLH2}^{prst}$	$\epsilon_{im}\epsilon_{jn} (\overline{d}_p L_r^i) (\overline{Q}_s^{cj} L_t^m) H^n$
	$\mathcal{O}_{\bar{Q}uLLH}^{prst}$	$\epsilon_{ij} (\overline{Q}_p u_r) (\overline{L}_s^c L_t^i) H^j$

# Why dimension-7 SMEFT operators?


 $\mathcal{O}_{LH}^{pr}$ 

$$\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^{ci}L_r^m)H^jH^n(H^\dagger H)$$

# Matching dimension-7 SMEFT operators with LEFT operators

Bottom-up recipe:

Experimental observable



Constraints on LEFT

(Single operator dominance)



Constraints on SMEFT

(Using matching relations)



UV theory

! Highly simplified !

! No correlations and cancellations !

$O$	Operator	Matching
$O_{ev;LL}^{S,prst}$	$(\overline{e_{Rp}}e_{Lr})(\overline{\nu_s^c}\nu_t)$	$\frac{4G_F}{\sqrt{2}}c_{ev;LL}^{S,prst} = -\frac{\sqrt{2}v}{8}(2C_{\bar{e}LLLH}^{prst} + C_{\bar{e}LLLH}^{psrt} + s \leftrightarrow t)$
$O_{ev;RL}^{S,prst}$	$(\overline{e_{Lp}}e_{Rr})(\overline{\nu_s^c}\nu_t)$	$\frac{4G_F}{\sqrt{2}}c_{ev;RL}^{S,prst} = -\frac{\sqrt{2}v}{2}(C_{LeHD}^{sr}\delta^{tp} + C_{LeHD}^{tr}\delta^{sp})$
$O_{ev;LL}^{T,prst}$	$(\overline{e_{Rp}}\sigma_{\mu\nu}e_{Lr})(\overline{\nu_s^c}\sigma^{\mu\nu}\nu_t)$	$\frac{4G_F}{\sqrt{2}}c_{ev;LL}^{T,prst} = +\frac{\sqrt{2}v}{32}(C_{\bar{e}LLLH}^{psrt} - C_{\bar{e}LLLH}^{ptrs})$
$O_{dv;LL}^{S,prst}$	$(\overline{d_{Rp}}d_{Lr})(\overline{\nu_s^c}\nu_t)$	$\frac{4G_F}{\sqrt{2}}c_{dv;LL}^{S,prst} = -\frac{\sqrt{2}v}{8}V_{xr}(C_{\bar{d}LQLH1}^{ptxs} + C_{\bar{d}LQLH1}^{psxt})$
$O_{dv;LL}^{T,prst}$	$(\overline{d_{Rp}}\sigma_{\mu\nu}d_{Lr})(\overline{\nu_s^c}\sigma^{\mu\nu}\nu_t)$	$\frac{4G_F}{\sqrt{2}}c_{dv;LL}^{T,prst} = -\frac{\sqrt{2}v}{32}V_{xr}(C_{\bar{d}LQLH1}^{ptxs} - C_{\bar{d}LQLH1}^{psxt})$
$O_{uv;RL}^{S,prst}$	$(\overline{u_{Lp}}u_{Rr})(\overline{\nu_s^c}\nu_t)$	$\frac{4G_F}{\sqrt{2}}c_{uv;RL}^{S,prst} = +\frac{\sqrt{2}v}{4}(C_{\bar{Q}uLLH}^{prst} + C_{\bar{Q}uLLH}^{ptrs})$
$O_{duve;LL}^{S,prst}$	$(\overline{d_{Rp}}u_{Lr})(\overline{\nu_s^c}e_{Lt})$	$\frac{4G_F}{\sqrt{2}}c_{duve;LL}^{S,prst} = +\frac{\sqrt{2}v}{8}(2C_{\bar{d}LQLH1}^{ptrs} + C_{\bar{d}LQLH2}^{ptrs} - C_{\bar{d}LQLH2}^{psrt})$
$O_{duve;RL}^{S,prst}$	$(\overline{d_{Lp}}u_{Rr})(\overline{\nu_s^c}e_{Lt})$	$\frac{4G_F}{\sqrt{2}}c_{duve;RL}^{S,prst} = +\frac{\sqrt{2}v}{2}V_{xp}^*C_{\bar{Q}uLLH}^{xrts}$
$O_{duve;LL}^{T,prst}$	$(\overline{d_{Rp}}\sigma_{\mu\nu}u_{Lr})(\overline{\nu_s^c}\sigma^{\mu\nu}e_{Lt})$	$\frac{4G_F}{\sqrt{2}}c_{duve;LL}^{T,prst} = +\frac{\sqrt{2}v}{32}(2C_{\bar{d}LQLH1}^{ptrs} + C_{\bar{d}LQLH2}^{ptrs} + C_{\bar{d}LQLH2}^{psrt})$
$O_{duve;LR}^{V,prst}$	$(\overline{d_{Lp}}\gamma_\mu u_{Lr})(\overline{\nu_s^c}\gamma^\mu e_{Rt})$	$\frac{4G_F}{\sqrt{2}}c_{duve;LR}^{V,prst} = +\frac{\sqrt{2}v}{2}V_{rp}^*C_{LeHD}^{st}$
$O_{duve;RR}^{V,prst}$	$(\overline{d_{Rp}}\gamma_\mu u_{Rr})(\overline{\nu_s^c}\gamma^\mu e_{Rt})$	$\frac{4G_F}{\sqrt{2}}c_{duve;RR}^{V,prst} = +\frac{\sqrt{2}v}{4}C_{\bar{d}LueH}^{psrt}$
$O_{dv;RL}^{S,prst}$	$(\overline{d_{Lp}}d_{Rr})(\overline{\nu_s^c}\nu_t)$	Not induced by $d = 7 \Delta L = 2$ SMEFT operators
$O_{uv;LL}^{S,prst}$	$(\overline{u_{Rp}}u_{Lr})(\overline{\nu_s^c}\nu_t)$	
$O_{uv;LL}^{T,prst}$	$(\overline{u_{Rp}}\sigma_{\mu\nu}u_{Lr})(\overline{\nu_s^c}\sigma^{\mu\nu}\nu_t)$	

SMEFT &  $0\nu\beta\beta$

# Neutrinoless double beta decay

$$(A, Z) \rightarrow (A, Z + 2) + 2 e^{-} + Q_{\beta\beta}$$

Half life

$$T_{1/2}^{0\nu} = (G |\mathcal{M}|^2 \langle m_{\beta\beta} \rangle^2)^{-1} \simeq 10^{27-28} \left( \frac{0.01 \text{ eV}}{\langle m_{\beta\beta} \rangle} \right)^2 \text{ y}$$

Cirigliano, Dekens, de Vries, Graesser, Mereghetti (2018)

Graf, Deppisch, Iachello, Kotila (2018)++

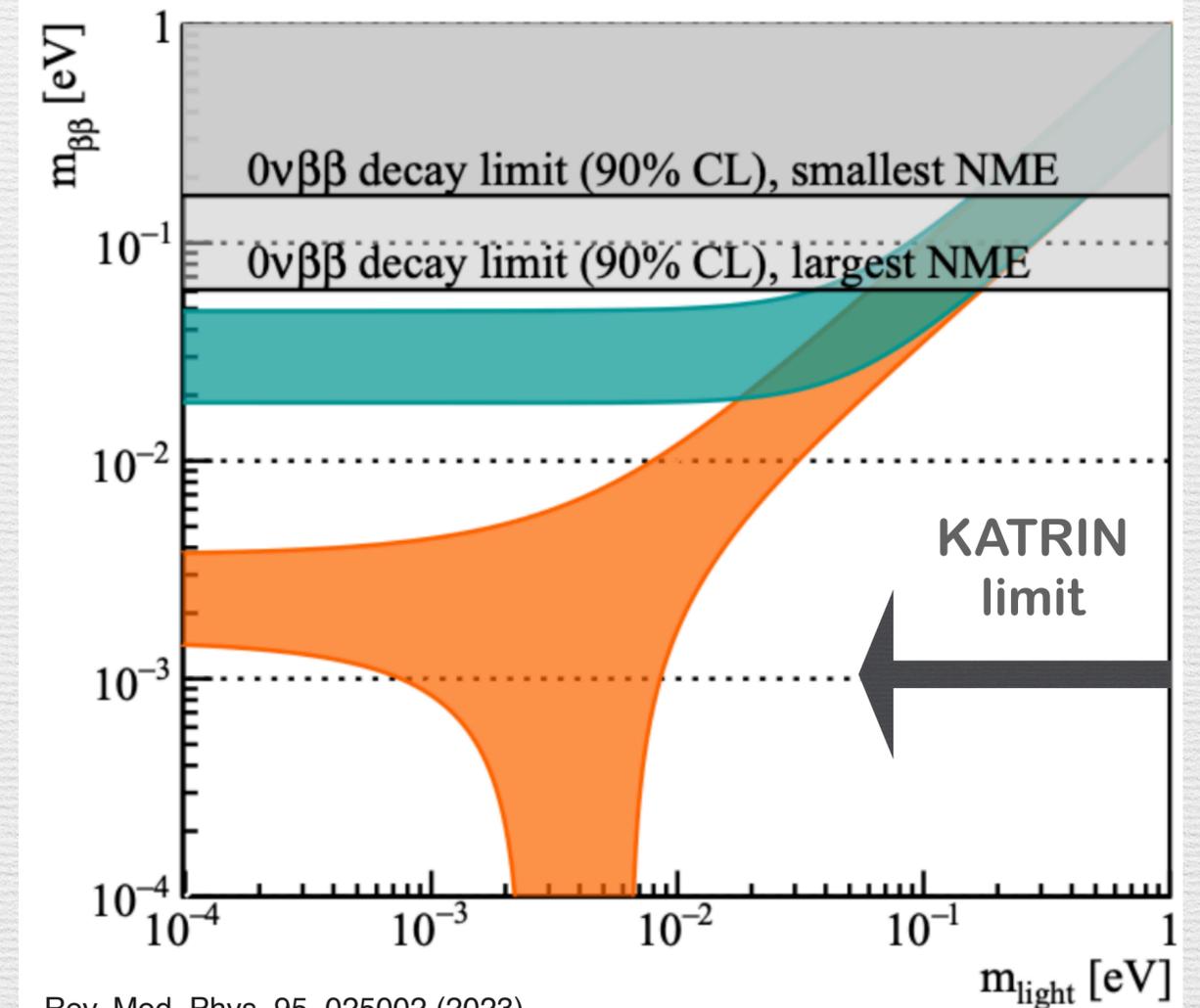
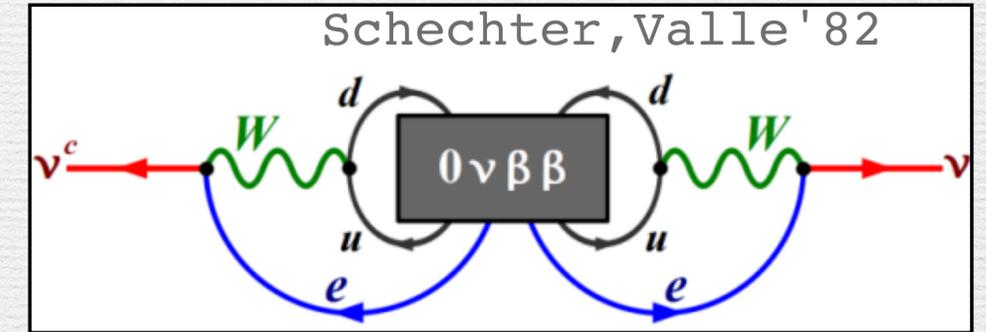
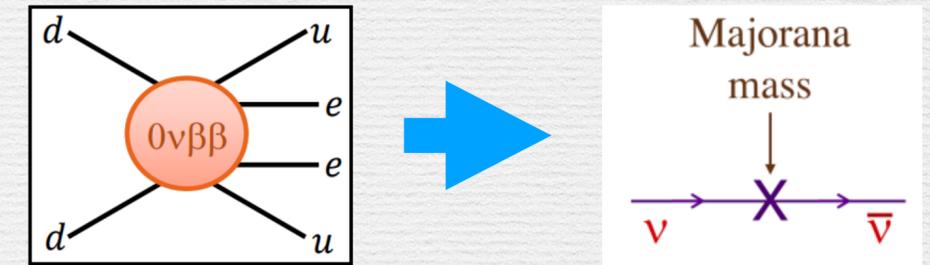
Effective mass

$$\langle m_{\beta\beta} \rangle = |U_{ei}^2 m_i|$$

Many experiments: KamLAND-Zen, LEGEND, CUORE, NEMO-3, ...

Main source of uncertainty: Nuclear Matrix elements!

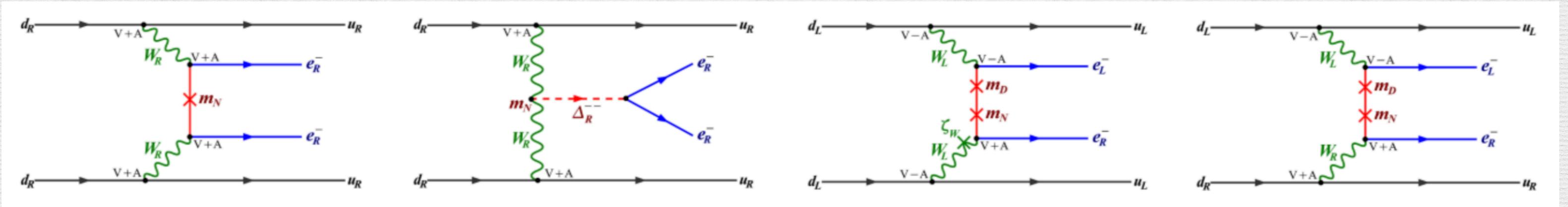
- Non-relativistic expansion or  $\chi$ -EFT
- Many body problem: isotope and operator dependent
- Different nuclear models



# Neutrinoless double beta decay

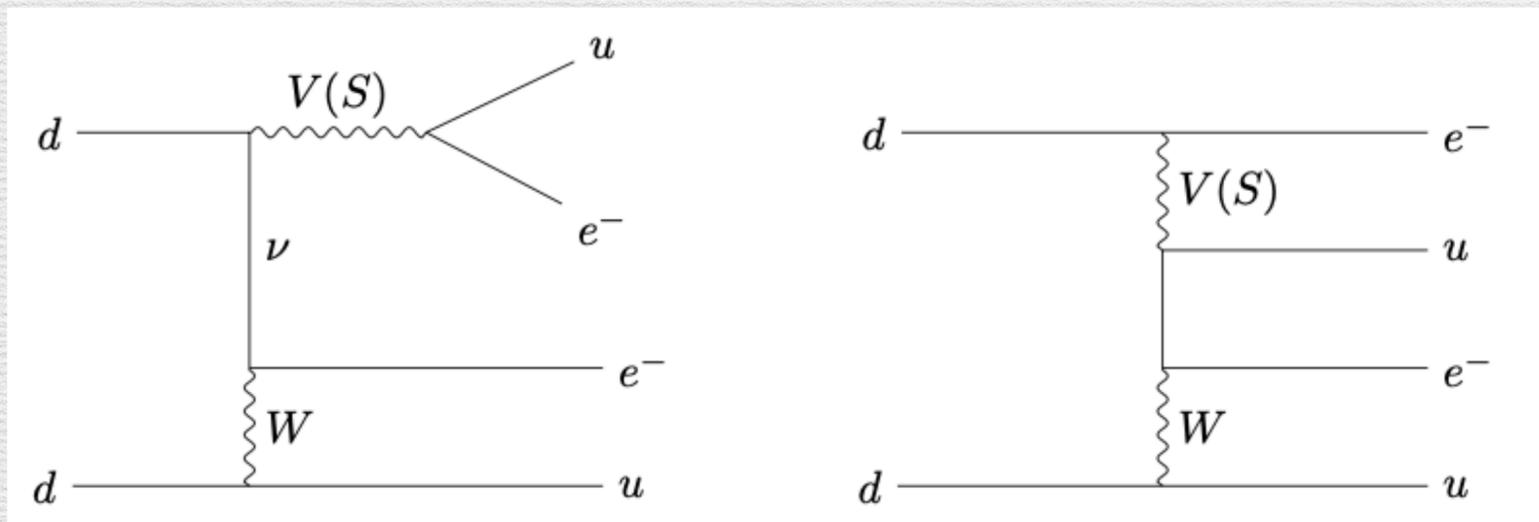
Many new physics scenarios can be responsible:

Left-Right Symmetric Model :  $SU(3)_C \otimes SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L}$



Deppisch, Hirsch, Päs '12

scalar and vector Leptoquarks:



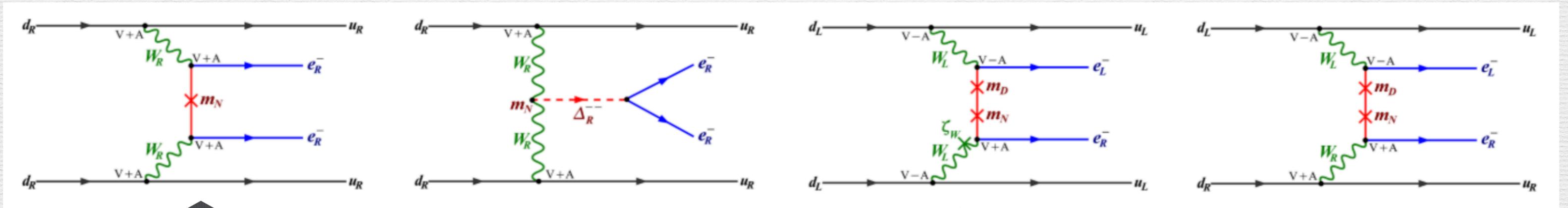
**EFT approach helps!**

RPV SUSY, Extra Dimensions, ++

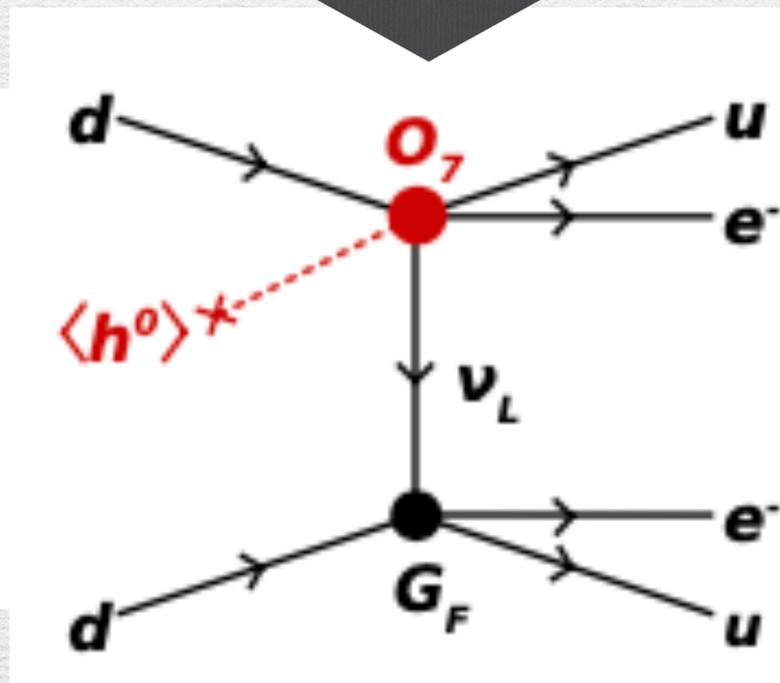
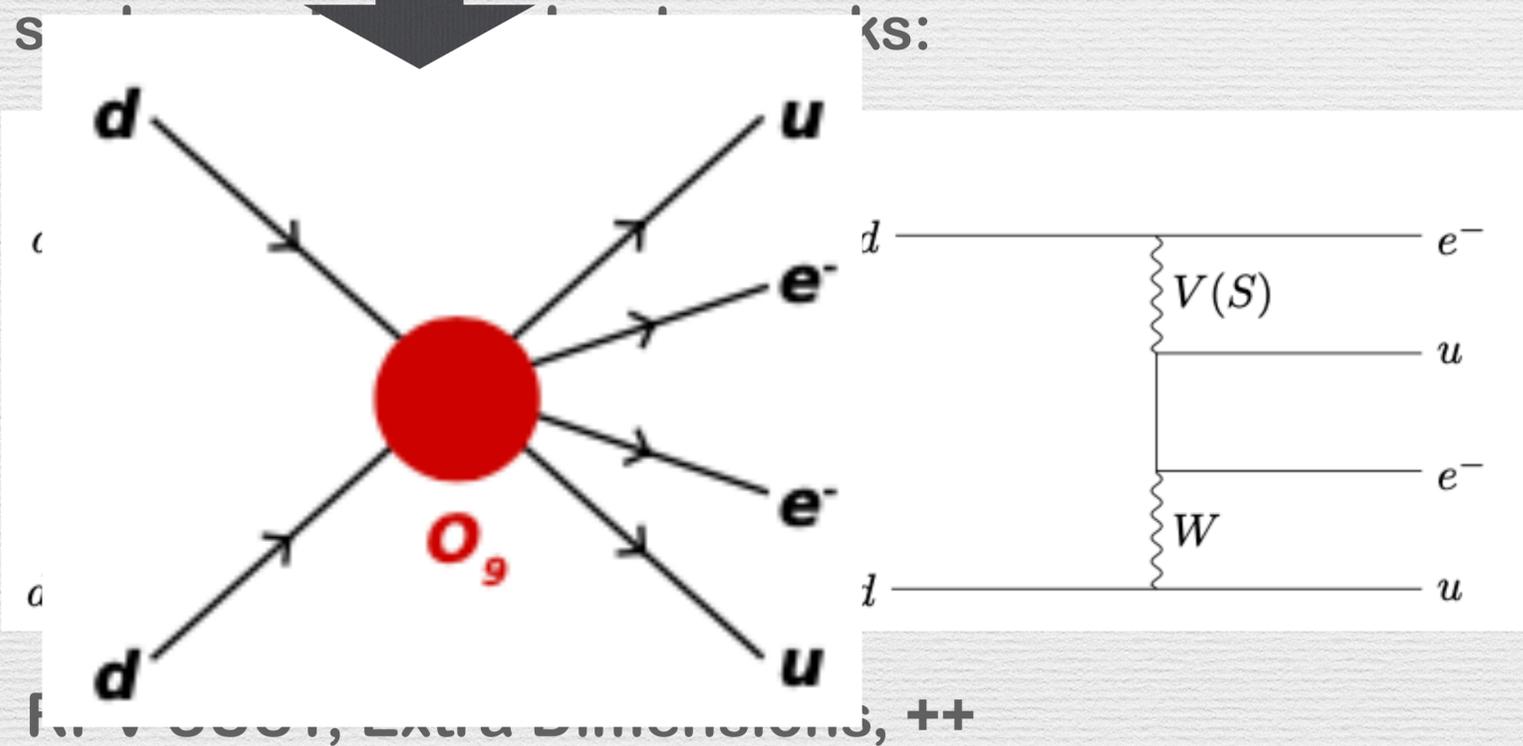
# Neutrinoless double beta decay

Many new physics scenarios can be responsible:

Left-Right Symmetric Model :  $SU(3)_C \otimes SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L}$



Deppisch, Hirsch, Päs '12



for  $V=SU(2)$ , Extra Dimensions, ++

# Neutrinoless double beta decay: EFT approach

Start from SMEFT and match to LEFT:

$$\mathcal{L}_{\Delta L=2}^{\text{LEFT}(d=6)} = \frac{4G_F}{\sqrt{2}} \left[ c_{duve;LR}^V (\bar{d}_L \gamma_\mu u_L) (\bar{\nu}^c \gamma^\mu e_R) + c_{duve;RR}^V (\bar{d}_R \gamma_\mu u_R) (\bar{\nu}^c \gamma^\mu e_R) \right. \\ \left. + c_{duve;LL}^S (\bar{d}_R u_L) (\bar{\nu}^c e_L) + c_{duve;RL}^S (\bar{d}_L u_R) (\bar{\nu}^c e_L) \right. \\ \left. + c_{duve;LL}^T (\bar{d}_R \sigma_{\mu\nu} u_L) (\bar{\nu}^c \sigma^{\mu\nu} e_L) \right] + \text{h.c.},$$

$$\mathcal{L}_{\Delta L=2}^{\text{LEFT}(d=7)} = \frac{4G_F}{\sqrt{2}v} \left[ c_{duve;LL}^{(7)V} (\bar{d}_L \gamma^\mu u_L) (\bar{\nu}_L^c \overleftrightarrow{D}_\mu e_L) + c_{duve;RL}^{(7)V} (\bar{d}_R \gamma^\mu u_R) (\bar{\nu}_L^c \overleftrightarrow{D}_\mu e_L) \right] + \text{h.c.}$$

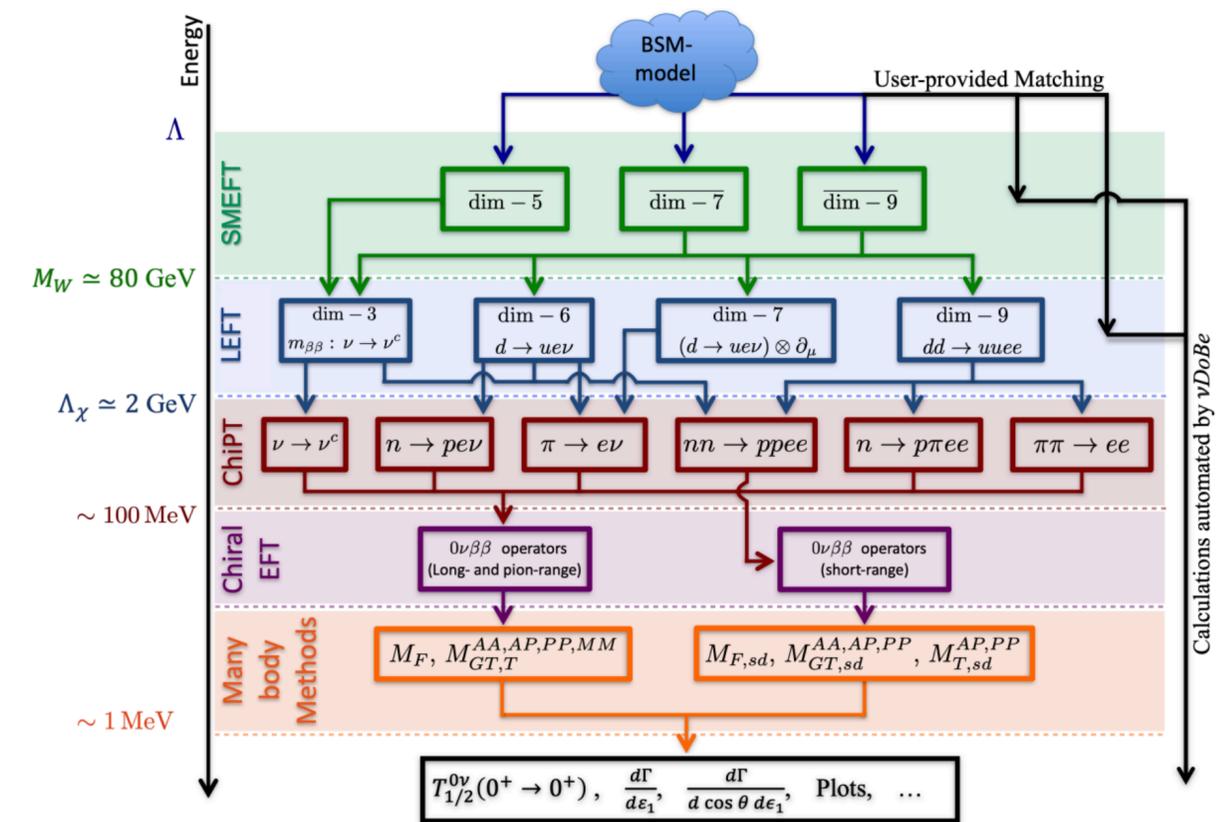
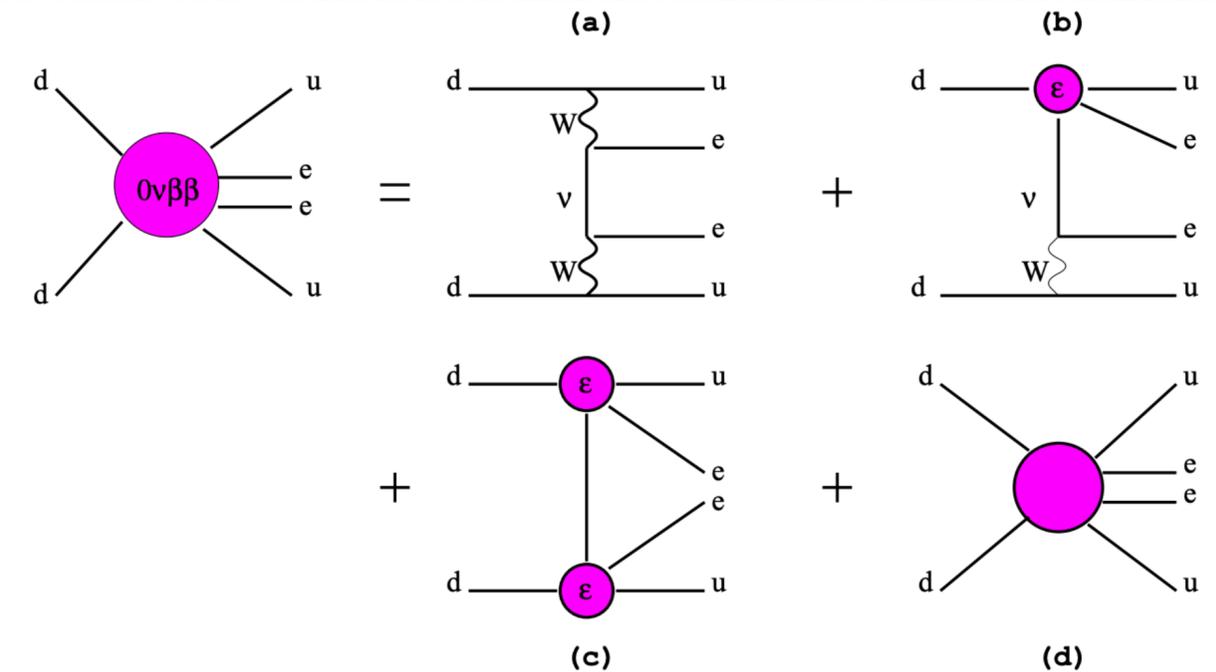
$$\mathcal{L}_{\Delta L=2}^{\text{LEFT}(d=9)} = \frac{8G_F^2}{v} \bar{e}_{L,i} C \bar{e}_{L,j}^T \left\{ c_{V;LL}^{(9);ij} \bar{u}_L \gamma^\mu d_L \bar{u}_L \gamma_\mu d_L + c_{V;LR}^{(9);ij} \bar{u}_L \gamma^\mu d_L \bar{u}_R \gamma_\mu d_R \right. \\ \left. + c_{V';LR}^{(9);ij} \bar{u}_L^\alpha \gamma^\mu d_L^\beta \bar{u}_R^\beta \gamma_\mu d_R^\alpha \right\} + \text{h.c.}$$

Automatization possibilities!

Scholer, de Vries, Graf '23

Multiple isotopes and correlations

Possibility to distinguish different mechanisms and operators



# LNV dim-7 SMEFT @Neutrinoless double beta decay

$\mathcal{O}$	Operator
$\mathcal{O}_{LH}^{pr}$	$\epsilon_{ij}\epsilon_{mn}(\bar{L}_p^{ci}L_r^m)H^jH^n(H^\dagger H)$
$\mathcal{O}_{LeHD}^{pr}$	$\epsilon_{ij}\epsilon_{mn}(\bar{L}_p^{ci}\gamma_\mu e_r)H^j(H^m iD^\mu H^n)$
$\mathcal{O}_{LHD1}^{pr}$	$\epsilon_{ij}\epsilon_{mn}(\bar{L}_p^{ci}D_\mu L_r^j)(H^m D^\mu H^n)$
$\mathcal{O}_{LHD2}^{pr}$	$\epsilon_{im}\epsilon_{jn}(\bar{L}_p^{ci}D_\mu L_r^j)(H^m D^\mu H^n)$
$\mathcal{O}_{LHB}^{pr}$	$g\epsilon_{ij}\epsilon_{mn}(\bar{L}_p^{ci}\sigma_{\mu\nu}L_r^m)H^jH^n B^{\mu\nu}$
$\mathcal{O}_{LHW}^{pr}$	$g'\epsilon_{ij}(\epsilon\tau^I)_{mn}(\bar{L}_p^{ci}\sigma_{\mu\nu}L_r^m)H^jH^n W^{I\mu\nu}$
$\mathcal{O}_{\bar{d}uLLD}^{prst}$	$\epsilon_{ij}(\bar{d}_p\gamma_\mu u_r)(\bar{L}_s^{ci}iD^\mu L_t^j)$
$\mathcal{O}_{\bar{e}LLLH}^{prst}$	$\epsilon_{ij}\epsilon_{mn}(\bar{e}_p L_r^i)(\bar{L}_s^{cj}L_t^m)H^n$
$\mathcal{O}_{\bar{d}LueH}^{prst}$	$\epsilon_{ij}(\bar{d}_p L_r^i)(\bar{u}_s^c e_t)H^j$
$\mathcal{O}_{\bar{d}LQLH1}^{prst}$	$\epsilon_{ij}\epsilon_{mn}(\bar{d}_p L_r^i)(\bar{Q}_s^{cj}L_t^m)H^n$
$\mathcal{O}_{\bar{d}LQLH2}^{prst}$	$\epsilon_{im}\epsilon_{jn}(\bar{d}_p L_r^i)(\bar{Q}_s^{cj}L_t^m)H^n$
$\mathcal{O}_{\bar{Q}uLLH}^{prst}$	$\epsilon_{ij}(\bar{Q}_p u_r)(\bar{L}_s^c L_t^i)H^j$

Assumption:

single LEFT operator dominance\*

LEFT Wilson Coefficient	Value	SMEFT Wilson Coefficient	Value [TeV <sup>-3</sup> ]	$\Lambda_{NP}$ [TeV]
$c_{duve;LL}^S$	$1.86 \cdot 10^{-10}$	$C_{\bar{d}LQLH1}$	$7.06 \cdot 10^{-8}$	242
$c_{duve;RL}^S$	$1.86 \cdot 10^{-10}$	$C_{\bar{Q}uLLH}$	$3.62 \cdot 10^{-8}$	302
$c_{duve;LR}^V$	$8.20 \cdot 10^{-10}$	$C_{LeHD}$	$1.55 \cdot 10^{-7}$	186
$c_{duve;RR}^V$	$5.93 \cdot 10^{-8}$	$C_{\bar{d}LueH}$	$1.12 \cdot 10^{-5}$	44.7
$c_{duve;LL}^T$	$4.51 \cdot 10^{-10}$	$C_{\bar{d}LQLH1}$	$6.83 \cdot 10^{-7}$	114
		$C_{\bar{d}LQLH2}$	$3.41 \cdot 10^{-7}$	143
$c_{duve;LL}^{(7)V}$	$9.87 \cdot 10^{-6}$	$C_{LHD1}$	$1.36 \cdot 10^{-3}$	9.03
		$C_{LHD2}$	$2.71 \cdot 10^{-3}$	7.17
		$C_{LHW}$	$3.39 \cdot 10^{-4}$	14.3
$c_{duve;RL}^{(7)V}$	$9.87 \cdot 10^{-6}$	$C_{\bar{d}uLLD}$	$1.32 \cdot 10^{-3}$	9.11
$c_{V;LL}^{(9);ij}$	$1.40 \cdot 10^{-5}$	$C_{LHD1}$	$9.91 \cdot 10^{-4}$	10.0
		$C_{LHW}$	$2.48 \cdot 10^{-4}$	15.9
$c_{V;LR}^{(9);ij}$	$2.66 \cdot 10^{-8}$	$C_{\bar{d}uLLD}$	$1.83 \cdot 10^{-6}$	81.7

Fridell, Graf, Harz, **CH** JHEP '24

Sensitive to 1st gen: What if LNV small in 1st gen but large for others?

*SMEFT &  
LNV Direct Collider Searches*

# LVN SMEFT at Colliders

**Dim-5: Weinberg operator**

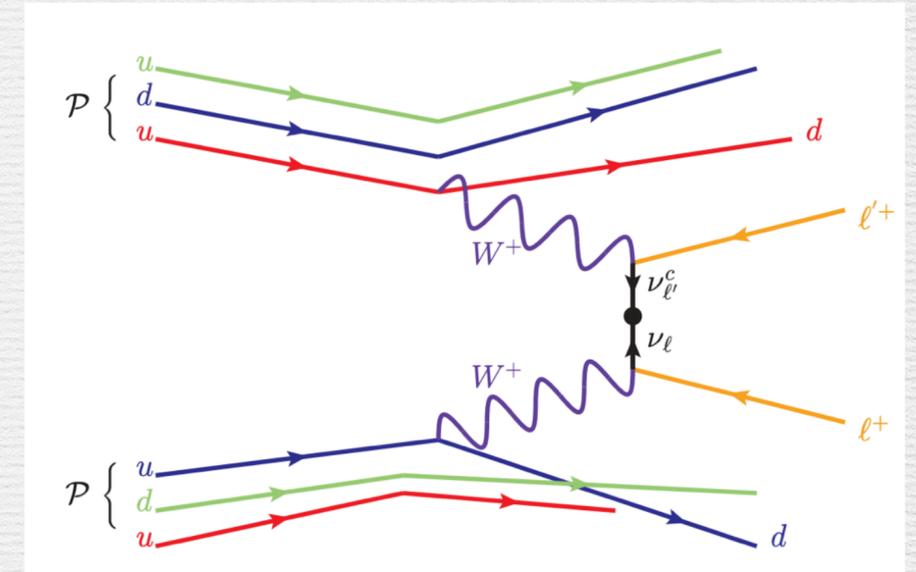
13 TeV LHC :  $\Lambda \lesssim 8.3$  (11) TeV

100TeV FCC :  $\Lambda \lesssim 48$  TeV

Fuks, Neundorff, Peters, Ruiz, Saimpert '21

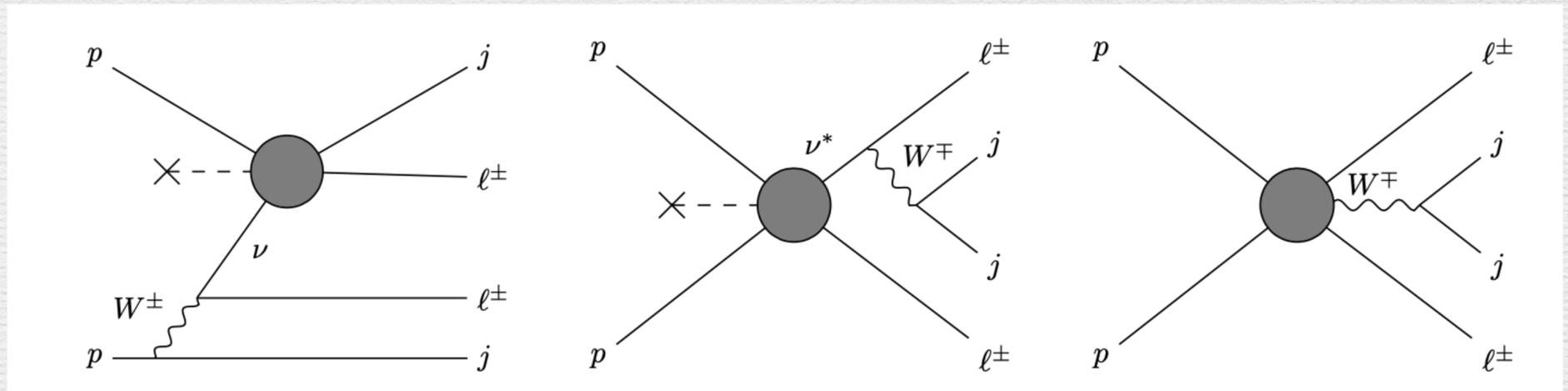
**Dim-7: comprehensively for the first time**

Fridell, Graf, Harz, **CH** JHEP '24



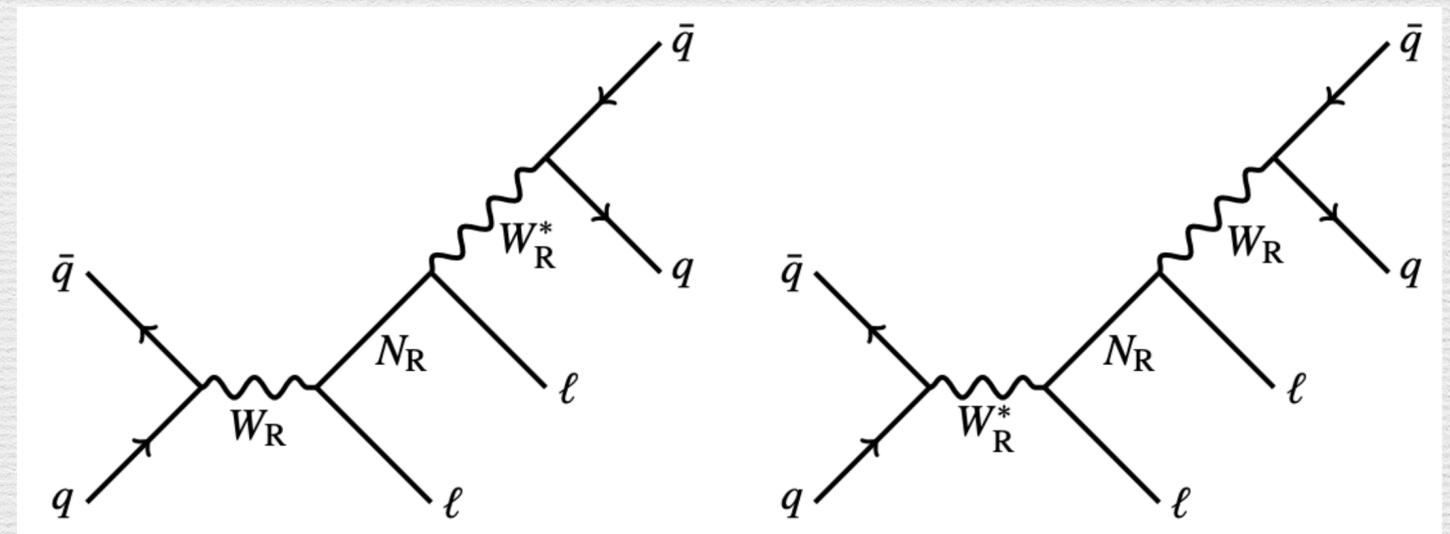
our main mode of interest:

$$pp \rightarrow \ell^\pm \ell^\pm jj + X$$



Recasting of the search for Keung–Senjanović (KS) process by ATLAS

ATLAS EPJC '23



$\mathcal{O}_{eLLLH}$ ,  $\mathcal{O}_{LHW}$ ,  $\mathcal{O}_{LHB}$  no signal at tree level

# LNV dim-7 SMEFT at LHC and FCC

LNV operators using FeynRule

LO cross sections with MadGraph5\_aMC@NLO  
using the basic generator level cuts

Hadronisation by Pythia8

Detector simulation by Delphes3: selection cuts

Cuts for $pp \rightarrow \mu^\pm \mu^\pm jj$ at $\sqrt{s} = 13$ TeV	
Object selection cuts	
$p_T^{\mu^{1(2)}} > 25$ GeV	$p_T^{j^{1(2)}} > 20$ GeV
$ \eta^{\mu^{1(2)}}  < 2.5$	$ \eta^{j^{1(2)}}  < 2.5$
Track-to-vertex association cuts	
$ z_0 \sin \theta  < 5$ mm	$ d_0  < 1$ $\mu$ m
Signal region cuts	
$p_T^{\mu^{\text{leading}}} > 40$ GeV	$p_T^{j^{1(2)}} > 100$ GeV
$H_T > 400$ GeV	$\Delta R_{\mu\mu} < 3.9$ GeV
$m_{\mu^1\mu^2} > 400$ GeV	$m_{j^1j^2} > 110$ GeV

Operator	$\sigma(pp \rightarrow \mu^\pm \mu^\pm jj)$ (pb)		$\Lambda_{\text{LNV}}$ [TeV]	$\Lambda_{\text{LNV}}^{\text{future}}$ [TeV]
	LHC	FCC		
$\mathcal{O}_{\bar{Q}uLLH}$	$2.4 \times 10^{-4}$	0.11	1.4	5.4
$\mathcal{O}_{\bar{d}LQLH2}$	$1.5 \times 10^{-5}$	$4.3 \times 10^{-3}$	0.90	3.1
$\mathcal{O}_{\bar{d}LQLH1}$	$6.9 \times 10^{-5}$	0.030	1.1	4.3
$\mathcal{O}_{\bar{d}LueH}$	$5.7 \times 10^{-5}$	0.035	1.1	4.5
$\mathcal{O}_{\bar{d}uLLD}$	0.64	210	5.0	19
$\mathcal{O}_{LHD2}$	$2.7 \times 10^{-12}$	$1.7 \times 10^{-10}$	0.075*	0.18
$\mathcal{O}_{LHD1}$	$1.9 \times 10^{-5}$	0.061	1.1	4.9
$\mathcal{O}_{LeHD}$	$1.2 \times 10^{-8}$	$3.1 \times 10^{-8}$	0.21*	0.44
$\mathcal{O}_{LH}$	$1.5 \times 10^{-8}$	$2.0 \times 10^{-6}$	0.35*	0.87

Major Caveats:

- (i) validity of EFT    (ii) resonant production

# Validity of the EFT approach for LNV Collider searches

Expansion of heavy mediator propagator

$$\frac{g^2}{Q^2 - M_{\text{med}}^2} = -\frac{g^2}{M_{\text{med}}^2} \left( 1 + \frac{Q^2}{M_{\text{med}}^2} + \mathcal{O}\left(\frac{Q^4}{M_{\text{med}}^4}\right) \right)$$

Fridell, Graf, Harz, **CH** JHEP '24

For collider searches  $Q$  can be quite high

$$Q = \sqrt{x_1 x_2} \sqrt{s}$$

Avg. momentum exchange:

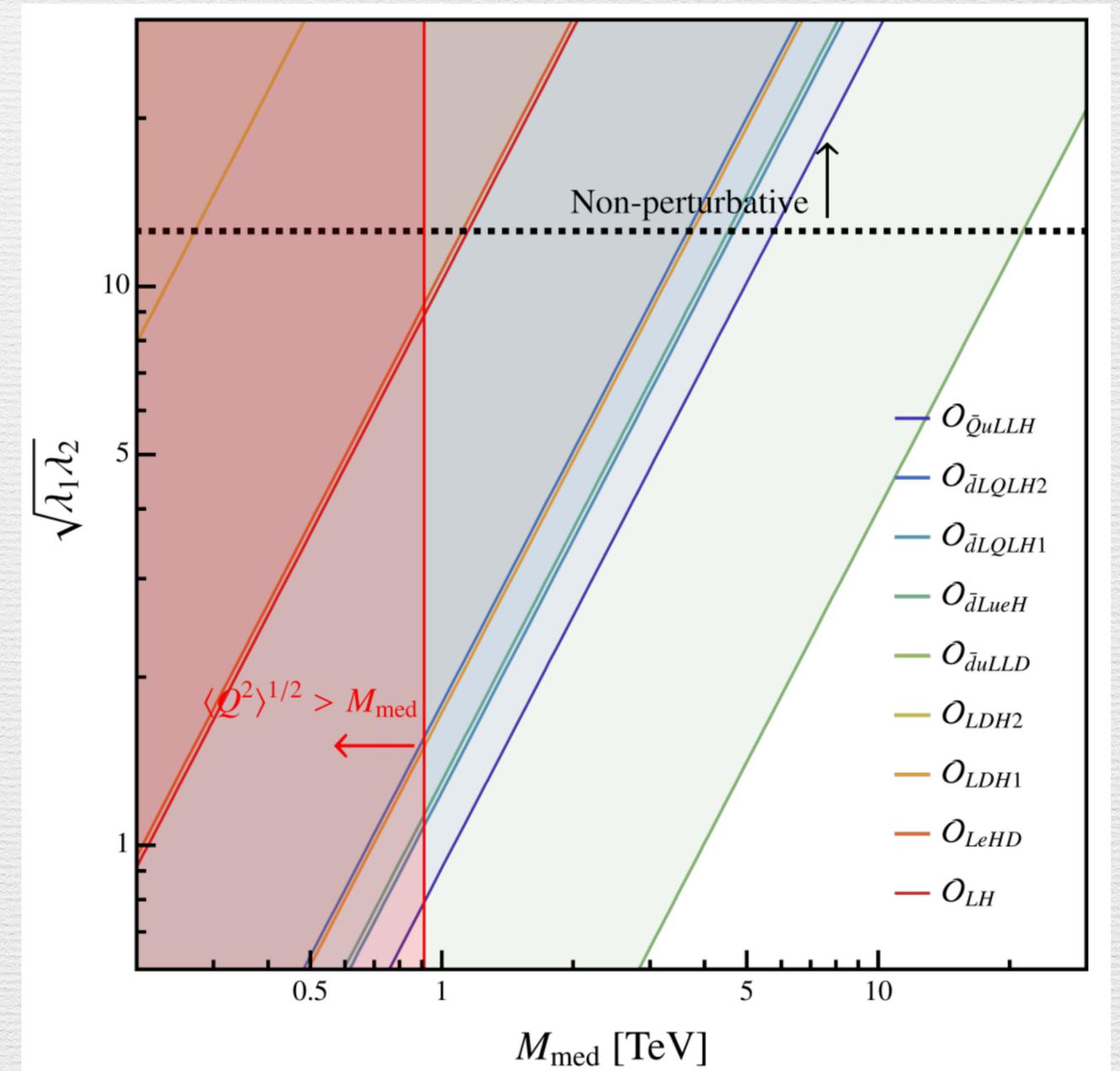
$$\langle Q^2 \rangle = \frac{\sum_{q_1=u,c} \sum_{q_2=d,s} \int dx_1 dx_2 (f_{q_1}(x_1) f_{\bar{q}_2}(x_2) + f_{q_1}(x_2) f_{\bar{q}_2}(x_1)) \Theta(Q - Q_0) Q^2}{\sum_{q_1=u,c} \sum_{q_2=d,s} \int dx_1 dx_2 (f_{q_1}(x_1) f_{\bar{q}_2}(x_2) + f_{q_1}(x_2) f_{\bar{q}_2}(x_1)) \Theta(Q - Q_0)}$$

$Q_0 \rightarrow$  Min final state invariant mass : controls avg. mom. exc.

For dim-7 SMEFT

$$\frac{\lambda_1 \lambda_2}{M_{\text{med}}^3} = \frac{1}{(\Lambda_{\text{LNV}})^3}$$

$\Lambda < Q_{\text{tr}} \implies$  large  $\lambda$  such that  $M_{\text{med}} > Q_{\text{tr}}$



# Validity of the EFT approach for Direct LNV Collider searches

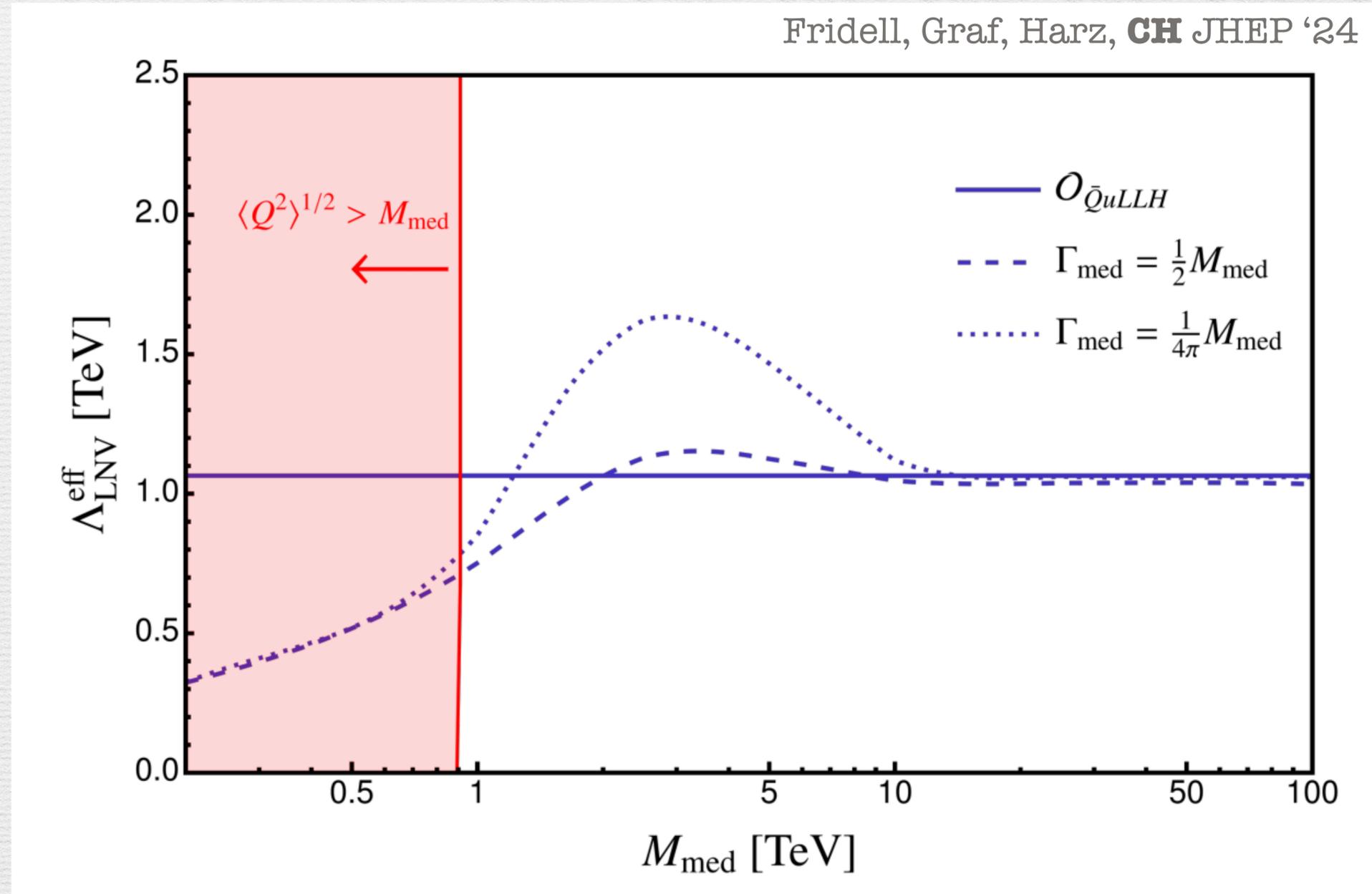
Resonant production is not captured by the EFT approach

$$\mathcal{L} \supset \lambda_1 \bar{d}_L u_R \chi^* + \lambda_2 \bar{e}_L^c \nu_L \chi + \text{h.c.}$$

$$\frac{\lambda_1 \lambda_2}{M_{\text{med}}^2} = \frac{v}{(\Lambda_{\text{LNV}}^{\text{eff}})^3}$$

For small mediator widths:

EFT approach underestimates the limits



*Many Other probes!*

# Neutral Current LNV@ low energy

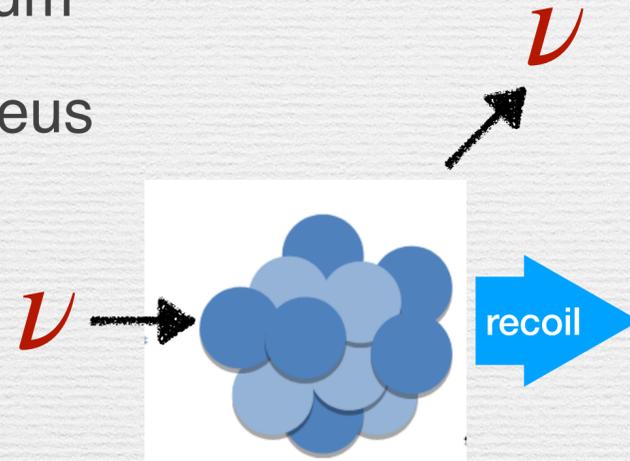
## CEνNS experiments

## LNV

First observation: Akimov et al. Science '17

Neutrino scatters with low-momentum transfer elastically from entire nucleus

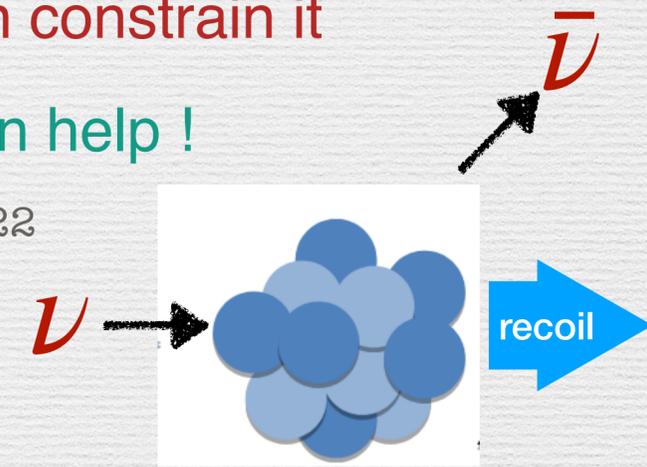
$$E_\nu \lesssim \frac{hc}{R_N} \sim \mathcal{O}(10 \text{ MeV})$$



Can't directly discover LNV but can constrain it

Distributions with  $\gamma$  in final state can help !

Bolton, Deppisch, Fridell, Harz, **CH**, Kulkarni '22



The nuclear recoil energy:  $E_r^{\max} = \frac{2E_\nu^2}{M_A} \sim \mathcal{O}(\text{KeV})$

SM allowed but hard to observe due to tiny recoil energy!

**GNI:**

Lindner, Rodejohann, Xu;  
Aristizabal Sierra, De Romeri, Rojas; ++

$$\mathcal{L}_{\text{eff}}^{\bar{\nu}^c \nu ff} = \frac{4G_F}{\sqrt{2}} \left[ c_{d\nu;LL}^{S,prst} (\bar{d}_{Rp} d_{Lr}) (\bar{\nu}_s^c \nu_t) + c_{d\nu;RL}^{S,prst} (\bar{d}_{Lp} d_{Rr}) (\bar{\nu}_s^c \nu_t) + c_{d\nu;LL}^{T,prst} (\bar{d}_{Rp} \sigma_{\mu\nu} d_{Lr}) (\bar{\nu}_s^c \sigma^{\mu\nu} \nu_t) \right. \\ \left. + c_{u\nu;LL}^{S,prst} (\bar{u}_{Rp} u_{Lr}) (\bar{\nu}_s^c \nu_t) + c_{u\nu;RL}^{S,prst} (\bar{u}_{Lp} u_{Rr}) (\bar{\nu}_s^c \nu_t) + c_{u\nu;LL}^{T,prst} (\bar{u}_{Rp} \sigma_{\mu\nu} u_{Lr}) (\bar{\nu}_s^c \sigma^{\mu\nu} \nu_t) \right].$$

Current Bound				
LEFT Wilson	Value	$C_{\bar{d}LQ_L H_1^1}$ [TeV <sup>-3</sup> ]	$\Lambda_{\text{NP}}$ [TeV]	Experiment
$c_{d\nu;LL(LR)}^{S,11\mu\mu}$	0.030	11.3	0.4	COHERENT
$c_{d\nu;LL}^{T,11st}$	0.178	540.2	0.1	COHERENT
Future Sensitivity				
$c_{d\nu;LL(LR)}^{S,11\alpha\alpha}$	0.008	3.0	0.7	Ge
$c_{d\nu;LL}^{T,11st}$	0.062	186.9	0.2	Ge

# Changed Current LNV NSI @ LBL Oscillation experiments

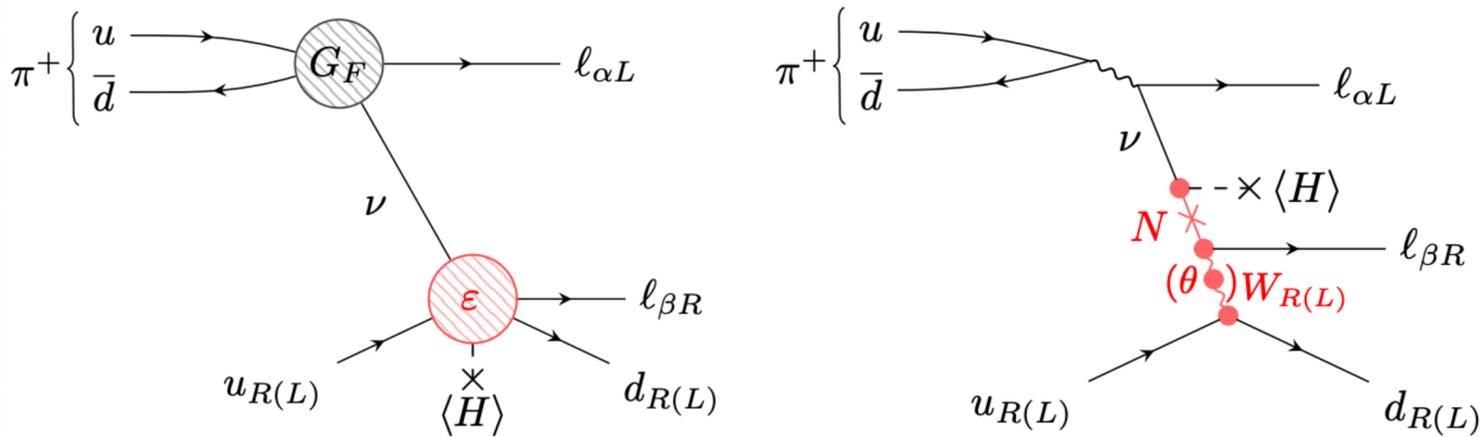
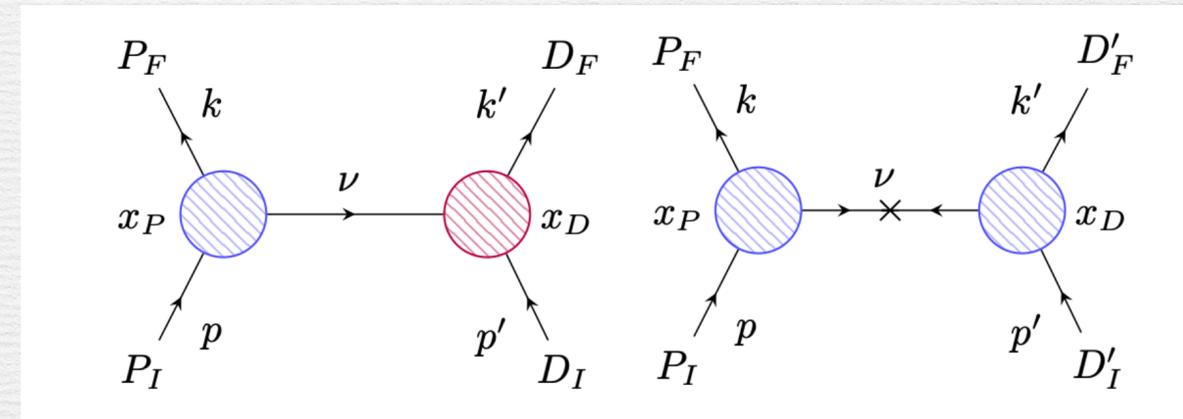
Bolton, Deppisch'19

Production charge blind

Detection sensitive to outgoing lepton charge

$$R_{\alpha\beta} \equiv \frac{N_{\ell_{\beta}^{+}}}{N_{\ell_{\beta}^{-}}} = \frac{\Gamma_{\nu_{\alpha} \rightarrow \bar{\nu}_{\beta}} + \Gamma_{\bar{\nu}_{\alpha} \rightarrow \bar{\nu}_{\beta}}}{\Gamma_{\nu_{\alpha} \rightarrow \nu_{\beta}} + \Gamma_{\bar{\nu}_{\alpha} \rightarrow \nu_{\beta}}}$$

$$S_{\mu\mu} \approx \frac{\int dE_{\mathbf{q}} \sum_{\rho,\sigma} \frac{d\Gamma_{\nu_{\mu}}}{dE_{\mathbf{q}}} \cdot P_{\nu_{\mu} \rightarrow \bar{\nu}_{\mu}}^{(\rho,\sigma)} \cdot \sigma_{\bar{\nu}_{\mu}}}{\int dE_{\mathbf{q}} \sum_{\rho,\sigma} \frac{d\Gamma_{\nu_{\mu}}}{dE_{\mathbf{q}}} \cdot P_{\nu_{\mu} \rightarrow \nu_{\mu}}^{(\rho,\sigma)} \cdot \sigma_{\nu_{\mu}}}$$



$$\mathcal{L}_{\text{LEFT}}^{d=6} \supset \frac{4G_F}{\sqrt{2}} \left[ c_{duve;LR}^{V,prst} (\bar{d}_{Lp} \gamma_{\mu} u_{Lr}) (\bar{\nu}_s^c \gamma^{\mu} e_{Rt}) + c_{duve;RR}^{V,prst} (\bar{d}_{Rp} \gamma_{\mu} u_{Rr}) (\bar{\nu}_s^c \gamma^{\mu} e_{Rt}) \right]$$

$$\mathcal{L}_{\text{LEFT}}^{d=6} = \frac{4G_F}{\sqrt{2}} \left[ c_{duve;LL}^{S,prst} (\bar{d}_{Rp} u_{Lr}) (\bar{\nu}_s^c e_{Lt}) + c_{duve;RL}^{S,prst} (\bar{d}_{Lp} u_{Rr}) (\bar{\nu}_s^c e_{Lt}) + c_{duve;LL}^{T,prst} (\bar{d}_{Rp} \sigma_{\mu\nu} u_{Lr}) (\bar{\nu}_s^c \sigma^{\mu\nu} e_{Lt}) \right].$$

LEFT Wilson Coefficient	Value	SMEFT Wilson Coefficient	Value [TeV <sup>-3</sup> ]	$\Lambda_{\text{NP}}$ [TeV]	Experiment
$c_{duve;LR}^{V,11ee(e\mu)}$	0.017	$C_{LeHD}^{ee(e\mu)}$	3.2	0.7	KamLAND
$c_{duve;RR}^{V,11ee(e\mu)}$	0.017	$C_{\bar{d}LueH}^{1e1e(1e1\mu)}$	6.4	0.5	KamLAND
$c_{duve;LR}^{V,11e\tau}$	0.015	$C_{LeHD}^{ee(e\tau)}$	2.8	0.7	KamLAND
$c_{duve;RR}^{V,11e\tau}$	0.015	$C_{\bar{d}LueH}^{1e1\tau}$	5.7	0.6	KamLAND
$c_{duve;LR}^{V,11\mu e}$	0.22 - 3.47	$C_{LeHD}^{\mu e}$	41.7-658.1	0.1-0.3	MINOS
$c_{duve;RR}^{V,11\mu e}$	0.22 - 3.47	$C_{\bar{d}LueH}^{1\mu 1e}$	83.4-1316.2	0.1-0.2	MINOS
$c_{duve;LR}^{V,11\mu\mu}$	0.16 - 0.63	$C_{LeHD}^{\mu\mu}$	30.3-119.5	0.2-0.3	MINOS
$c_{duve;RR}^{V,11\mu\mu}$	0.16 - 0.63	$C_{\bar{d}LueH}^{1\mu 1\mu}$	60.7-239.0	0.2-0.3	MINOS
$c_{duve;LR}^{V,11\mu\tau}$	0.16 - 0.71	$C_{LeHD}^{\mu\tau}$	30.3-134.7	0.2-0.3	MINOS
$c_{duve;RR}^{V,11\mu\tau}$	0.16 - 0.71	$C_{\bar{d}LueH}^{1\mu 1\tau}$	60.7-269.31	0.2-0.3	MINOS

# LVN dim-7 SMEFT @ Rare meson and $\tau$ decays

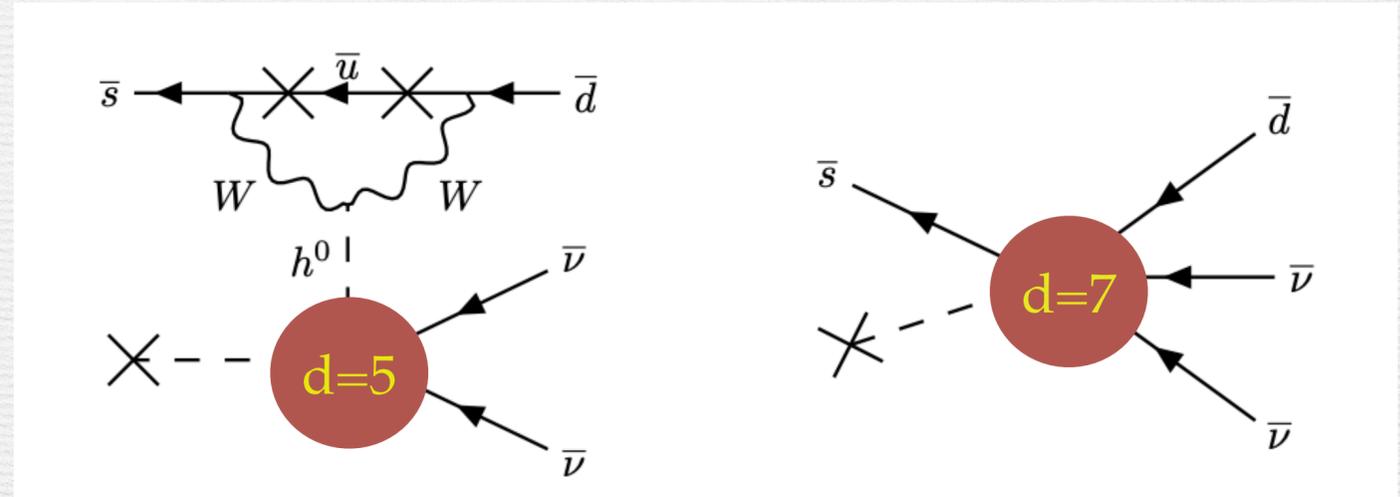
Weak constraints from

$$\tau^\pm \rightarrow \ell_\alpha^\mp P_i^\pm P_j^\pm \quad K^+ \rightarrow \pi^- \ell^+ \ell^+$$

$$M \rightarrow M' \nu \nu$$

well discussed in literature  
in the context of dim-7 SMEFT

Li, Ma, Schmidt PRD '20  
Deppisch, Fridell, Harz JHEP '20  
Felkl, Li, Schmidt JHEP '21



Current Bound

LEFT Wilson Coefficient	Value	$C_{\bar{d}LQLH1}$ [TeV <sup>-3</sup> ]	$\Lambda_{NP}$ [TeV]	Observable
$c_{d\nu;LL}^{S,ds\gamma\gamma}$	$1.3 \times 10^{-6}$	$4.8 \times 10^{-4}$	12.8	$K_L \rightarrow \nu\nu$
$c_{d\nu;LL}^{S,ds\gamma\gamma}$	$2.5 \times 10^{-7}$	$9.6 \times 10^{-5}$	21.8	$K^+ \rightarrow \pi^+ \nu\nu$
$c_{d\nu;LL}^{S,ds\gamma\gamma}$	$2.6 \times 10^{-7}$	$9.9 \times 10^{-5}$	21.6	$K^0 \rightarrow \pi^0 \nu\nu$
Future Sensitivity				
$c_{d\nu;LL}^{S,ds\gamma\gamma}$	$8.4 \times 10^{-8}$	$3.2 \times 10^{-5}$	31.5	$K^+ \rightarrow \pi^+ \nu\nu$
$c_{d\nu;LL}^{S,ds\gamma\gamma}$	$1.4 \times 10^{-7}$	$5.2 \times 10^{-5}$	26.8	$K^0 \rightarrow \pi^0 \nu\nu$

Current Bound

LEFT Wilson Coefficient	Value	$C_{\bar{d}LQLH1}$ [TeV <sup>-3</sup> ]	$\Lambda_{NP}$ [TeV]	Observable
$c_{d\nu;LL}^{S,sb\gamma\gamma}$	$3.6 \times 10^{-4}$	0.14	1.9	$B \rightarrow K^{(*)} \nu\nu$
$c_{d\nu;LL}^{S,sb\gamma\delta}$	$2.7 \times 10^{-4}$	0.21	1.7	$B \rightarrow K^{(*)} \nu\nu$
$c_{d\nu;LL}^{T,sb\gamma\delta}$	$0.6 \times 10^{-4}$	0.18	1.75	$B \rightarrow K^* \nu\nu$
Future Sensitivity (50 ab <sup>-1</sup> )				
$c_{d\nu;LL}^{S,sb\gamma\gamma}$	$0.6 \times 10^{-4}$	0.02	3.5	$B \rightarrow K \nu\nu$
$c_{d\nu;LL}^{S,sb\gamma\delta}$	$0.6 \times 10^{-4}$	0.05	2.8	$B \rightarrow K \nu\nu$
$c_{d\nu;LL}^{T,sb\gamma\delta}$	$0.3 \times 10^{-4}$	0.08	2.3	$B \rightarrow K^* \nu\nu$

**Assumptions:**

1. single LEFT operator dominance\*
2. lepton flavour universality\*\*

Dipole type of contributions can be present but suppressed  
Charged Kaon decays @NA62 provide the best limits

# $\mathcal{O}_{\bar{e}LLLH}$ and leptonic $\mu^+$ decay

$\mathcal{O}_{\bar{e}LLLH}$  doesn't contribute to  $0\nu\beta\beta$  decay at tree level

After the EW symmetry breaking at the LEFT level:

$$\mathcal{L} = -\frac{4G_F}{\sqrt{2}} \left\{ c_{ev;LL}^{S,\mu ee\mu} (\bar{\mu}_R e_L) (\bar{\nu}_e^c \nu_\mu) + c_{ev;LL}^{S,e\mu e\mu} (\bar{e}_R \mu_L) (\bar{\nu}_e^c \nu_\mu) \right. \\ \left. + c_{ev;LL}^{T,\mu ee\mu} (\bar{\mu}_R \sigma_{\mu\nu} e_L) (\bar{\nu}_e^c \sigma^{\mu\nu} \nu_\mu) + c_{ev;LL}^{T,e\mu e\mu} (\bar{e}_R \sigma_{\mu\nu} \mu_L) (\bar{\nu}_e^c \sigma^{\mu\nu} \nu_\mu) \right\} + \text{h.c.}$$

Only  $c_{ev;LL}^{S(T),\mu ee\mu}$  can mediate the experimentally searched  $\mu^+ \rightarrow e^+ \bar{\nu}_e \bar{\nu}_\mu$

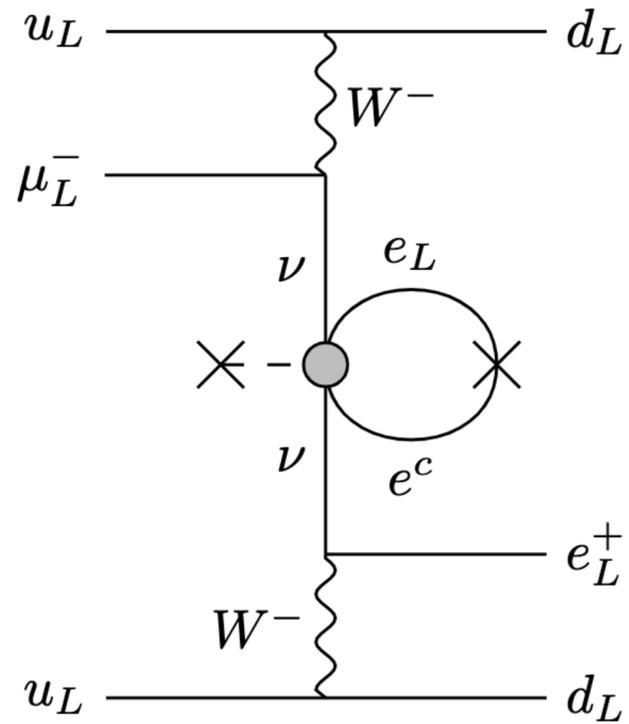
CC process  $p \bar{\nu}_e \rightarrow e^+ n$  was used to identify  $\bar{\nu}_e$

B. Armbruster et al PRL '03

LEFT Wilson		Current Bound		
Coefficient	Value	$C_{\bar{e}LLLH}$ [TeV <sup>-3</sup> ]	$\Lambda_{NP}$ [TeV]	Observable
$c_{ev;LL}^{S,\mu ee\mu}$	0.06	15.2	0.4	$\mu^+ \rightarrow e^+ \bar{\nu}_e \bar{\nu}_\mu, \tilde{\rho} = 0.75$
$c_{ev;LL}^{T,\mu ee\mu}$	0.04	121.6	0.2	$\mu^+ \rightarrow e^+ \bar{\nu}_e \bar{\nu}_\mu, \tilde{\rho} = 0.25$

# LNV ( $\mu^- - e^+$ ) conversion

$$R_{\mu^- e^+} \equiv \frac{\Gamma(\mu^- + N \rightarrow e^+ + N')}{\Gamma(\mu^- + N \rightarrow \nu_\mu + N')}$$



$\mathcal{O}_{\bar{e}LLLH}$

Best limits: SINDRUM II ; Future: Mu2e and COMET P-I

$$\frac{|g_{e\mu}|^2 \left(\frac{G_F}{\sqrt{2}}\right)^4 \left(\frac{1}{q^2}\right)^2 \left(\frac{y_\tau v \Lambda^2}{16\pi^2}\right)^2 v^2 \left(\frac{1}{\Lambda^3}\right)^2 Q^8 |\psi_{100}(0)|^2}{\left(\frac{G_F}{\sqrt{2}}\right)^2 Q^2 |\psi_{100}(0)|^2}$$

Berryman, de Gouvêa et al '16

For  $\Lambda \sim 1 \text{ TeV}$   $R_{\mu^- e^+} \sim 10^{-24}$

**Small contributions for dim-7 SMEFT**

# Neutrino magnetic moment

$$\mathcal{L}_M \supset \frac{1}{2} \begin{pmatrix} \nu_1 & \nu_2 & \nu_3 \end{pmatrix} \sigma_{\mu\nu} \begin{pmatrix} 0 & \mu_{12} & \mu_{13} \\ -\mu_{12} & 0 & \mu_{23} \\ -\mu_{13} & -\mu_{23} & 0 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} F^{\mu\nu} + \text{h.c.}$$

$$c_{\nu\nu F}^{5\gamma}/e \equiv \mu_{ij} = \frac{1}{2v} \left( v^3 C_{LHB}^{ij} - v^3 \frac{C_{LHW}^{ij} - C_{LHW}^{ji}}{2} \right)$$

Solar: Borexino

Reactor: GEMMA, TEXONO, CONUS

Accelerator: LSND, DUNE

$$|C_{LHB}^{ij} - C_{LHW}^{ij}|_{i \neq j} \lesssim \frac{10^{-11}}{4m_e v^2}$$

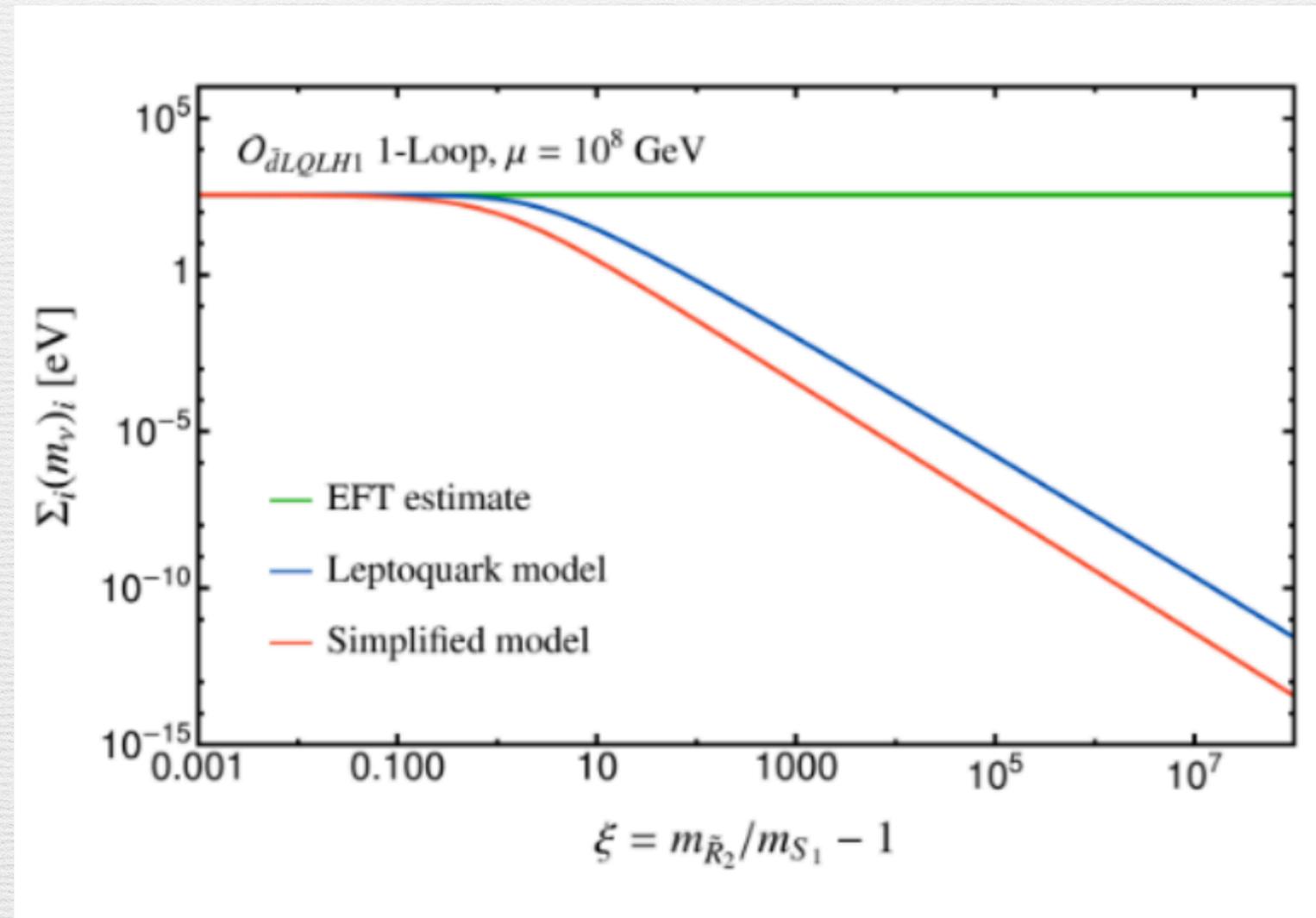
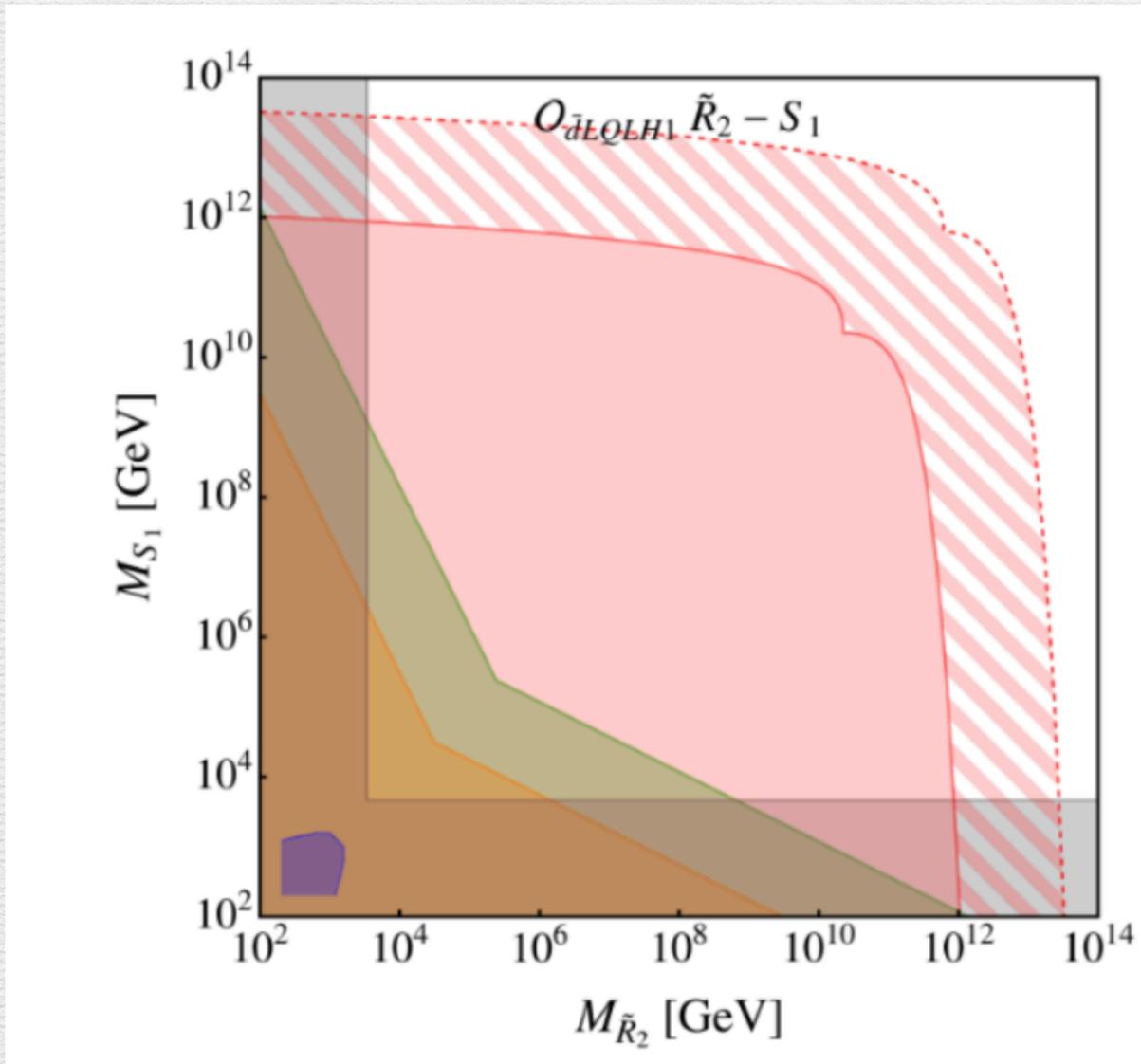
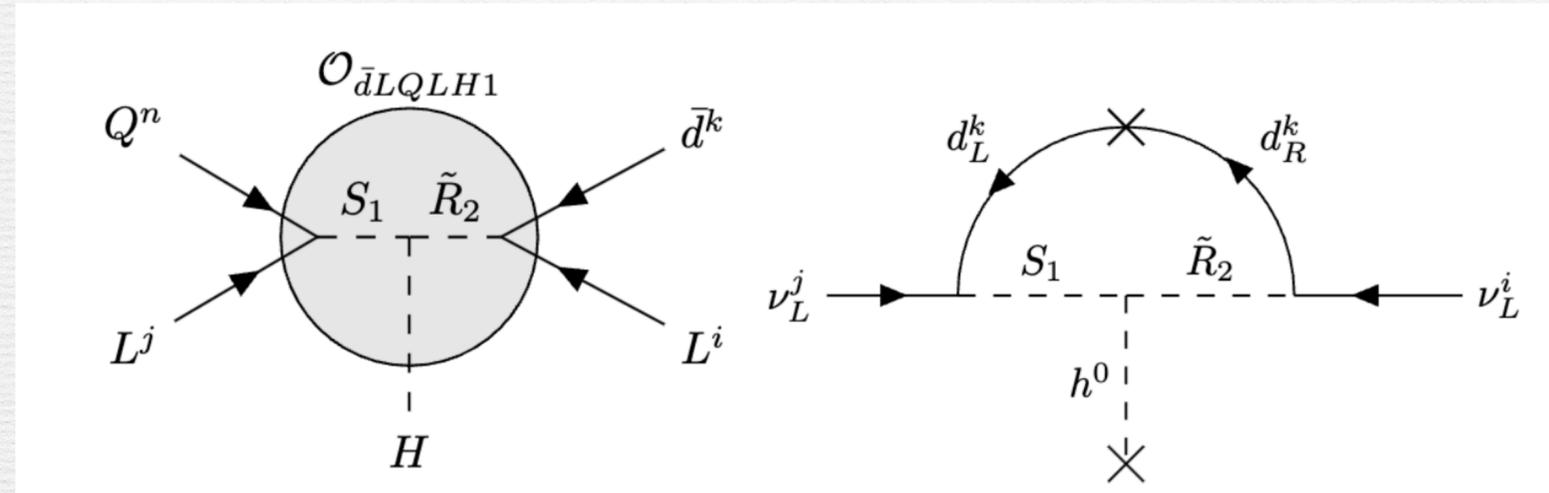
$\Lambda > 10 \text{ TeV}$

**Competitive with  $0\nu\beta\beta$**

Constraints from  
Light Neutrino Masses

# Light neutrino mass: UV example

Limitation of cut-off regularization:  
hierarchy between NP scales



# Light neutrino mass and “naturalness”

Tree level contribution from  $\mathcal{O}_{LH}$ :

$$(\delta m_\nu)_{ij} = -\frac{v}{2} (v^3 \mathcal{C}_{LH,ij})$$



$$(\delta m_\nu)_{ij} < 1 \text{ eV} \implies C_{LH} : \Lambda > 1200 \text{ TeV}$$

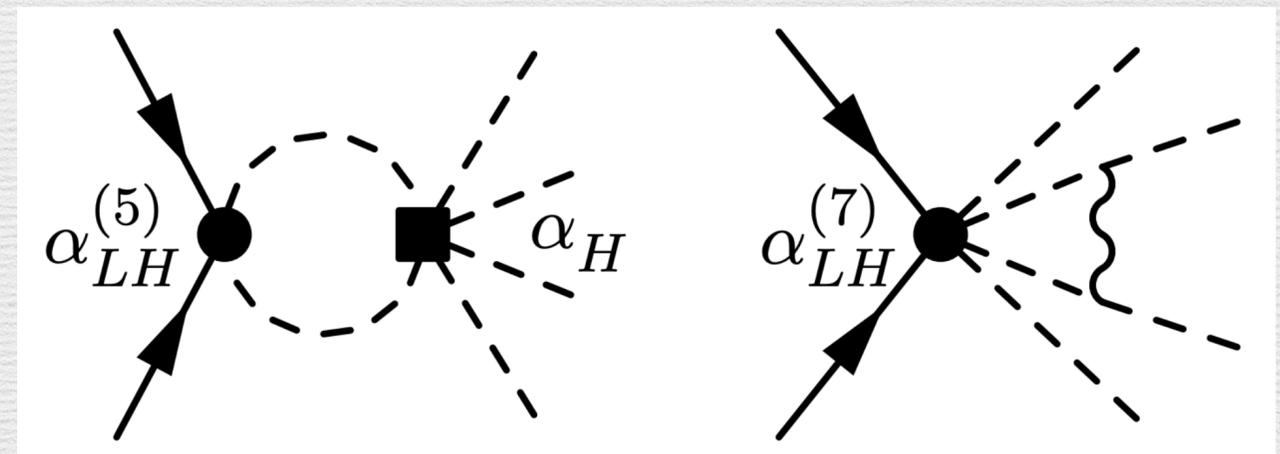
$$C_{LeHD} : \Lambda > 6 \text{ TeV} \quad C_{LHW} : \Lambda > 460 \text{ TeV}$$

$$C_{LHD1} : \Lambda > 280 \text{ TeV} \quad C_{LHD2} : \Lambda > 350 \text{ TeV}$$

Dim reg provides a robust approach

$$\mu \frac{dC_5}{d\mu} = \gamma^{(5,5)} C_5 + \hat{\gamma}^{(5,5)} C_5 C_5 C_5 + \gamma_i^{(5,6)} C_5 C_6^i + \gamma_i^{(5,7)} C_7^i$$

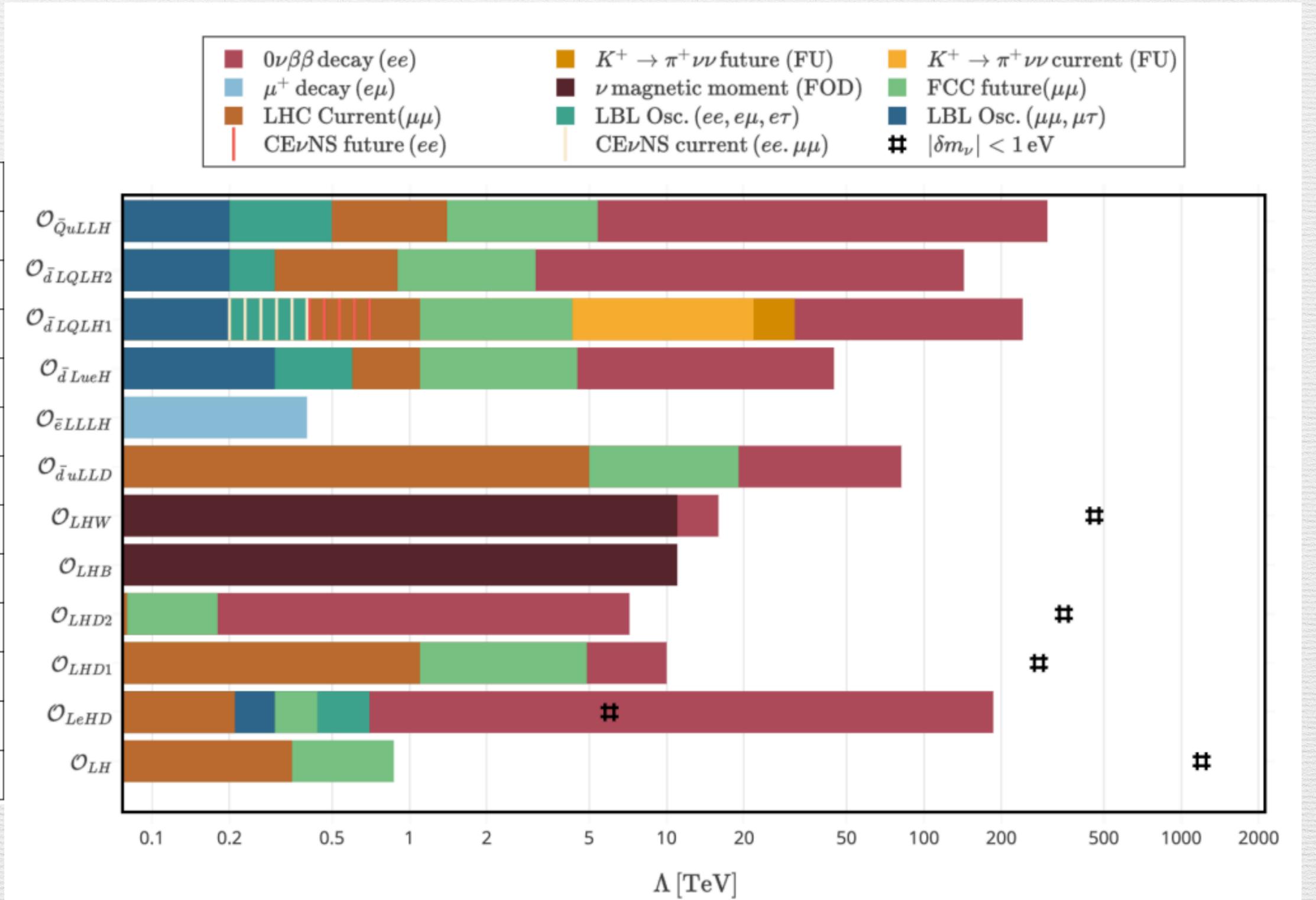
$$\mu \frac{dC_7^i}{d\mu} = \gamma_{ij}^{(7,7)} C_7^j + \gamma_i^{(7,5)} C_5 C_5 C_5 + \gamma_{ij}^{(7,6)} C_5 C_6^j$$



Chala, Titov '21; Di Zhang '23,24 ++

# Bird's eye view of the constraints on LNV dim-7 SMEFT operators

$\mathcal{O}$	Operator
$\mathcal{O}_{LH}^{pr}$	$\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^c L_r^m)H^j H^n (H^\dagger H)$
$\mathcal{O}_{LeHD}^{pr}$	$\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^c \gamma_\mu e_r)H^j (H^m i D^\mu H^n)$
$\mathcal{O}_{LHD1}^{pr}$	$\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^c D_\mu L_r^j)(H^m D^\mu H^n)$
$\mathcal{O}_{LHD2}^{pr}$	$\epsilon_{im}\epsilon_{jn}(\overline{L}_p^c D_\mu L_r^j)(H^m D^\mu H^n)$
$\mathcal{O}_{LHB}^{pr}$	$g\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^c \sigma_{\mu\nu} L_r^m)H^j H^n B^{\mu\nu}$
$\mathcal{O}_{LHW}^{pr}$	$g'\epsilon_{ij}(\epsilon\tau^I)_{mn}(\overline{L}_p^c \sigma_{\mu\nu} L_r^m)H^j H^n W^{I\mu\nu}$
$\mathcal{O}_{\bar{d}uLLD}^{prst}$	$\epsilon_{ij}(\overline{d}_p \gamma_\mu u_r)(\overline{L}_s^c i D^\mu L_t^j)$
$\mathcal{O}_{\bar{e}LLLH}^{prst}$	$\epsilon_{ij}\epsilon_{mn}(\overline{e}_p L_r^i)(\overline{L}_s^c L_t^m)H^n$
$\mathcal{O}_{\bar{d}LueH}^{prst}$	$\epsilon_{ij}(\overline{d}_p L_r^i)(\overline{u}_s^c e_t)H^j$
$\mathcal{O}_{\bar{d}LQLH1}^{prst}$	$\epsilon_{ij}\epsilon_{mn}(\overline{d}_p L_r^i)(\overline{Q}_s^c L_t^m)H^n$
$\mathcal{O}_{\bar{d}LQLH2}^{prst}$	$\epsilon_{im}\epsilon_{jn}(\overline{d}_p L_r^i)(\overline{Q}_s^c L_t^m)H^n$
$\mathcal{O}_{\bar{Q}uLLH}^{prst}$	$\epsilon_{ij}(\overline{Q}_p u_r)(\overline{L}_s^c L_t^i)H^j$



# Conclusions

Operator	Collider	$0\nu\beta\beta$	LBL Osc.	$\mu_\nu$	$\mu^+$ -decay	CE $\nu$ NS	Meson decay
$\mathcal{O}_{LH}$	✓	✓	-	-	-	-	-
$\mathcal{O}_{LeHD}$	✓	✓	✓	-	-	-	-
$\mathcal{O}_{LHD1}$	✓	✓	-	-	-	-	-
$\mathcal{O}_{LHD2}$	✓	✓	-	-	-	-	-
$\mathcal{O}_{LHB}$	-	-	-	✓	-	✓	-
$\mathcal{O}_{LHW}$	-	✓	-	✓	-	✓	-
$\mathcal{O}_{\bar{d}uLLD}$	✓	✓	-	-	-	-	-
$\mathcal{O}_{\bar{e}LLLH}$	-	-	-	-	✓	-	-
$\mathcal{O}_{\bar{d}LueH}$	✓	✓	✓	-	-	-	-
$\mathcal{O}_{\bar{d}LQLH1}$	✓	✓	✓	-	-	✓	✓
$\mathcal{O}_{\bar{d}LQLH2}$	✓	✓	✓	-	-	-	-
$\mathcal{O}_{\bar{Q}uLLH}$	✓	✓	✓	-	-	✓	-

EFTs provide robust frameworks to parametrize and constrain LNV BSM physics

The new physics scale hierarchy, EFT loop effects requires a more careful approach

Hvala  
vam!  
